

# Constraints On Dark Energy And Modified Gravity Models From CFHTLenS



Colloquium  
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[www.cfhtlens.org](http://www.cfhtlens.org)



# OUTLINE

- Weak gravitational lensing
- The **CFHT Lensing** survey; data, galaxy shape measurement, systematics
- **CFHTLenS** results: constraints on dark energy, modified gravity (+ Wiggle-Z), mass maps
- Outlook, future lensing surveys, Euclid



# ALL THE FUSS ABOUT LENSING

## From the CFHTLS web page:

[The CFHTS Wide] allows the study of the large scale structures and matter distribution in the universe through [weak lensing](#) and galaxy distribution, as well as the study of clusters of galaxies through morphology and photometric properties of galaxies.

## From the ESO description of KiDS:

The primary science driver for the design of this project has been [weak gravitational lensing](#).

## From Sanchez et al. (2011), “The Dark Energy Survey”:

will start in the fall of 2011 and will study the dark energy properties using four independent methods: galaxy clusters counts and distributions, [weak gravitational lensing](#) tomography, baryon acoustic oscillations and supernovae Ia distances. Obtaining the four measurements

## From the Euclid Red Book:

### Main Scientific Objectives

*Understand the nature of Dark Energy and Dark Matter by:*

- Reach a dark energy  $FoM > 400$  using only [weak lensing](#) and galaxy clustering; this roughly corresponds to 1 sigma errors on  $w_p$  and  $w_a$  of 0.02 and 0.1, respectively.

# WHY ALL THE FUSS?

## Weak gravitational lensing

... probes the matter distribution on large scales

... is sensitive to the total (dark + baryonic) mass

... probes the Universe between  $z \approx 0.1$  and  $\geq 1$

... measures the expansion history and growth rate

outskirts of galaxies, clusters, large-scale structure, cosmology

no assumption needed for relation between galaxies and dark matter

epoch of acceleration

can distinguish between dark energy and modified gravity

# WEAK LENSING OVERVIEW



# HOW DOES IT WORK?

Mass deflects light (Einstein 1915)

Point mass:

