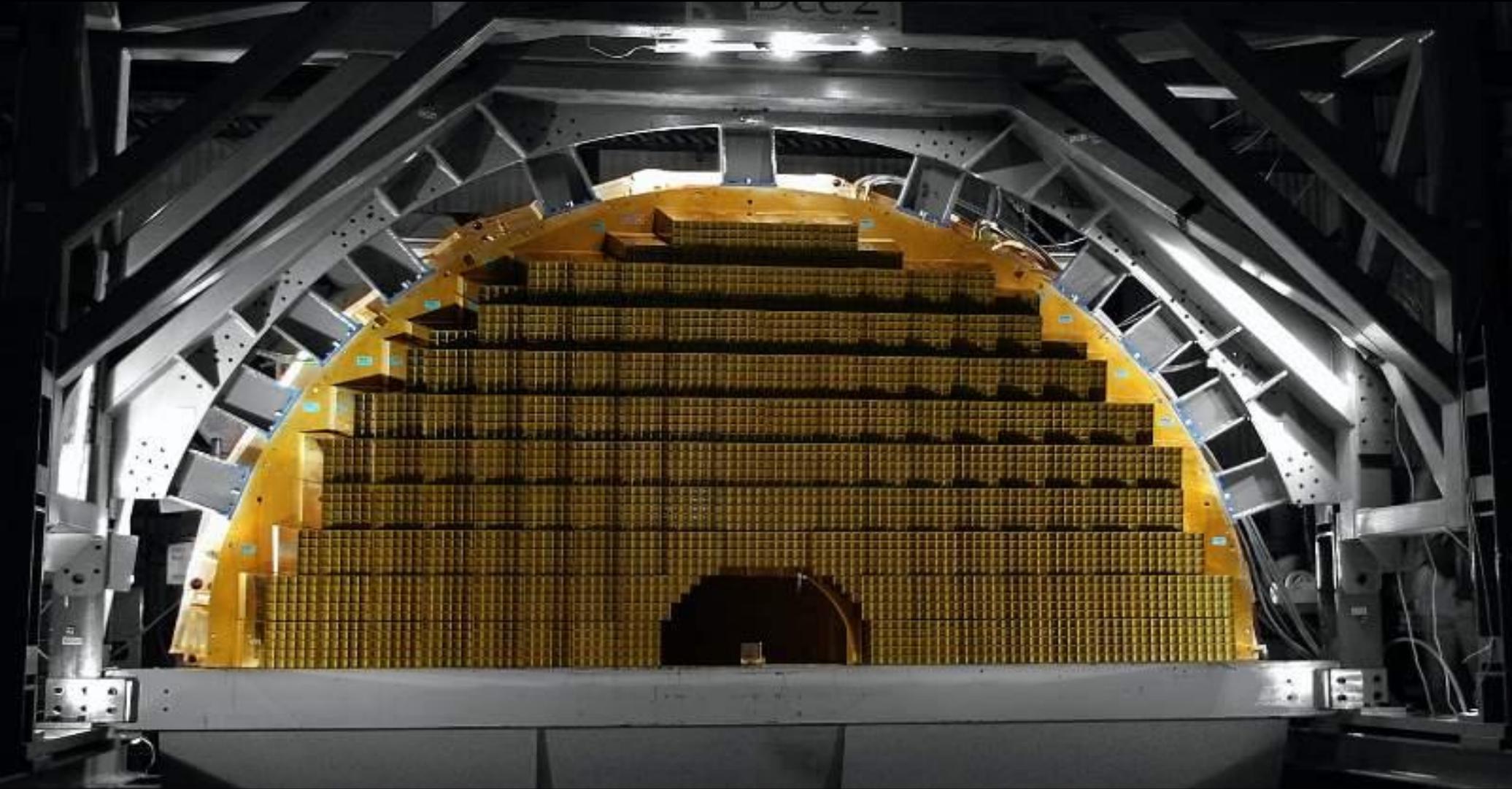


# Introduction to Calorimeters



- Introduction
- Electromagnetic Calorimetry
- Hadron Calorimetry
- Jets and Particle Flow
- Future directions in Calorimetry
- Summary

## Calorimetry

One of the most important and powerful detector techniques in experimental particle physics

### Two main categories of Calorimeter:

**Electromagnetic calorimeters** for the detection of

$e^\pm$  and neutral particles  $\gamma$

**Hadron calorimeters** for the detection of

$\pi^\pm, p^\pm, K^\pm$  and neutral particles  $n, K^0_L$

$\mu^\pm$  usually traverse the calorimeters losing small amounts of energy by ionisation

**The 13 particle types above completely dominate the particles from high energy collisions reaching and interacting with the calorimeters**

All other particles decay ~instantly, or in flight, usually within a few hundred microns from the collision, into one or more of the particles above

Neutrinos, and neutralinos,  $\chi^0$ , undetected but with **hermetic calorimetry** can be inferred from measurements of missing transverse energy in collider experiments

# Introduction

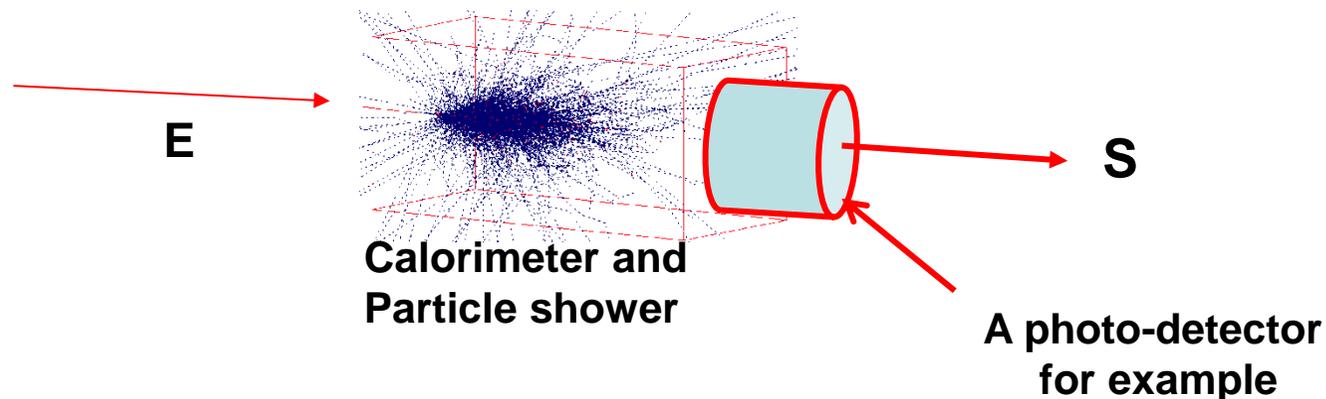
## Calorimeters

**Calorimeters designed to stop and fully contain their respective particles**  
**'End of the road' for the incoming particle**

**Measure** - **energy** of incoming particle(s) by total absorption in the calorimeter  
- **spatial location** of the energy deposit  
- (sometimes) **direction** of the incoming particle

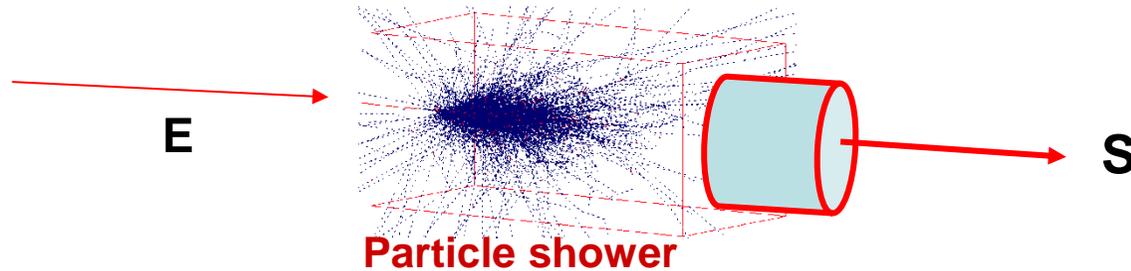
Convert energy  $E$  of the incident particle into a detector response  $S$

**Detector response**  $S \propto E$



# Introduction

Incoming particle  
(can be at O(TeV) at LHC)



## Calorimetry: basic mechanism

Energy lost by the formation of **electromagnetic** or **hadronic** cascades /showers in the material of the calorimeter

Many charged particles in the shower

The charged particles ionize or excite the calorimeter medium

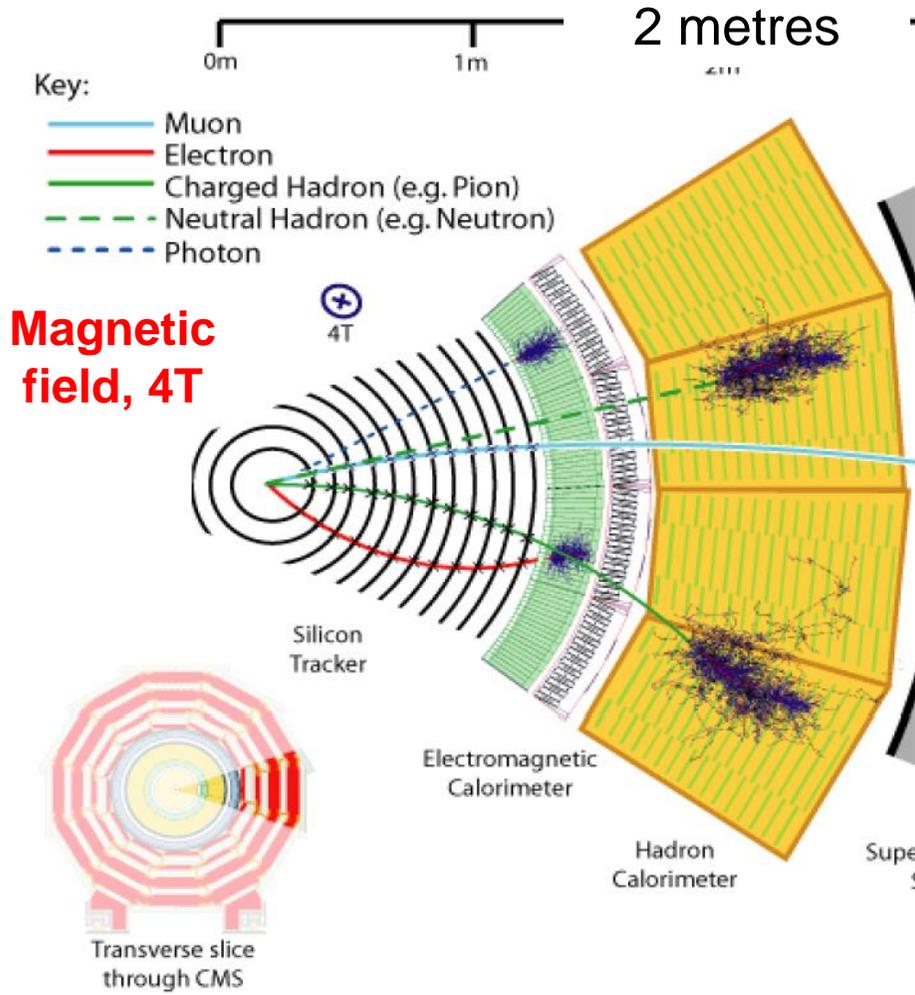
The ionisation or excitation can give rise to:

- The emission of visible photons, O(eV), via scintillation
- The release of ionisation electrons, O(eV)

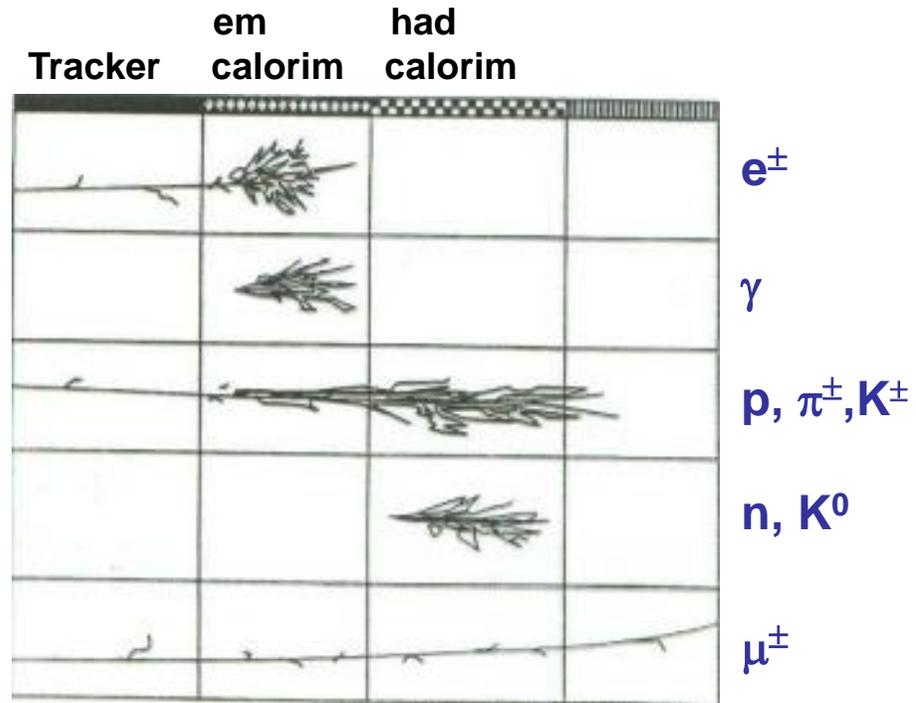
Photo-detectors or anodes/dynodes then detect these “quanta”

# Introduction

Where you STOP is what you ARE !!!



A 'wedge' end on view of the CMS experiment at the LHC



Get sign of charged particles from the Tracker

Tracker to be of minimum material to avoid losing particle energy before the calorimeters.

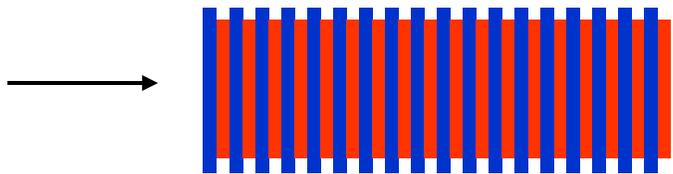
# Introduction

There are two general types of calorimeter design:

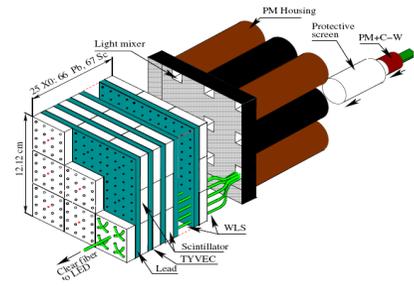
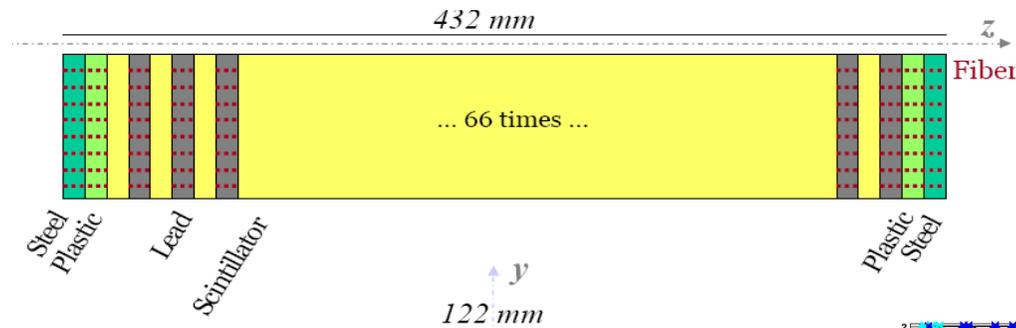
## 1) Sampling calorimeters

Layers of passive absorber (ie Pb or Cu) alternating with active detector layers such as plastic scintillator, liquid argon or silicon

- Only part of the energy is sampled
- Used for both electromagnetic and hadron calorimetry
- Cost effective



ATLAS ECAL & HCAL  
ALICE EMCAL  
CMS HCAL  
LHCb ECAL

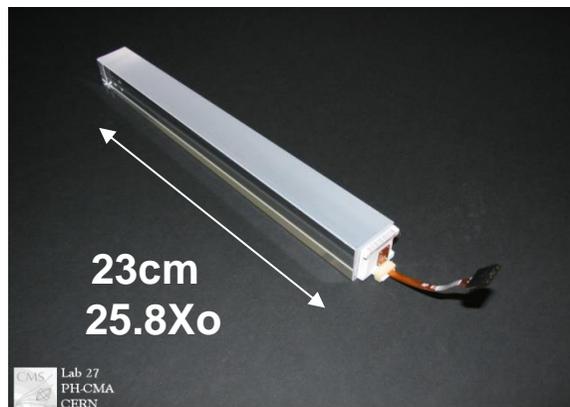
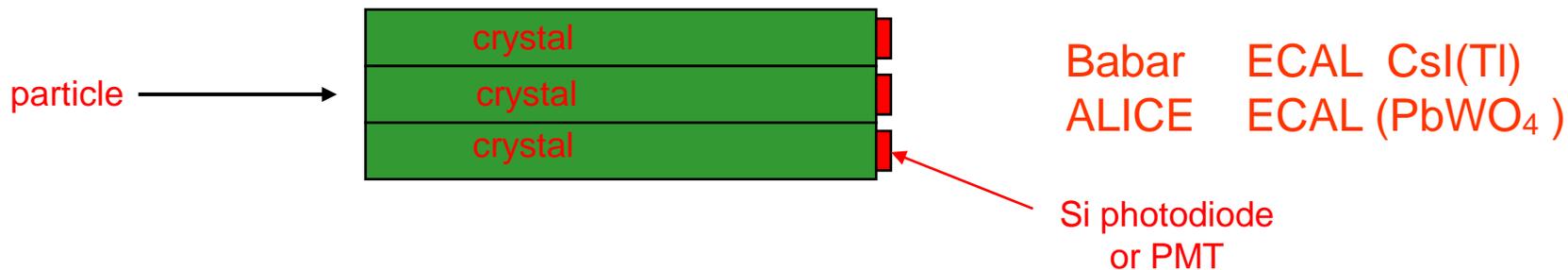


## 2) Homogeneous calorimeters

Single medium, both absorber and detector

- Liquified Ar/Xe/Kr
- Organic liquid scintillators, large volumes, Kamland, Borexino, Daya Bay
- Dense crystal scintillators: **PbWO<sub>4</sub>**, CsI(Tl), BGO and many others
- Lead loaded glass

Almost entirely for electromagnetic calorimetry



CMS ECAL (PbWO<sub>4</sub>)

## Electromagnetic Calorimetry

# Electromagnetic Cascades

## Electromagnetic cascades

- $e^\pm$  bremsstrahlung and photon pair production**

By far the most important processes for energy loss by electrons/positrons/photons with energies above 1 GeV  
Leads to an e.m. cascade or shower of particles

- Bremsstrahlung**

Characterised by a 'radiation length',  $X_0$ , in the absorbing medium over which an electron loses, on average, 63.2% of its energy by bremsstrahlung.

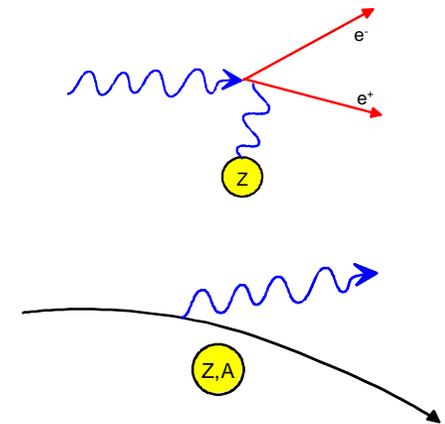
$$E = E_0 e^{-x/X_0} \quad \text{where} \quad -\frac{dE}{dx} = 4\alpha N_A \frac{Z^2}{A} r_e^2 E \ln \frac{183}{Z^{1/3}}$$

$$-\frac{dE}{dx} = \frac{E}{X_0}$$

$$X_0 = \frac{A}{4\alpha N_A Z^2 r_e^2 \ln \frac{183}{Z^{1/3}}}$$

$$X_0 \sim 180 A/Z^2 \text{ [g cm}^{-2}\text{]}$$

In Pb (Z=82)  $X_0 \sim 5.6 \text{ mm}$



$1/m_e^2$  dependence

$$-\frac{dE}{dx} \propto \frac{Z^2 E}{m_e^2}$$

Favours the use of high Z materials for a compact e.m. calorimeter

Due to the  $1/m^2$  dependence for bremsstrahlung, muons only emit significant bremsstrahlung above  $\sim 1 \text{ TeV}$  ( $m_\mu \sim 210 m_e$ )

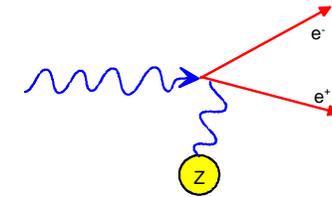
# Electromagnetic Cascades

## Pair production

Characteristic mean free path before pair production,  $\lambda_{\text{pair}} = 9/7 X_0$

$$E_\gamma \geq 2m_e c^2$$

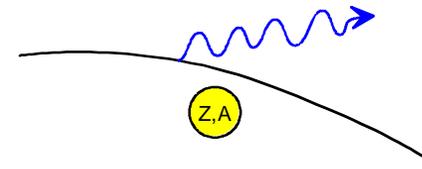
Intensity of a photon beam entering calorimeter reduced to  $1/e$  of the original intensity,  $I = I_0 \exp(-7/9 x/X_0)$ .  $\lambda_{\text{pair}} = 7.2 \text{ mm in Pb}$



Brem and pair production dominate the processes that degrade the incoming particle energy

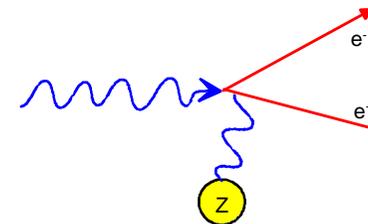
## 50 GeV electron

Loses 32 GeV over 1  $X_0$  by bremsstrahlung



## 50 GeV photon

Pair production to  $e^+ e^-$ , 25 GeV to each particle  
Energy regime degraded by 25 GeV



## Minimum ionising particle (m.i.p)

In Pb, over 1  $X_0$ , ionization loss  $\sim O(10s)$  of MeV  
Factor of  $\sim 1000$  less than the above

# Electromagnetic Cascades

Below a certain critical energy,  $E_c$  :

$e^\pm$  energy losses are greater through ionisation than bremsstrahlung

The multiplication process runs out

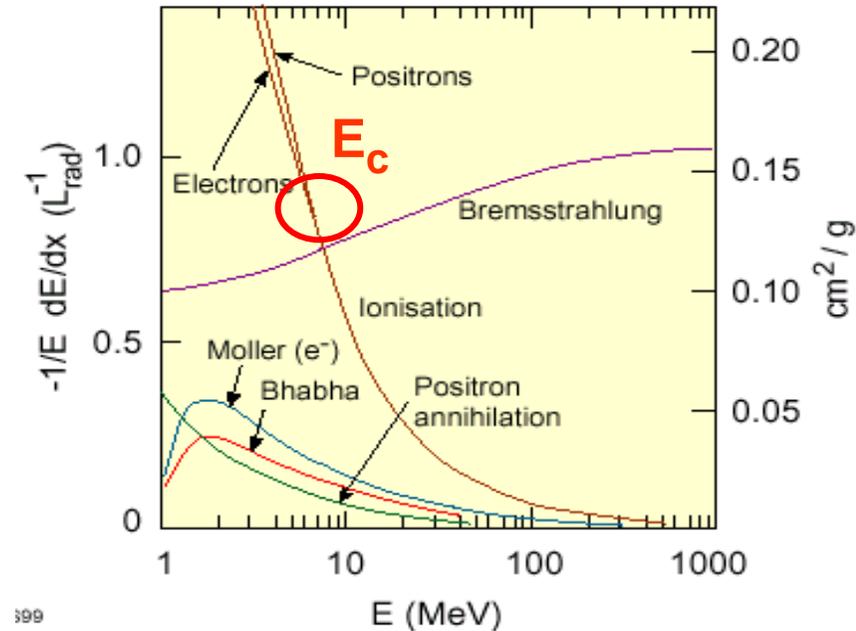
- Slow decrease in number of particles in the shower
- Electrons/positrons are stopped

Photons progressively lose energy by Compton scattering, converting to electrons via the photo-electric effect, and absorption

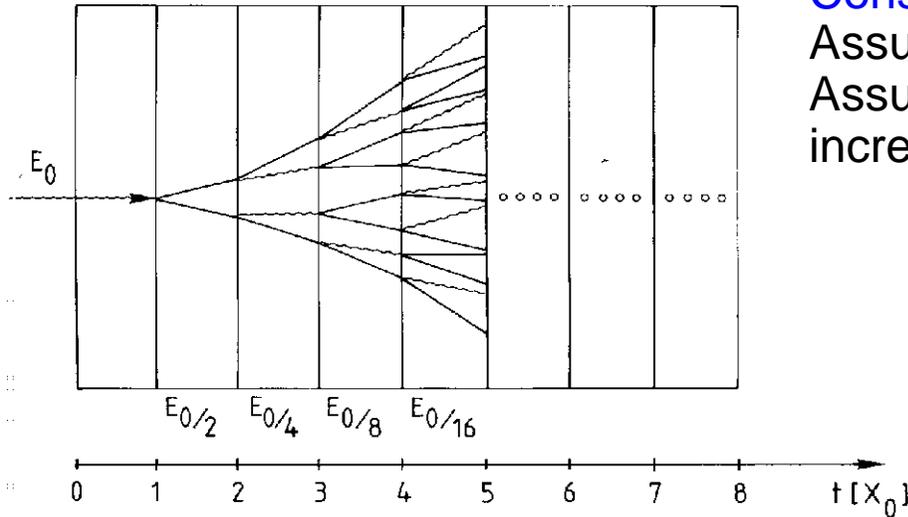
$$E_c \approx \frac{610 \text{ MeV}}{Z + 1.24} \quad \longrightarrow \quad \text{Pb (Z=82), } E_c = 7.3 \text{ MeV}$$

