



# MCMA2017



## A ROBUST MONTE CARLO TREATMENT PLANNING OPTIMIZATION ALGORITHM FOR DOSE PAINTING CLINICAL IMPLEMENTATION

Elisa Jiménez-Ortega<sup>a,b,\*</sup>, Ana Ureba<sup>b,c</sup>, Ana Rita Barbeiro<sup>a,b</sup>,  
Marcin Balcerzyk<sup>d</sup>, Ángel Parrado Gallego<sup>d</sup>, Amadeo Wals-Zurita<sup>e</sup>,  
Francisco Javier García-Gómez<sup>f</sup>, Antonio Leal<sup>a,b</sup>.

a. Dpto. Fisiología Médica y Biofísica, Universidad de Sevilla, Seville (Spain).

b. Instituto de Biomedicina de Sevilla, IBIS, Seville (Spain).

c. Medical Radiation Physics, Stockholm University, Karolinska Institutet, Stockholm (Sweden).

d. Centro Nacional de Aceleradores (CNA). Seville (Spain).

e. Hospital Universitario Virgen Macarena, Servicio de Radioterapia, Seville (Spain).

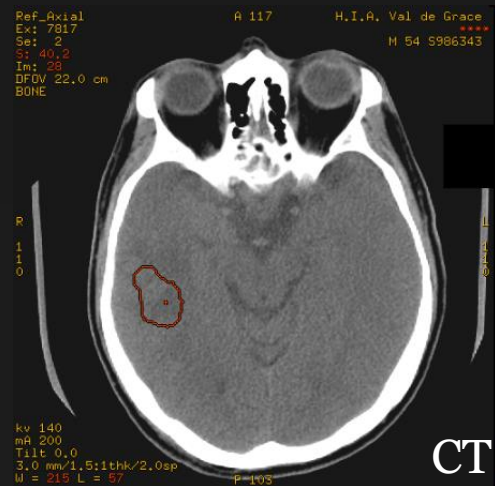
f. Hospital Universitario Virgen Macarena, Servicio de Medicina Nuclear, Seville (Spain).



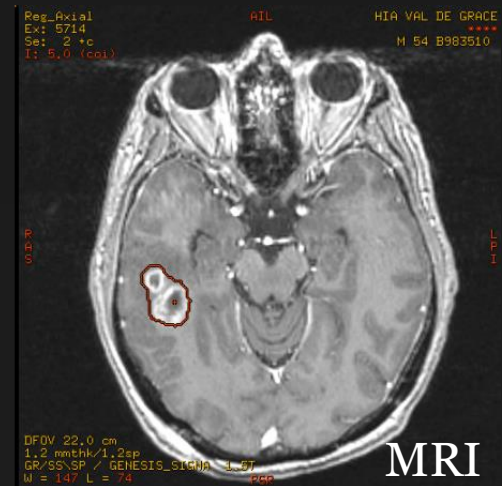
# Introduction

## Medical imaging in radiotherapy treatment planning.

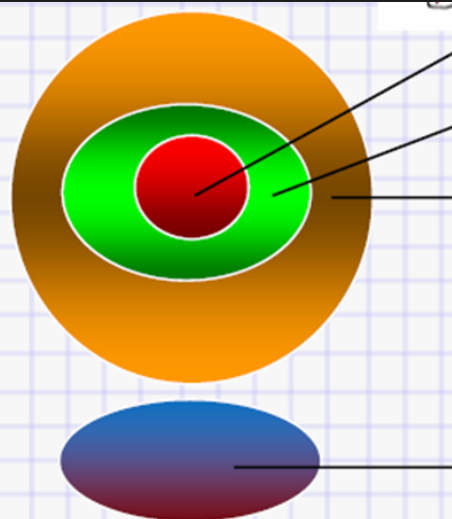
- Classic role
  - Delimitation based on morphological information
  - Margins for incorporating functional information (movements, extension)



CT



MRI



**Gross Tumor Volume (GTV)**  
**Clinical Target Volume (CTV)**  
**Planning Target Volume (PTV)**

$$GTV \leq CTV \leq PTV$$

**Organ At Risk (OAR)**

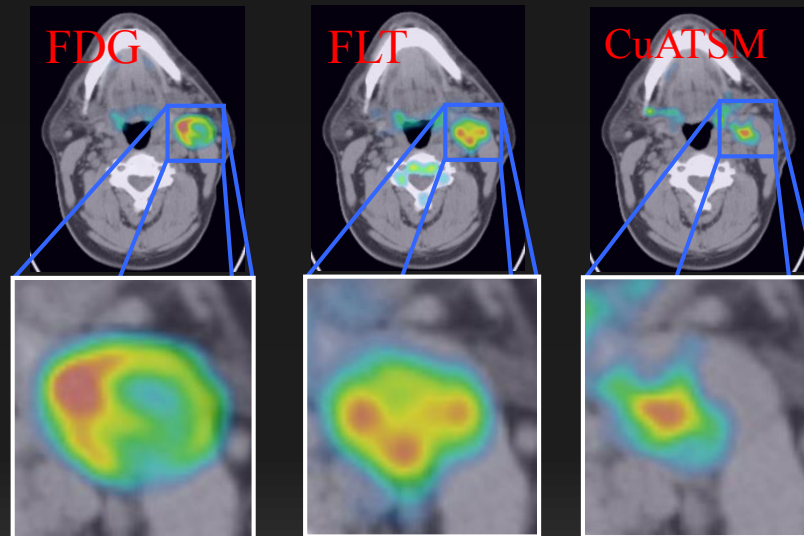




# Introduction

- New role → Functional Information
- Evolution and characteristics of the lesion

- PET
  - Metabolism
  - Proliferation
  - O<sub>2</sub> concentration
  - Differentiation...
- SPECT
- fMRI



*Nyflot et al, Radiother Oncol, 2012*

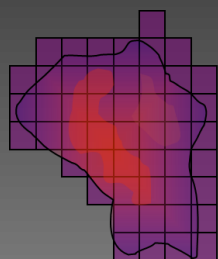
**BTV**

*(Biological Target Volume)*



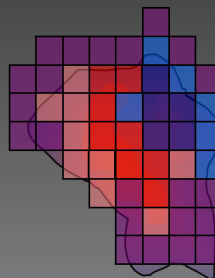
**New concepts and protocols**

**Conventional**



- Homogeneous dose to volumes
- Few targets
- Conventional prescription

**Dose Painting**

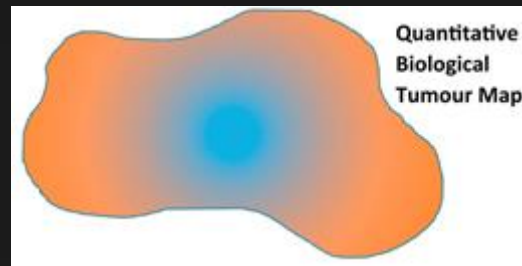


- Heterogeneous doses
- Multiple targets
- Dose escalation according to functional information



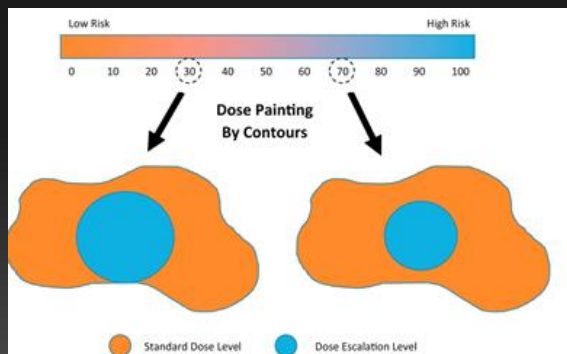
# Introduction

## Heterogeneous distributions



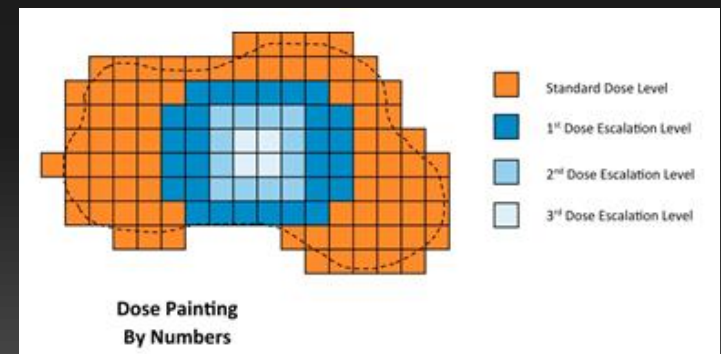
*Alonzi et al., Clin Oncol, 2015*

### Dose Painting by Contour (DPBC)



- Dose escalation based on thresholds
- Dose-to-volume restrictions
- Simultaneous boost strategies in TPS

### Dose Painting by Numbers (DPBN)



- Dose escalation based on individual values: TRUE DP
- Dose-to-voxel restrictions
- Commercial TPS: approximations based on dose-volume optimization



# Introduction

DP means a new scenario for planning RT

New tools should be incorporated to TPS

(Our proposal)

**Dose calculation:**

Higher dose gradients within the target require the most accurate dose calculation engine:

**Monte Carlo Treatment Planning (MCTP)**

**Optimization procedure:**

A more important role for image into the algorithms

**BIOMAP**

New restrictions and robustness at the voxel level

**Linear Programming (LP)**





# Material and Methods

<http://grupos.us.es/medicalphysics/>

Full Monte Carlo Treatment Planning System



- MATLAB platform
- Image processing
- fMC planning
- Optimization
- Evaluation



# Material and Methods

## PLANNING PROCESS

Functional image processing  
Reconstruction protocols and uncertainty assessment

Optimization

Segmentation and Sequencing  
(DPBC / DPBN)

- Inverse planning
- Generation of apertures based on the image:

**BIOMAP**

MU weighting  
(Voxel level constraints)

Robust optimization  
based on Linear  
Programming (LP)

Dose Calculation

As accurate as possible → **Full Monte Carlo planning**



# Material and Methods

## • Functional imaging processing

PET/CT Images (Siemens Biograph mCT 64 scanner of CNA):

- Location and size of the disease
  - Prescription of the dose
- } Need for **standardized accreditation**

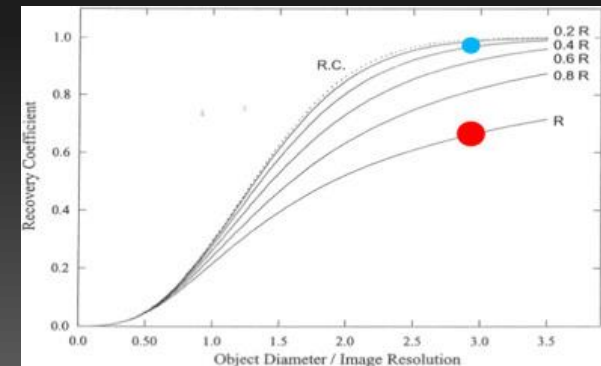
**PET reconstruction protocols: EARL / “Radiotherapy”**



- Patient protocol simulation
- RT table fitting
- Study of different reconstructions
- Assessment of uncertainties



Recovery coefficients  
(partial volume effects)



Adapted from: M.E. Phelps. *PET: Molecular Imaging and Its Biological Applications* (2004)

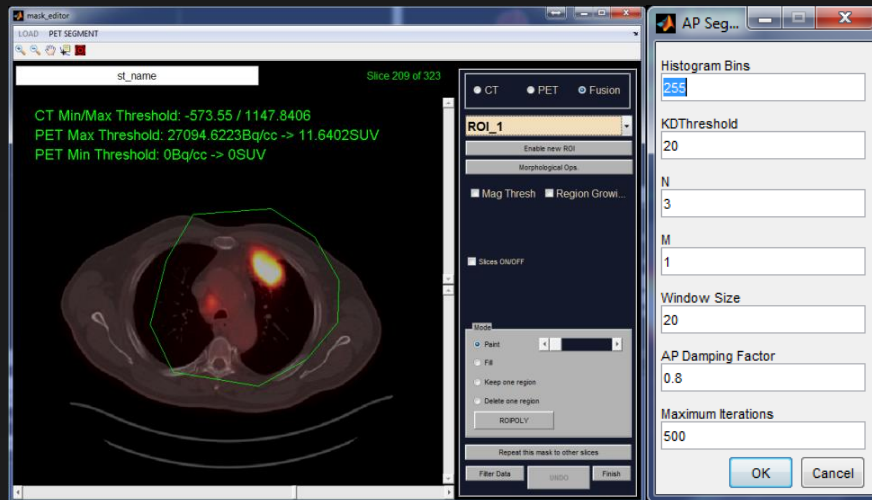
$$RC = \frac{\text{Activity concentration (measure)}}{\text{Real activity concentration}}$$





# Material and Methods

- Functional imaging processing

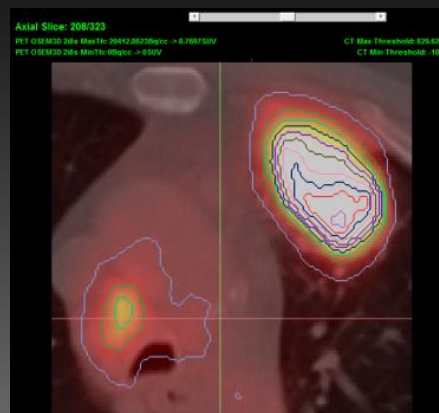


## SEGMENTATION ALGORITHM

(Foster et al., IEEE Trans Biomed Eng, 2014):

- Clustering according to SUV
- Based on affinity propagation
- Taking into account diffusion PET
- Reduction of uncertainties

Dose prescription map generation



	Structure	Vol (cm <sup>3</sup> )	Average SUV	Prescription Dose
1	ST_by_AP_Segmentation_2	17.5552	4.0544	0
2	ST_by_AP_Segmentation_3	8.8234	5.4744	66
3	ST_by_AP_Segmentation_4	6.1111	6.8982	67.2961
4	ST_by_AP_Segmentation_5	5.8823	8.3578	68.6247
5	ST_by_AP_Segmentation_6	6.0196	9.8687	70
6	ST_by_AP_Segmentation_7	4.4403	11.3754	71.3715
7	ST_by_AP_Segmentation_8	3.5248	12.8997	72.7590
8	ST_by_AP_Segmentation_9	2.0599	14.3269	74.0581
9	ST_by_AP_Segmentation_10	0.4120	15.7546	75.3577

$$D_i = D_{low} + \frac{S_i - S_{low}}{S_{high} - S_{low}} (D_{high} - D_{low}), \quad \text{for } S_{low} \leq S_i \leq S_{high}, i = 1, \dots, N$$



# Material and Methods

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- Inverse planning
- Generation of apertures based on the image:

**BIOMAP**

MU weighting  
(Voxel level constraints)

Robust optimization  
based on Linear  
Programming (LP)

Dose Calculation

As accurate as possible → **Full Monte Carlo planning**



# Material and Methods

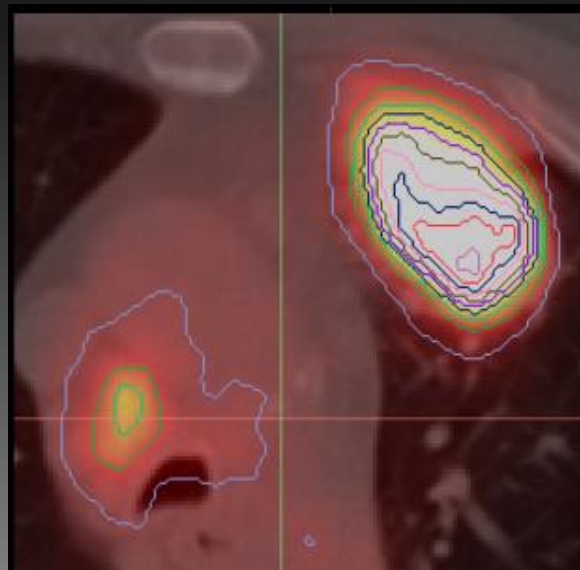
- Optimization: Segmentation and sequencing

## Dose Painting By Contours

- Conventional distribution of prescription doses
- Weight optimization: Dose-volume restrictions
- Two planning options:

**INVERSE PLANNING**

**CONTOURS**



**PLANNING BASED ON  
DIRECT APERTURES**

**BIOMAP** algorithm

*Ureba et al., Med Phys, 2014*



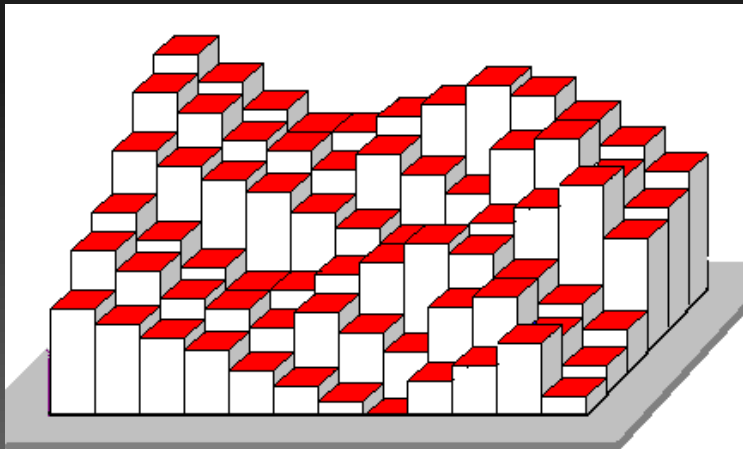
# Material and Methods

- Optimization: Segmentation and sequencing

## BIOMAP algorithm

*Ureba et al., Med Phys, 2014*

- Based on matrix generation
- Morphological and functional information recruitment