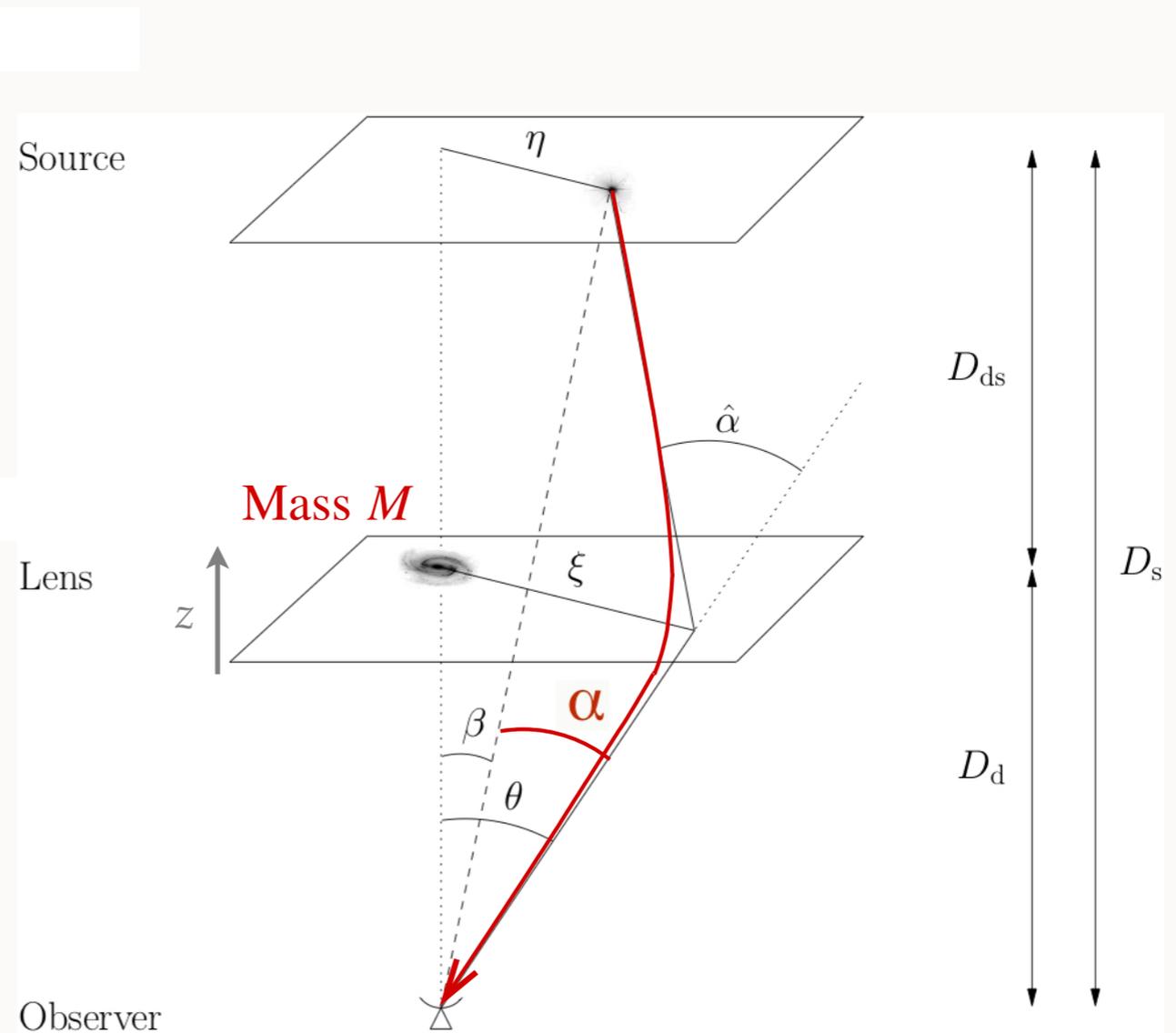
Deflection angle

$$\hat{\alpha} = \frac{4GM}{c^2 \xi}$$

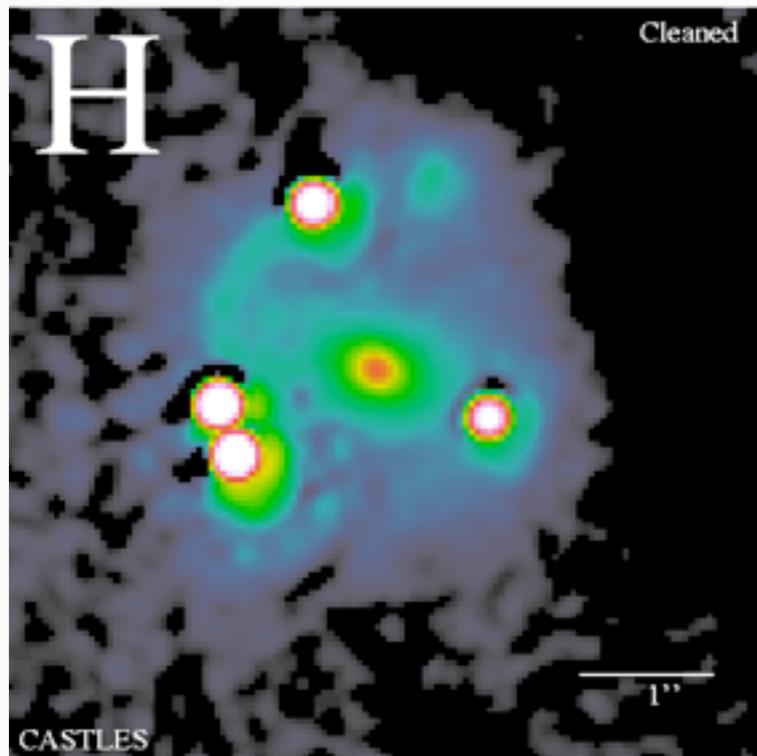
impact parameter

Extended mass distribution:

Deflection angle depends on  
integral over the  
**projected mass distribution**

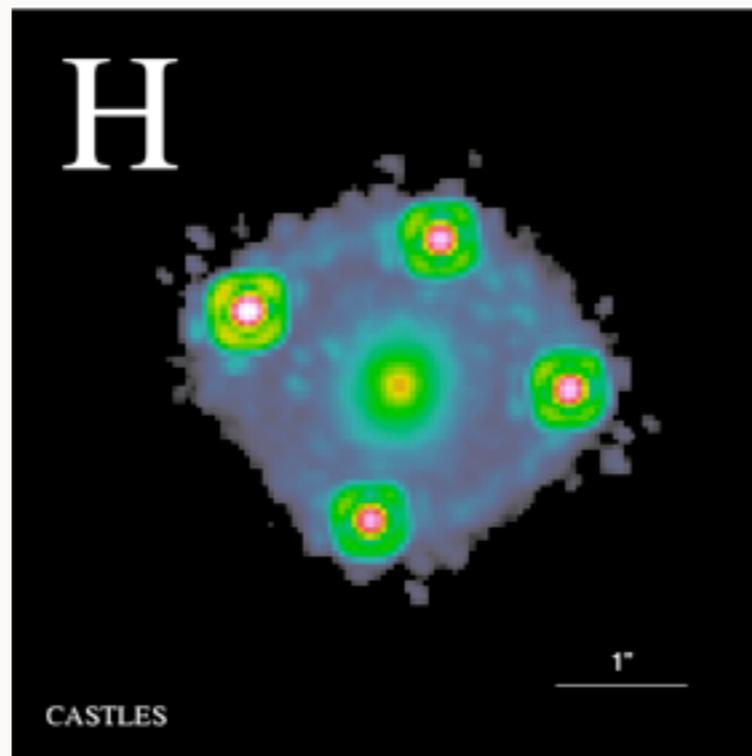


# LENSING MULTIPLICATION



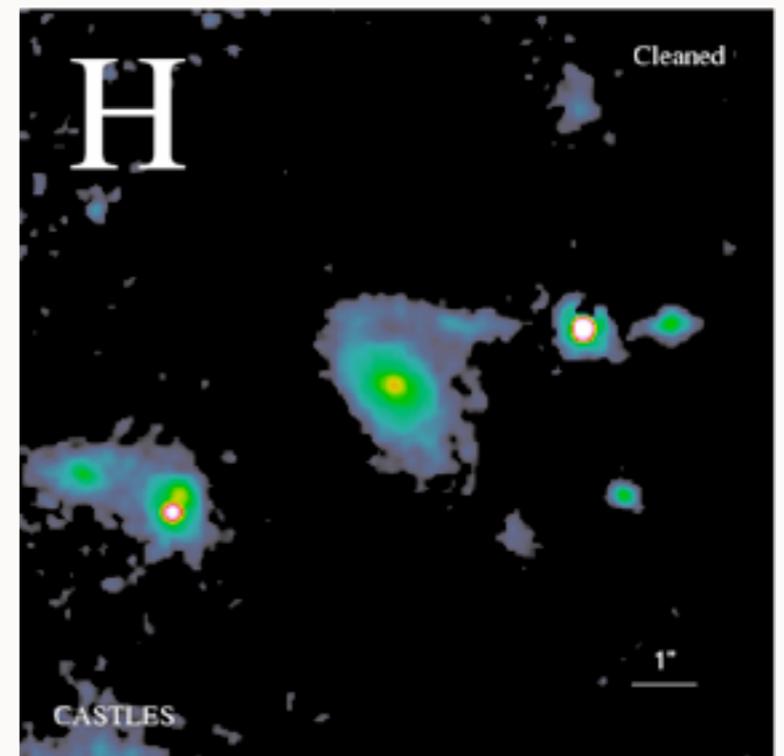
MG0414+0534

$Z_{\text{source}}$  2.64  
 $Z_{\text{lens}}$  0.96



HE0435-1223

1.689  
0.46



RXJ0921+4529

1.65  
0.31

CASTLES survey,

<http://www.cfa.harvard.edu/castles>

# A CLOSER LOOK

- **First order** effect: Deflection of a point source

- **Second order** effect: Differential deflection of an extended source, distortion,