Liquids and solids

Fractional Energy Loss by Electrons



# EM Cascades: a simple model



Consider only Bremsstrahlung and pair production  
 Assume: Incident energy =  $E_0$ ,  $\lambda_{\text{pair}}$  and  $X_0$  are equal  
 Assume: after each  $X_0$ , the number of particles increases by factor 2

After ' $t$ ' layers, each of thickness  $X_0$ :

$$\text{Number of particles} = N(t) = 2^t$$

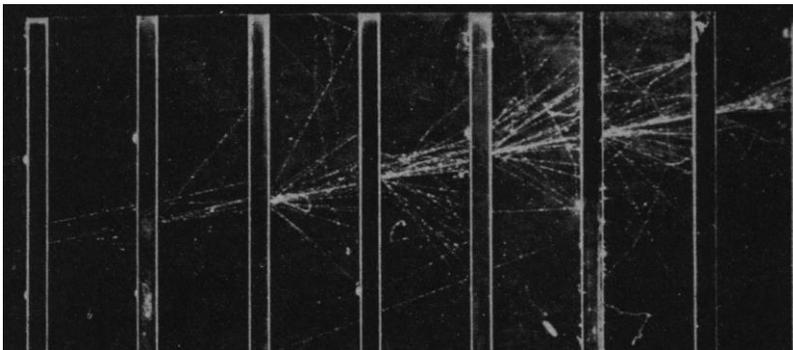
$$\text{Average energy per particle} = E(t) = E_0 / 2^t$$

Process continues until  $E(t) < E_c$

This layer contains the maximum number of particles:

$$t_{\text{max}} = \frac{\ln E_0 / E_c}{\ln 2}$$

$$N^{\text{total}} = \sum_{t=0}^{t_{\text{max}}} 2^t = 2^{(t_{\text{max}} + 1)} - 1 \approx 2 \cdot 2^{t_{\text{max}}} = 2 \frac{E_0}{E_c}$$



Electron shower in a cloud chamber with lead absorbers

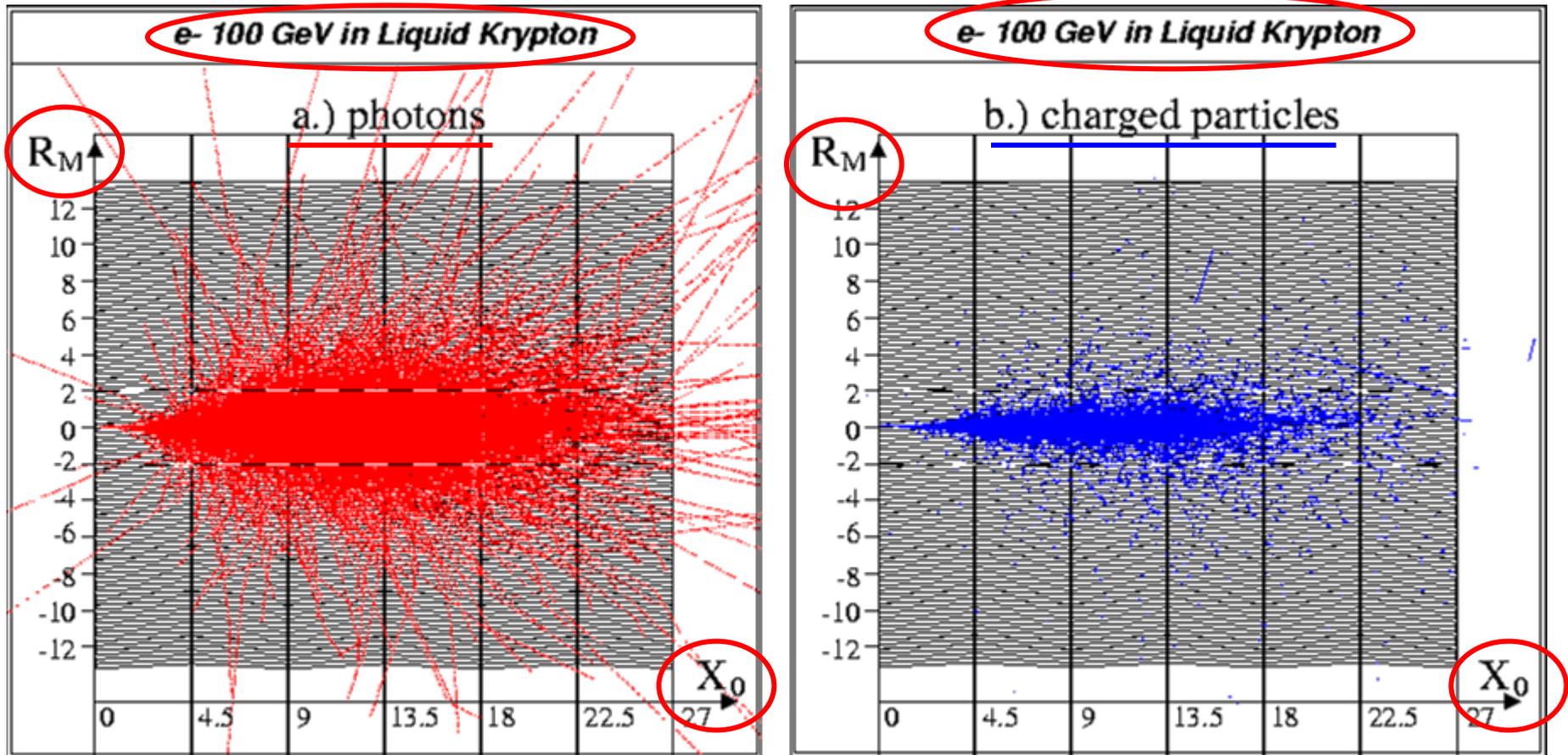
**For a 50 GeV electron on Pb**

**$N^{\text{total}} \sim 14000$  particles**

**$t_{\text{max}}$  at  $\sim 13 X_0$  (an overestimate)**

# EM Cascade Profiles

EM shower development in Krypton ( $Z=36$ ,  $A=84$ )



Photons created

Charged particles created

GEANT simulation: 100 GeV electron shower in the NA48 liquid Krypton calorimeter

# EM Cascade Profiles

## Longitudinal Shower Development

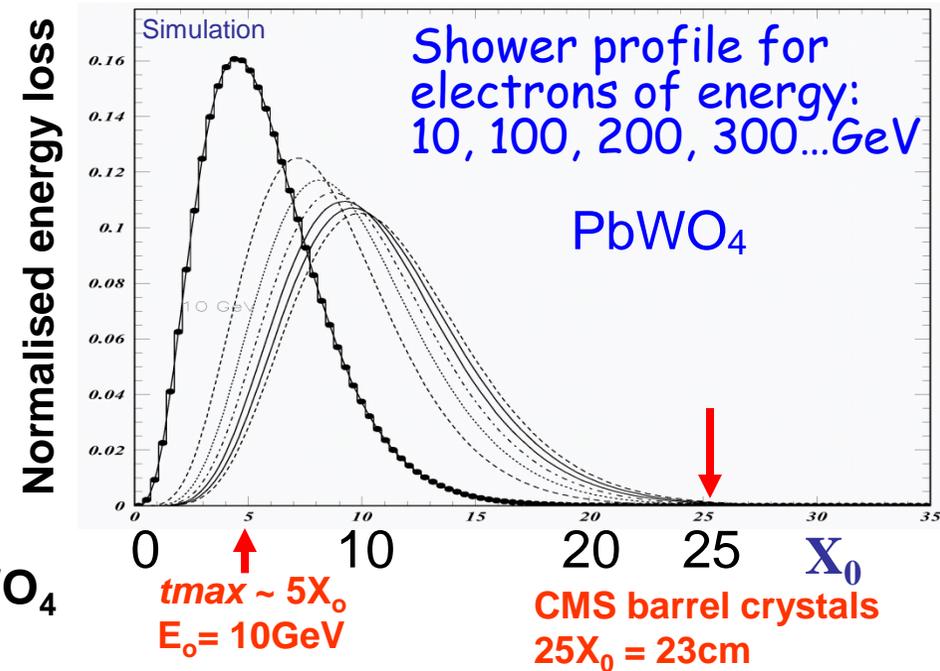
Shower only grows logarithmically with  $E_0$

Shower maximum, where most energy deposited,

$$t_{max} \sim \ln(E_0/E_c) - 0.5 \quad \text{for } e^\pm$$

$$t_{max} \sim \ln(E_0/E_c) + 0.5 \quad \text{for } \gamma$$

$t_{max} \sim 5 X_0$ , 4.6 cm, for 10 GeV electrons in  $\text{PbWO}_4$



How many  $X_0$  to adequately contain an em shower?

Rule of thumb: RMS spread in shower leakage at the back  $\sim 0.5$  \* average leakage at the back

CMS Require the rms spread on energy measurement to be  $< 0.3\%$   
Therefore require leakage  $< 0.65\%$

**Require crystals  $25 X_0$  / 23 cm long**

Amount of shower containment as a function of  $t_{max}$  - see additional slides

# EM Cascade Profiles

## Transverse Shower Development

Mainly multiple Coulomb scattering by  $e^\pm$  in shower

- 95% of shower cone located in cylinder of radius  $2 R_M$  where  $R_M = \text{Moliere Radius}$

$$R_M = \frac{21 \text{ MeV}}{E_c} X_0 \quad [g/cm^2]$$

$R_M = 2.19 \text{ cm}$  in  $\text{PbWO}_4$  ( $X_0 = 0.89 \text{ cm}$ ,  $E_c \sim 8.5 \text{ MeV}$ )

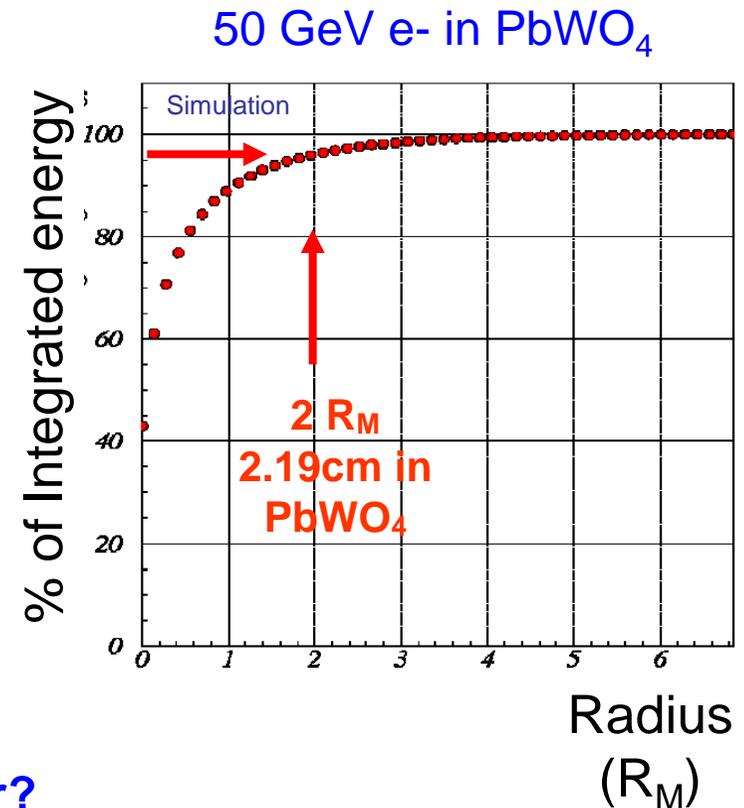
## How many $R_M$ to adequately measure an em shower?

Lateral leakage degrades the energy resolution

An additional contribution to the stochastic term (see later)

In CMS, keep contribution to  $< 2\%/\sqrt{E}$

Achieved by summing energy over 3x3 (or 5x5) arrays of  $\text{PbWO}_4$  crystals



## Detectors for Electromagnetic Calorimetry

# Homogeneous calorimeters

## PbWO<sub>4</sub> crystals: CMS and ALICE

### Vital properties for use at LHC:

#### Compact and radiation tolerant

Density 8 g/cc

X<sub>0</sub> 0.89 cm

R<sub>M</sub> 2.2 cm

Sum over 3x3 or  
5x5 crystals

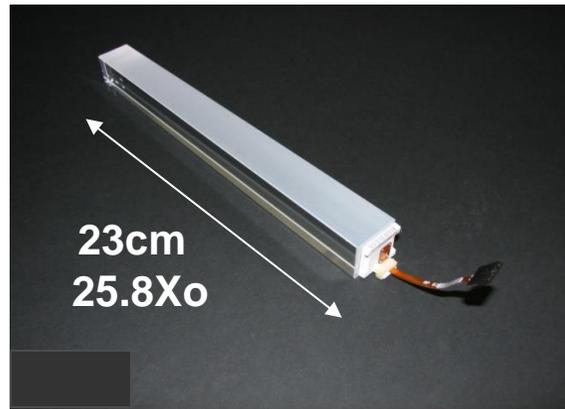
#### Fast scintillation

Emission ~80% in 25 ns

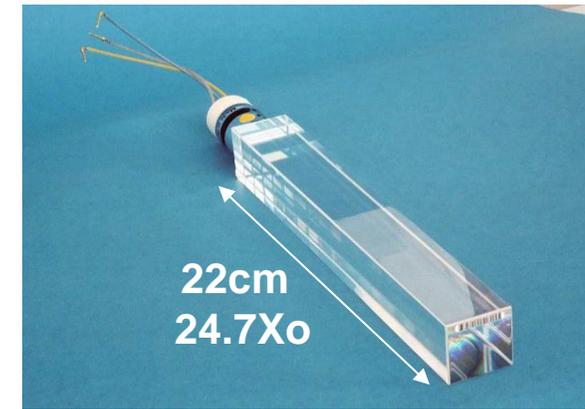
Wavelength 425 nm

Output 150 photons / MeV (low, only 1% wrt NaI)

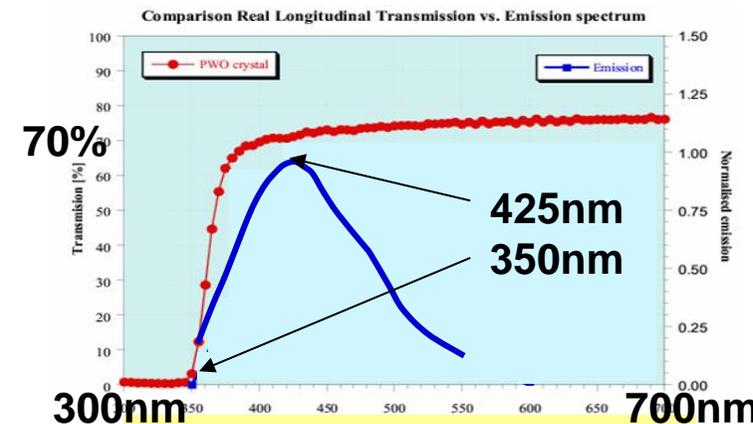
(See backup slide to compare to other crystals/liquids)



CMS Barrel crystal, tapered  
~2.6x2.6 cm<sup>2</sup> at rear  
Avalanche Photo Diode  
readout, gain = 50



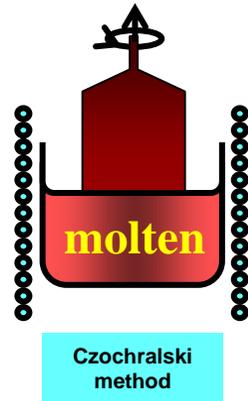
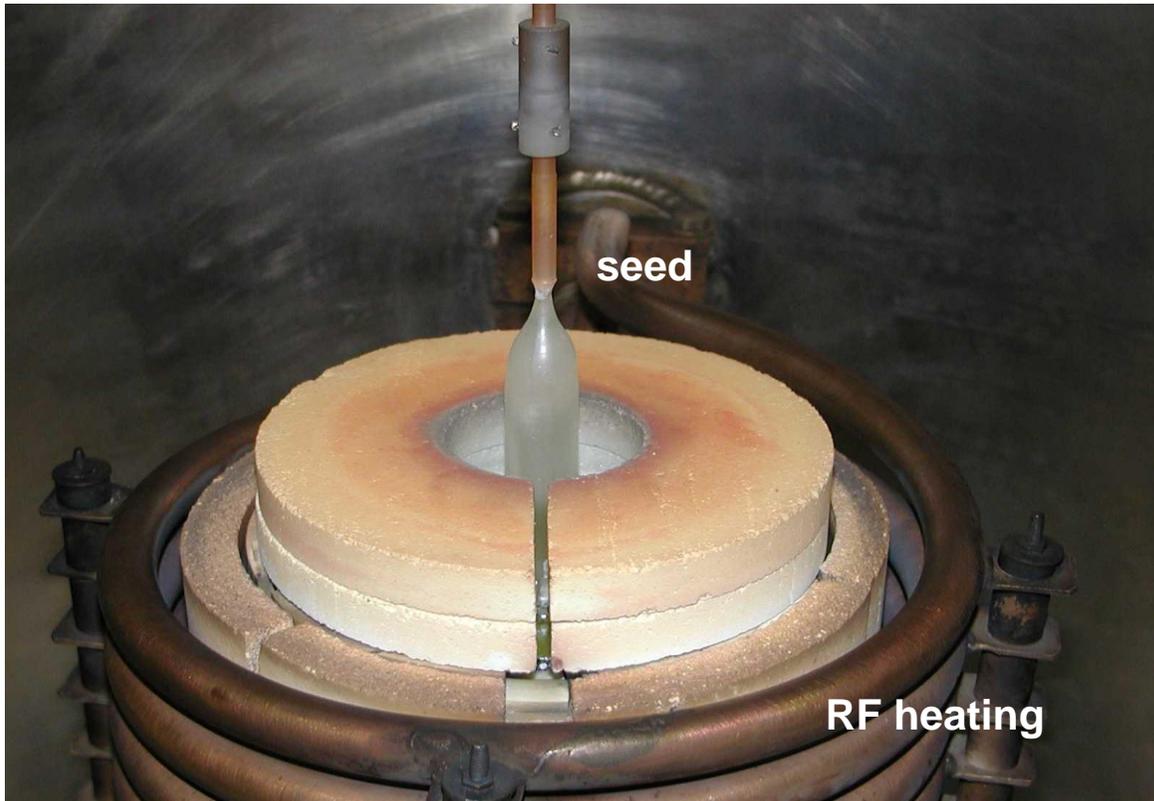
CMS Endcap crystal,  
tapered, 3x3 cm<sup>2</sup> at rear  
Vacuum Photo Triode  
readout, gain ~ 8



Emission spectrum (blue)  
and transmission curve

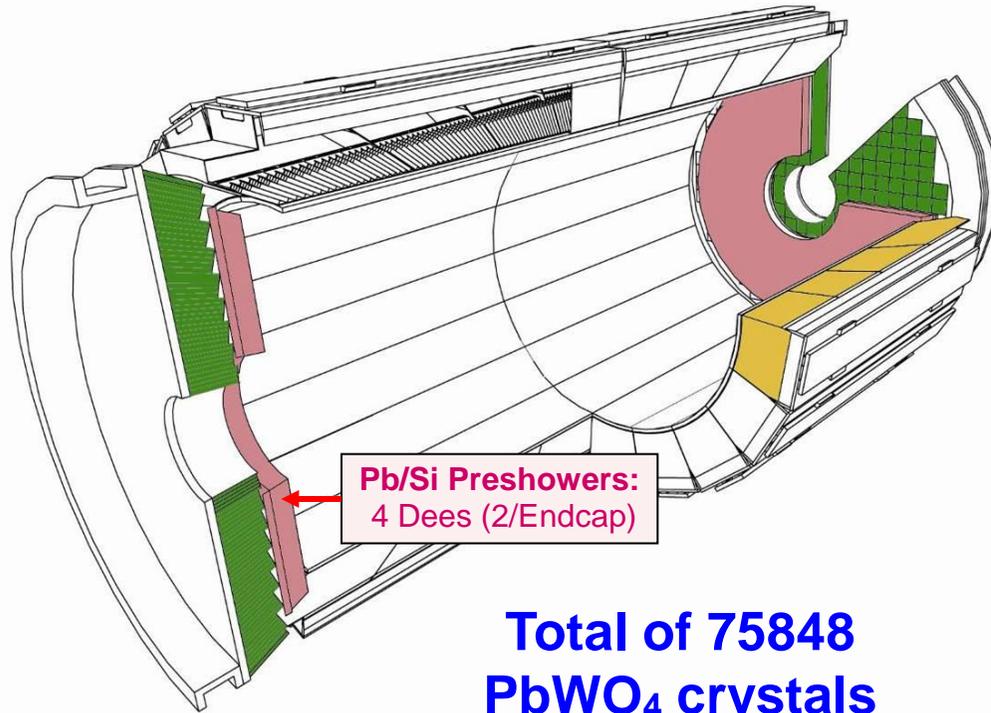
# Homogeneous calorimeters

A CMS  $\text{PbWO}_4$  crystal 'boule' emerging from its  $1123^\circ\text{C}$  melt



# Homogeneous electromagnetic calorimeters

## CMS at the LHC – scintillating $\text{PbWO}_4$ crystals

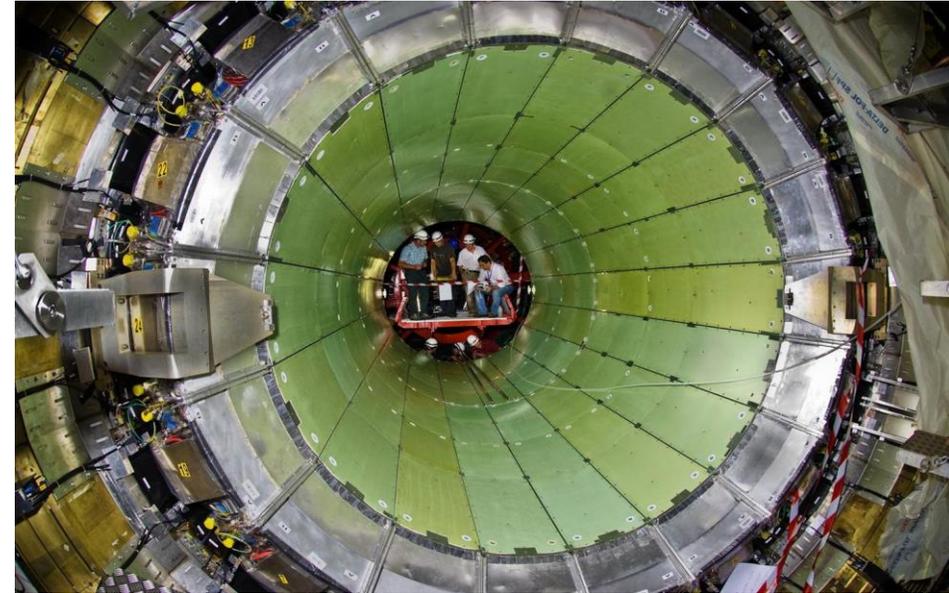


**Pb/Si Preshowers:**  
4 Dees (2/Endcap)

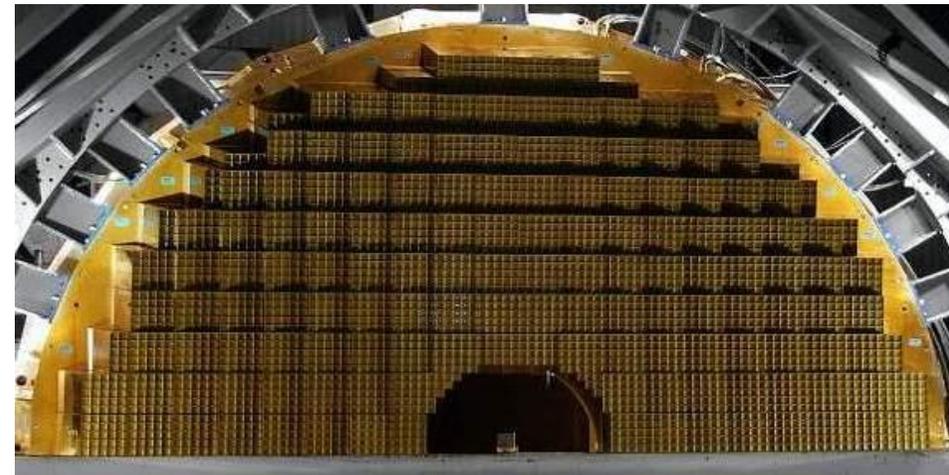
**Total of 75848  
 $\text{PbWO}_4$  crystals**