**Biophysical maps**

BIOMAP algorithm

$$(\alpha_k^l, \beta_k^m, \gamma_k^r)$$

$$A_k^l, C_k^r, D_k^{l,r}$$

$$(\lambda_k^l, \omega_k^r, \tau_k^{r,l})$$



Biophysical maps



# Material and Methods

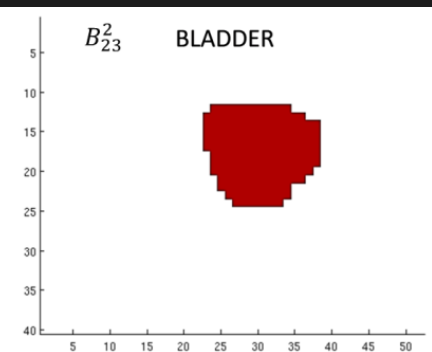
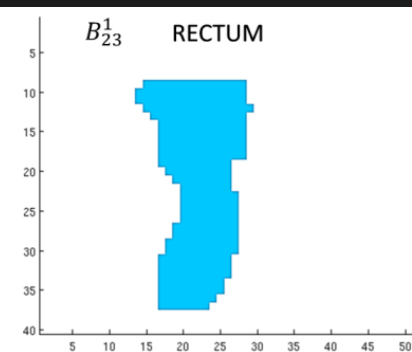
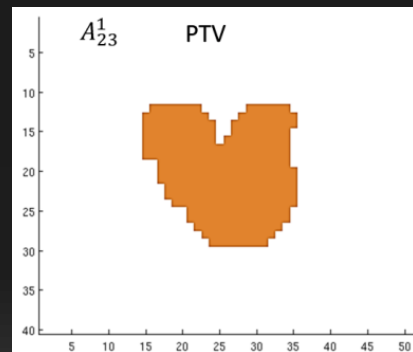
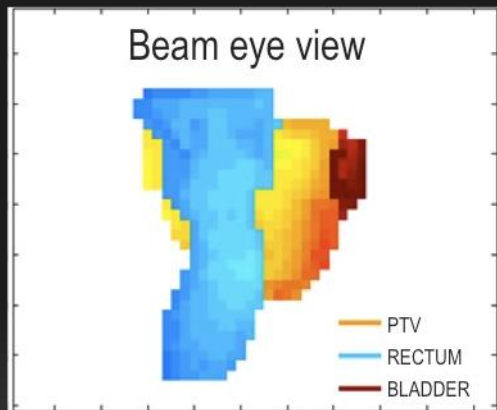
- Optimization: Segmentation and sequencing

## BIOMAP algorithm

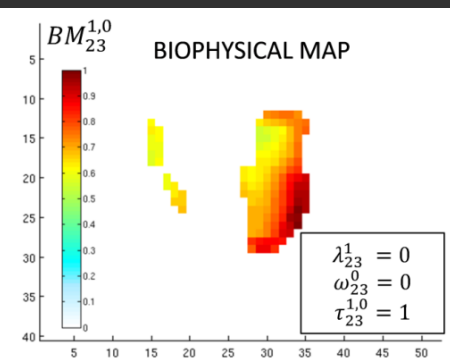
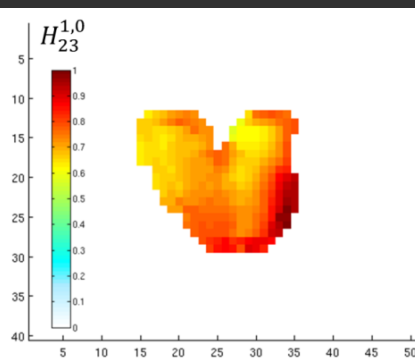
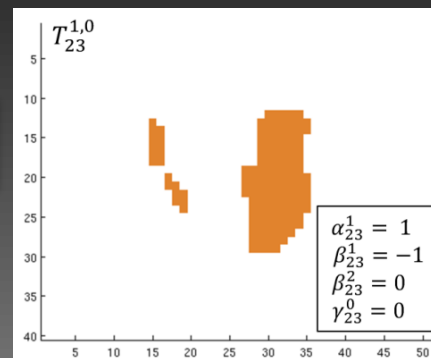
*Ureba et al., Med Phys, 2014*

Based on morphological and functional images:

## Adaptive radiation therapy



## Biophysical maps







# Material and Methods

- Optimization: Segmentation and sequencing

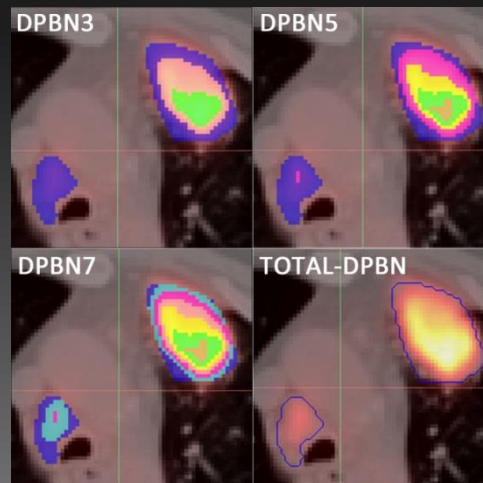
## Dose Painting By Numbers

- Heterogeneous distribution of prescription doses
- Weights optimization: dose-voxel restrictions
- Two planning options

### INVERSE PLANNING

- LP optimization of beamlets fluence
- Segmentation and sequencing
- 2nd LP optimization of apertures

### CLUSTERING



*Jiménez-Ortega et al., Phys Med, 2017*

### PLANNING BASED ON DIRECT APERTURES

#### BIOMAP algorithm

*Ureba et al., Med Phys, 2014*

Clusters for apertures generation



# Material and Methods

## PLANNING PROCESS

Functional image processing

Reconstruction protocols and uncertainty assessment

Optimization

Segmentation and Sequencing  
(DPBC / DPBN)

- Inverse planning
- Generation of apertures  
based on the image:

**BIOMAP**

MU weighting  
(Voxel level constraints)

Robust optimization  
based on Linear  
Programming (LP)

Dose Calculation

As accurate as possible → **Full Monte Carlo planning**



# Material and Methods

- Optimization: Monitor Units Weighting

$$\begin{aligned}
 \text{o.f. } & \sum_{i=1}^{N_{org}} P_i \sum_{j=1}^{N_{vox}^i} x_j^i + \sum_{i=1}^{N_{org}} Q_i \sum_{j=1}^{N_{vox}^i} y_j^i \\
 \text{subject to } & \sum_{j=1}^{N_{total\ beamlets}} \omega_j B_{kj} - x_k^i \leq D_k^i \quad k = 1, \dots, N_{vox} \\
 & \sum_{j=1}^{N_{total\ beamlets}} \omega_j B_{kj} + y_k^i \leq d_k^i \quad i = 1, \dots, N_{org}
 \end{aligned}$$

*Ureba et al., Med Phys, 2014*

## LINEAR PROGRAMMING (LP) OPTIMIZATION

Simplification of the problem by random selection of voxels

Dose constraints at the voxel level, rather than volumes



**TRUE DPBN option**



# Material and Methods

- Optimization: Monitor Units Weighting

$$\min \text{ o.f.} \equiv P_{\text{target}}^{\max} \sum_{i=1}^{N_{\text{target}}} x_i + P_{\text{target}}^{\min} \sum_{i=1}^{N_{\text{target}}} y_i + P_{\text{OAR}}^{\max} \sum_{i=N_{\text{target}}+1}^N x_i$$

sujeto a

$$\sum_{j=1}^M \omega_j d_{ij} - x_i \leq D_i^{\max} \Delta_i \quad i = 1, \dots, N_{\text{target}}$$

$$\sum_{j=1}^M \omega_j d_{ij} + y_i \geq D_i^{\min} \Delta_i \quad i = 1, \dots, N_{\text{target}}$$

$$\sum_{j=1}^M \omega_j d_{ij} - x_i \leq D_{\text{OAR}}^{\max} \quad i = N_{\text{target}} + 1, \dots, N$$

$$x_i, y_i, \omega_j \geq 0 \quad \forall i, j$$

*Jiménez-Ortega et al., Phys Med, 2017*

## LINEAR PROGRAMMING (LP) OPTIMIZATION

Simplification of the problem by random selection of voxels

Dose constraints at the voxel level, rather than volumes



**TRUE DPBN option**

## ROBUST OPTIMIZATION

- Image uncertainties (dose prescription)
- Geometric uncertainties (positioning / movement)