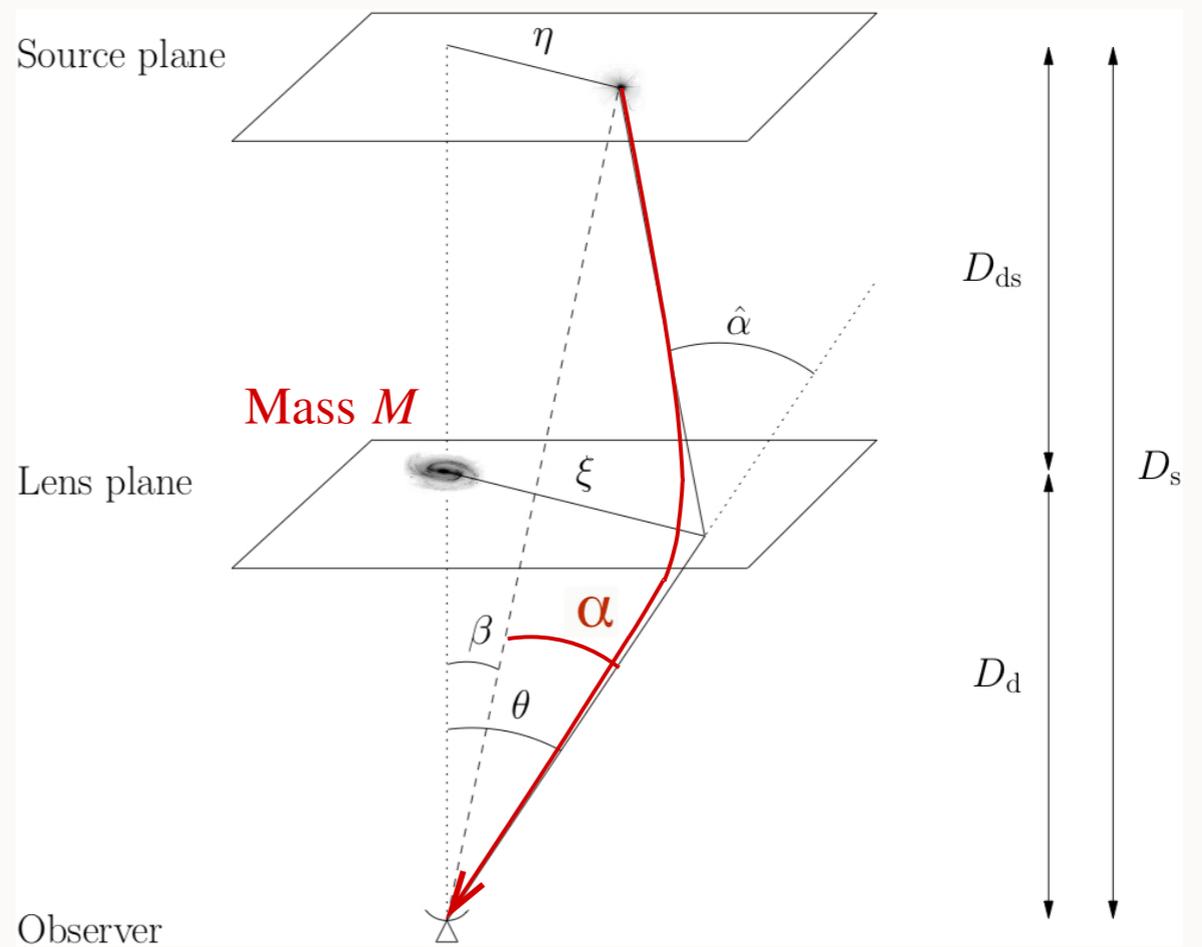
$$\vec{\alpha} = \vec{\alpha}(\vec{\theta})$$

2D angular coordinates

- Deflection angle is a gradient:

$$\vec{\alpha} = \vec{\nabla} \phi$$

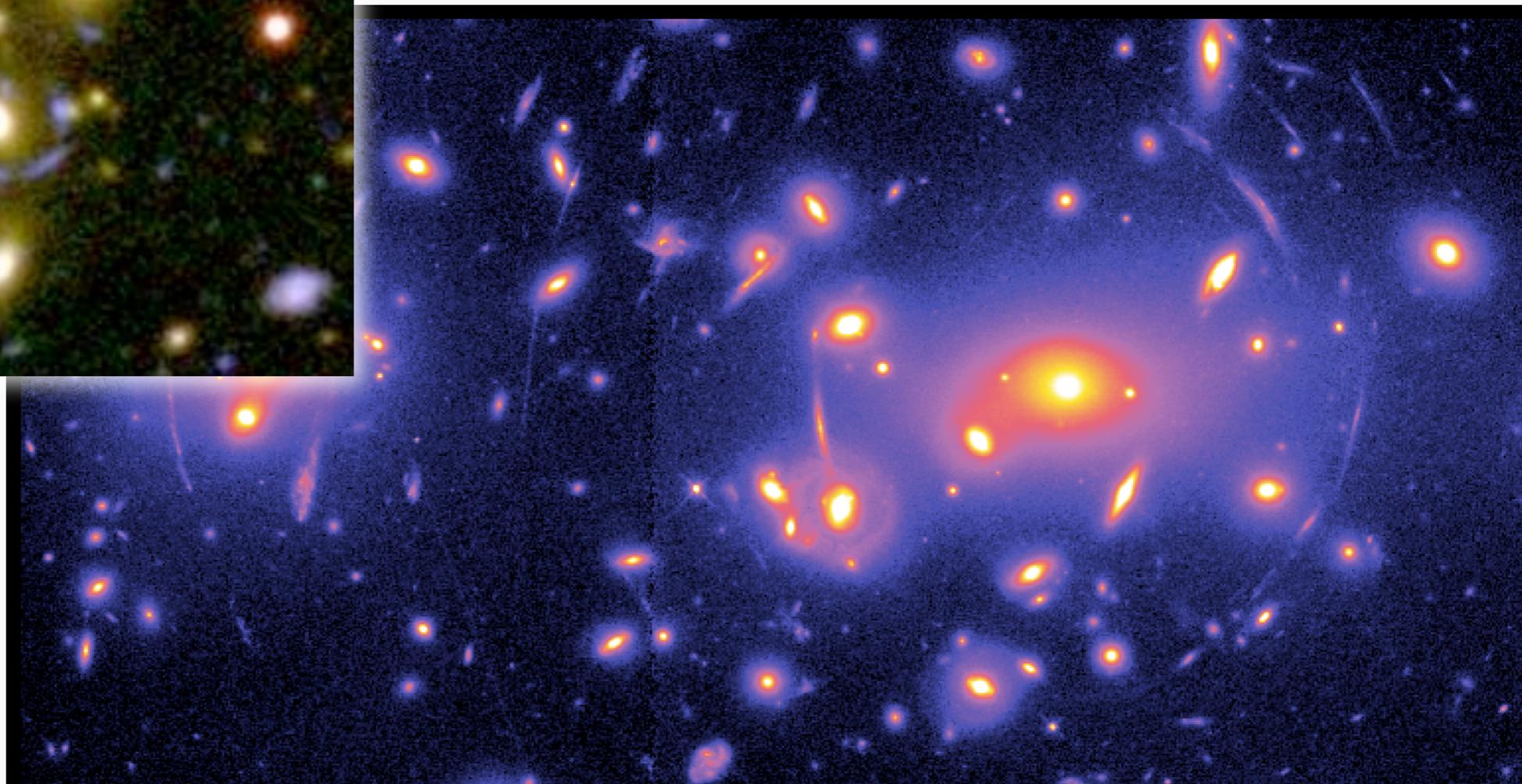
2D lensing potential



# LENSING DISTORTIONS



CFHTL12k lens candidate, Czoske et al. 2001,  
 $z_l = 0.49, z_s = ?$



The cluster of galaxies Abell 2218

# A CLOSER LOOK

- Deflection angle is a gradient:

$$\vec{\alpha} = \vec{\nabla} \phi$$

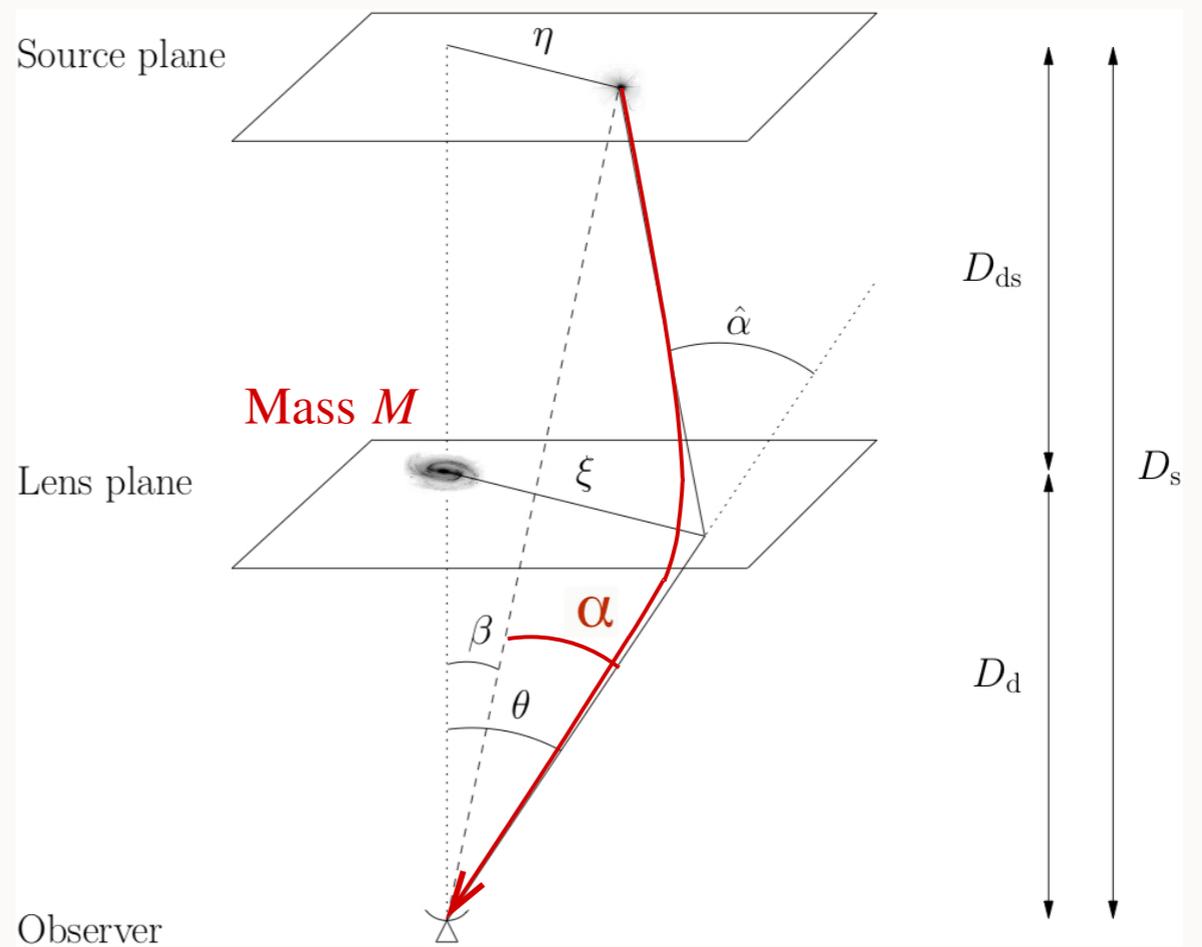
2D lensing potential

- **Second order** effect:  
Differential deflection of an extended source, distortion,  
 $\vec{\alpha} = \vec{\alpha}(\vec{\theta})$

2D angular coordinates

- Linearize deflection:

$$\frac{\partial \alpha_i}{\partial \theta_j} = \begin{pmatrix} \kappa + \gamma_1 & \gamma_2 \\ \gamma_2 & \kappa - \gamma_1 \end{pmatrix}$$

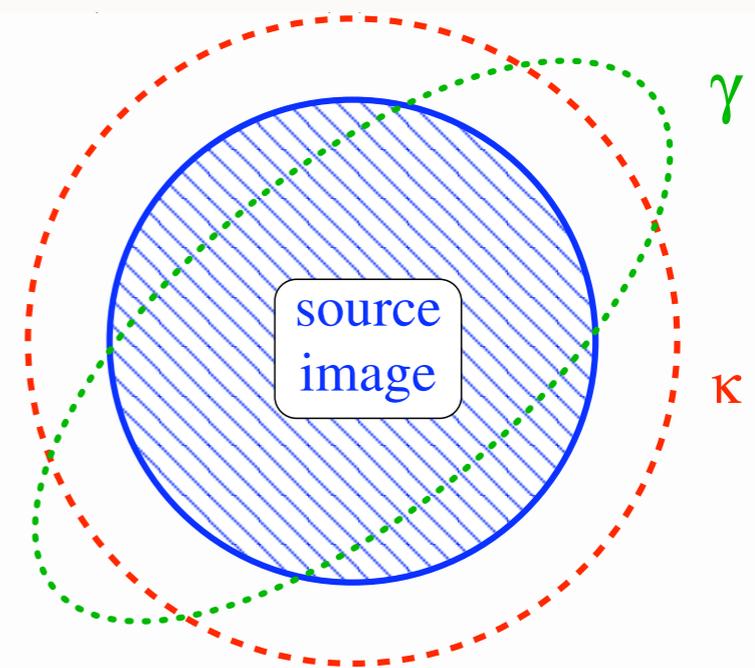


# CONVERGENCE & SHEAR

Gravitational lensing effect, locally:

- Convergence  $\kappa$ : isotropic magnification
- Shear  $\gamma$ : anisotropic stretching
- $\kappa$  and  $\gamma$  are second derivatives of the “lensing potential”  $\Phi$ , which describes the projected 2D mass distribution.