**Barrel:** 36 Supermodules (18 per half-barrel)  
**61200 Crystals** (34 types) – total mass 67.4 t

**Endcaps:** 4 Dees (2 per Endcap)  
**14648 Crystals** (1 type) – total mass 22.9 t



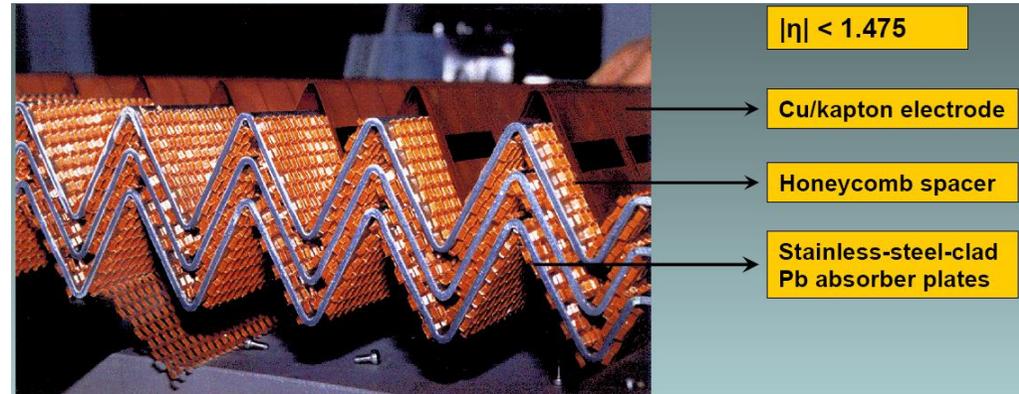
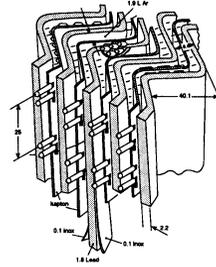
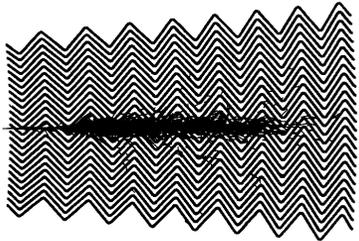
CMS Barrel



An endcap Dee, 3662 crystals awaiting transport

# Sampling electromagnetic calorimeters

## ATLAS 'Accordion' sampling liquid argon calorimeter at the LHC



Corrugated stainless steel clad Pb absorber sheets, 1-2 mm thick

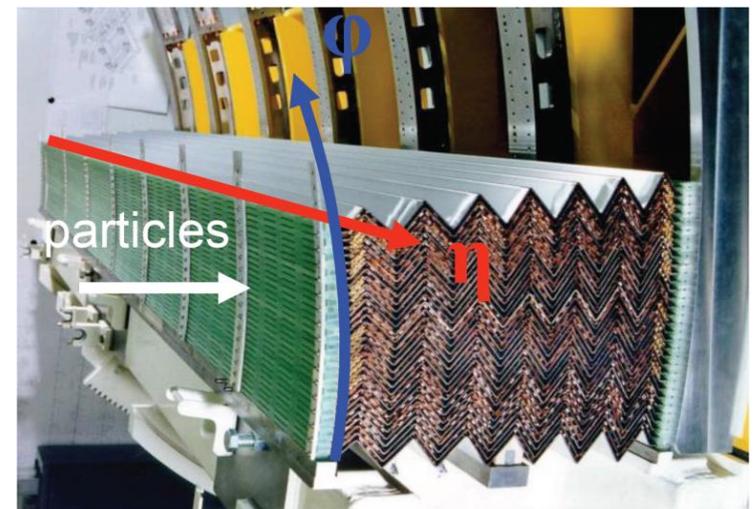
Immersed in liquid argon (90K)

Multilayer Cu-polyimide readout boards

Collect ionisation electrons with an electric field across 2.1 mm liquid Argon drift gap

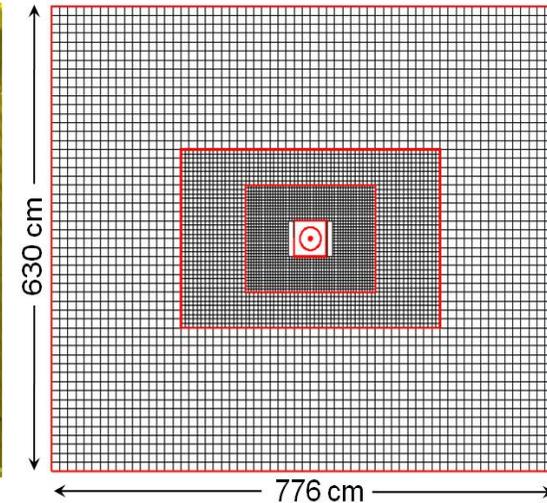
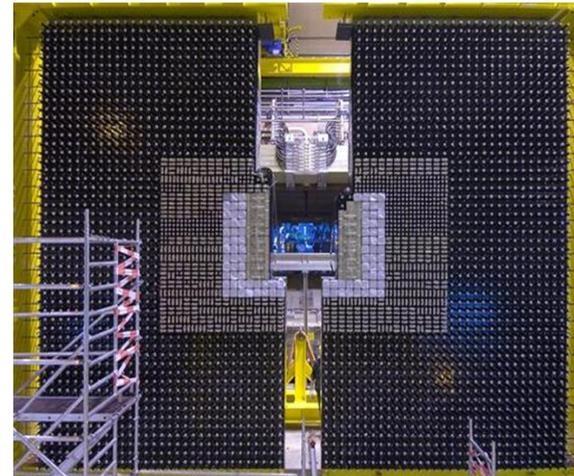
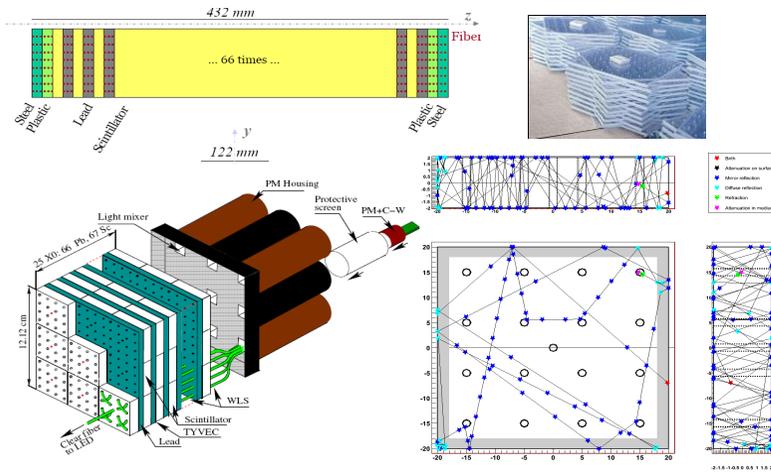
1 GeV energy deposit  $\rightarrow$  collect  $5 \cdot 10^6 e^-$

Accordion geometry minimises dead zones  
**Liquid argon intrinsically radiation hard**  
Readout board allows fine segmentation  
(azimuth, rapidity, longitudinal)



# Sampling electromagnetic calorimeters

## The LHCb sampling electromagnetic calorimeter at the LHC



Wall of 3312 modules

### LHCb module

67 scintillator tiles, each 4 mm thick  
 Interleaved with 66 lead plates, each 2 mm thick

Readout through wavelength shifting fibres  
 running through plates to Avalanche Photodiodes



3 types of modules

# Liquid Scintillator Calorimeters

## Borexino

Detect **0.862 MeV neutrinos** from  ${}^7\text{Be}$  decays in the sun

**300 t ultra pure organic liquid scintillator**. Less than  $10^{-16}$  g/g of  ${}^{238}\text{U}$  and  ${}^{232}\text{Th}$

**$10^4$  photons / MeV at 360 nm**

3 ns decay time

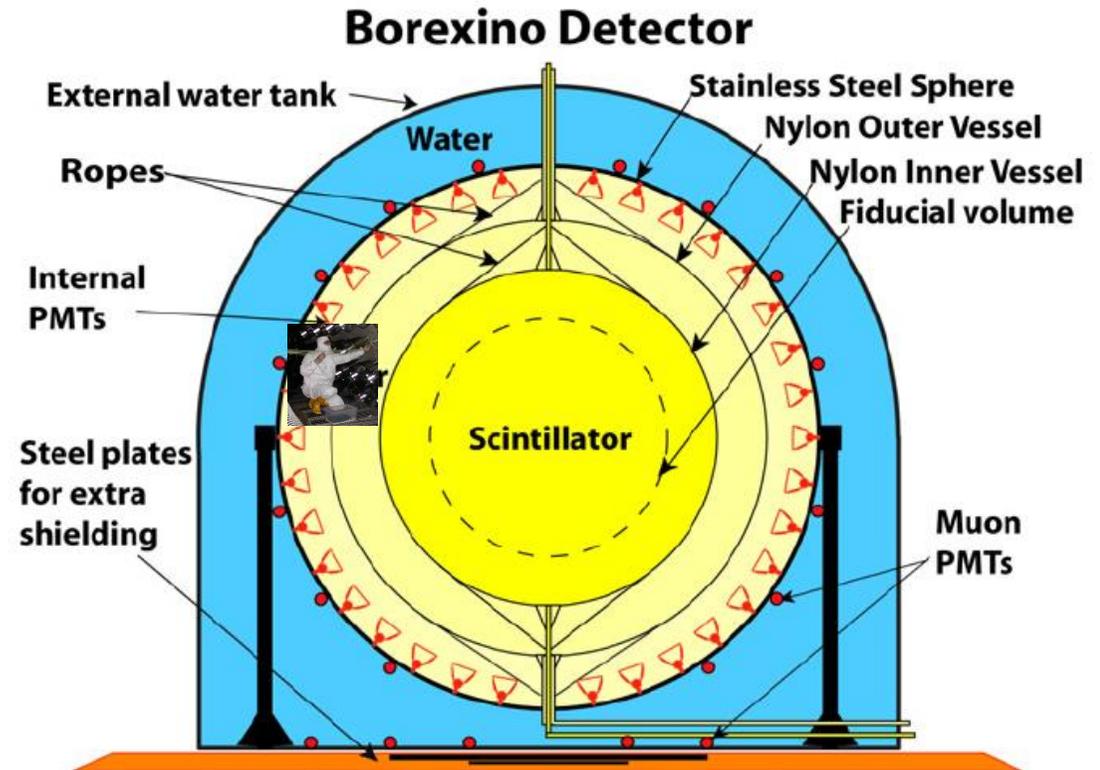
Photon mean free path 8 m

## Readout

2,212 photo-multiplier 8 inch tubes

Timing 1 ns

Cluster position resolution 16 cm



Inner sphere, 4.25 m radius

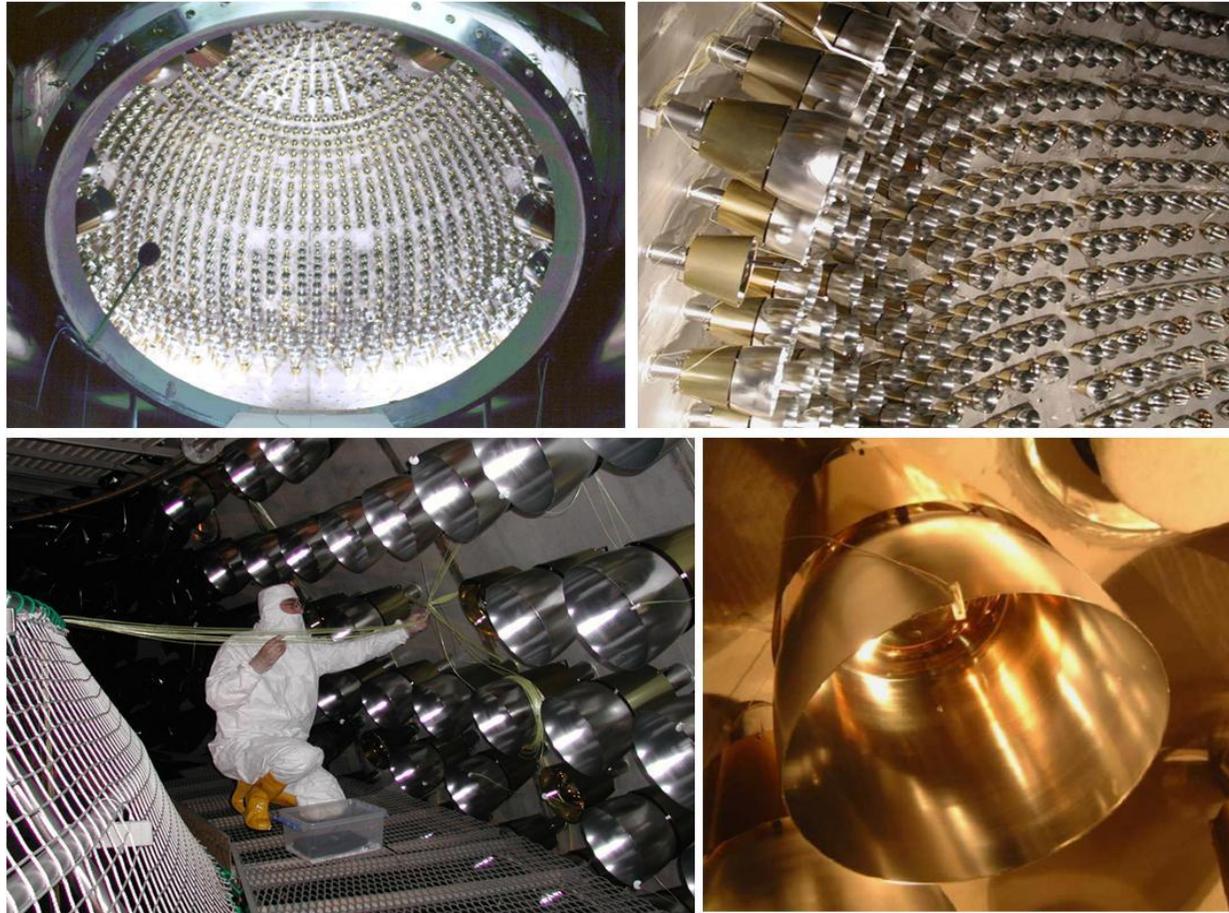
Outer vessel

5.5 m radius

Steel holding vessel

6.85 m radius

# Liquid Scintillator Calorimeters



## Borexino

**Top:** Internal surface of stainless steel support sphere + PMTs + their optical concentrators.

**Bottom:** Preparation of outer vessel + close-up of an optical concentrator.

## Energy Resolution

# Energy Resolution

Energy resolution of a calorimeter where  $E$  is energy of incoming particle:

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

**$a$  , stochastic term**

Fluctuations in the number of signal generating processes, ie on the number of photo-electrons generated

**$b$  , noise term**

Noise in readout electronics  
'pile-up' due to other particles from other collision events arriving close in time

# Energy Resolution

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

## **$c$ , constant term**

Imperfections in calorimeter construction (dimension variations)  
Non-uniform detector response

Channel to channel intercalibration errors  
Fluctuations in longitudinal energy containment

Energy lost in dead material, before or in detector

**Crucial to have small constant term for good energy resolution at the highest particle energies**



## Intrinsic resolution of homogeneous e.m. calorimeters

Energy released in the detector material mainly ionisation and excitation

Mean energy required to produce a 'visible' scintillation photon in a crystal or an electron-ion pair in a noble liquid  $Q$

Mean number of quanta produced  $\langle n \rangle = E_0 / Q$

The intrinsic energy resolution is given by the fluctuations on 'n'

$$\sigma_E / E = \sqrt{n} / n = \sqrt{Q / E}$$

Typically obtain  $\sigma_E / E$  1% - 3% /  $\sqrt{E}$  (GeV)

However, in certain cases:

Energy of the incident particle is **only** transferred to making quanta, and to no other energy dissipating processes, for example in Germanium.

Fluctuations much reduced:

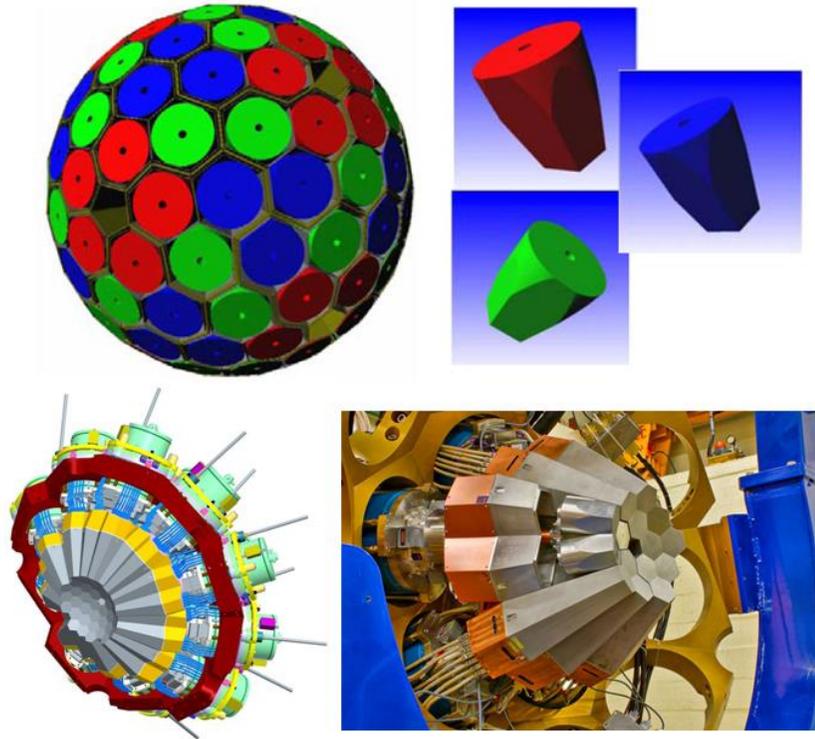
$$\sigma_E / E = \sqrt{FQ / E} \quad \text{where } F \text{ is the 'Fano' factor .}$$

**F ~ 0.1 in Ge**

Detector resolution in **AGATA** 0.06% (rms) for 1332 keV photons

# Intrinsic em energy resolution for homogeneous calorimeters

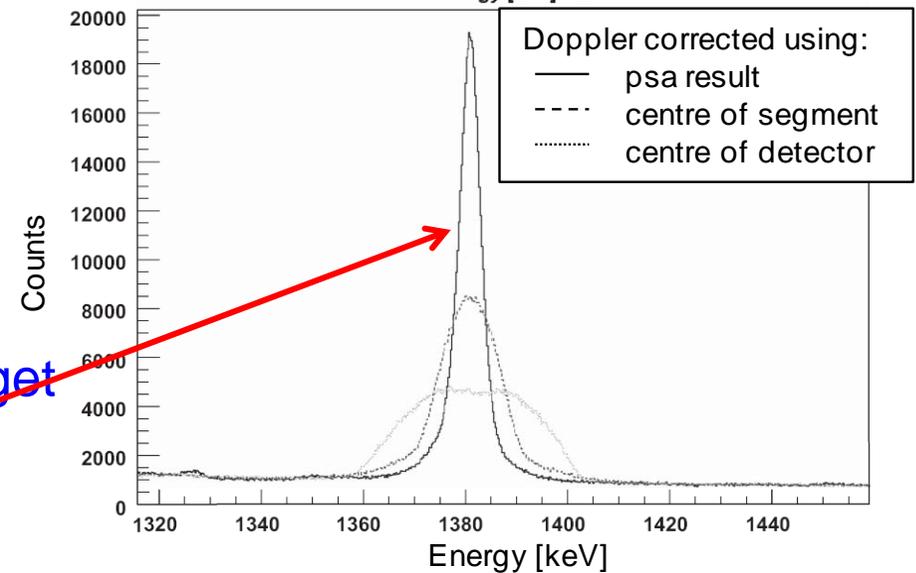
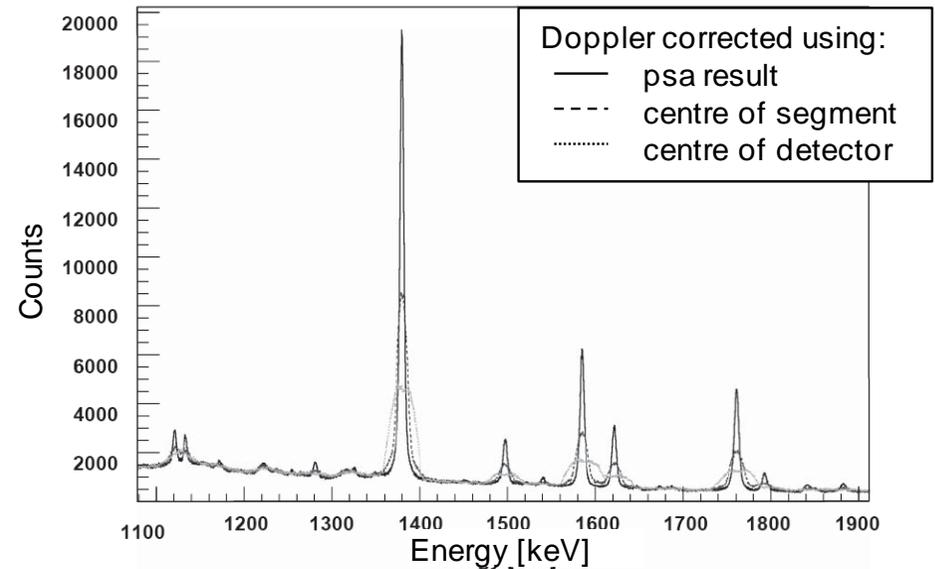
## The AGATA Germanium detector



Experiment with excited nuclei from a target  
1382 keV line width 4.8 keV (fwhm)

Resolution 0.15%

**Resolution 0.06% with a source**



# Energy resolution for crystal em calorimeters

## Energy resolution - the CMS PbWO<sub>4</sub> crystal calorimeter

Scintillation emission only small fraction of energy loss in crystal, so  $F \sim 1$

**However** - fluctuations in the avalanche process in the Avalanche Photodiodes (APDs) used for the photo-detection  
- gives rise to an **excess noise factor** for the gain of the device

**$F \sim 2$  for the crystal + APD combination**

**$N_{pe} \sim 4500$  photo-electrons released by APD, per GeV of deposited energy**

**Stochastic term**      $a_{pe} = \sqrt{F / N_{pe}} = \sqrt{(2 / 4500)} = 2.1\%$

This assumes total lateral shower containment

In practice energy summed over limited 3x3 or 5x5 arrays of crystals, to minimise added noise

Expect  $a_{leak} = 2\%$  from an energy sum over a 3x3 array of crystals

**Expect a stochastic term of**      **$a = a_{pe} \oplus a_{leak} = 2.9\%$**   
**Measured value**     **2.8%**

# Energy resolution in homogeneous em calorimeters

## Energy resolution

CMS ECAL , 3x3 array of  $\text{PbWO}_4$  crystals

Test beam electrons

$a$  , stochastic term = 2.83%

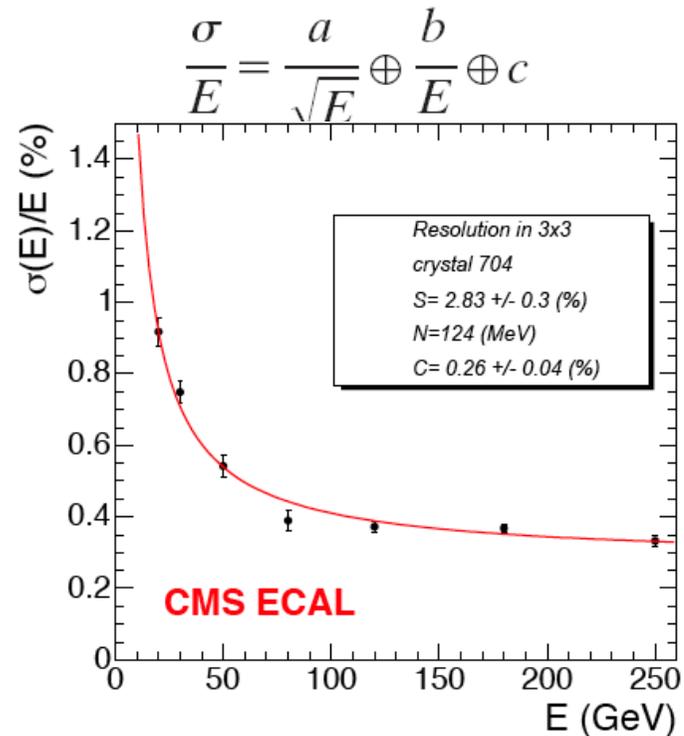
$c$  , constant term = 0.26%

## Borexino

Photoelectron yield  $\sim 500$  per MeV

Expect  $\sqrt{500} / 500 = 4.4\%$

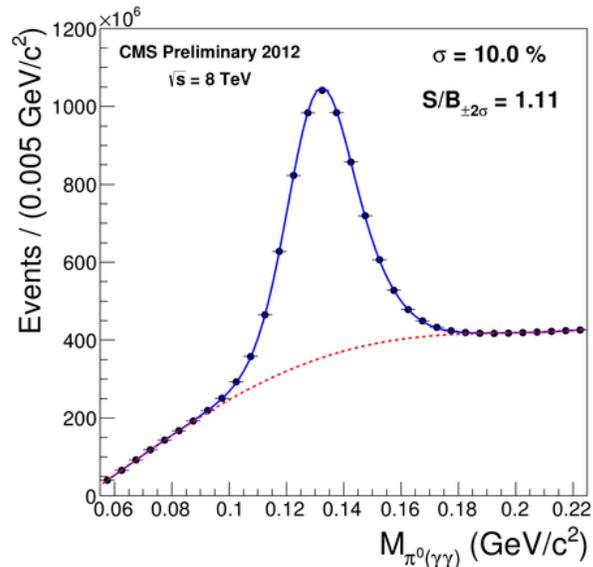
Measured  $\sim 5\%$  at 1 MeV



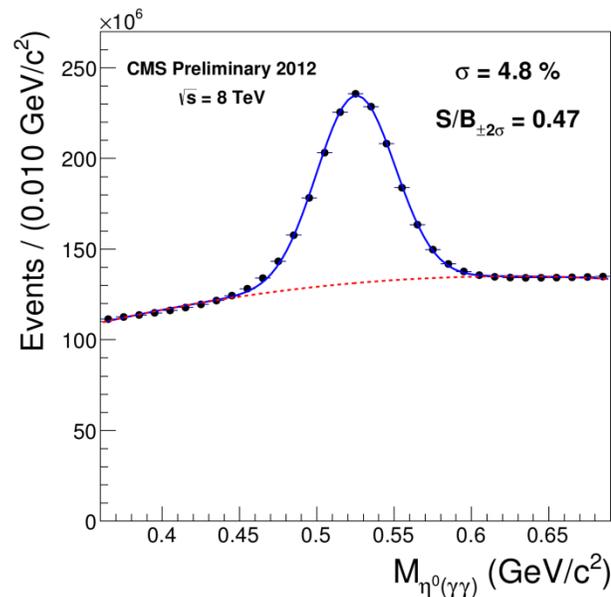
# Calibration of the detector

**Prior to installation:** modules taken to test beams at CERN and elsewhere

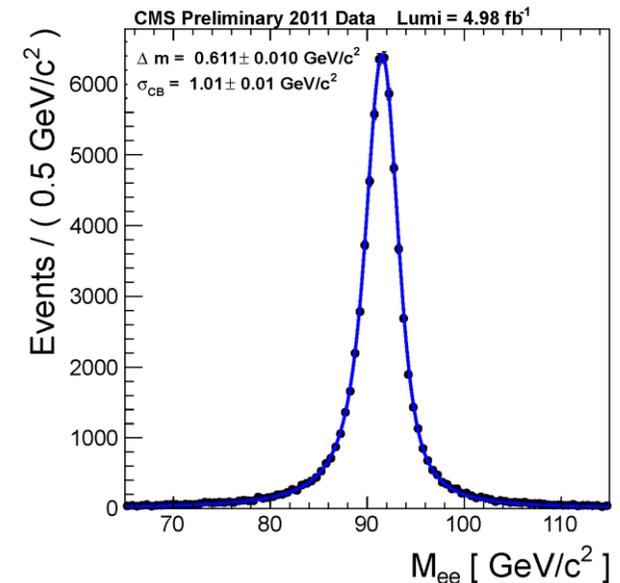
**In situ in CMS:** trigger, record and use known resonances to calibrate the crystals