**VOXEL LEVEL**



# Material and Methods

## PLANNING PROCESS

Functional image processing

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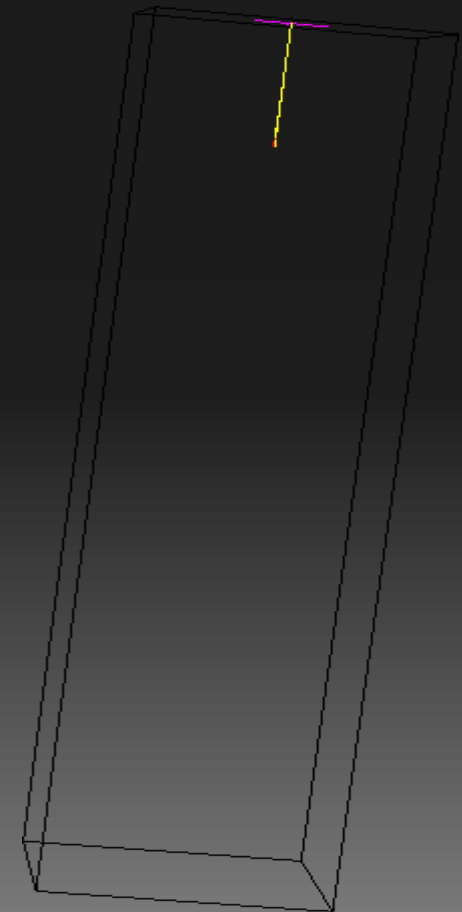
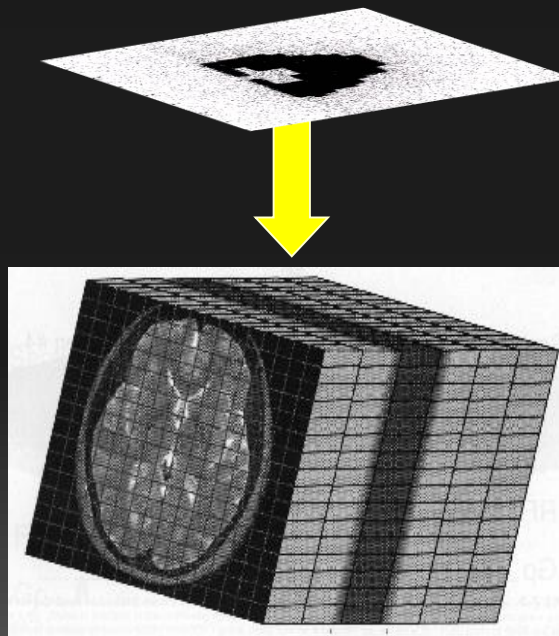
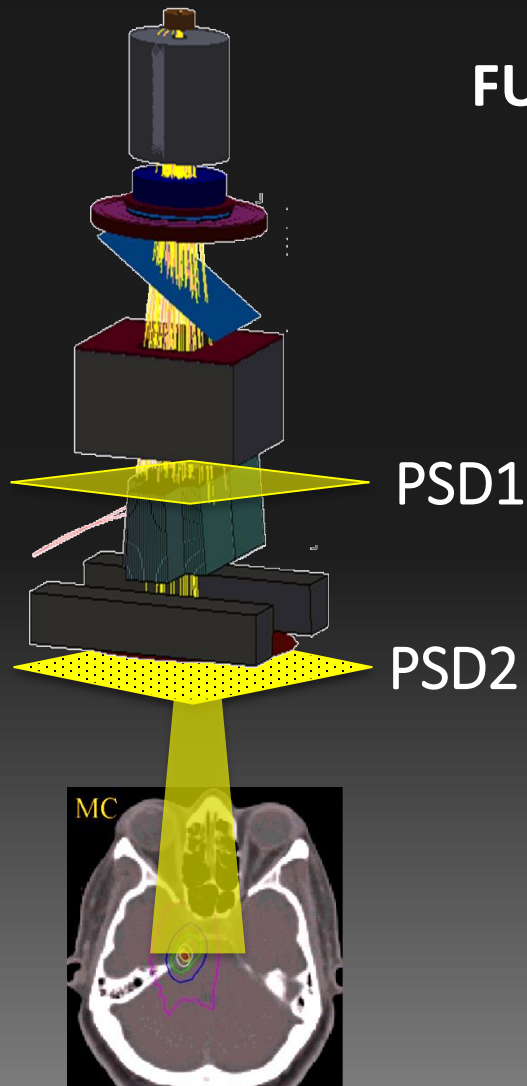




# Material and Methods

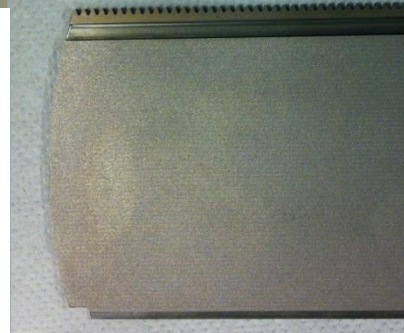
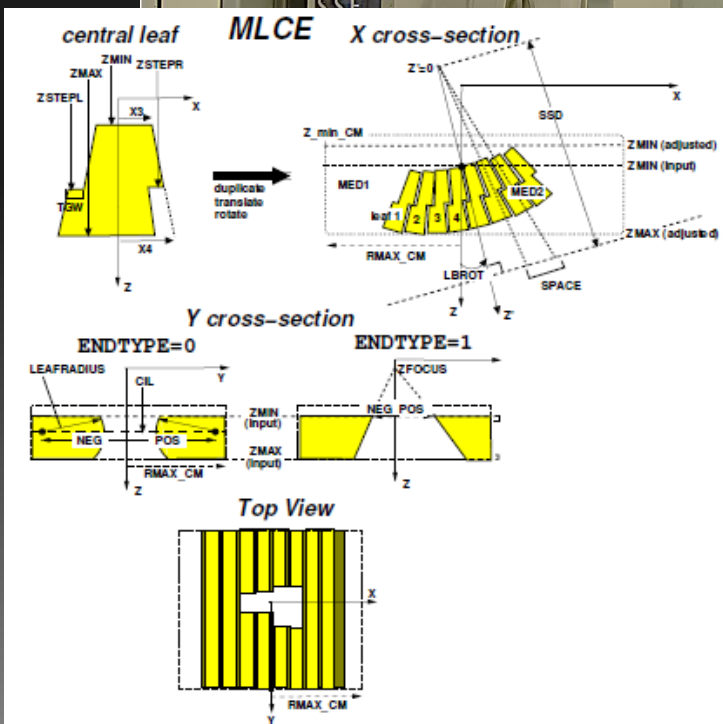
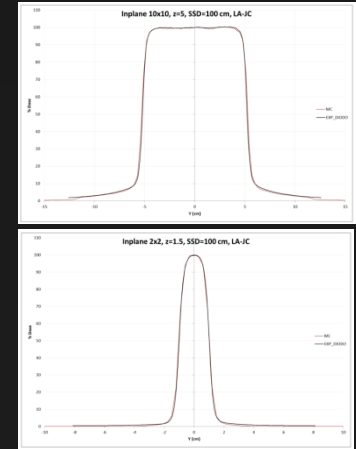
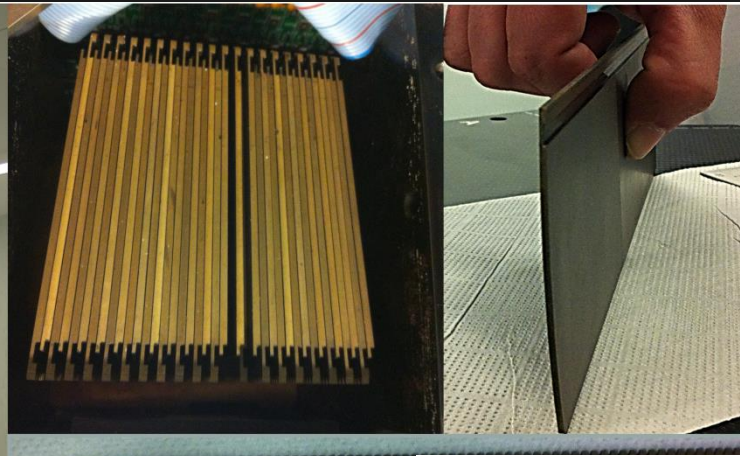
- Dose Calculation

## FULL MONTE CARLO PLANNING

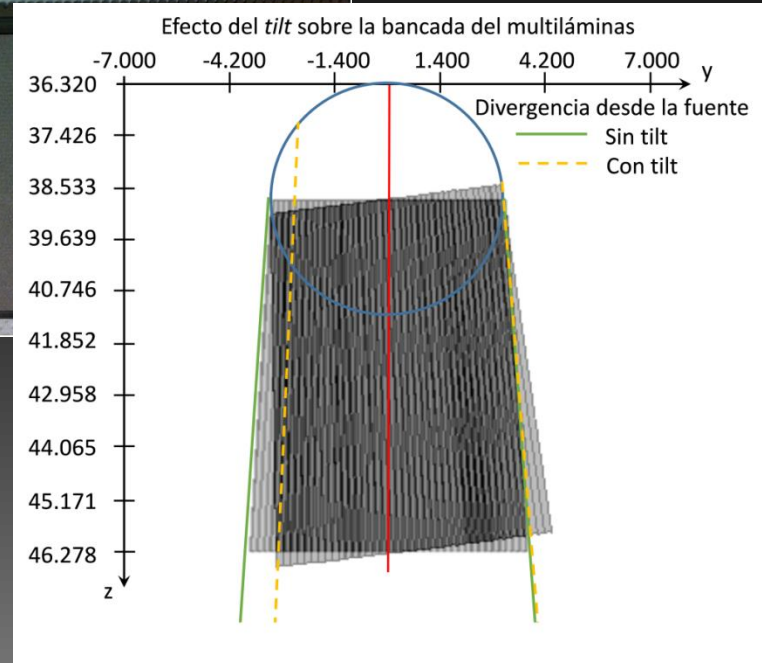




# Material and Methods



**EXPLICIT  
TRANSPORT  
OF  
PARTICLES**





# Material and Methods

- Dose Calculation

**EGSnrc/DOSXYZnrc/BEAMDOSE**

- Linac head: BEAMnrc (*Rogers et al., 2011; Walters et al., 2009*)
- CT patient: BEAMDOSE (*Salguero Castaño, 2008*)
- Parallel Computing (*Leal et al., 2004b; Leal et al., 2001b*)