[In particular,  $\kappa$  is the scaled projected mass density, related to  $\Phi$  via a Poisson equation:  $2\kappa = \Delta\Phi$ ]

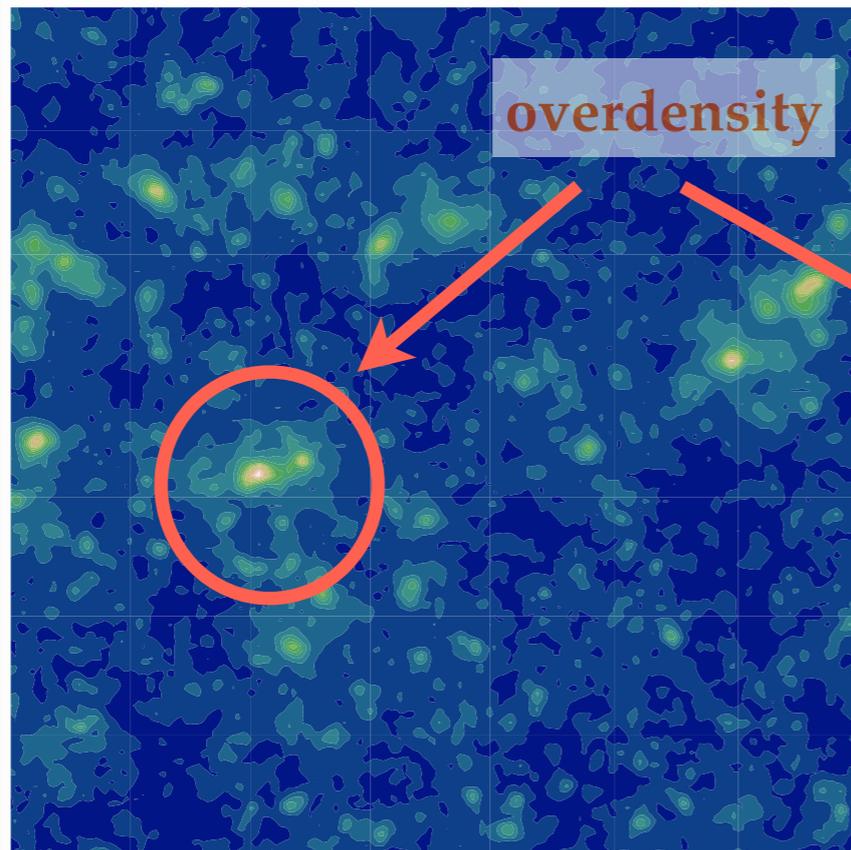


Typical in weak cosmological lensing: 3% distortion,  $\gamma \approx 0.03$

# MASS AND SHEAR

Projected matter density

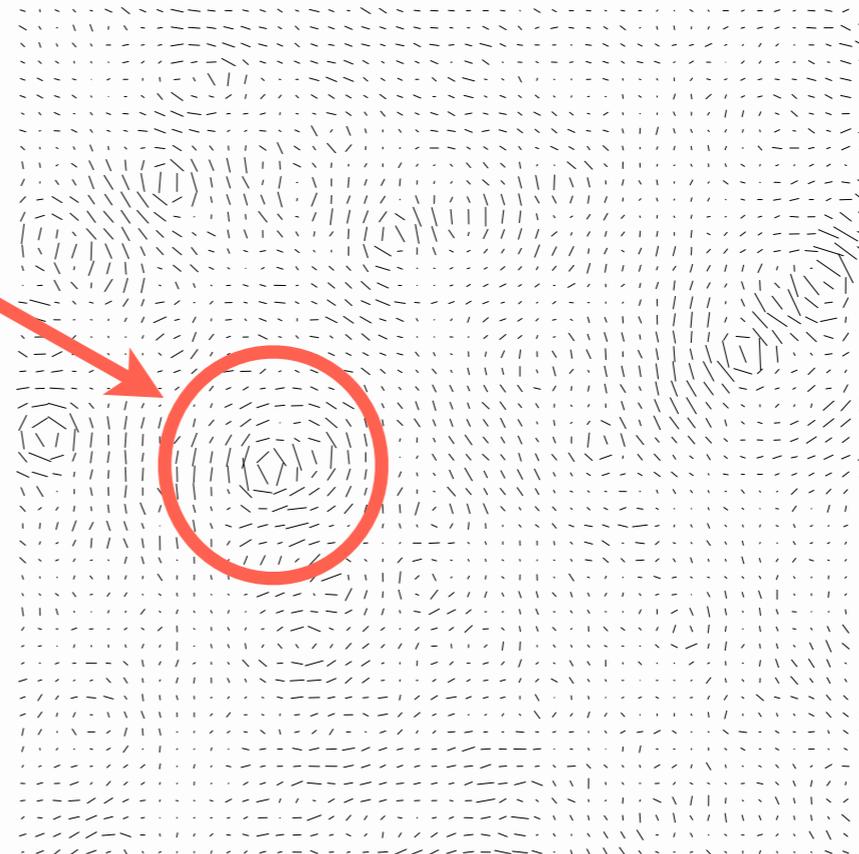
convergence  $\kappa$



Distortion field

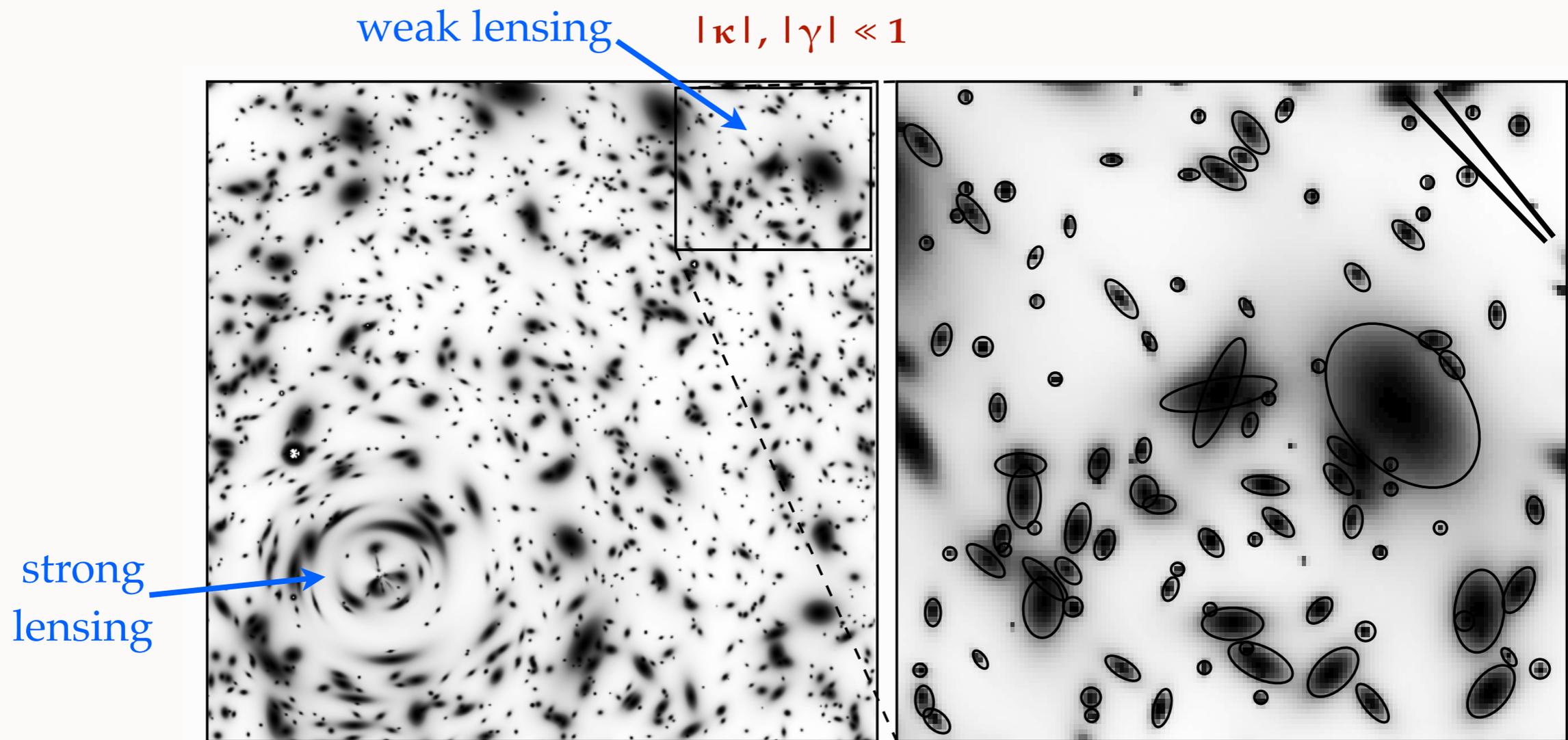
shear  $\gamma$

tangential distortions around mass peaks



Source galaxies at  $z = 1$ , ray-tracing simulations by T. Hamana

# GALAXIES ESTIMATE SHEAR



[from Y. Mellier]

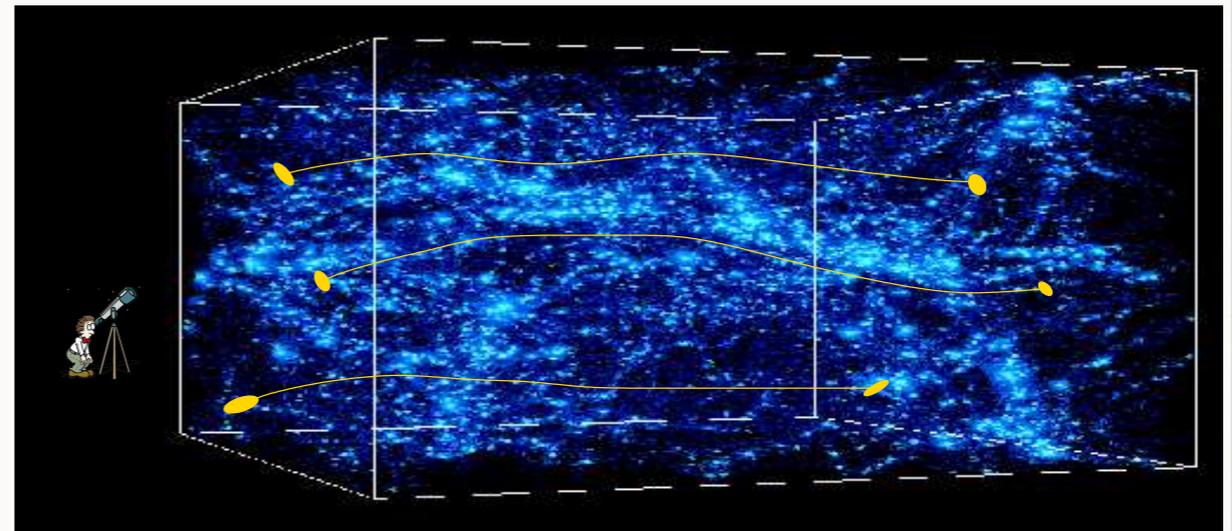
Galaxy ellipticities are an estimator of the local shear.