$\pi^0 \rightarrow \gamma\gamma$



$\eta \rightarrow \gamma\gamma$



$Z \rightarrow ee$

peak at 91 GeV

width of Gaussian 1.01 GeV

Crucial input for resolution

estimates for  $H \rightarrow \gamma\gamma$  at 125 GeV

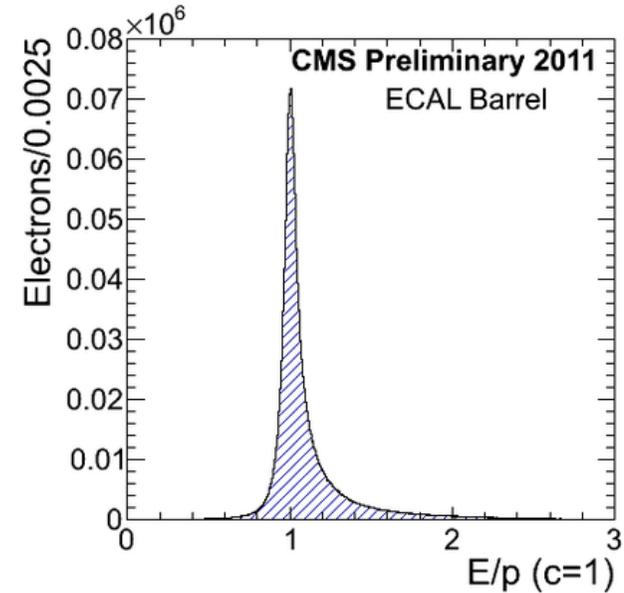
## In situ in CMS also use:

### W decays, $W \rightarrow e^\pm \nu$

Electron energy,  $E$ , measured in the ECAL

Electron momentum,  $p$ , measured in the Tracker

Optimize the  $E/p$  distributions ( $E/p = 1$  ideally)

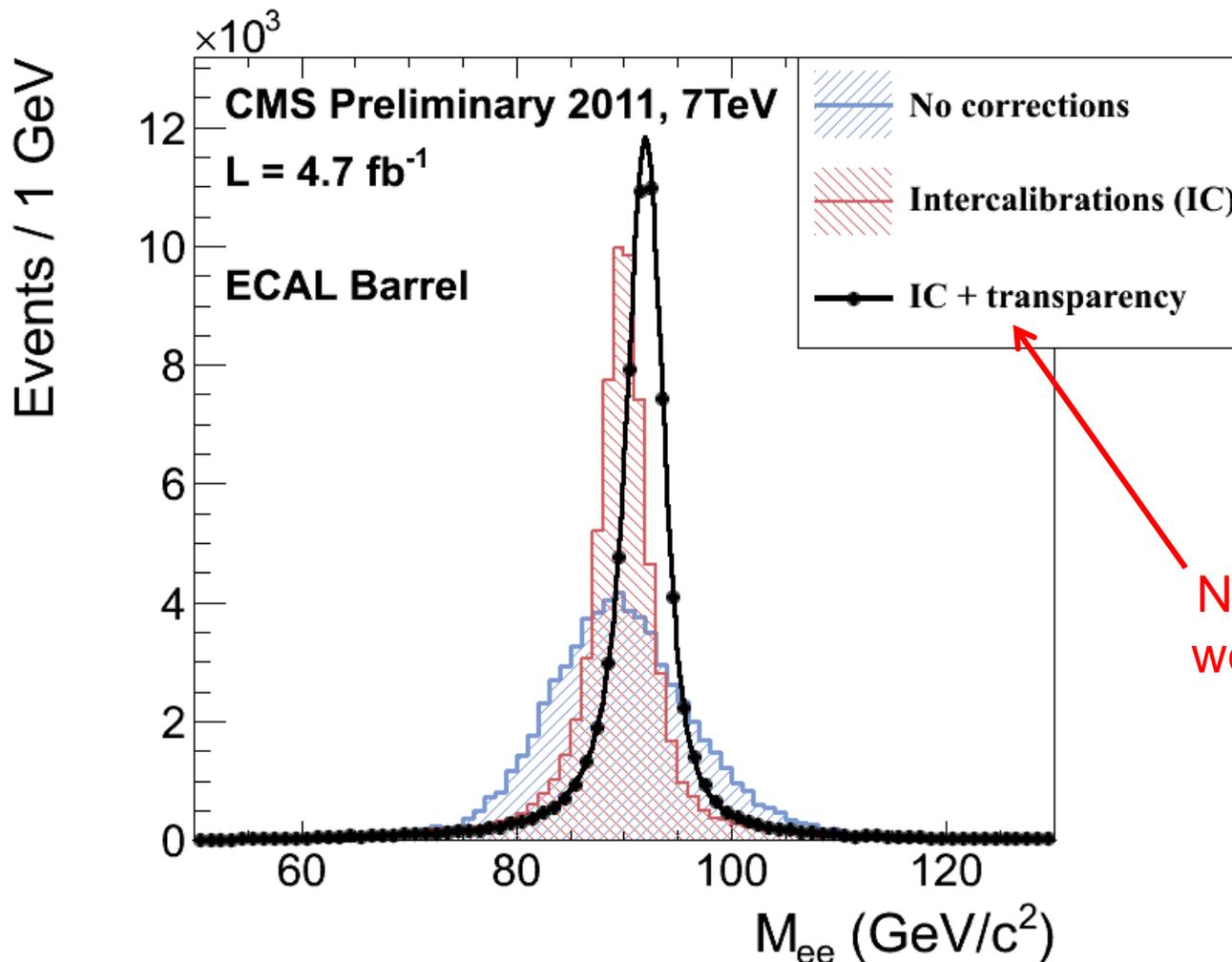


### Phi symmetry (gives quick initial values)

The transverse energy flow, summed over many “minimum bias” collisions, should be the same towards any phi angle

Use this symmetry to calibrate rings of individual crystals sitting at the same pseudorapidity

# Getting excellent energy resolution – in a real detector !!



Note the crucial work needed for the various corrections

**Instrumental resolution of 1.01 GeV from Z  $\rightarrow$  ee decays in the CMS ECAL Barrel**

## Intrinsic resolution of sampling electromagnetic calorimeters

Sampling fluctuations arise due to variations in the number of charged particles crossing the active layers

$$n_{\text{charged}} \propto E_0 / t \quad (t = \text{thickness of each absorber layer})$$

If each sampling is independent  $\sigma_{\text{samp}} / E = 1 / \sqrt{n_{\text{charged}}} \propto \sqrt{t / E}$

Need ~100 sampling layers to compete with homogeneous devices.

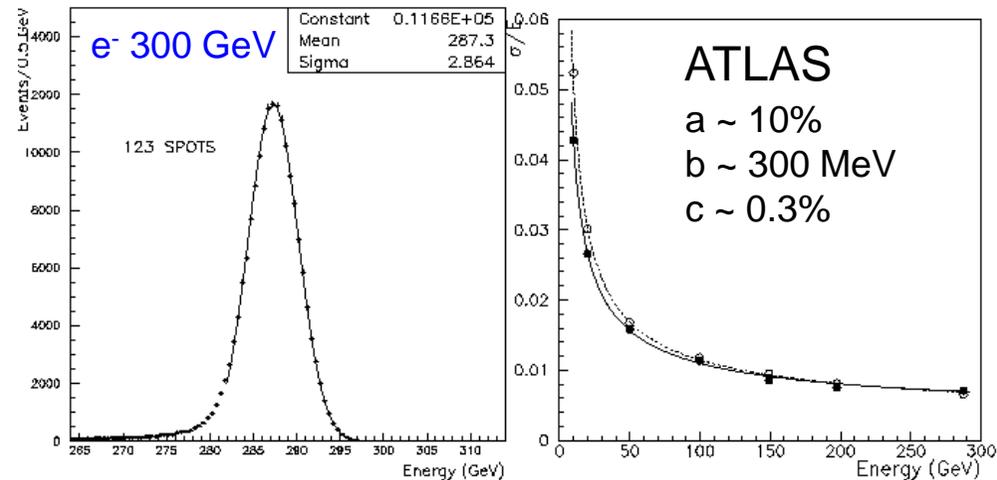
**Typically  $\sigma_{\text{samp}}/E \sim 10\%/\sqrt{E}$**

# Intrinsic energy resolution for sampling e.m. calorimeters

## Intrinsic resolution of sampling electromagnetic calorimeters

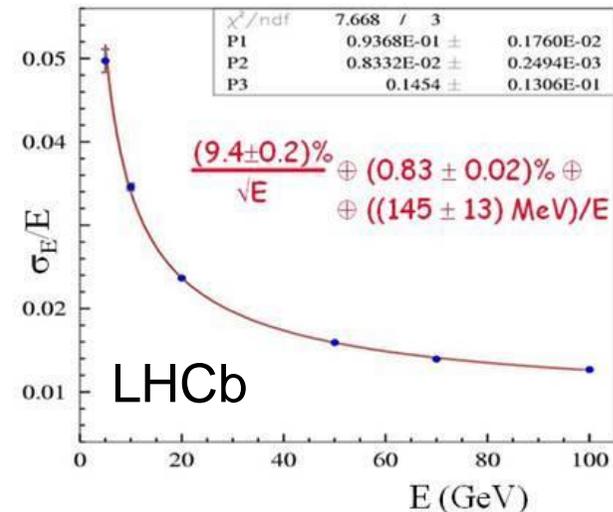
ATLAS stochastic term ~10%  
 constant term 0.3%

Thickness of the 1-2 mm thick absorber sheets controlled to 6.6  $\mu\text{m}$  to achieve a constant term of 0.3%



Also: ATLAS spatial resolution  $\sim 5\text{mm} / \sqrt{E}$  (GeV)

LHCb stochastic term 9.4%  
 constant term 0.83%



## Hadronic Calorimetry

# Hadronic Cascades

Hadronic cascades much more complex than e.m. cascades

Shower development determined by the mean free path,  $\lambda_I$ , between inelastic collisions

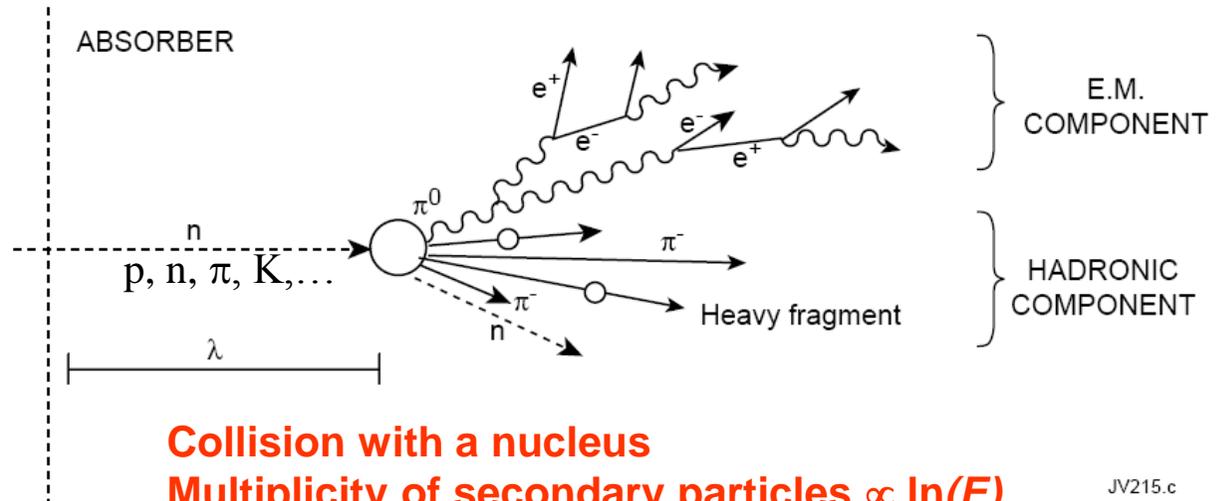
The nuclear interaction length is given by  $\lambda_I = A / (N_A \cdot \sigma_{inel})$ ,  $\sigma_{inel} \approx \sigma_0 A^{0.7}$   $\sigma_0 \approx 35 \text{ mb}$

Expect  $\sigma_I \propto A^{2/3}$  and thus  $\lambda_I \propto A^{1/3}$ .

In practice  $\lambda_I \sim 35 A^{1/3}$

High energy hadrons interact with nuclei producing secondary particles, mostly  $\pi^\pm$  and  $\pi^0$

Lateral spread of shower from transverse energy of secondaries,  $\langle p_T \rangle \sim 350 \text{ MeV}/c$



**Collision with a nucleus**

**Multiplicity of secondary particles  $\propto \ln(E)$**

**$n(\pi^0) \sim \ln E (\text{GeV}) - 4.6$**

**For a 100 GeV incoming hadron,  $n(\pi^0) \approx 18$**

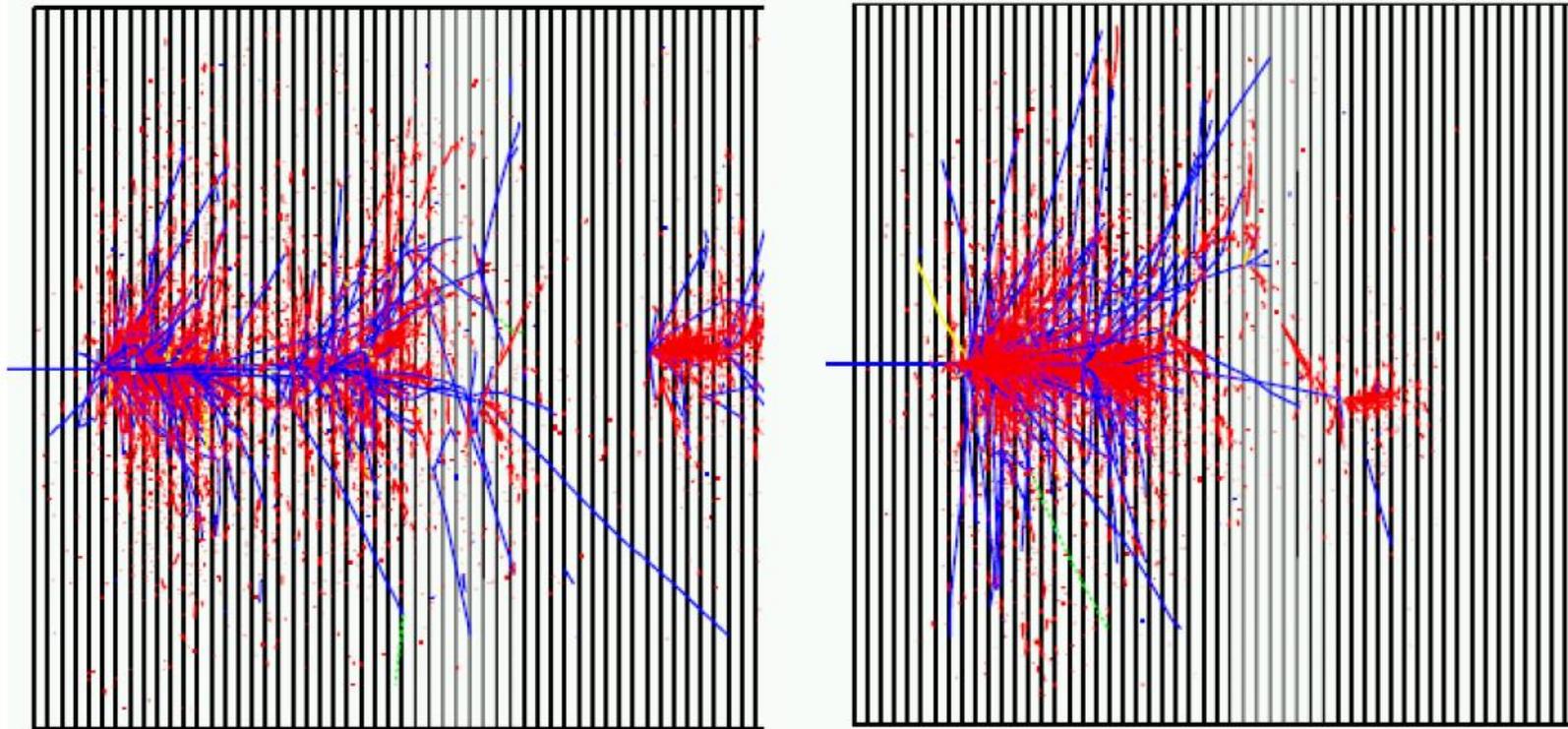
JV215.c

$\sim 1/3$  of the pions produced are  $\pi^0$  with  $\pi^0 \rightarrow \gamma\gamma$  in  $\sim 10^{-16} \text{ s}$

Thus the cascades have two distinct components: hadronic and electromagnetic

# Hadronic Cascades

## Simulations of hadron showers



**Red** - e.m. component      **Blue** – charged hadrons

Unlike electromagnetic showers, hadron showers do not show a uniform deposition of energy throughout the detector medium

# Hadronic Cascades

## Hadronic longitudinal shower development

The e.m. component more pronounced at the start of the cascade than the hadronic component

Shower profile characterised by a peak close to the first interaction, Then, an exponential fall off with scale  $\lambda_1$

$$t_{\max}(\lambda_1) \approx 0.2 \ln E[\text{GeV}] + 0.7$$

$$t_{95\%}(\text{cm}) \approx a \ln E + b$$

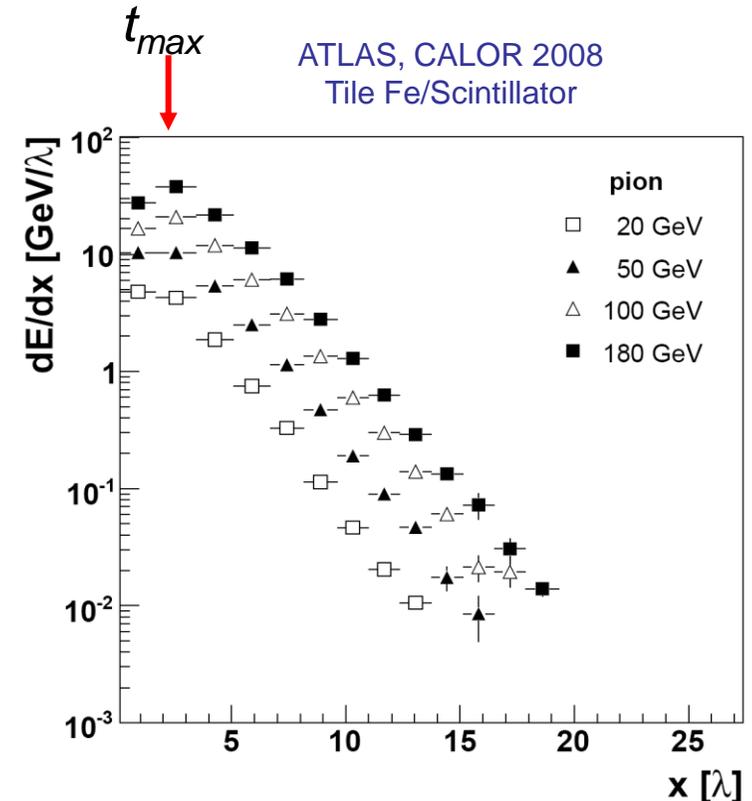
**For Iron:**  $a = 9.4$ ,  $b=39$   $\lambda_1 = 16.7$  cm  
**E = 100 GeV,  $t_{95\%} \approx 80$  cm**  
For adequate containment, need  $\sim 10 \lambda_1$   
**Iron 1.67m Copper 1.35m**

## Hadronic lateral shower development

The shower consists of core + halo

**95% containment : cylinder of radius  $\lambda_1 = 16.7$  cm in iron**

Compare to a radius of 2.19 cm for an em cascade in  $\text{PbWO}_4$



Longitudinal profile of pion induced showers at various energies

# Comparison – electromagnetic showers vs hadronic showers

## Electromagnetic versus hadronic scale for calorimetry

$$X_0 \sim 180 A / Z^2 \quad \ll \quad \lambda_I \sim 35 A^{1/3}$$

E.M shower size in PbWO4 **23 cm deep x 2.19 cm radius**

Hadron shower size in Iron **80 cm deep x 16.7 cm radius**

Hadron cascades much longer and broader than electromagnetic cascades

Hadron calorimeters much larger than em calorimeters

## Detectors for Hadronic Calorimetry

# Hadron Sampling Calorimeters

CMS Hadron calorimeter at the LHC

Brass absorber preparation

**Workers in Murmansk**  
sitting on brass casings of  
**decommissioned shells of**  
**the Russian Northern Fleet**

**Explosives previously**  
**removed!**

Casings melted in St  
Petersburg and turned into  
raw brass plates

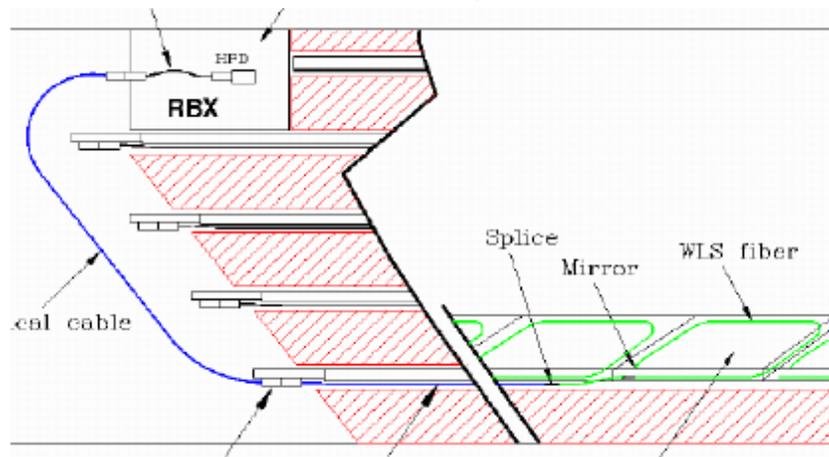
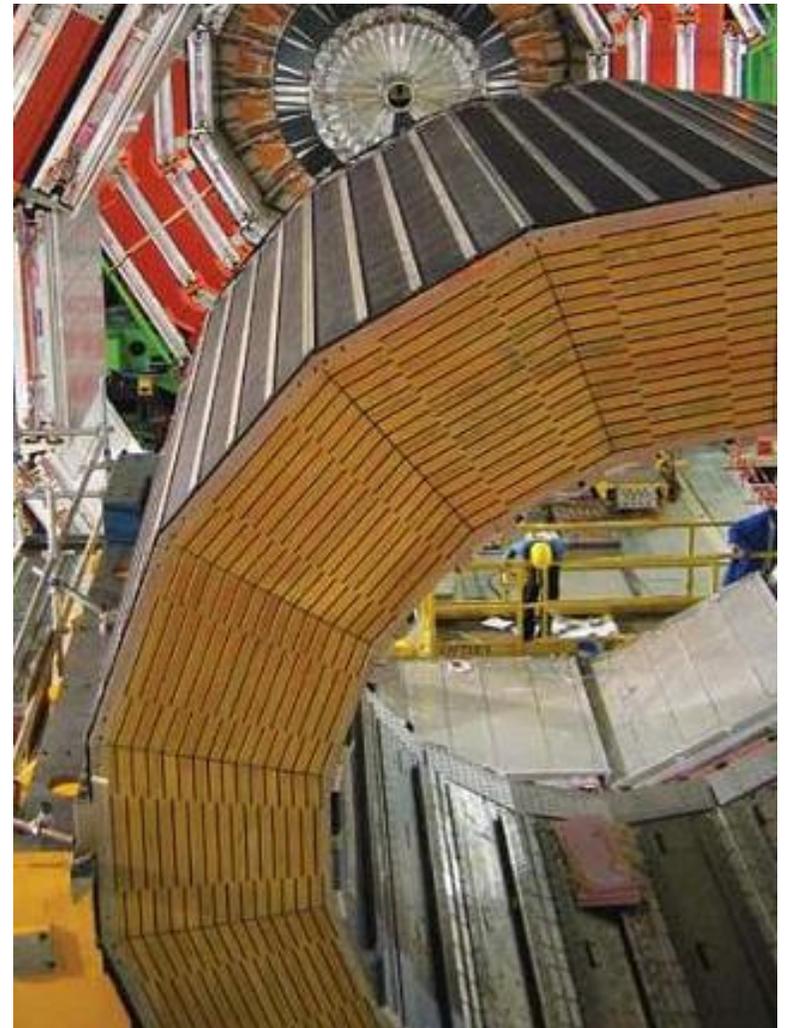
Machined in Minsk and  
mounted to become  
absorber plates for the CMS  
Endcap Hadron Calorimeter



# CMS Hadron sampling calorimetry

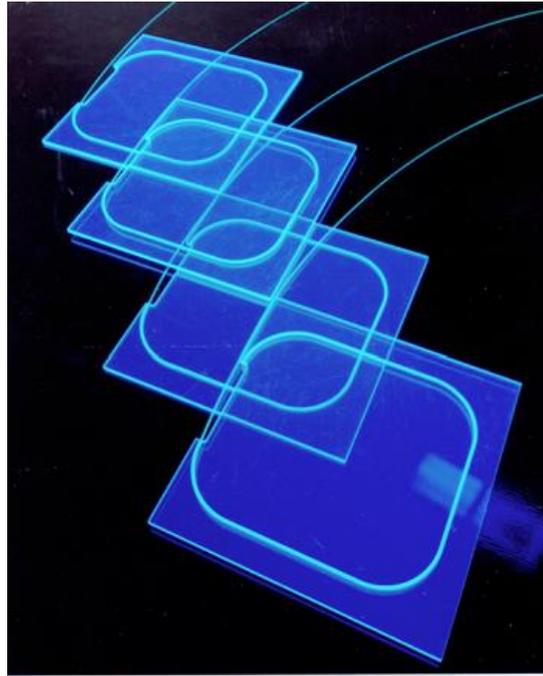
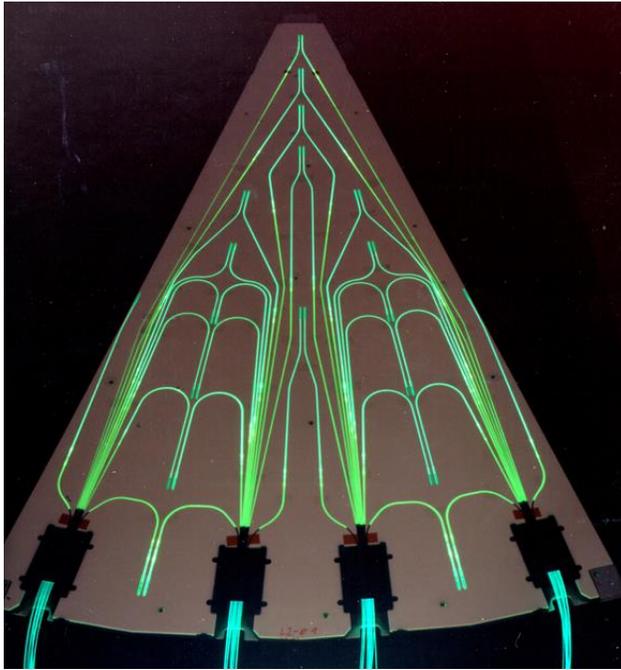


The CMS HCAL being inserted into the solenoid



Light produced in the scintillators is transported through optical fibres to Hybrid Photo Diode (HPD) detectors

# CMS HCAL – fibre readout



Scintillator tile inspection

Light emission from the scintillator tiles blue-violet,  $\lambda = 410-425$  nm.