HP ProLiant DL585 G7  
Performance 4 processors  
Opteron 2.2 GHz with 12 nodes





# Material and Methods

- Dose Calculation: Evaluation

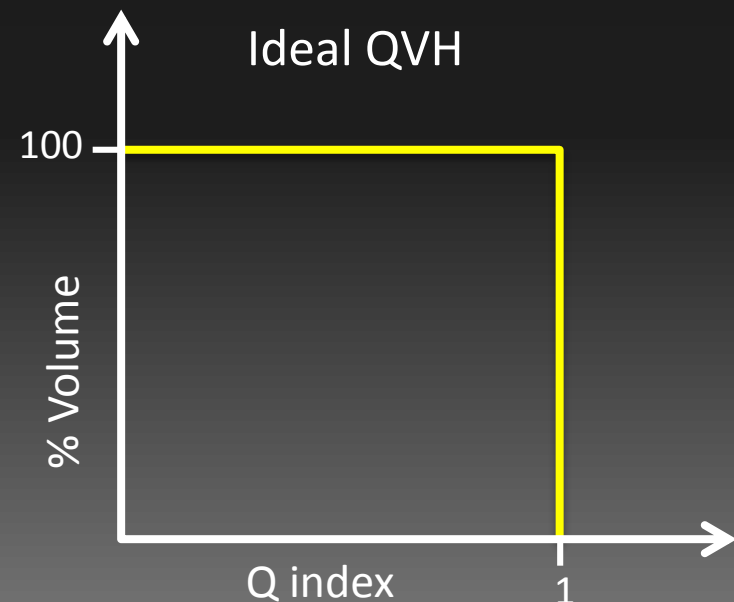
## Dose Painting By Numbers

NEW EVALUATION

Quality index per voxel ( $Q$ )  $\rightarrow$  QVH

$$Q = \frac{\text{Planned dose matrix}}{\text{Prescribed dose matrix}}$$

$Q_{q_1-q_2}$   
= percentage of  $Q$  values  
between  $q_1$  and  $q_2$





# Material and Methods

## ROBUSTNESS

### CONSIDERATION OF SYSTEMATIC AND RANDOM ERRORS FOR CLINICAL IMPLEMENTATION

#### Image processing

- Reconstruction protocol: EARL / Radiotherapy
- Segmentation algorithm (Affinity propagation clustering by Foster)

#### LP Robust Optimisation

$$\begin{aligned} \min \quad & o.f. \equiv P_{target}^{max} \sum_{i=1}^{N_{target}} x_i + P_{target}^{min} \sum_{i=1}^{N_{target}} y_i + P_{OAR}^{max} \sum_{i=N_{target}+1}^N x_i \\ \text{subject to} \quad & \sum_{j=1}^M \omega_j d_{ij} - x_i \leq D_i^{max} \Delta_i \quad i = 1, \dots, N_{target} \\ & \sum_{j=1}^M \omega_j d_{ij} + y_i \geq D_i^{min} \Delta_i \quad i = 1, \dots, N_{target} \\ & \sum_{j=1}^M \omega_j d_{ij} - x_i \leq D_{OAR}^{max} \quad i = N_{target} + 1, \dots, N \\ & x_i, y_i, \omega_j \geq 0 \quad \forall i, j \end{aligned}$$

Voxel uncertainty

- Dose prescription
- Geometric uncertainties

#### Full Monte Carlo

- Statistical errors in dose calculation (parallelized framework)
- Adaptive anisotropic diffusion filtering (and others)

#### Evaluation of results

$D$  = MC dose ( $\Delta D$  statistical error)

$D_p$  = Prescribed dose ( $\Delta D_p$  systematic error)

$$Q(D, D_p) = \frac{D}{D_p};$$

$$\Delta Q(D, D_p) = \sqrt{\left(\frac{\partial Q}{\partial D}\right)^2 (\Delta D)^2 + \left(\frac{\partial Q}{\partial D_p}\right)^2 (\Delta D_p)^2}$$

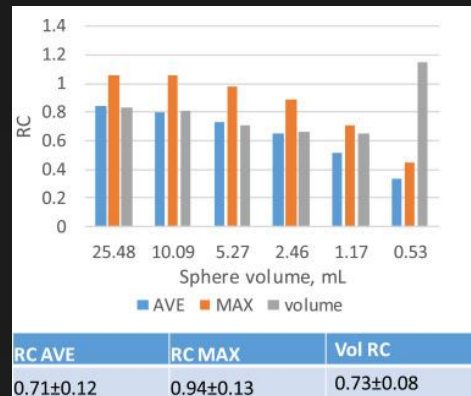




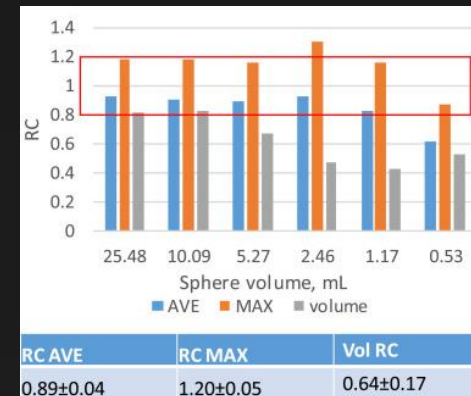
# Results

- Functional imaging processing

## EARL

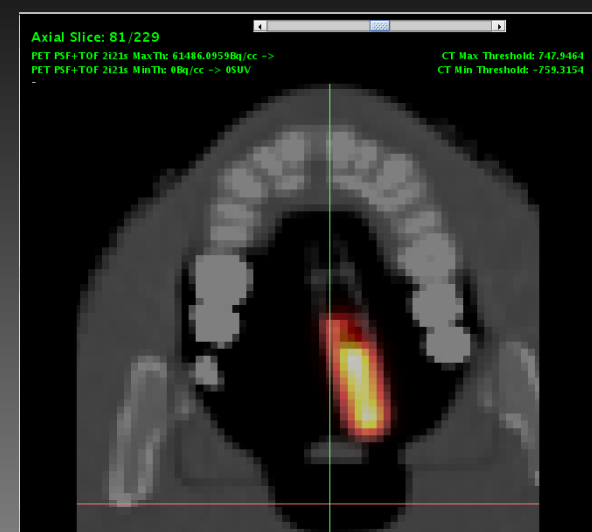
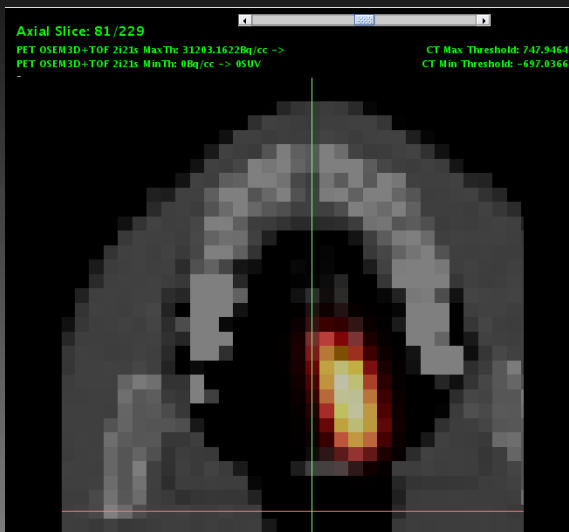