**Noise:** intrinsic galaxy shapes

# COSMIC SHEAR

## Weak lensing by the **large-scale structure**

- Continuous distortion along light ray path
- Lensing distortion strength depends on properties of projected 2D density contrast
- Sensitive to geometry of the Universe and growth of structures



$$\kappa(\vec{\theta}) = \int_0^{\chi_{\text{lim}}} d\chi G(\chi) \delta(\chi\vec{\theta}, \chi)$$

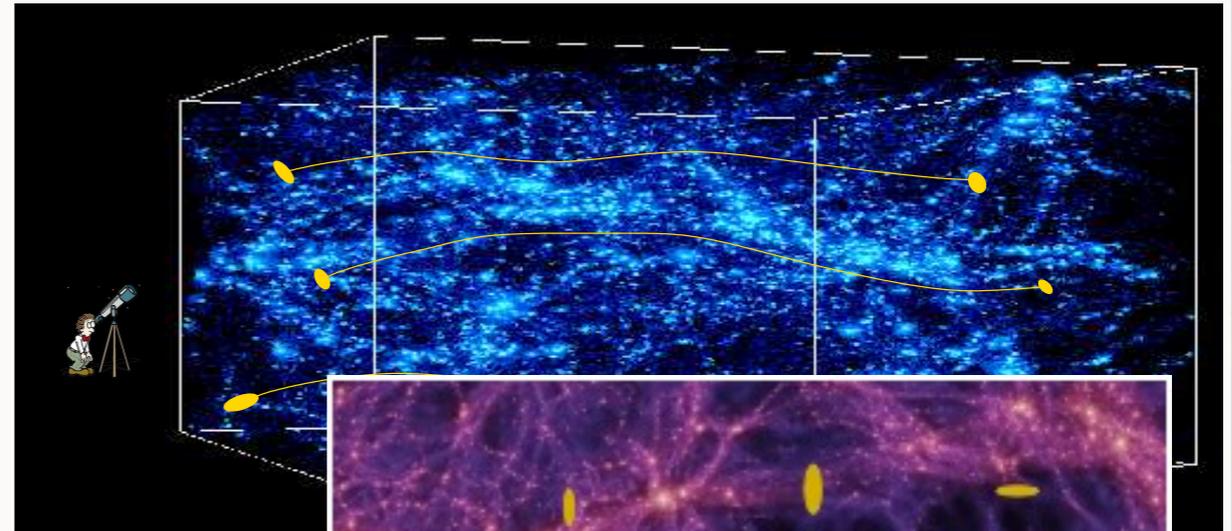
comoving coordinates (pointing to  $\chi$ )  
lensing efficiency (pointing to  $G(\chi)$ )  
density contrast (pointing to  $\delta(\chi\vec{\theta}, \chi)$ )

$$G(\chi) = \frac{3}{2} \left( \frac{H_0}{c} \right)^2 \frac{\Omega_m}{a} \int_{\chi}^{\chi_{\text{lim}}} d\chi' p(\chi') \frac{\chi(\chi' - \chi)}{\chi'}$$

redshift distribution of background galaxies (pointing to  $p(\chi')$ )