This light is absorbed by wavelength shifting fibers which fluoresce in the green,  $\lambda = 490$  nm.

The green light is conveyed via clear fiber waveguides to connectors at the ends of the scintillator megatiles.

# Energy resolution of hadronic calorimeters

## Hadron calorimetry resolution

Strongly affected by the energy lost as ‘invisible energy’:

- nuclear excitation followed by delayed photons (by up to to  $\sim 1\mu\text{sec}$ , so usually undetected )
- soft neutrons
- nuclear binding energy

Fluctuations in the ‘invisible energy’ play an important part in the degradation of the intrinsic energy resolution

## Further degradation

If the calorimeter responds differently as a function of energy to the em component of the cascade ( $\pi^0 \rightarrow \gamma\gamma$ )

$F_{\pi^0} \sim 1/3$  at low energies

$F_{\pi^0} \sim a \log(E)$  (the em part increases or ‘freezes out’ with energy)

**In general, hadronic component of hadron shower produces smaller signal than the em component, so  $e/h > 1$**

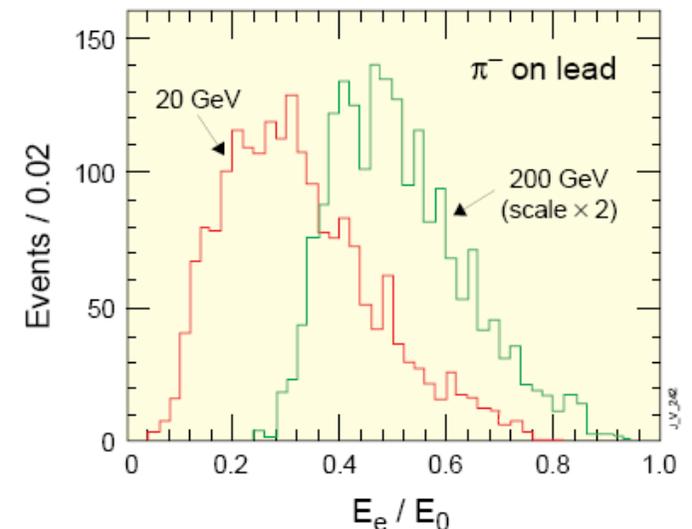
## Hadron energy dissipation in Pb

Nuclear break-up (invisible) 42%

Charged particle ionisation 43%

Neutrons with  $T_N \sim 1 \text{ MeV}$  12%

Photons with  $E_\gamma \sim 1 \text{ MeV}$  3%



EM fraction for 20GeV and 200GeV pions on lead

## Consequences for $e/h \neq 1$

- response with energy is non-linear
- fluctuations on  $F_{\pi^0}$  contribute to  $\sigma_E/E$

Since the fluctuations are non-Gaussian

- $\sigma_E/E$  scales more weakly than  $1/\sqrt{E}$ , more as  $1/E$

‘Compensating’ sampling hadron calorimeters seek to restore  $e/h = 1$  (see backup slide) and achieve higher resolution and linearity

# Single hadron energy resolution in CMS at the LHC

Compensated hadron calorimetry & high precision em calorimetry are usually incompatible

In CMS, hadron measurement combines **HCAL** (Brass/scint) and ECAL(PbWO<sub>4</sub>) data

Effectively a hadron calorimeter divided in depth into two compartments

Neither compartment is 'compensating':

$e/h \sim 1.6$  for ECAL

$e/h \sim 1.4$  for HCAL

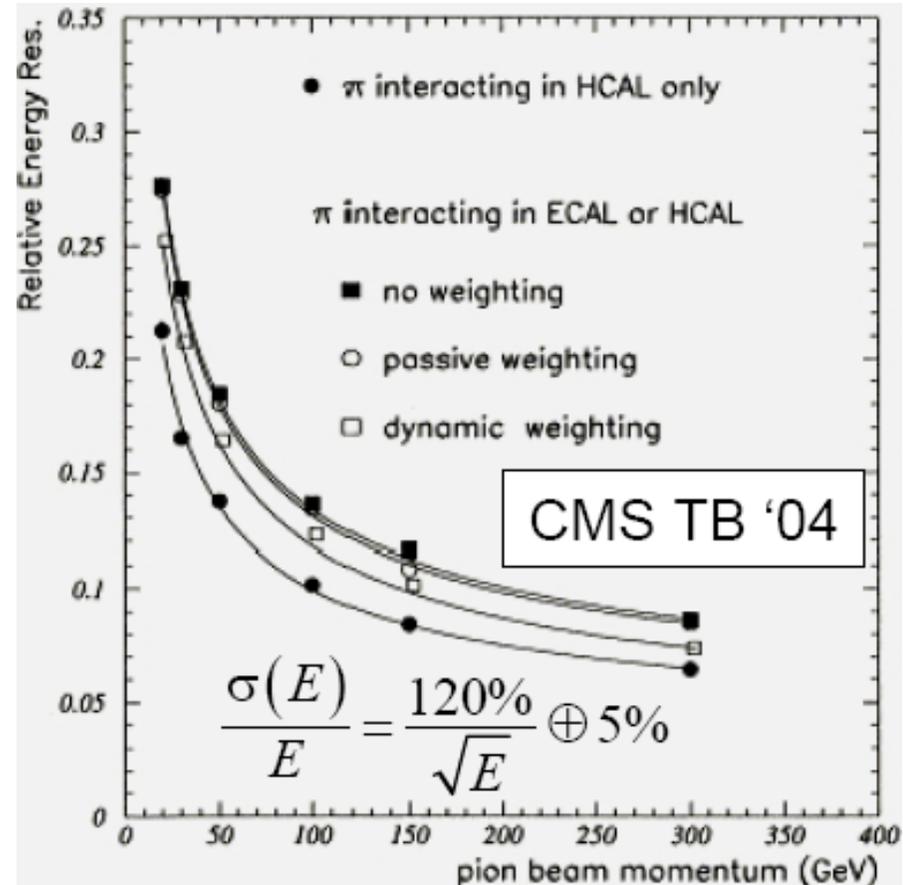
**Hadron energy resolution is degraded and response is energy-dependent**

**Stochastic term**

**a = 120%**

**Constant term**

**c = 5%**



CMS energy resolution for single pions up to 300GeV

## Jets and Particle Flow

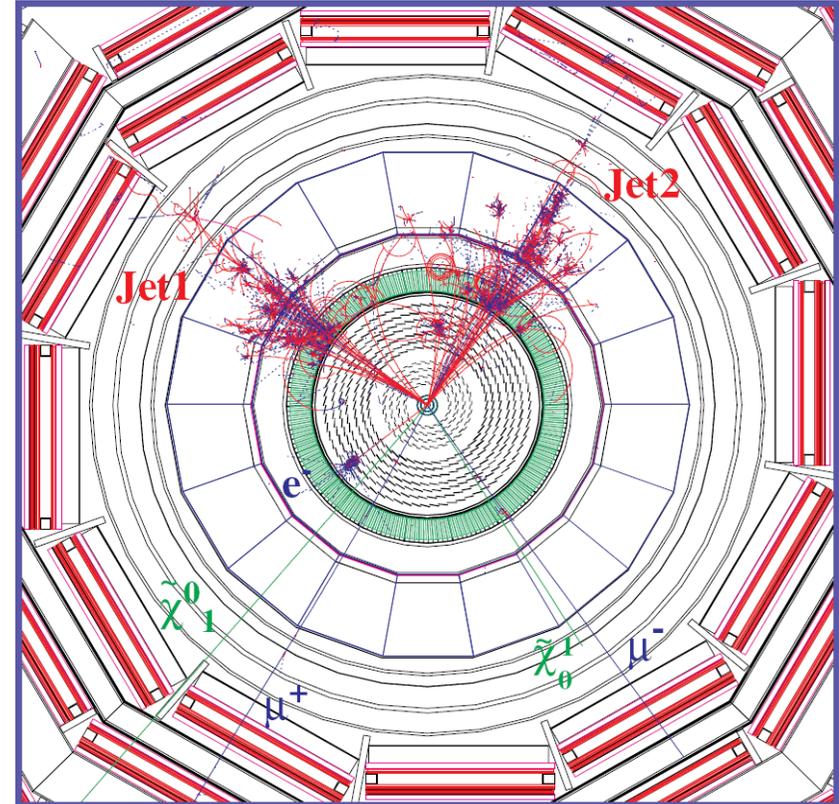
# The measurement of Jets and Particle Flow

At colliders, hadron calorimeters serve primarily to measure jets and missing  $E_T$

Single hadron response gives an indication of the level to be expected for jet energy resolution

Make combined use of

- Tracker information
- fine grained information from the ECAL and HCAL detectors



Jets from a simulated event in CMS

## Traditional approach

Components of jet energy only measured in ECAL and HCAL

In a typical jet

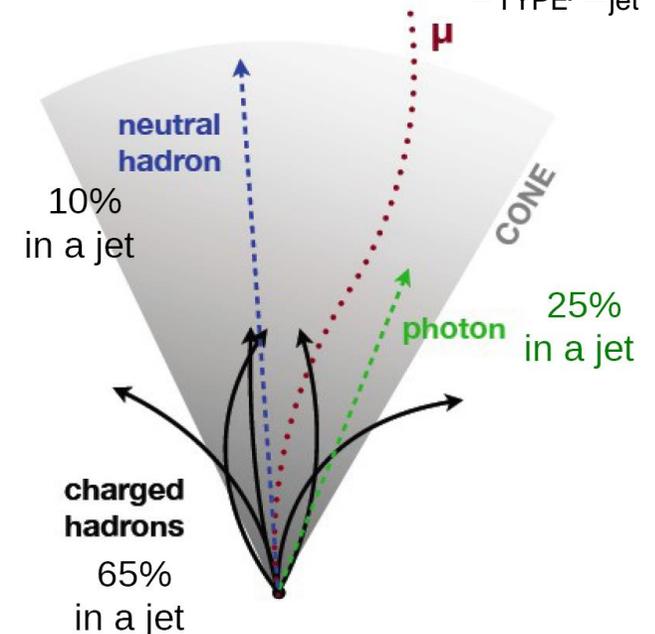
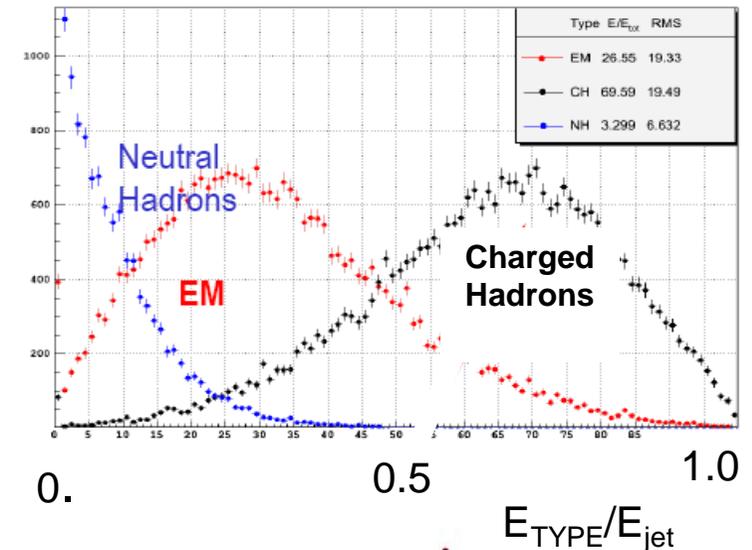
- 65% of jet energy in **charged** hadrons
- 25% in **photons** (mainly from  $\pi^0 \rightarrow \gamma\gamma$ )
- 10% in **neutral hadrons**

## Particle Flow Calorimetry

- Charged particles measured with tracker when better
- Photons measured in ECAL
- Leaves only neutral hadrons in HCAL (+ECAL)

Only 10% of the jet energy (the neutral hadrons) left to be measured in the poorer resolution HCAL

**Dramatic improvements for overall jet energy resolution**



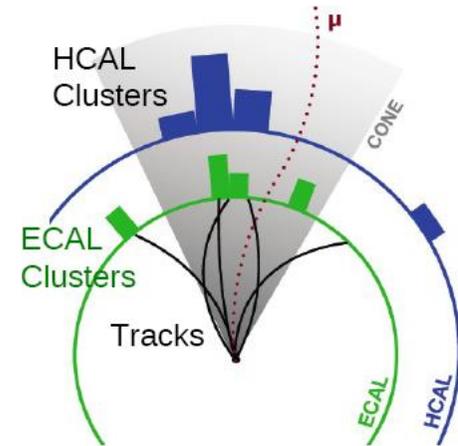
# Jet measurements with Particle Flow

## Momenta of particles inside a jet

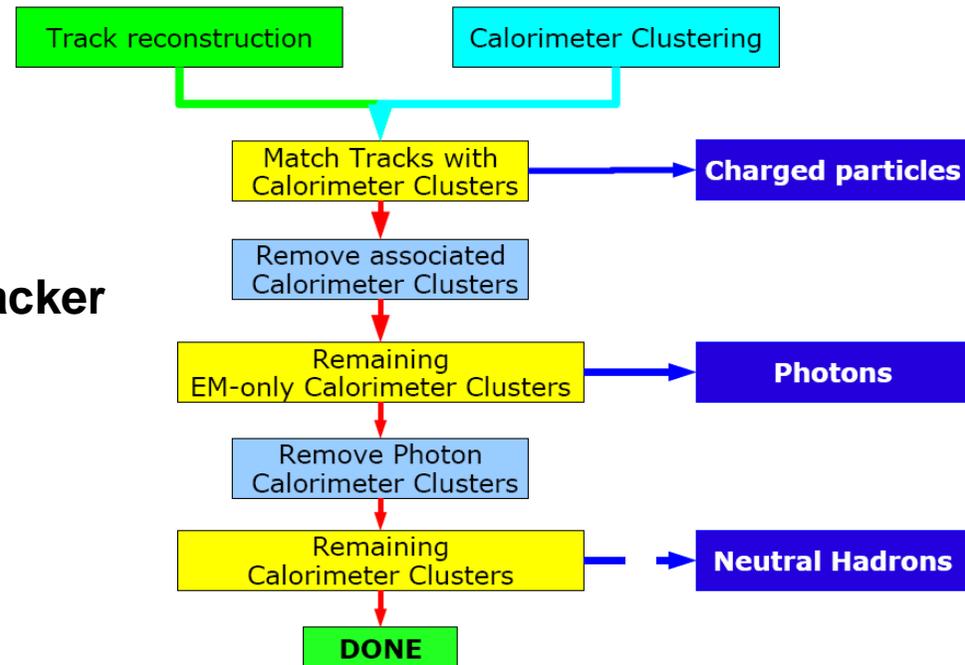
Consider a quark/gluon jet, total  $p_T = 500 \text{ GeV}/c$

Average  $p_T$  carried by the stable constituent particles of the jet  $\sim 10 \text{ GeV}$

Jets with  $p_T < 100 \text{ GeV}$ , constituents  $\mathcal{O}(\text{GeV})$



For charged particles with momenta  $\mathcal{O}(\text{GeV})$ :  
Better to use momentum resolution of the Tracker

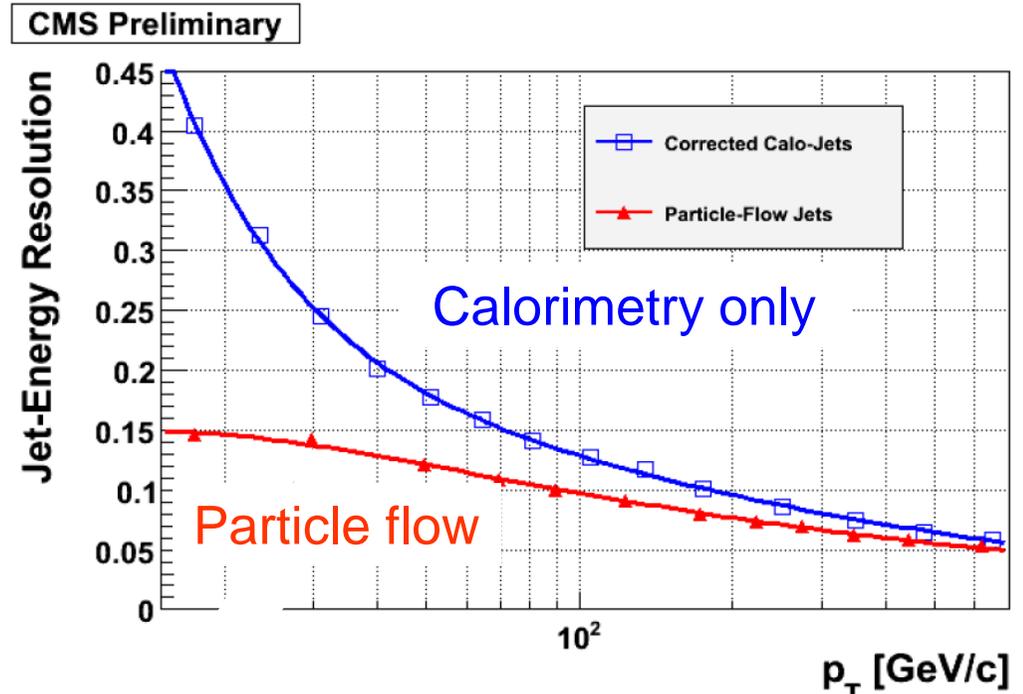


## Particle Flow versus Calorimetry alone

- CMS - large central magnetic field of 4T
- Very good charged particle track momentum resolution
- Good separation of charged particle energy deposits from others in the calorimeters
- Good separation from other tracks

**Large improvement in jet resolution at low  $P_T$  using the combined resolution of the Calorimetry and Tracking systems**

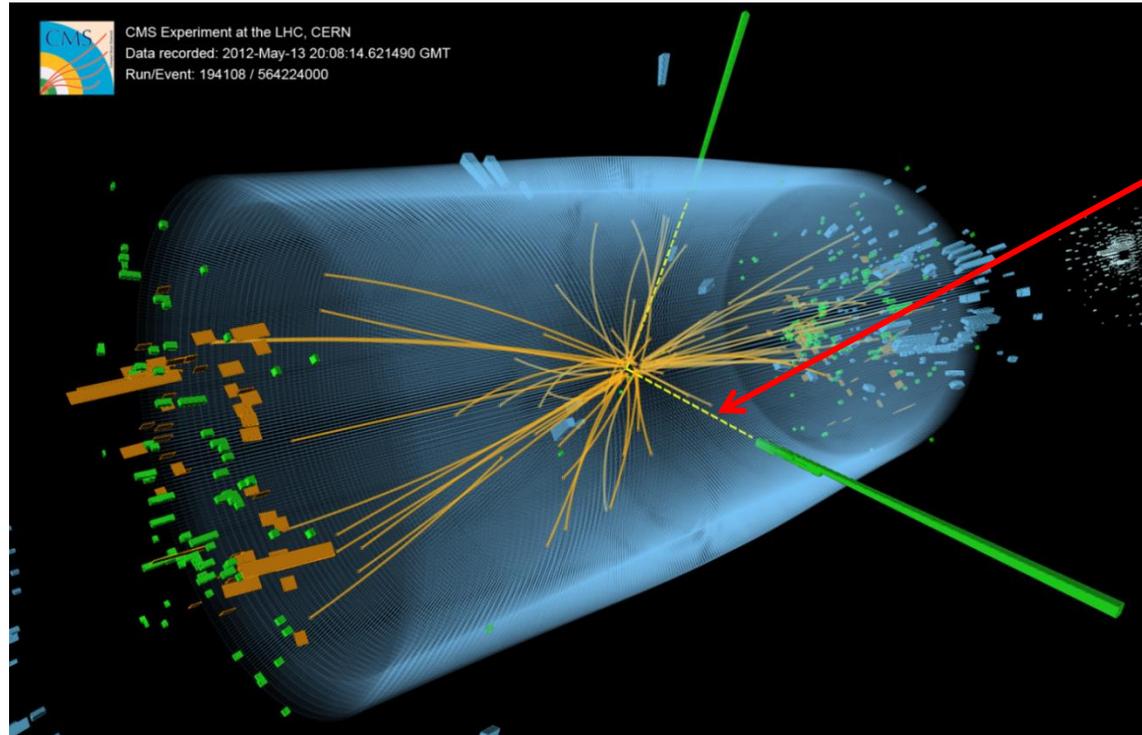
## Simulated QCD-multijet events, CMS barrel section: $|\eta| < 1.5$



**Jet energy resolution as a function of  $P_T$**

# The crowning glory of CMS (and ATLAS) calorimetry!

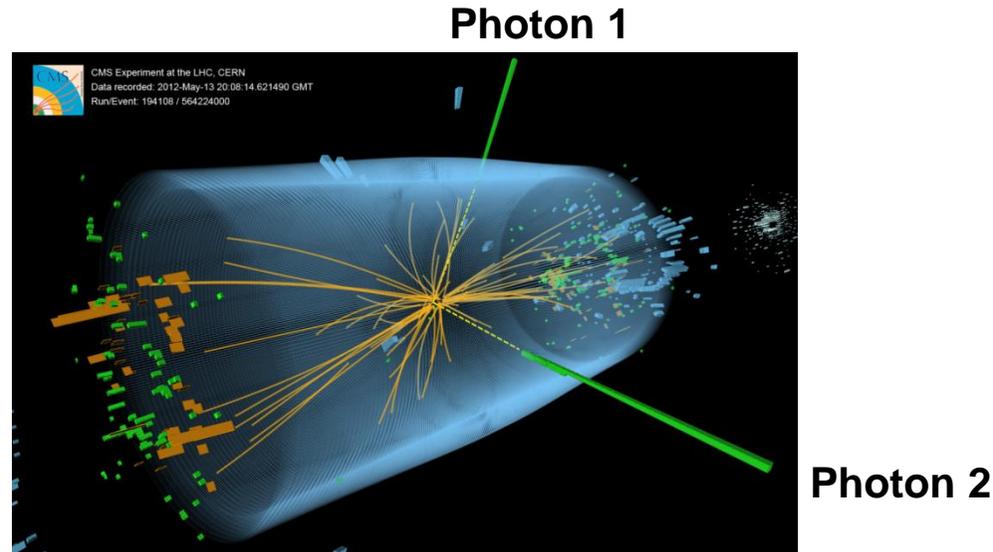
## Event recorded with the CMS detector in 2012 Characteristic of Higgs boson decay to 2 photons



<u>EM calorimetry</u>	<u>Hadronic calorimeter</u>	<u>Tracker</u>	<u>Muon detector</u>
E.m. energy proportional to green tower heights	Hadron energy proportional to orange tower heights	Charged tracks Orange curves	Muon detector hits Blue towers

# CMS ECAL DATA

Can **YOU** calculate the **Effective mass** for the 2 high energy photons in the event??