## RADIOTHERAPY



Balcerzyk et al., Nuclear Instruments and Methods A, 2017

Study of uncertainties  
in SUV values





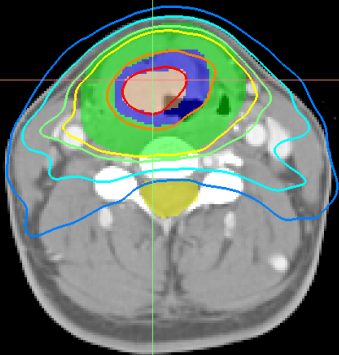
# Results

## DPBC

### BIOMAP

Isolines

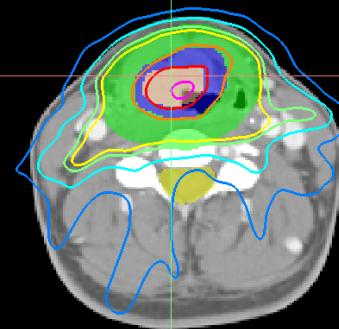
147  
137  
120  
100  
90  
63  
40



### INVERSE

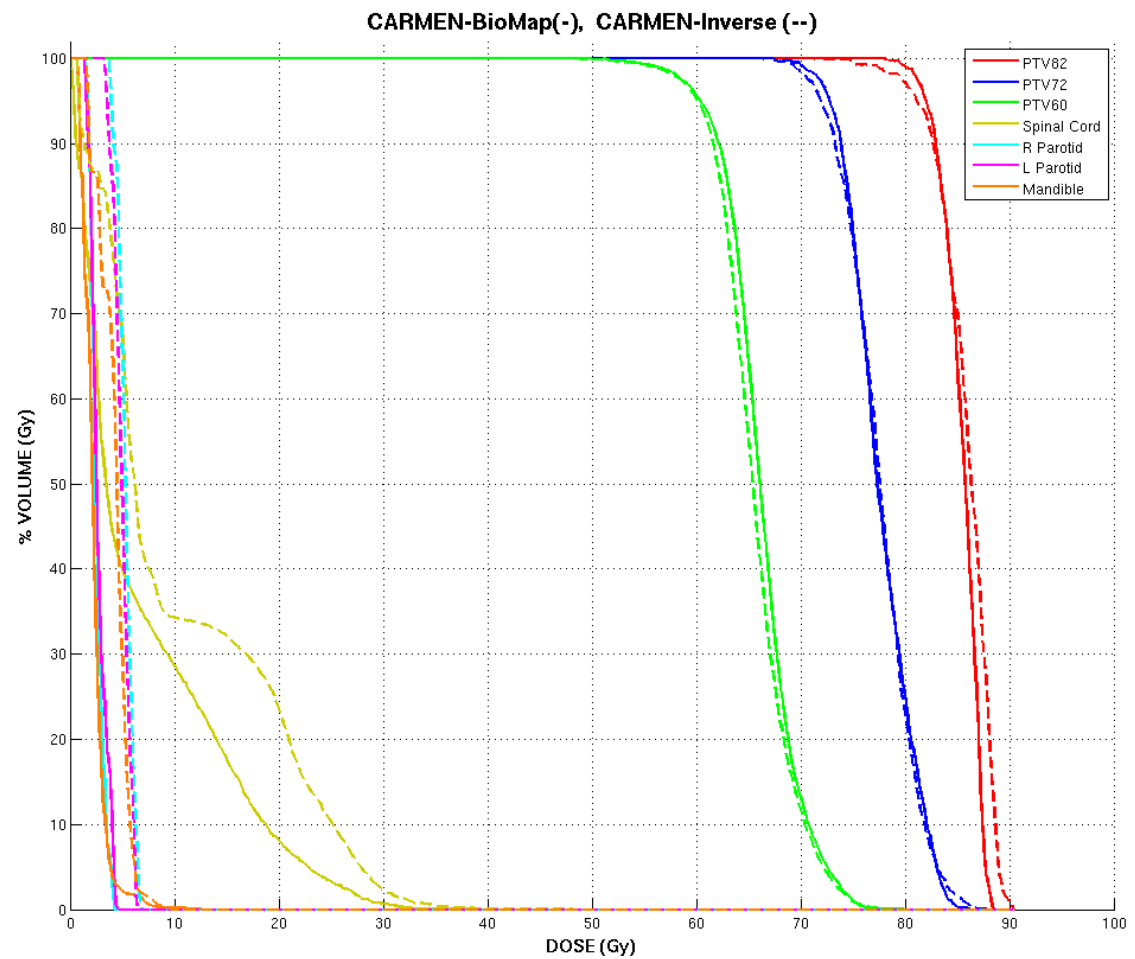
Isolines

147  
137  
120  
100  
90  
63  
40



## CARMEN: BIOMAP vs Inverse planning

## DVH





# Results

**DPBN**

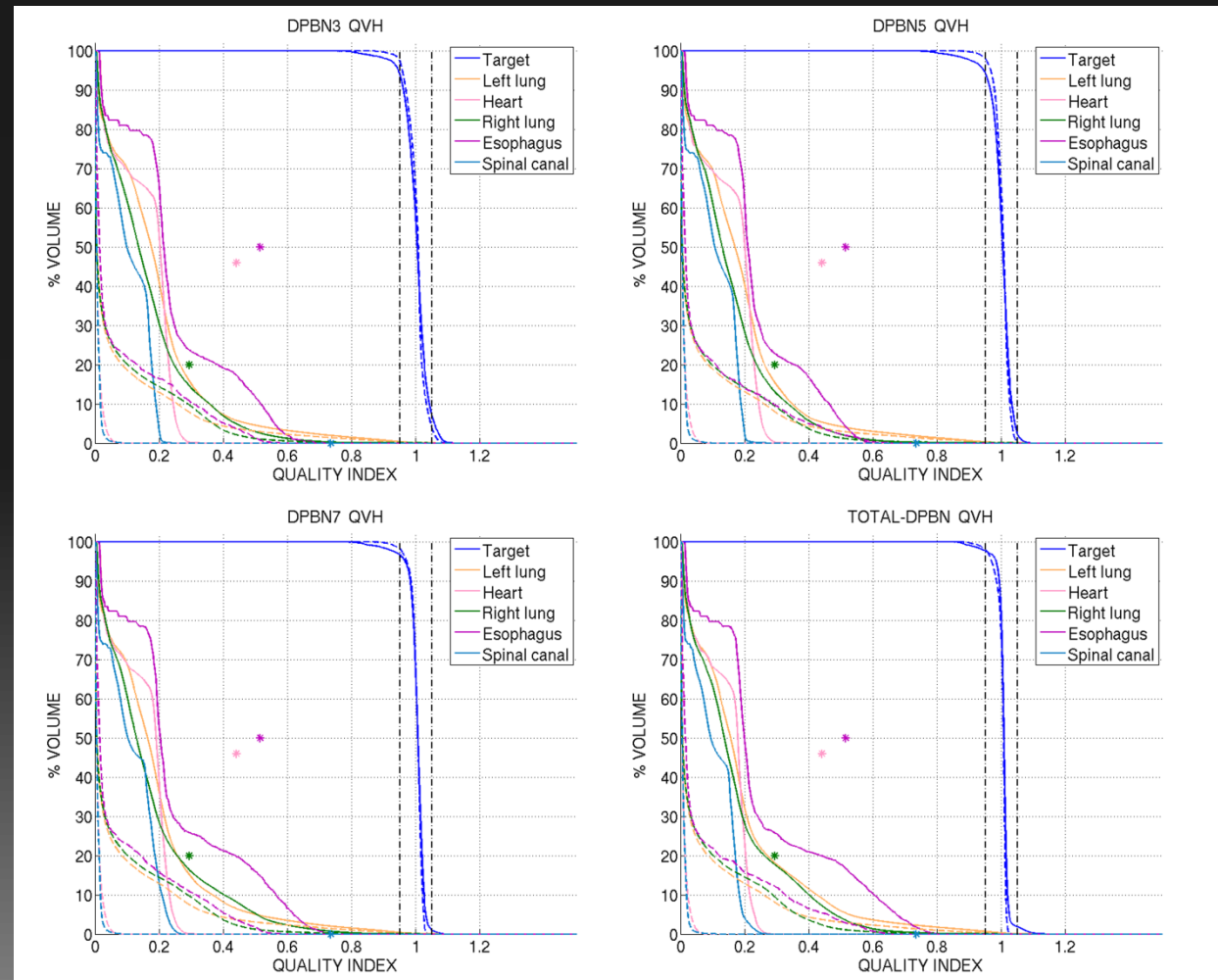
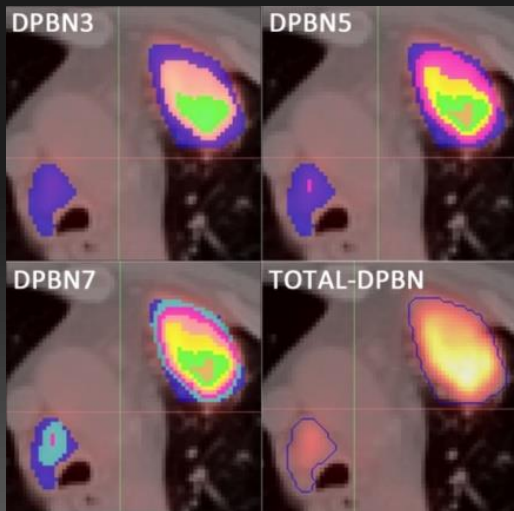
**CARMEN: Inverse planning (IMRT)**

**QVH**

Apertures ———

Beamlets - - - -

Elekta Axesse  
(leaves: 4mm)