# COSMIC SHEAR

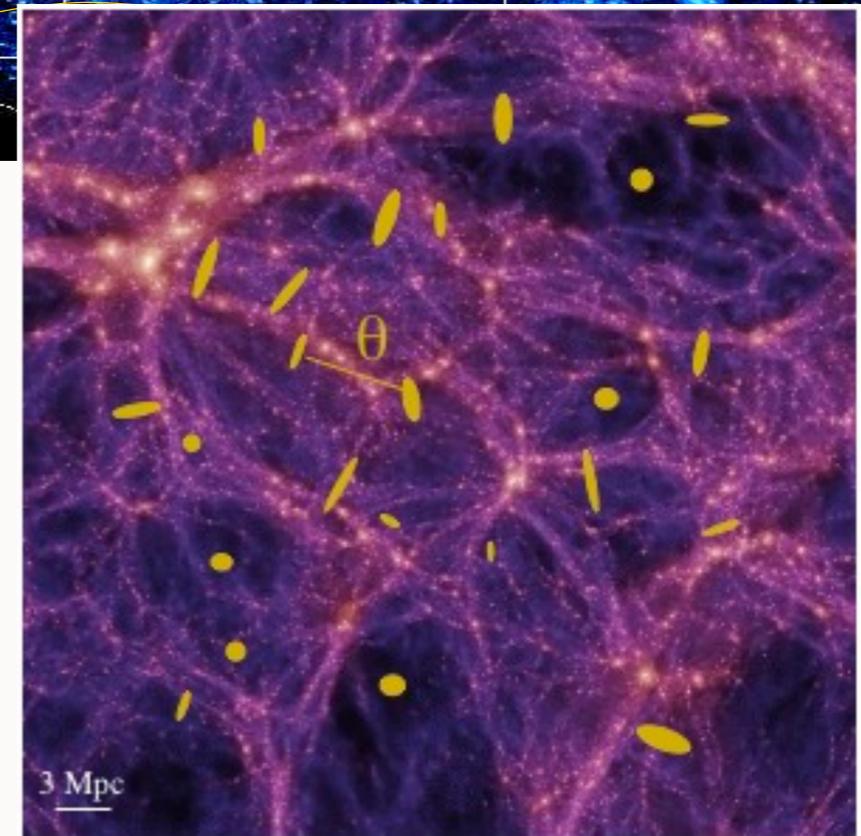
Weak lensing by the **large-scale structure**



- Coherent distortions of galaxy images  
→ measure shape correlations

$$\langle |\gamma|^2 \rangle (\theta) = \langle \kappa^2 \rangle (\theta) \propto \langle \delta^2 \rangle (\theta)$$

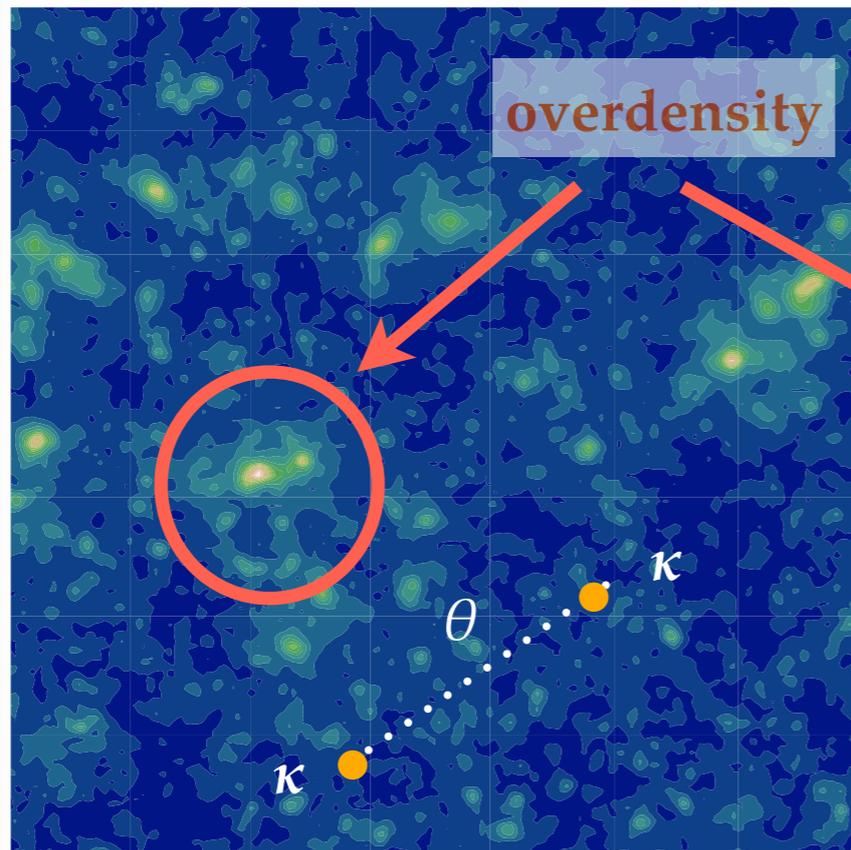
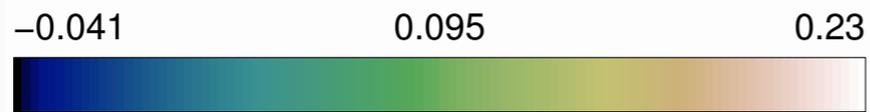
shear variance