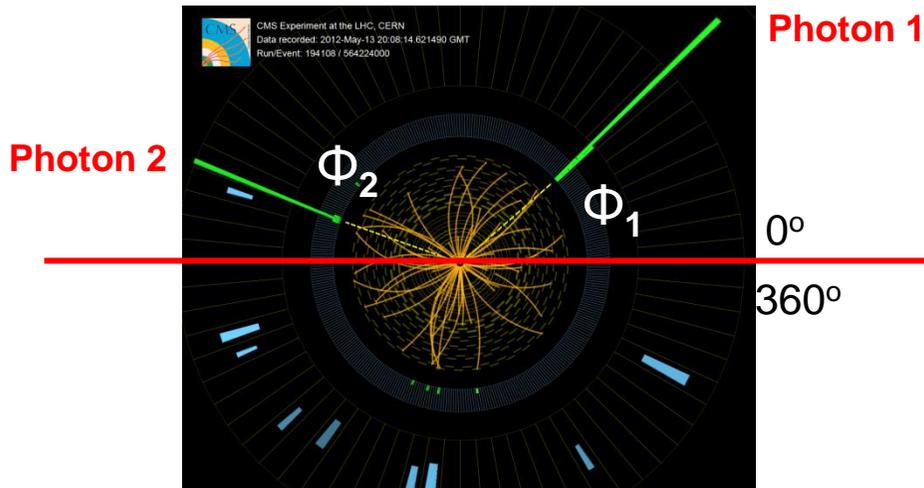


	ECAL Energy (GeV)	Angle Phi ** (radians)	Pseudo-rapidity ** ( $\eta$ )
<b>Photon 1</b>	90.0264	0.719	0.0623
<b>Photon 2</b>	62.3762	2.800	-0.811

**\*\*** see definitions in next slide

**You can also ask Professor Moretti for his estimate !**

# CMS Event – angle definitions

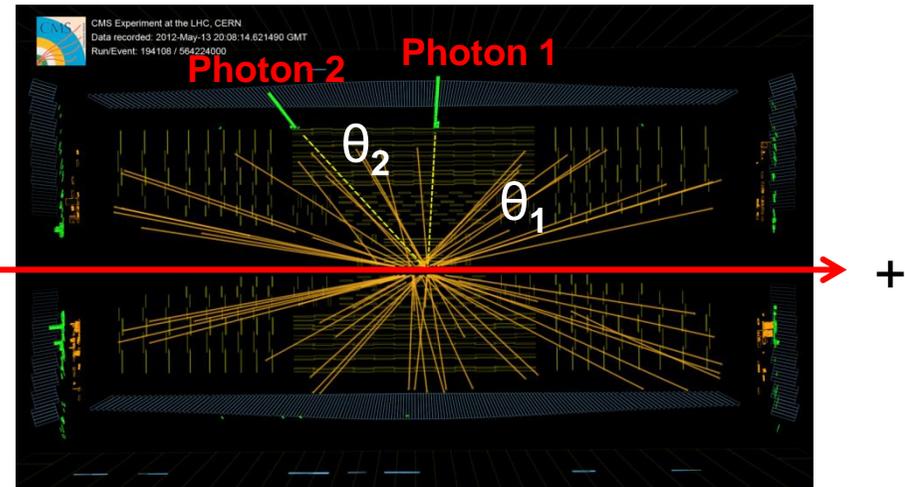


## Transverse view

Angle of the photons in the r-phi plane,  $\Phi_1$  and  $\Phi_2$

$$\Phi_1 = 0.719 \text{ radians}$$

$$\Phi_2 = 2.800 \text{ radians}$$



## Longitudinal view

Angle of the photons wrt the +ve direction of the beam axis,  $\theta_1$  and  $\theta_2$

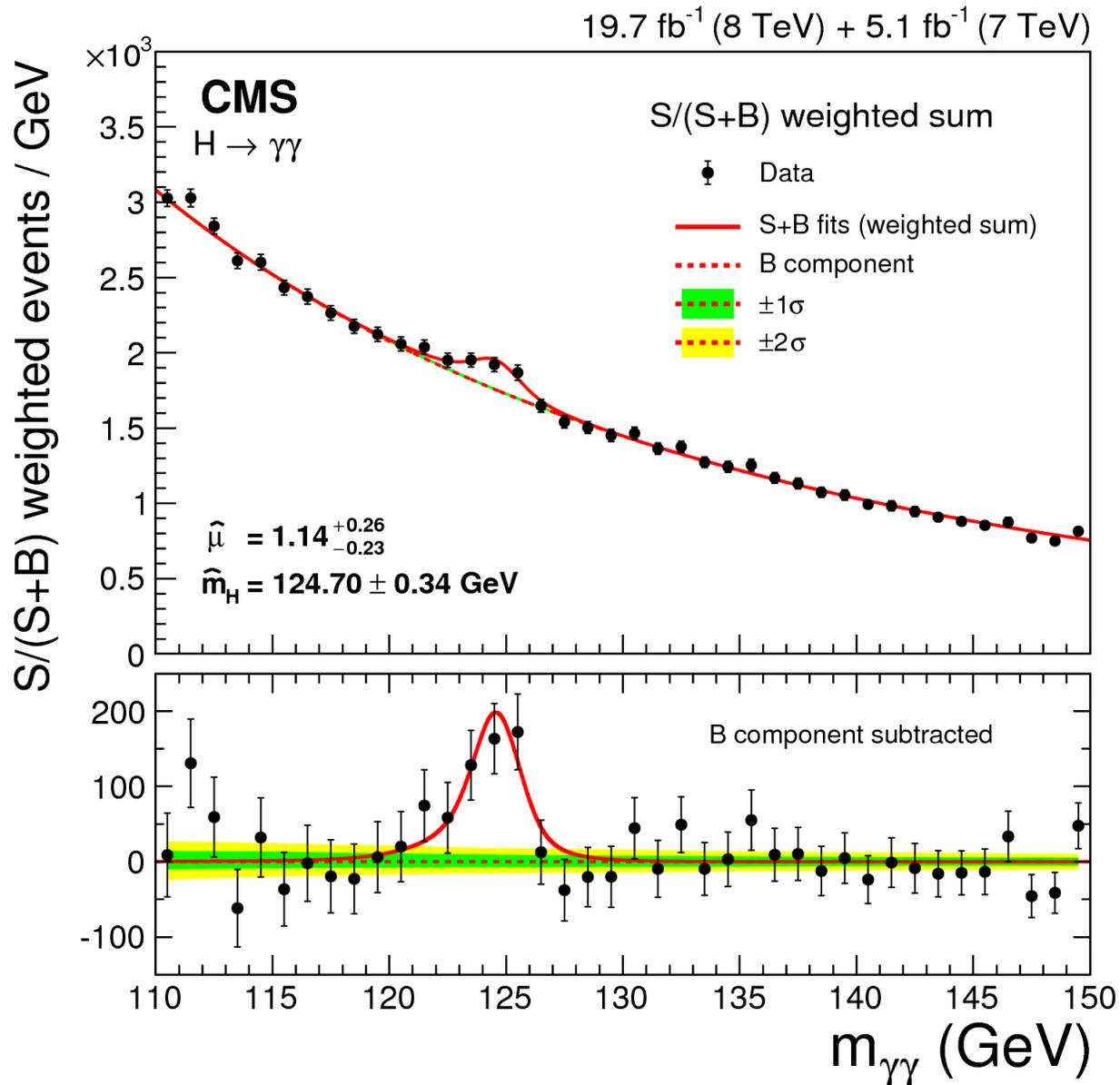
$\theta$  related to pseudo-rapidity ( $\eta$ ) by

$$\eta = -\ln [ \tan ( \theta/2 ) ]$$

$$\eta_1 = 0.0623$$

$$\eta_2 = -0.8110$$

# The crowning glory of CMS (and ATLAS) calorimetry!



# Summary

## Calorimetry a key detector technique for particle physics

In this talk, calorimetry for photons/electrons from  $\sim 1$  MeV, to  $O(50$  GeV) for Z decays, to  $O(1$  TeV) for jets

Calorimeters playing a crucial role for physics at the LHC, eg  $H \rightarrow \gamma\gamma$ ,  $Z' \rightarrow ee$ , SUSY (missing  $E_T$ )

Calorimeters indispensable for neutrino physics

Wide variety of technologies available. Calorimeter design is dictated by physics goals, experimental constraints and cost. Compromises necessary.

### References:

Electromagnetic Calorimetry, Brown and Cockerill, NIM-A 666 (2012) 47–79

Calorimetry for particle physics, Fabian and Gianotti, Rev Mod Phys, 75, 1243 (2003)

Calorimetry, Energy measurement in particle physics, Wigmans, OUP (2000)

# Backups

# Future directions in Calorimetry

## The International Linear Collider (ILC)

### Use Particle Flow, aided by finely segmented calorimetry

Very high transverse segmentation

ECAL  $\sim 1 \times 1 \text{ cm}^2$  SiW cells – CALICE

HCAL  $\sim 3 \times 3 \text{ cm}^2$  Steel/scintillator

High longitudinal sampling

30 layers ECAL and 40 layers HCAL

## CALICE prototype

1.4/2.8/4.2 mm thick W plates ( $30X_0$ )

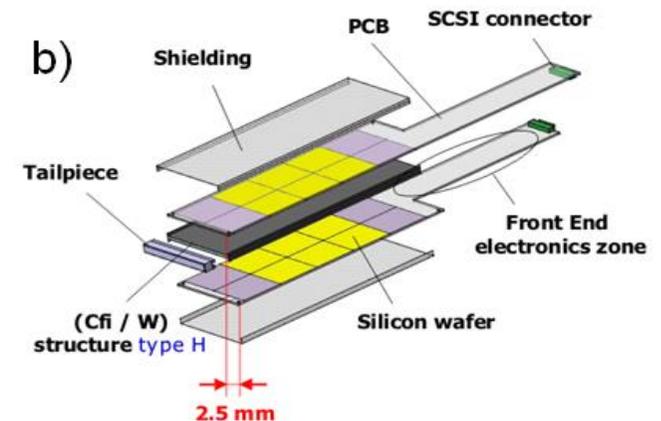
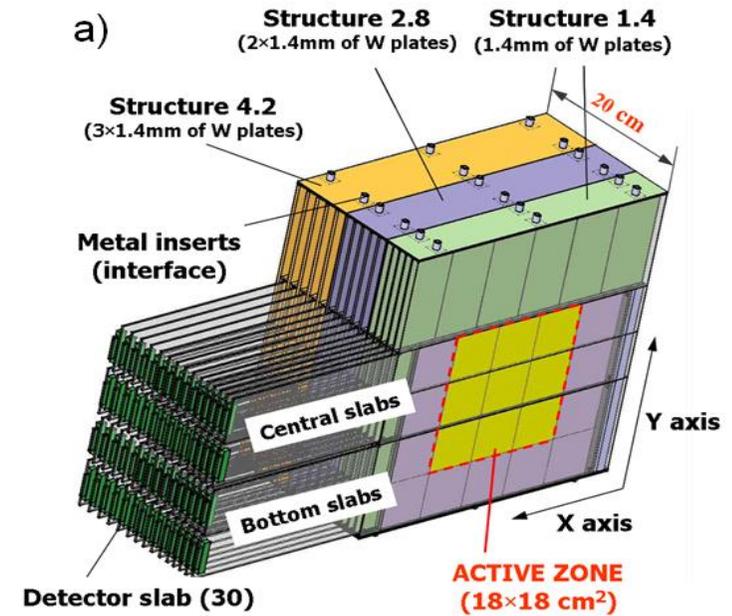
Interleaved with Silicon wafers

Read out at level of  $1 \times 1 \text{ cm}^2$  pads

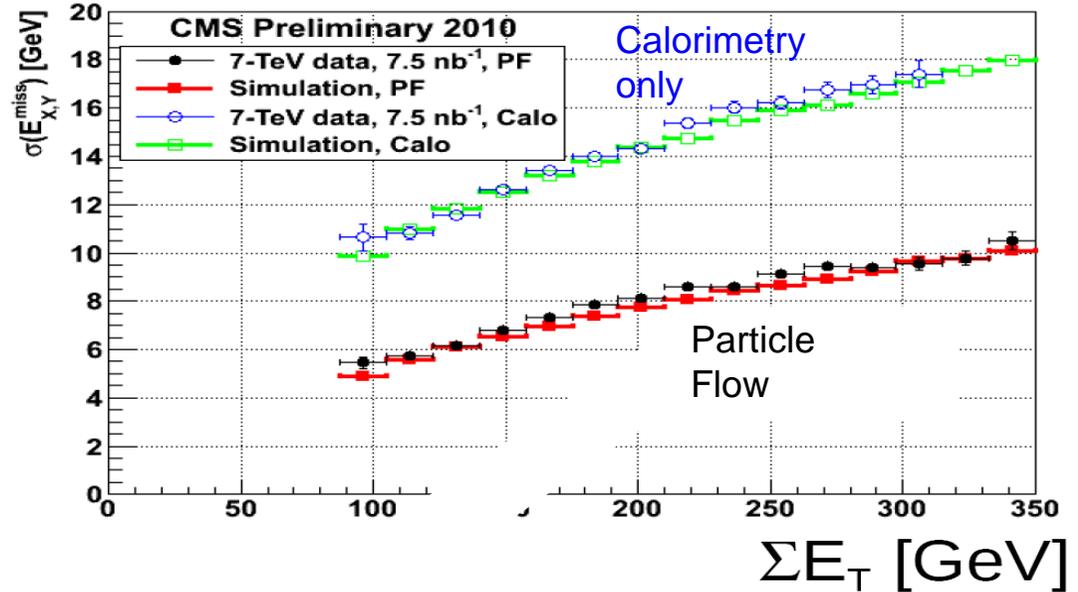
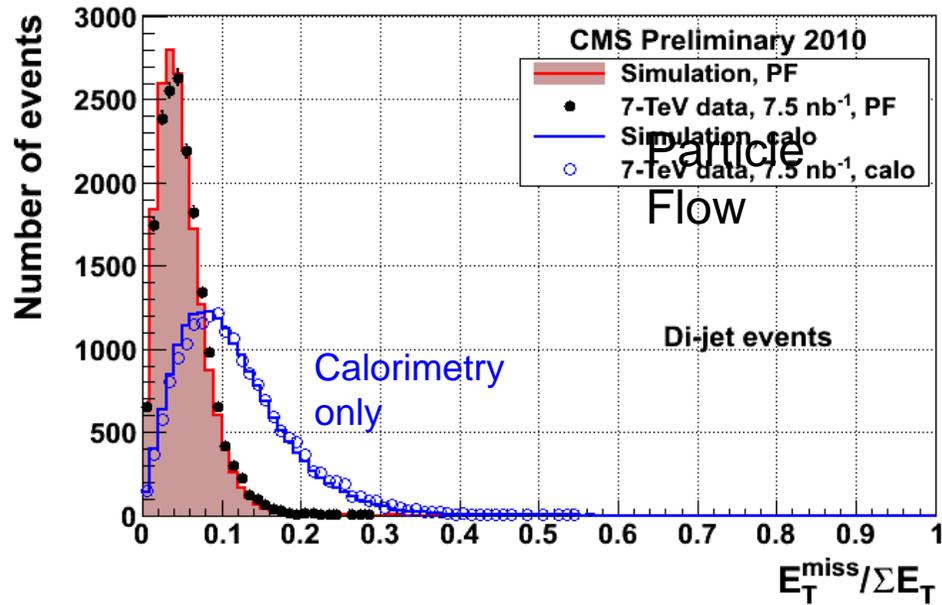
## Resolution for electrons

Stochastic term  $a \sim 17\%$

Constant term  $c \sim 1.1\%$



# Particle Flow Calorimetry in CMS



Missing  $E_T$  normalised to the total transverse energy for Di-jet events in CMS

Missing  $E_T$  resolution for Di-jet events

CMS missing  $E_T$  resolution  $< 10$  GeV over whole  $\Sigma E_T$  range up to 350 GeV  
 Factor 2 improvement on calorimetry by using Particle Flow technique

# Energy resolution of hadronic calorimeters

## Consequences for $e/h \neq 1$

- response with energy is non-linear
- fluctuations on  $F_{\pi^0}$  contribute to  $\sigma_E/E$

Since the fluctuations are non-Gaussian,

- $\sigma_E/E$  scales more weakly than  $1/\sqrt{E}$ , more as  $1/E$

Deviations from  $e/h = 1$  also contribute to the constant term

## 'Compensating' sampling hadron calorimeters

Retrieve  $e/h = 1$  by compensating for the loss of invisible energy, several approaches:

- Weighting energy samples with depth
- Use large elastic cross section for MeV neutrons scattering off hydrogen in the organic scintillator
- Use  $^{238}\text{U}$  as absorber.  $^{238}\text{U}$  fission is exothermic. Release of additional neutrons

## Neutrons liberate recoil protons in the active material

Ionising protons contribute directly to the signal

Tune absorber/scintillator thicknesses for  $e/h = 1$

Example Zeus:  $^{238}\text{U}$  plates (3.3mm)/scintillator plates (2.6mm), total depth 2m,  $e/h = 1$   
Stochastic term  $0.35/\sqrt{E(\text{GeV})}$

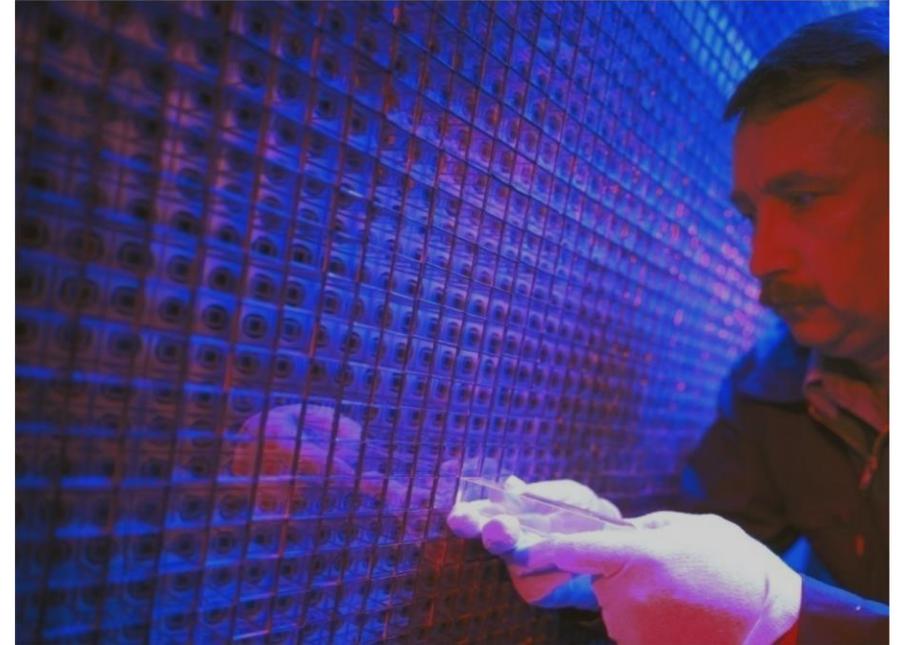
Additional degradation to resolution, calorimeter imperfections :

Inter-calibration errors, response non-uniformity (laterally and in depth), energy leakage, cracks

# Homogeneous electromagnetic calorimeters

## ALICE at the LHC – scintillating $\text{PbWO}_4$ crystals

Avalanche photo diode readout



Some of the 17,920  $\text{PbWO}_4$  crystals for ALICE (PHOS)

# Homogeneous calorimeters

## Homogeneous calorimeters

Three main types: Scintillating crystals    Glass blocks (Cerenkov radiation)    Noble liquids

Crystals	NaI(Tl)	<u>CsI(Tl)</u>	CsI	BGO	<u>PbWO<sub>4</sub></u>
Density (g/cm <sup>3</sup> )	3.67	4.53	4.53	7.13	8.28
$X_0$ (cm)	2.59	1.85	1.85	1.12	0.89
$R_M$ (cm)	4.5	3.8	3.8	2.4	2.2
<u>Decay time (ns)</u>	250	<u>1000</u>	10	300	<u>5</u>
slow component			36		15
Emission peak (nm)	410	565	305	410	440
slow component			480		
<u>Light yield <math>\gamma</math>/MeV</u>	$4 \times 10^4$	<u><math>5 \times 10^4</math></u>	$4 \times 10^4$	$8 \times 10^3$	<u><math>1.5 \times 10^2</math></u>
Photoelectron yield (relative to NaI)	1	0.4	0.1	0.15	0.01
Rad. hardness (Gy)	1	10	$10^3$	1	$10^5$

### Lead glass, SF-6

OPAL at LEP

$X_0 = 1.69\text{cm}$ ,

$\rho = 5.2\text{ g/cm}^3$

**Barbar  
@PEPII  
10ms  
inter'n rate  
good light  
yield, good**

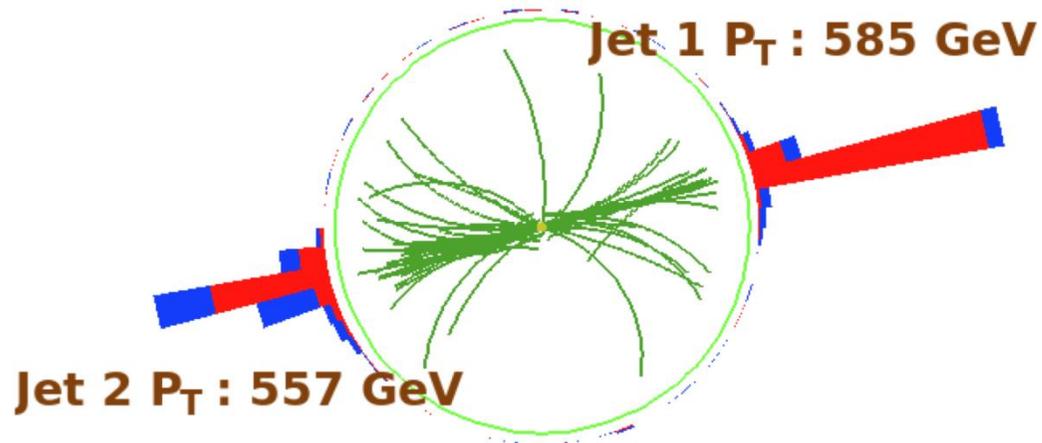
**KTeV at  
Tevatron,  
High rate,  
Good  
resolution**

**L3@LEP,  
25 $\mu$ s bunch  
crossing,  
Low rad'n  
dose**

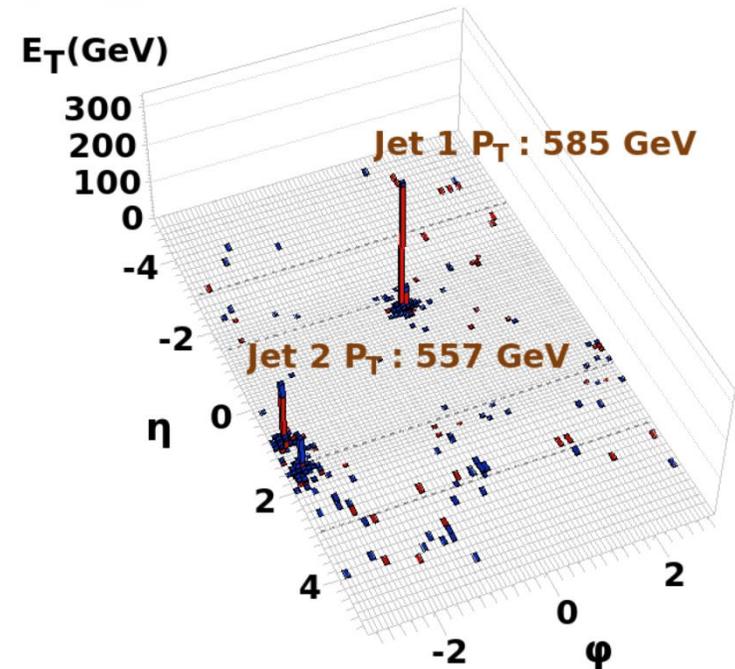
**CMS at LHC  
25ns bunch  
crossing,  
high radiation  
dose  
ALICE  
PANDA**

# The Power of Calorimetry

## A high energy DiJet event in CMS



**Run : 138919**  
**Event : 32253996**  
**Dijet Mass : 2.130 TeV**



Calorimeter energy  
deposits on  $\eta \times \phi$  map  
ECAL red, HCAL blue

**A high mass dijet event in the first  $120\text{nb}^{-1}$  of data, at 2.13 TeV  
taken in CMS with pp collisions at 7 TeV, July 2010**

## Extra info – em shower depth

How many  $X_0$  to adequately contain an em shower?

Rule of thumb

RMS spread in shower leakage at the back  $\sim 0.5$  \* average leakage at the back

CMS - keep rms spread  $< 0.3\%$   $\Rightarrow$  leakage  $< 0.65\%$   $\Rightarrow$  crystals  $25X_0$  (23cm) long

Other relations

$$\langle t_{95\%} \rangle \sim t_{max} + 0.08Z + 9.6$$

$$\langle t_{98\%} \rangle \sim 2.5 t_{max}$$

$$\langle t_{98\%} \rangle \sim t_{max} + 4 \lambda_{att}$$

Tail of cascade - photons of a few MeV  $\sim$  at the min in the mass attenuation coefficient

$\lambda_{att} \sim 3.4X_0$   $\sim$  photon mean free path.