*Jiménez-Ortega et al.,  
Phys Med, 2017*

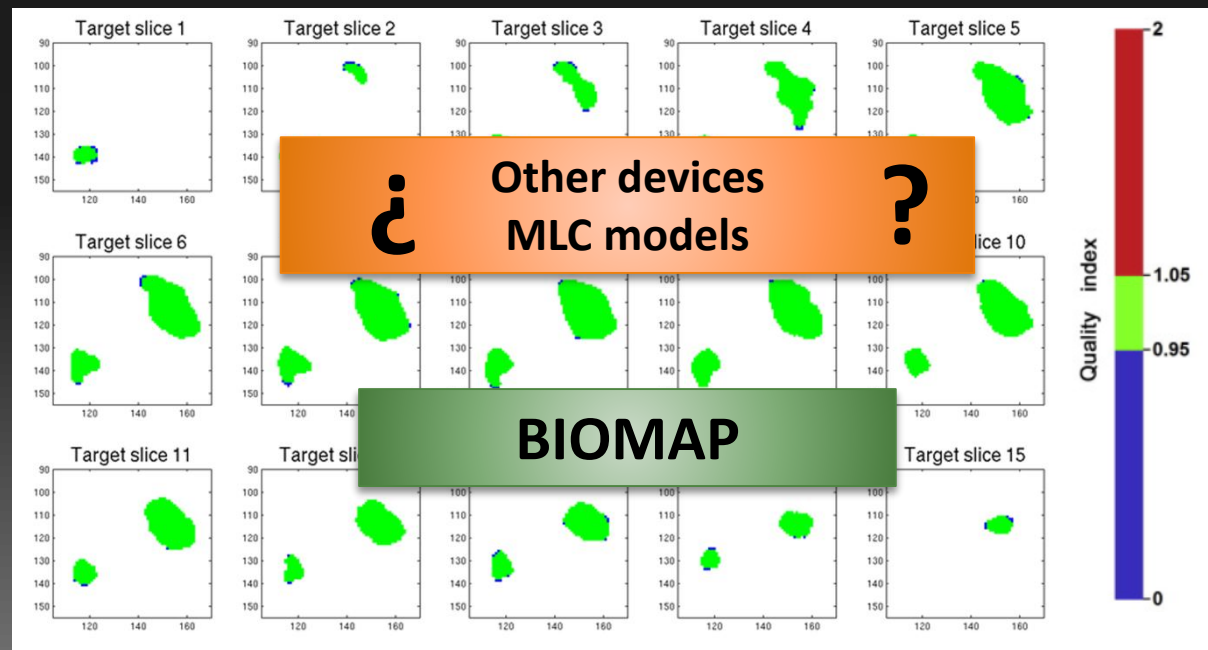
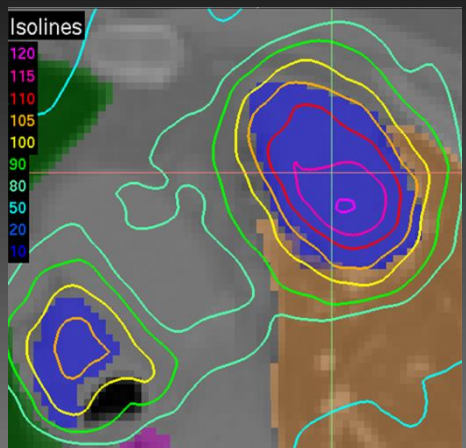
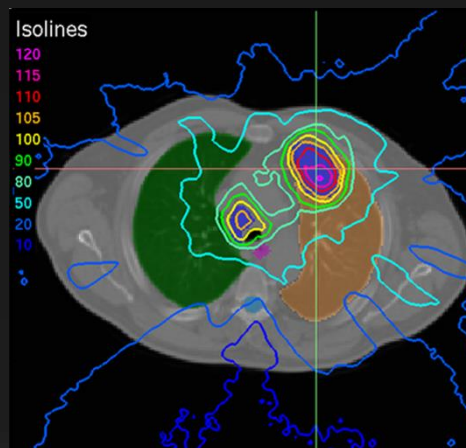


# Results

## DPBN

## CARMEN: Inverse planning (IMRT)

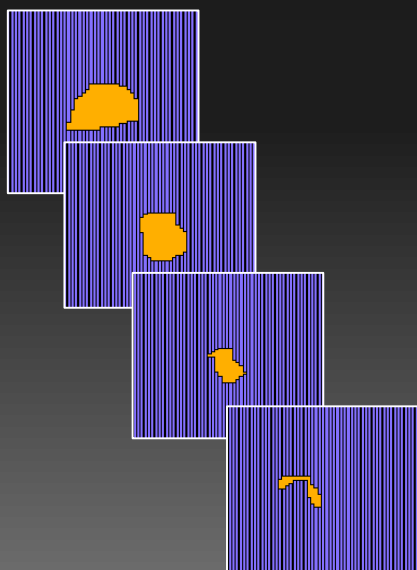
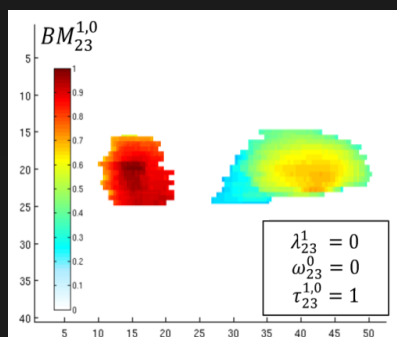
Study	$Q_{0.95-1.05}$ (beamlets)	$Q_{0.95-1.05}$ (segments)	Segments number	MU/fraction
DPBN3	93.3%	86.9%	235	2337
DPBN5	97.7%	91.8%	235	2286
DPBN7	98.1%	95.6%	291	2157
<b>TOTAL-DPBN</b>	<b>97.8%</b>	<b>95.7%</b>	<b>351</b>	<b>2057</b>