$\lambda_{att}$  is associated with the exponential decrease of the shower after  $t_{max}$

### Comment, em longitudinal profile, Pb versus Cu:

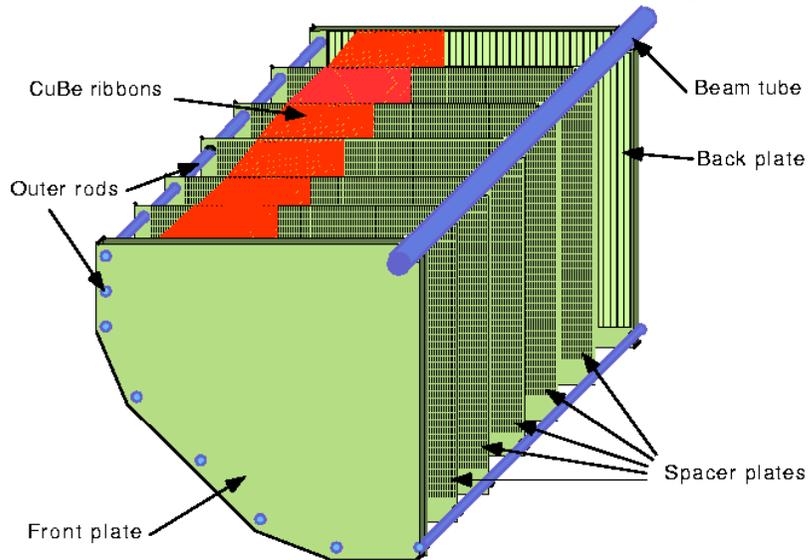
The coulomb field in Pb,  $Z=82$  with  $E_c = 7.3$  MeV means that bremstrahlung dominates over ionisation to much lower shower particle energies than for example in Cu,  $Z=29$  with  $E_c = 20.2$  MeV

As a consequence the depth (in  $X_0$ ) of a shower proceeds further in Pb than in Cu.

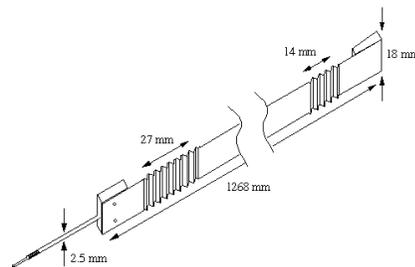
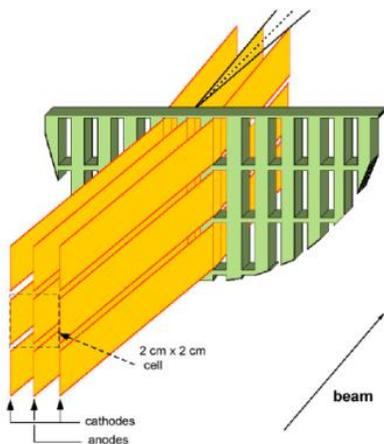
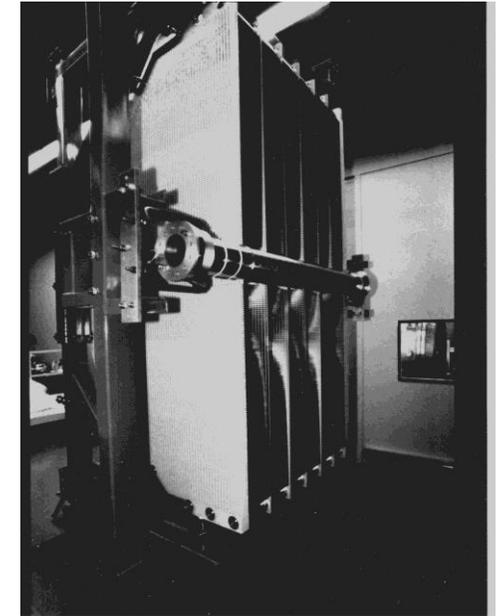
# Homogeneous liquid Kr electromagnetic calorimeters

NA48 Liquid Krypton Ionisation chamber (T = 120K)

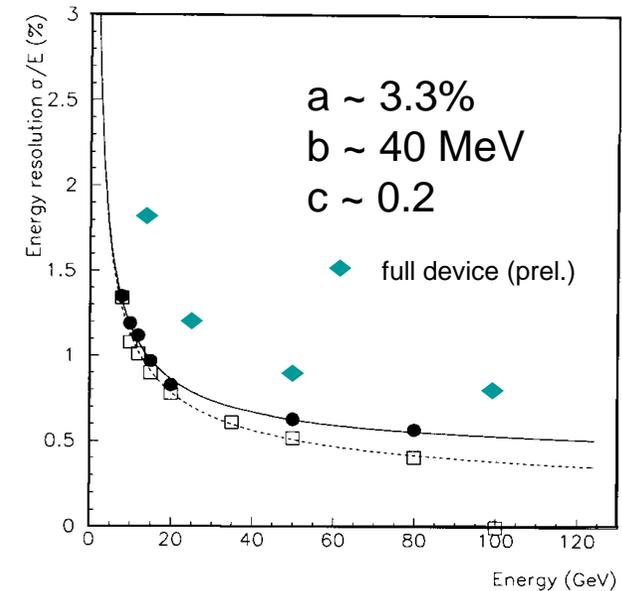
No metal absorbers: quasi homogeneous



**NA48 Liquid Krypton**  
**2cmx2cm cells**  
 $X_0 = 4.7\text{cm}$   
**125cm length (27 $X_0$ )**  
 $\rho = 5.5\text{cm}$



Cu-Be ribbon electrode



# Homogeneous calorimetry

## CMS PbWO<sub>4</sub> - photodetectors

### Barrel

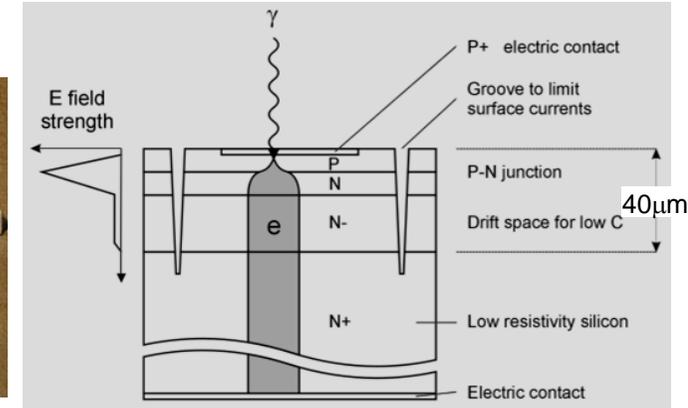
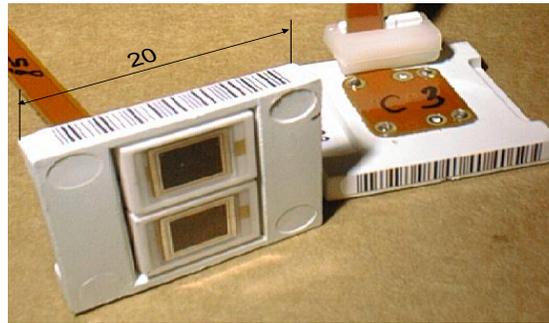
#### Avalanche photodiodes(APD)

Two 5x5 mm<sup>2</sup> APDs/crystal

Gain 50

QE ~75%

Temperature dependence -2.4%/°C

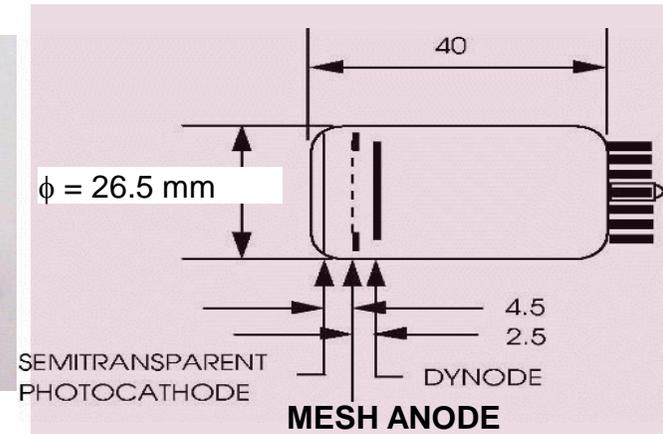


### Endcaps

#### Vacuum phototriodes(VPT)

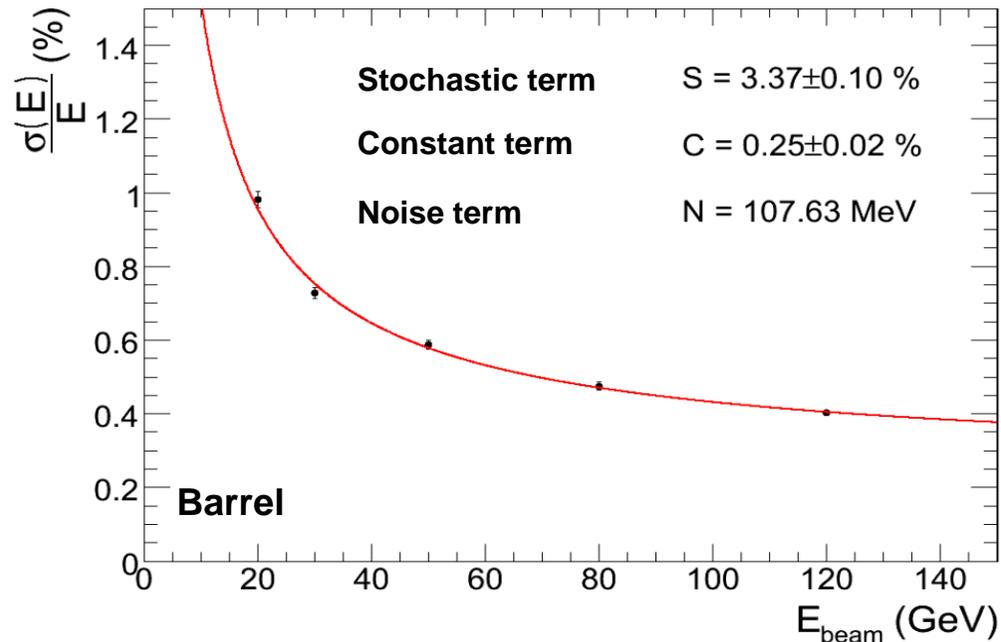
More radiation resistant than Si diodes

- UV glass window
- Active area ~ 280 mm<sup>2</sup>/crystal
- Gain 8 -10 (B=4T)
- Q.E. ~20% at 420nm



# Homogeneous e.m. calorimeters

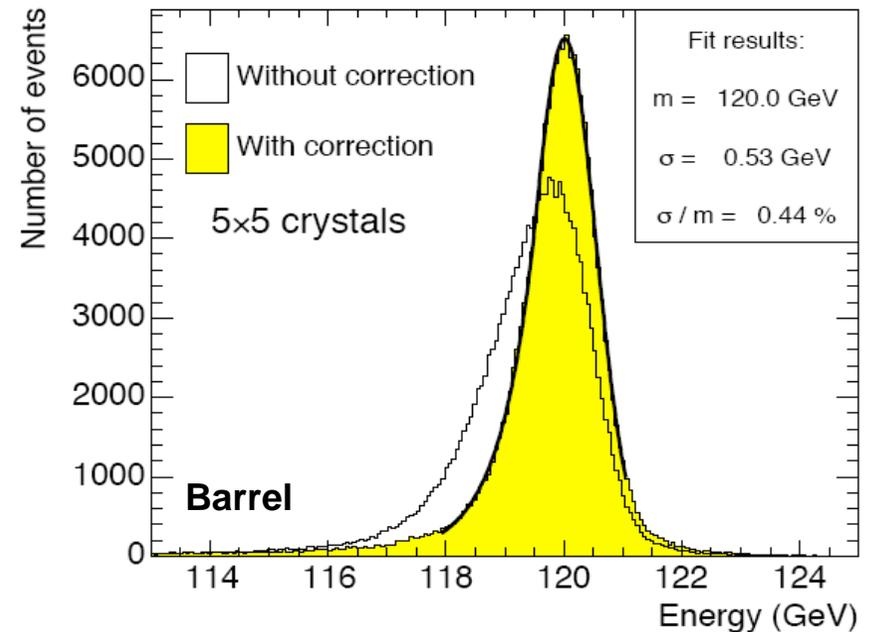
## PbWO<sub>4</sub> - CMS ECAL energy resolution



**Electron energy resolution  
as a function of energy**

**Electrons centrally (4mmx4mm)  
incident on crystal**

**Resolution 0.4% at 120 GeV**



**Energy resolution at 120 GeV**

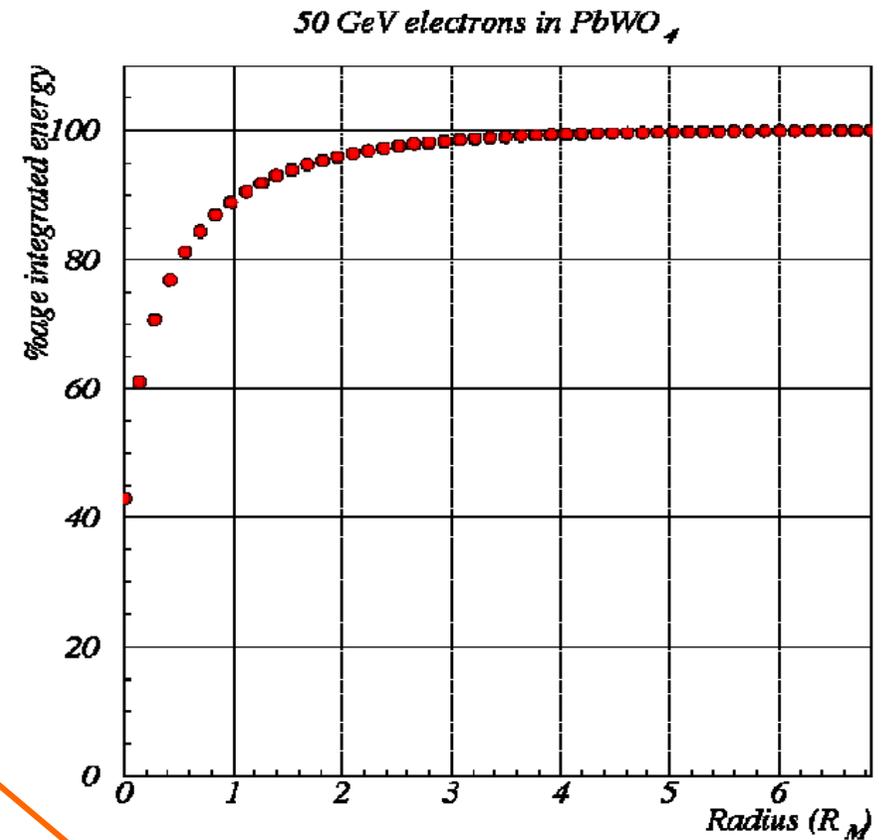
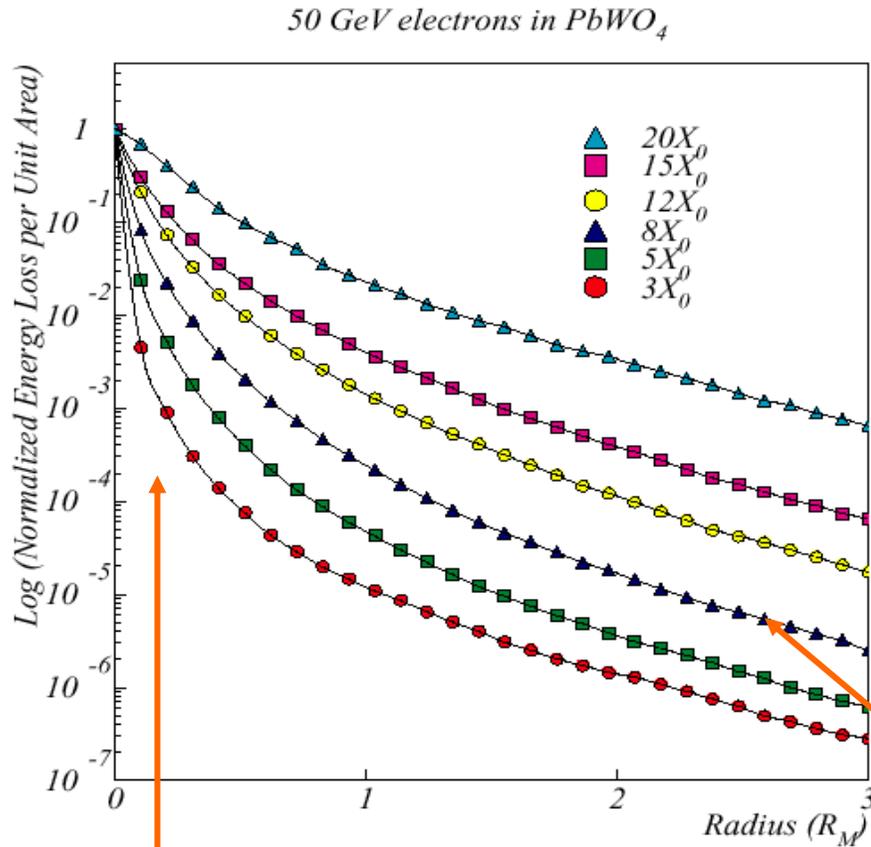
**Electrons incident over full crystal face**

**Energy sum over 5x5 array wrt hit crystal.**

**Universal position 'correction function' for  
the reconstructed energy applied**

**Resolution 0.44%**

# EM showers: transverse profile



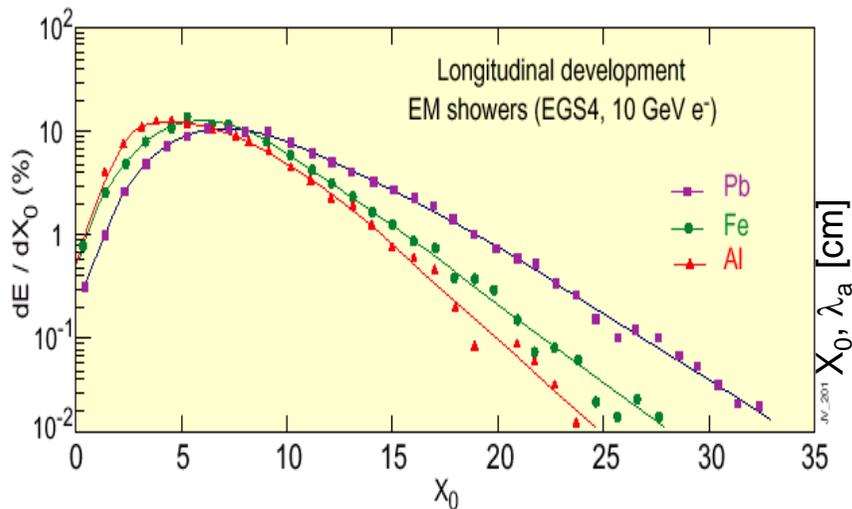
Central core: multiple scattering

Peripheral halo: propagation of less attenuated photons, widens with depth of the shower

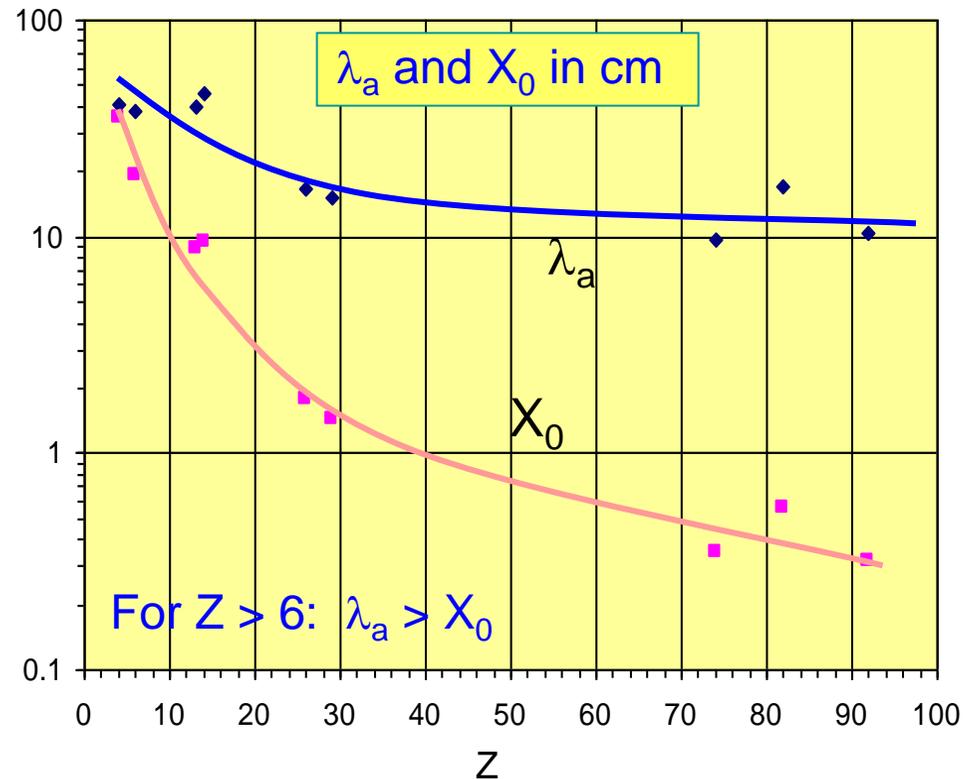
# EM showers, longitudinal profile

## Shower parametrization

$$\frac{dE}{dt} \propto t^\alpha e^{\beta t}$$

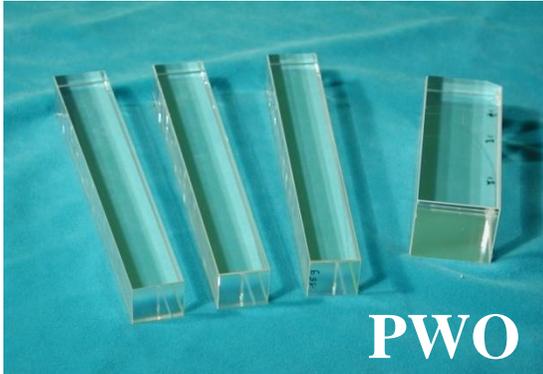


Material	Z	A	$\rho$ [g/cm <sup>3</sup> ]	$X_0$ [g/cm <sup>2</sup> ]	$\lambda_a$ [g/cm <sup>2</sup> ]
Hydrogen (gas)	1	1.01	0.0899 (g/l)	63	50.8
Helium (gas)	2	4.00	0.1786 (g/l)	94	65.1
Beryllium	4	9.01	1.848	65.19	75.2
Carbon	6	12.01	2.265	43	86.3
Nitrogen (gas)	7	14.01	1.25 (g/l)	38	87.8
Oxygen (gas)	8	16.00	1.428 (g/l)	34	91.0
Aluminium	13	26.98	2.7	24	106.4
Silicon	14	28.09	2.33	22	106.0
Iron	26	55.85	7.87	13.9	131.9
Copper	29	63.55	8.96	12.9	134.9
Tungsten	74	183.85	19.3	6.8	185.0



# Crystals: building blocks

These crystals make light!



Crystals are basic components of electromagnetic calorimeters aiming at precision

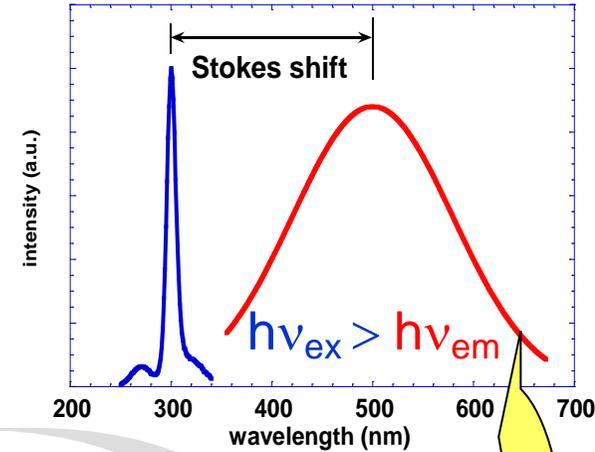


# Scintillation: a three step process

Scintillator + Photo Detector = Detector

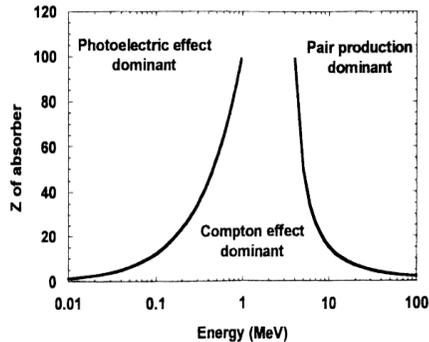
PMT, PD, APD

How does it work



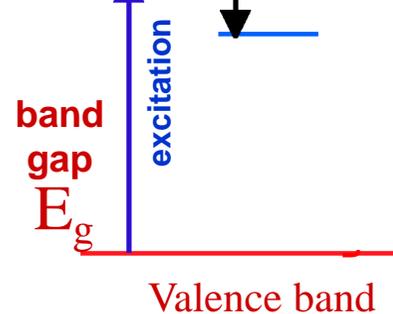
absorption e.g.  $\gamma$

$$I(E) = I_0(E)e^{-\mu d}$$

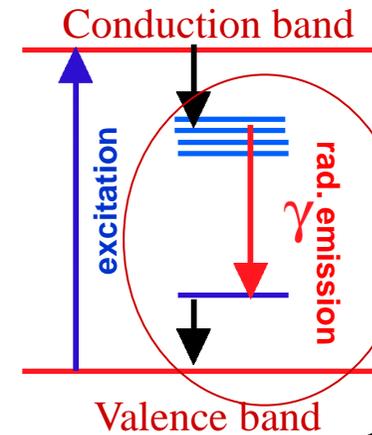


conversion

Energy  $\rightarrow$  Excitation  
Conduction band



emission



# Scintillating crystals

Variation in the lattice  
(e.g. defects and impurities)



local electronic energy levels in the energy gap

If these levels are unoccupied electrons moving in the conduction band may enter these centres

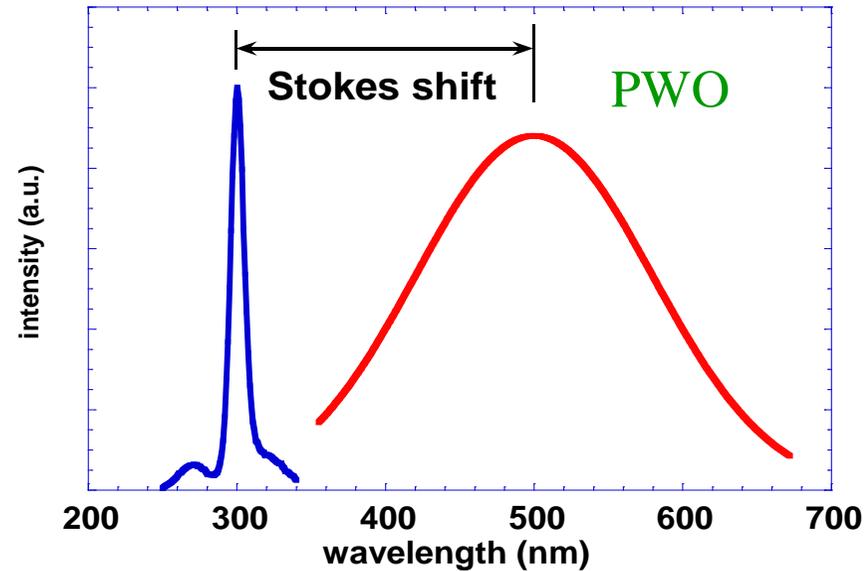
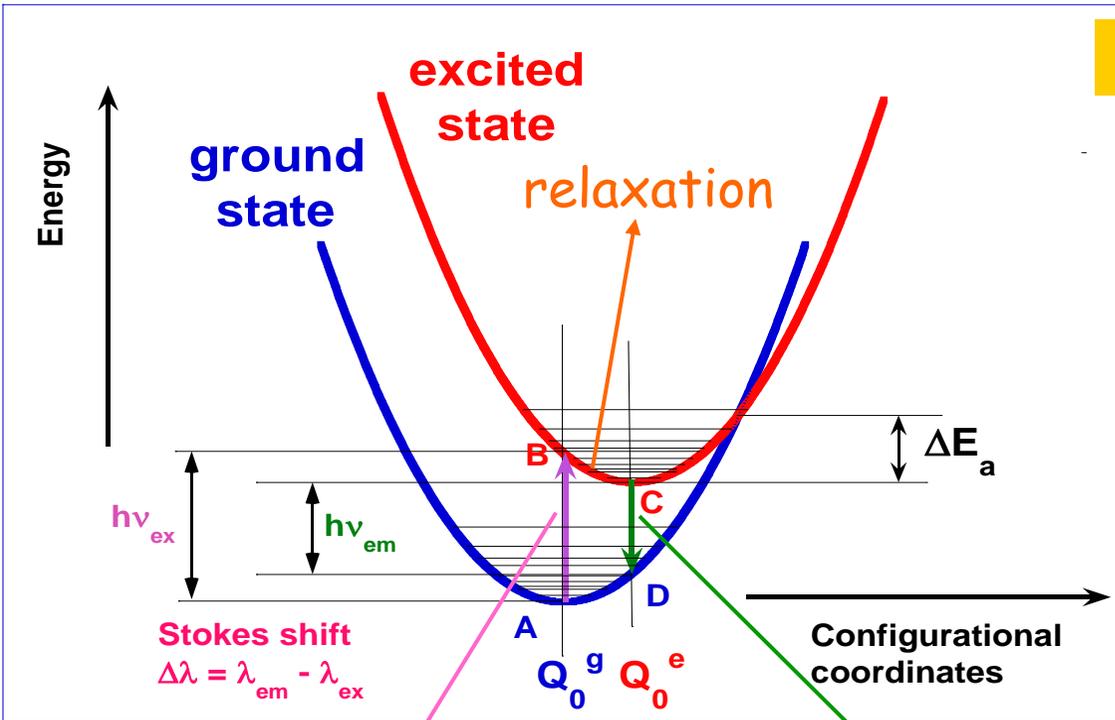
The centres are of three main types:

- **Luminescence centres** in which the transition to the ground state is accompanied by photon emission
- **Quenching centres** in which radiationless thermal dissipation of excitation energy may occur
- **Traps** which have metastable levels from which the electrons may subsequently return to the conduction band by acquiring thermal energy from the lattice vibrations or fall to the valence band by a radiationless transition

# Scintillating crystals



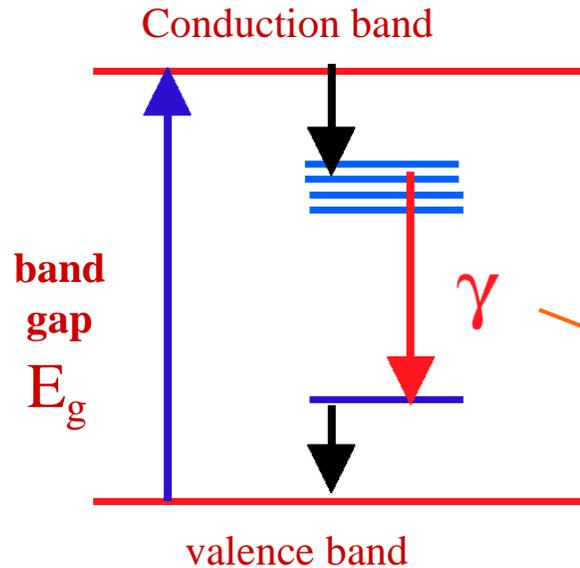
**PbWO<sub>4</sub>:  $\lambda_{\text{excit}}=300\text{nm}$  ;  $\lambda_{\text{emiss}}=500\text{nm}$**



excitation

radiative emission

# Scintillating crystals



$$E_{\text{dep}} \rightarrow \text{e-h}$$

$$E_s = \beta E_g \quad \beta > 1$$

$$N_{\text{eh}} = E_{\text{dep}} / \beta E_g$$

$$N_\gamma = SQN_{\text{eh}}$$

Efficiency of transfer to luminescent centres

radiative efficiency of luminescent centres

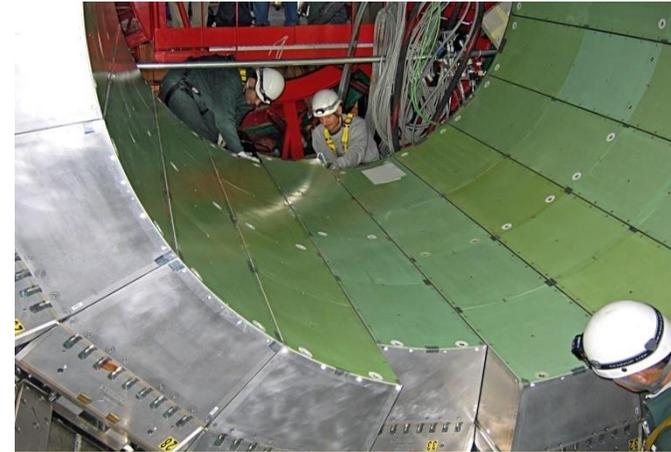
$$\eta_\gamma = N_\gamma / E_{\text{dep}} = SQN_{\text{eh}} / E_{\text{dep}} = SQ / \beta E_g$$

- $S, Q \approx 1$ ,  $\beta E_g$  as small as possible
- medium transparent to  $\lambda_{\text{emiss}}$

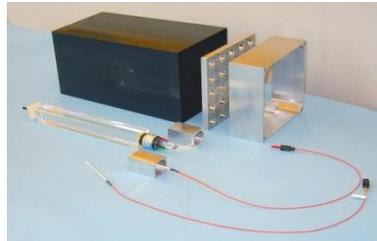
# CMS Barrel and Endcap Homogeneous ECAL



**A CMS Supermodule with 1700 tungstate crystals**



**Installation of the last SM into the first half of the barrel**

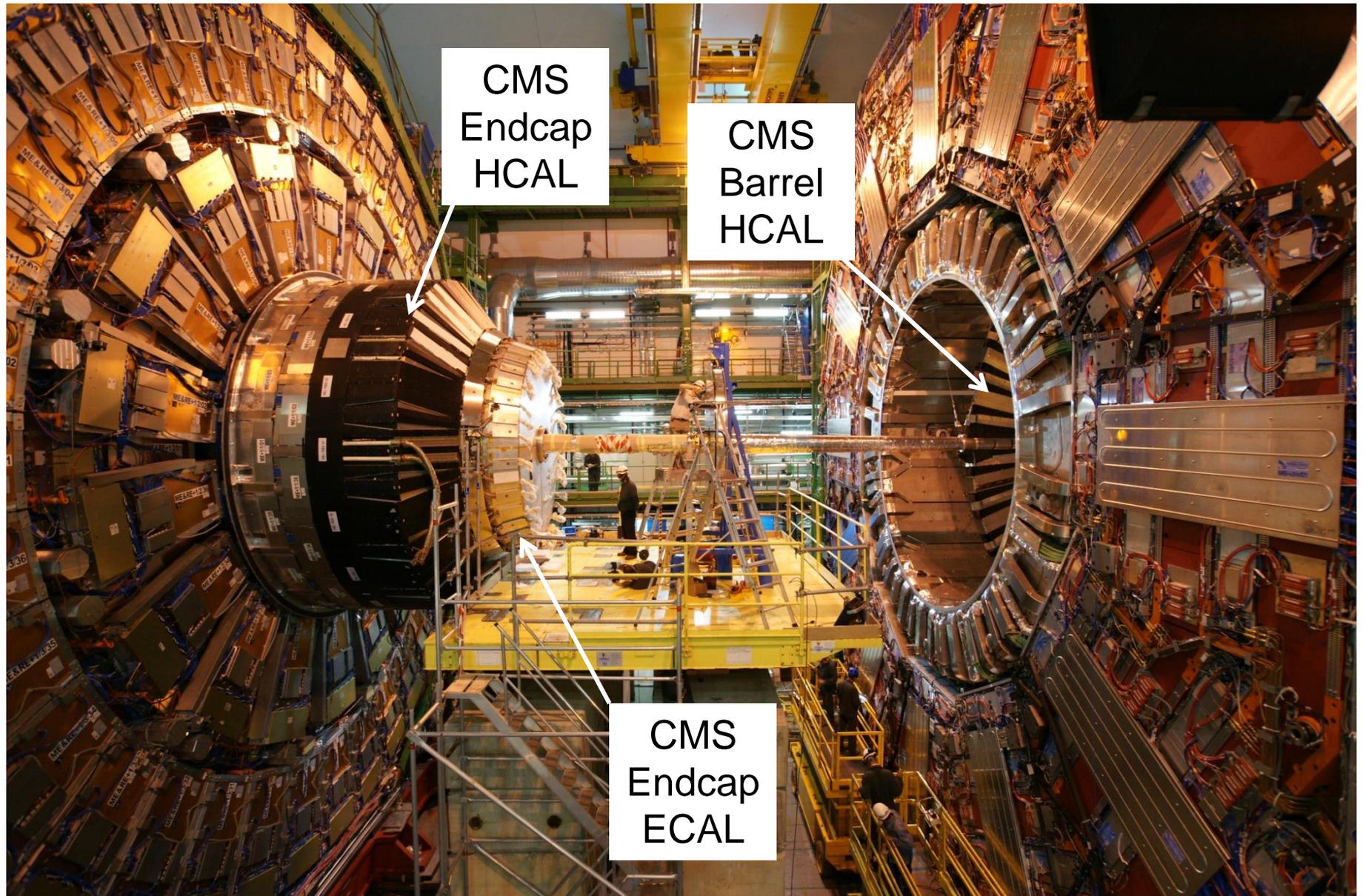


**A CMS endcap 'supercrystal' 25 crystals/VPTs**

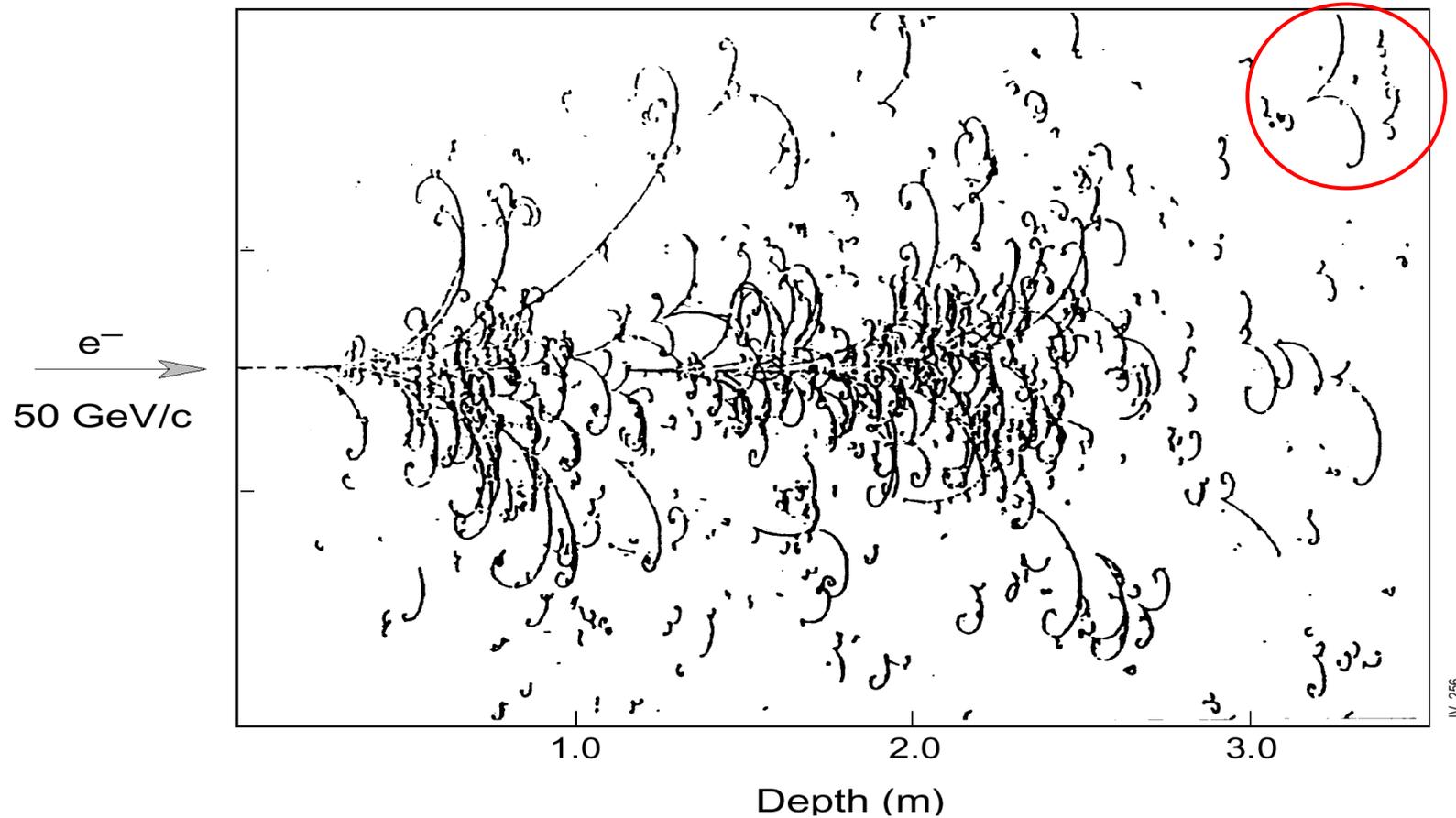
Copper has been selected as the absorber material because of its density. The HB is constructed of two half-barrels each of 4.3 meter length. The HE consists of two large structures, situated at each end of the barrel detector and within the region of high magnetic field. Because the barrel HCAL inside the coil is not sufficiently thick to contain all the energy of high energy showers, additional scintillation layers (HOB) are placed just outside the magnet coil. The full depth of the combined HB and HOB detectors is approximately 11 absorption lengths.

The hadron barrel (HB) and hadron endcap (HE) calorimeters are sampling calorimeters with 50 mm thick copper absorber plates which are interleaved with 4 mm thick scintillator sheets.

# CMS Hadron sampling calorimetry



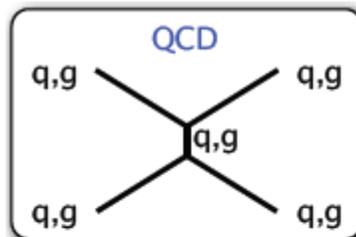
# Electromagnetic shower



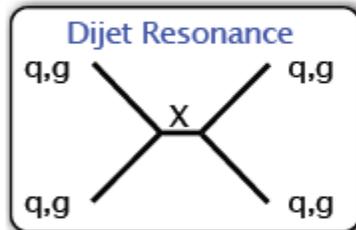
**Big European Bubble Chamber filled with Ne:H<sub>2</sub> = 70%:30%,  
3T Field, L=3.5 m, X<sub>0</sub>≈34 cm, 50 GeV incident electron**

# Di-jets

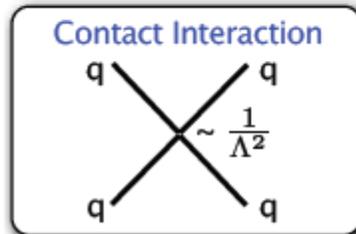
- ◆ We study the inclusive dijet final state using the **dijet mass spectrum** and the **dijet centrality ratio** observables.
- ◆ Together the Dijet Mass and Ratio provide a **test of QCD** and a **sensitive search** for new physics beyond the Standard Model.



- ▶ Dijet mass distribution is a simple check of rate vs dijet mass from QCD and PDFs.
- ▶ Dijet centrality ratio is a detailed measure of QCD dynamics from angular distribution.



- ▶ Dijet mass provides most sensitive “bump” hunt for new particles decaying to dijets.
- ▶ Dijet centrality ratio can confirm that a “bump” is not QCD fluctuation.



- ▶ Dijet centrality ratio is more sensitive than the dijet mass to contact interactions from quark compositeness.
  - when all experimental uncertainties are considered.

# Jet Energy Resolution with stand alone calorimetry

For a single hadronic particle:  $\sigma_E / E = a / \sqrt{E} \oplus c$  (neglect electronic noise)

Jet with low particle energies, resolution is dominated by **a**,  
and at high particle energies by **c**

If the stochastic term, **a**, dominates:

- error on Jet energy  $\sim$  same as for  
a single particle of the same energy

If the constant term dominates:

- error on Jet energy is less than for  
a single particle of the same energy

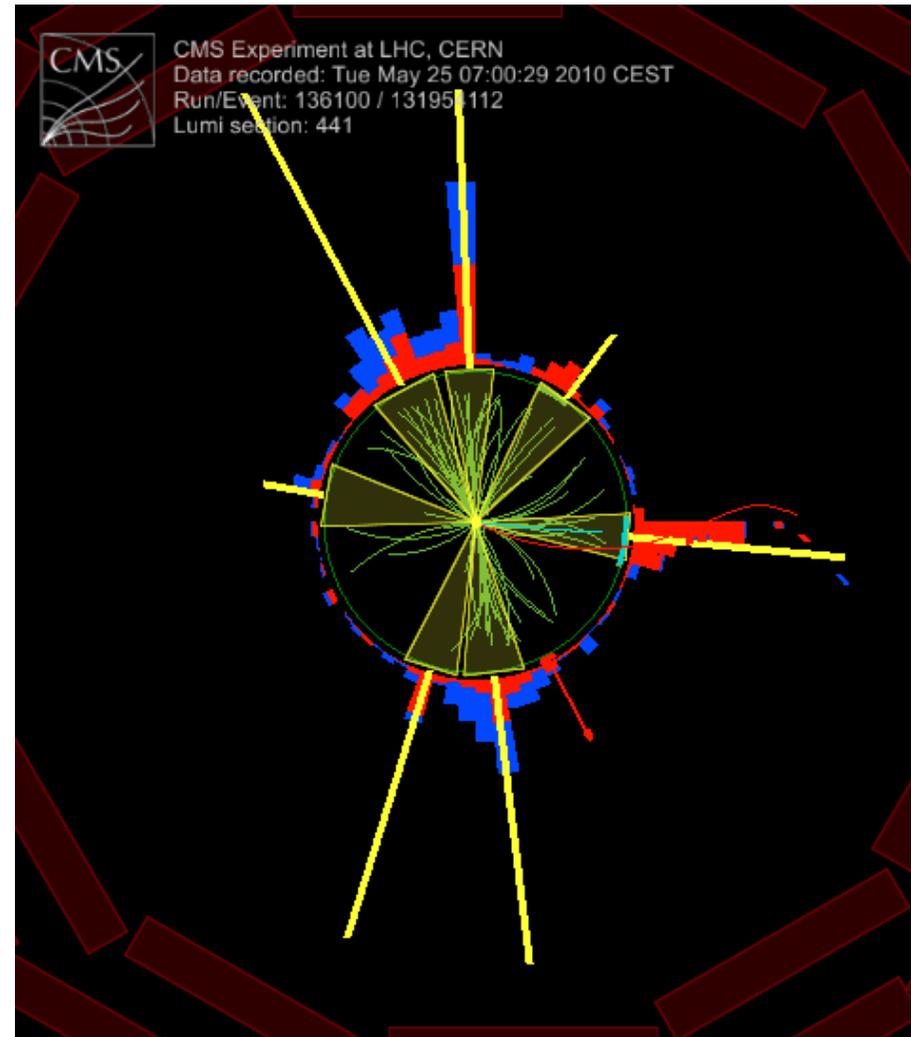
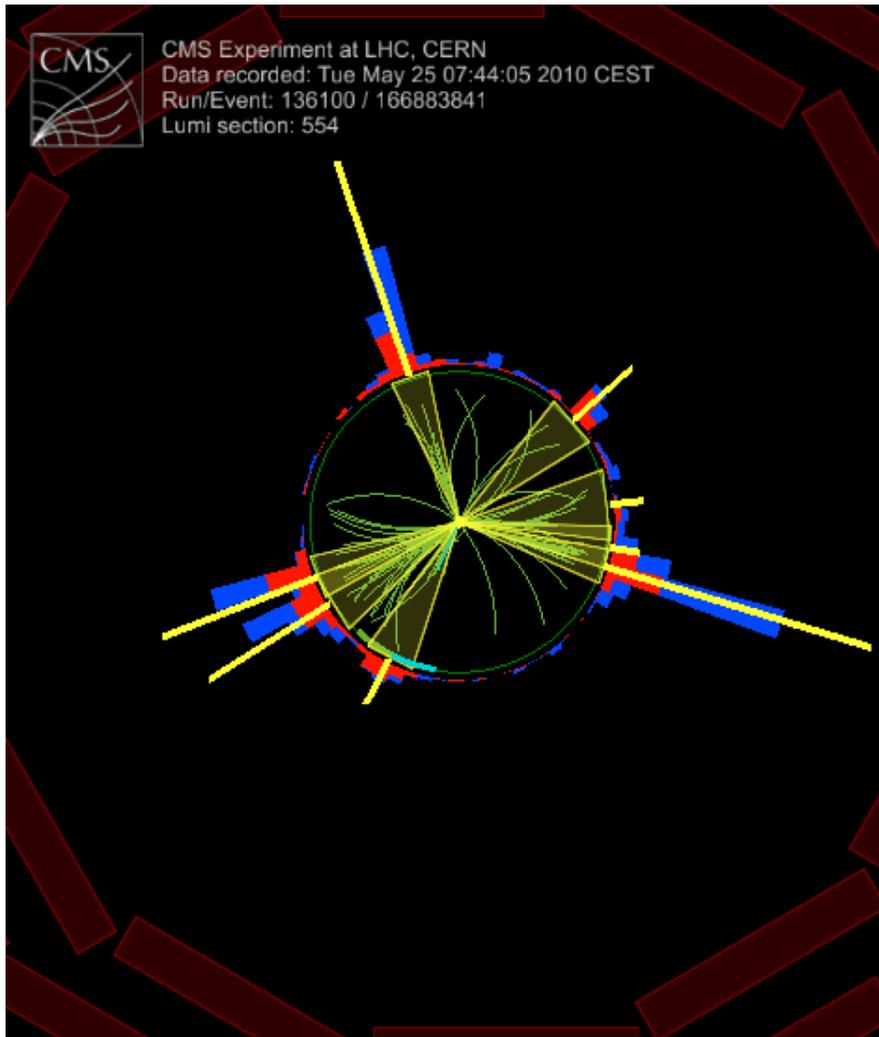
For example:

1 TeV jet composed of four hadrons of equal energy

Calorimeter with  $\sigma_E / E = 0.3 / \sqrt{E} \oplus 0.05$

compared to  $\delta E_{Jet} = 25 \text{ GeV}$ ,  
 $\delta E = 50 \text{ GeV}$ , for a single 1 TeV hadron

# Jet s in CMS at the LHC, pp collisions at 7TeV



Red - ECAL, Blue - HCAL energy deposits  
Yellow – Jet energy vectors