# Results

**DPBN**

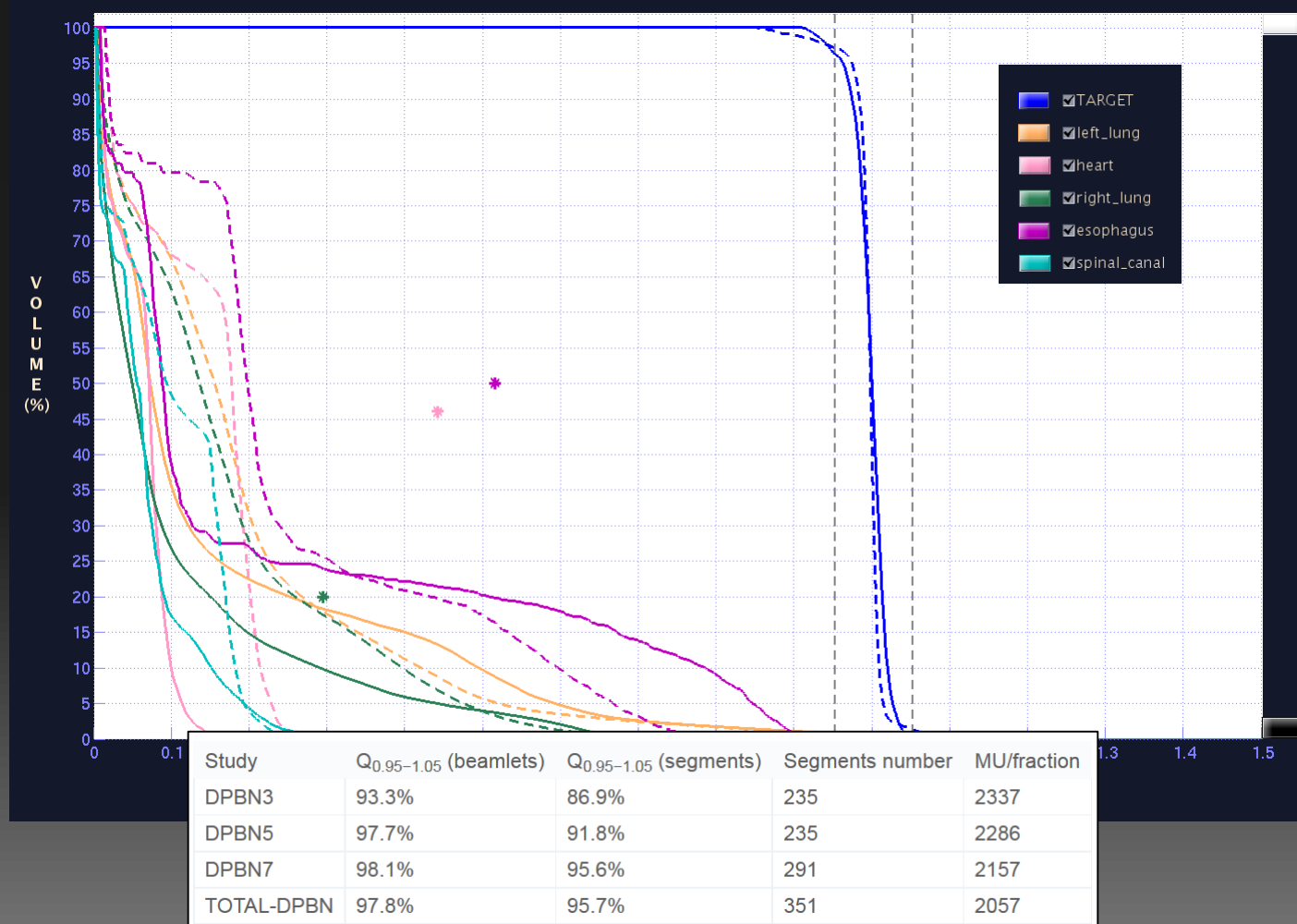


## BIOMAP Algorithm and Robust LP Optimization

**QVH**

**BIOMAP**

**INVERSE**



**CLINICALLY ACCEPTABLE**

**BIOMAP**

**98.7%**

**63**

**699**

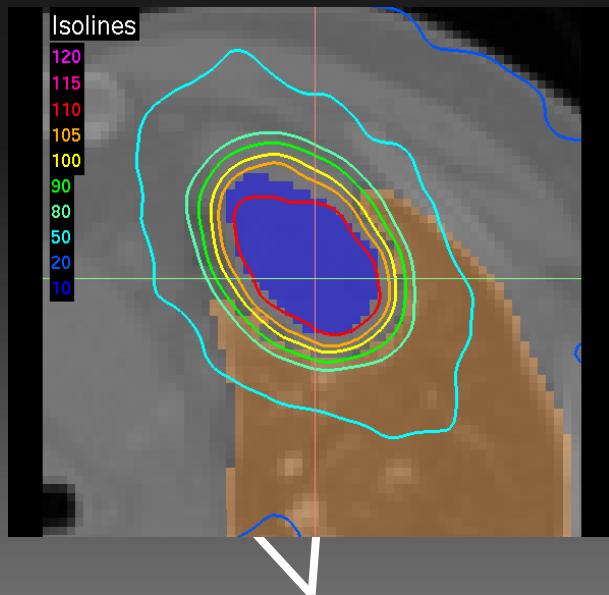




# Results

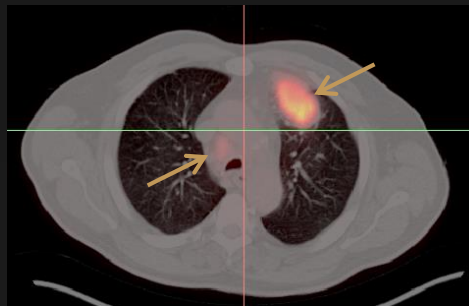
DPBN

Changes in images:  
New biological targets and  
dose prescription map

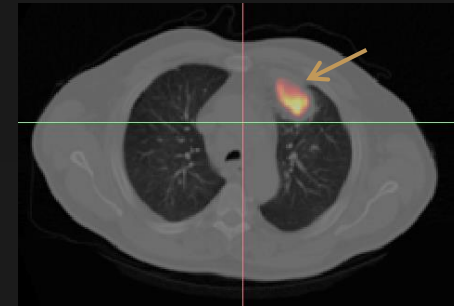


Normal tissue overdosage

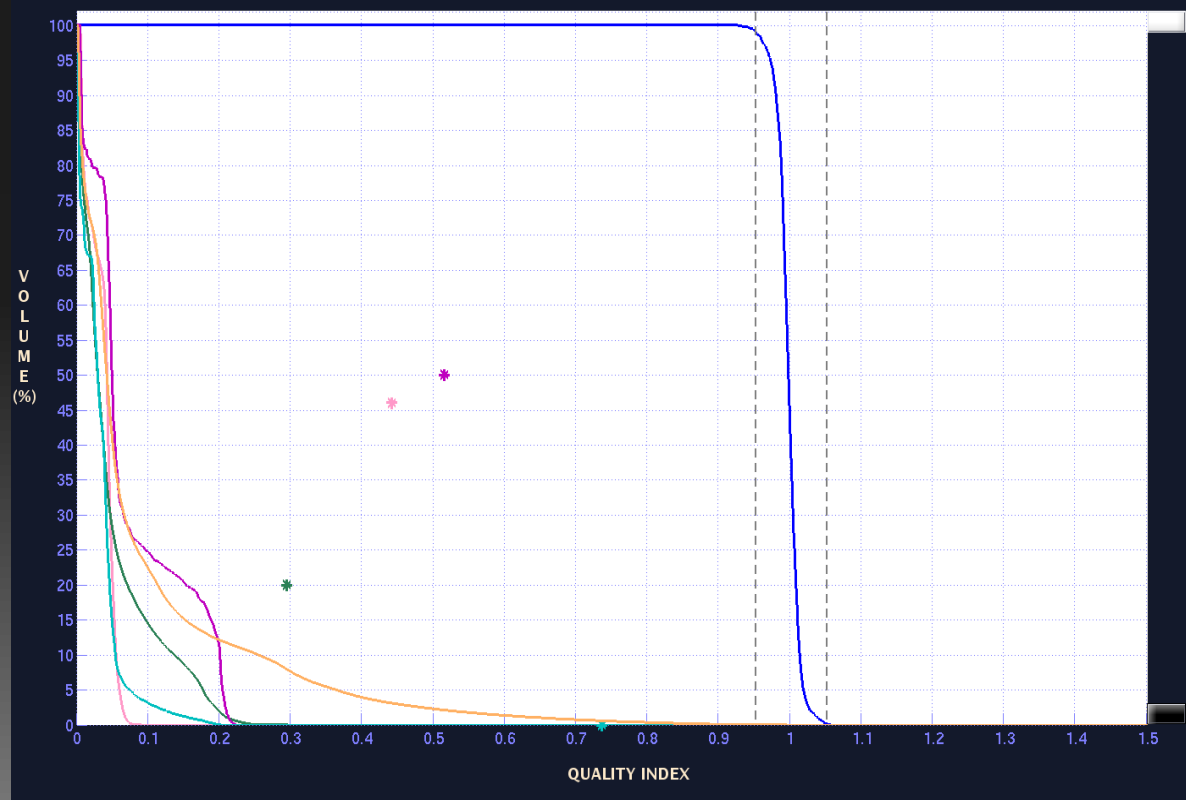
INITIAL PET



FOLLOW-UP PET



CONSEQUENCES OF NO ADAPTATION.





# Results

## DPBN

Adaptive RT by BIOMAP at the voxel level

VOXEL LEVEL:

DEFORMABLE REGISTRATION NOT NECESSARY

## TOTAL TREATMENT EVALUATION

$$Q_v = \sum_{i=1}^N f_i Q_v^i$$

$Q_v$ : Q index of voxel  $v$

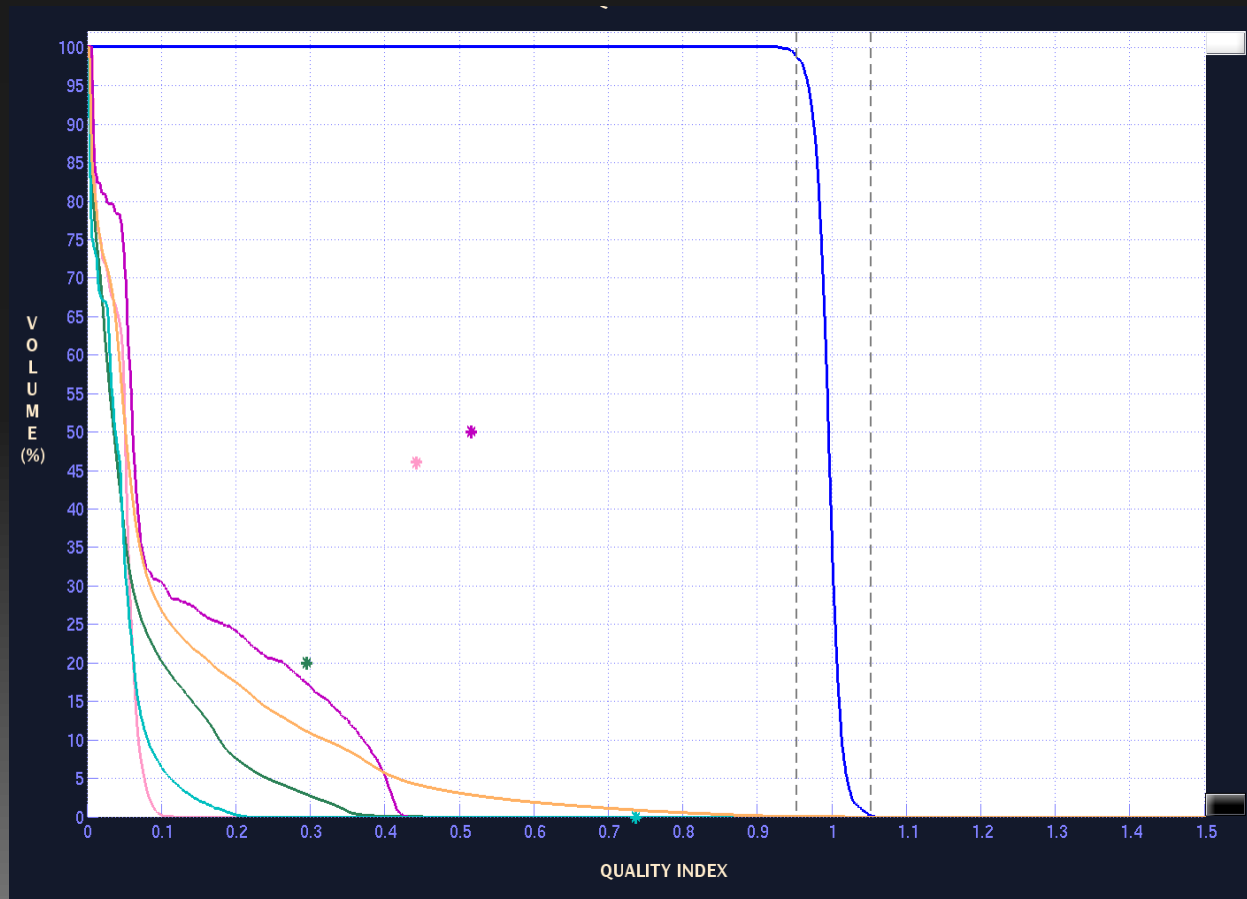
$f_i$ : fraction weight

$N$ : number of fractions

$Q_v^i$ : Q index of voxel  $v$  in fraction  $i$

$$Q_{0.95-1.05} = 98.9\%$$

$$Q_{0.97-1.03} = 96.2\%$$





## Conclusions

- In these conditions of **accuracy** and **robustness** (through fMC planning, LP-based optimization and BIOMAP algorithm), we feel confident to move our system for DPBN application into the clinical environment.
- The BIOMAP algorithm, based on the image information, allows the **adaptive** radiation therapy planning at voxel level.
- This solution can be easily extended to other types of functional information such as MRI.



# Thanks for your attention



## Unión Europea

Fondo Europeo  
de Desarrollo Regional  
Fondo Social Europeo



FISEVI 552 PIE 2012 LEAL PLAZA ANTONIO CTS-2482 G-MC 15/06/2016



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