# MASS AND SHEAR

Projected matter density

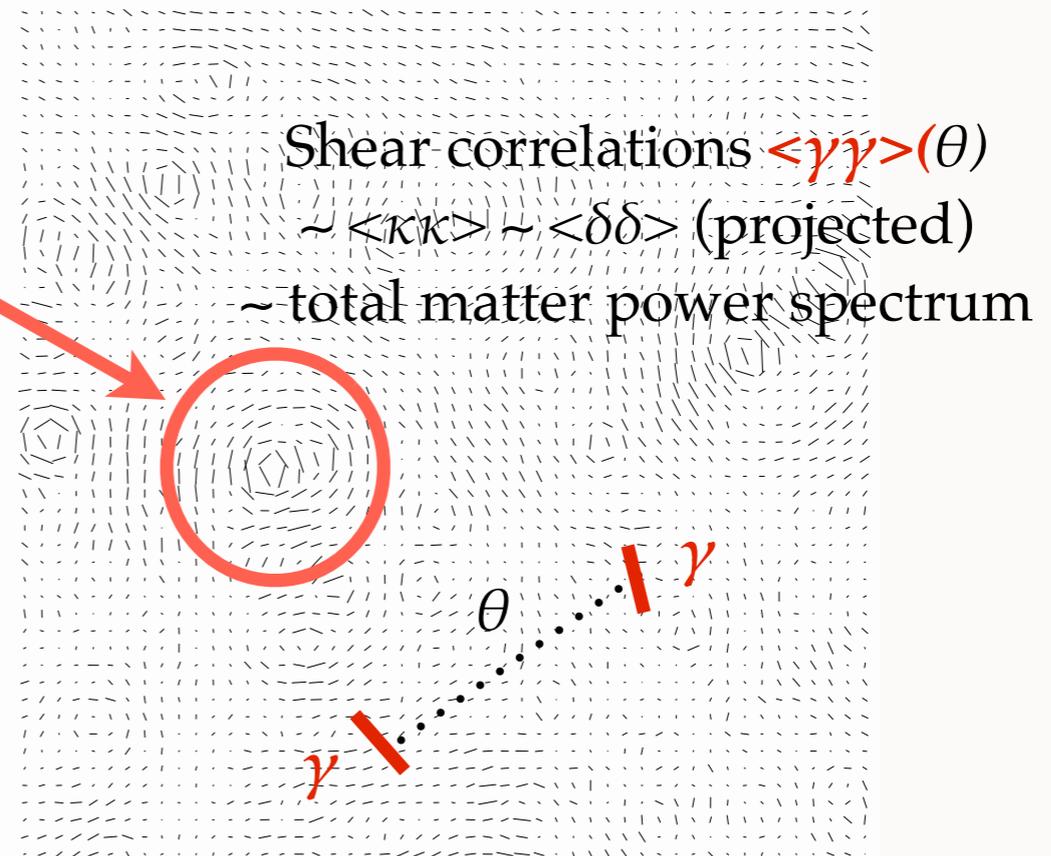
convergence  $\kappa$



Distortion field

shear  $\gamma$

tangential distortions around mass peaks



Source galaxies at  $z = 1$ , ray-tracing simulations by T. Hamana

# CFHT LENSING SURVEY





# The CFHTLenS team



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E. Semboloni  
M. Smit



B. Rowe



C. Bonnett



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F. Simpson  
E. Grocutt

University of  
**Waterloo**



M. Hudson  
B. Gillis



L. Fu

上海师范大学  
Shanghai Normal University since 1954



Y. Mellier  
R. Gavazzi



L. Miller  
M. Velander



M. Kilbinger



A  
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f  
A

T. Erben  
P. Simon  
T. Schrabback  
E. van Uitert



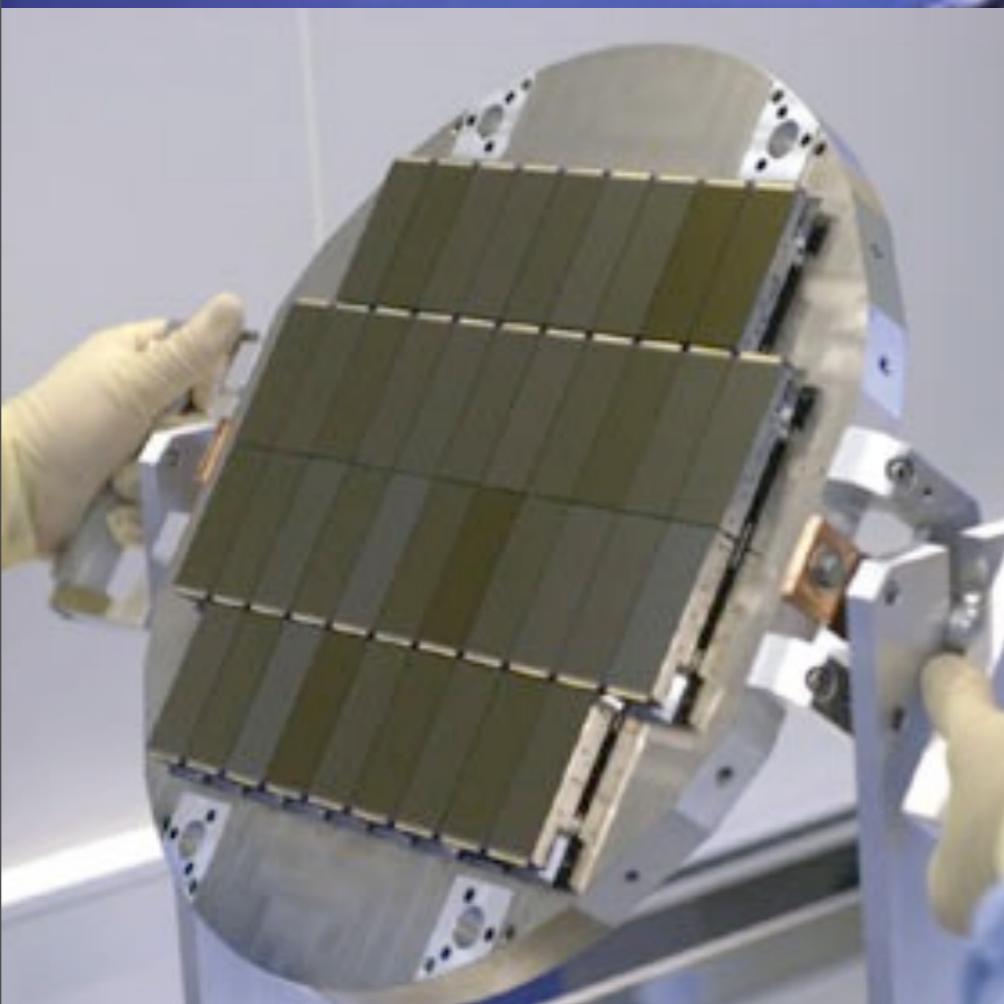
J. Coupon



K. Holhjem

# CFHTLenS

- The state-of-the-art cosmological survey with 155 sq degrees, ugriz to  $i < 24.7$  ( $7\sigma$  extended source)
- Uses 5 yrs of data from the Deep, Wide and Pre-survey components of the CFHT Legacy Survey





# Canada-France-Hawaii Telescope Legacy Survey: Canada-France collaboration

Legend  
 --- g  
 --- i  
 --- r  
 --- u  
 --- z

- 500 nights between June 2003 and June 2008

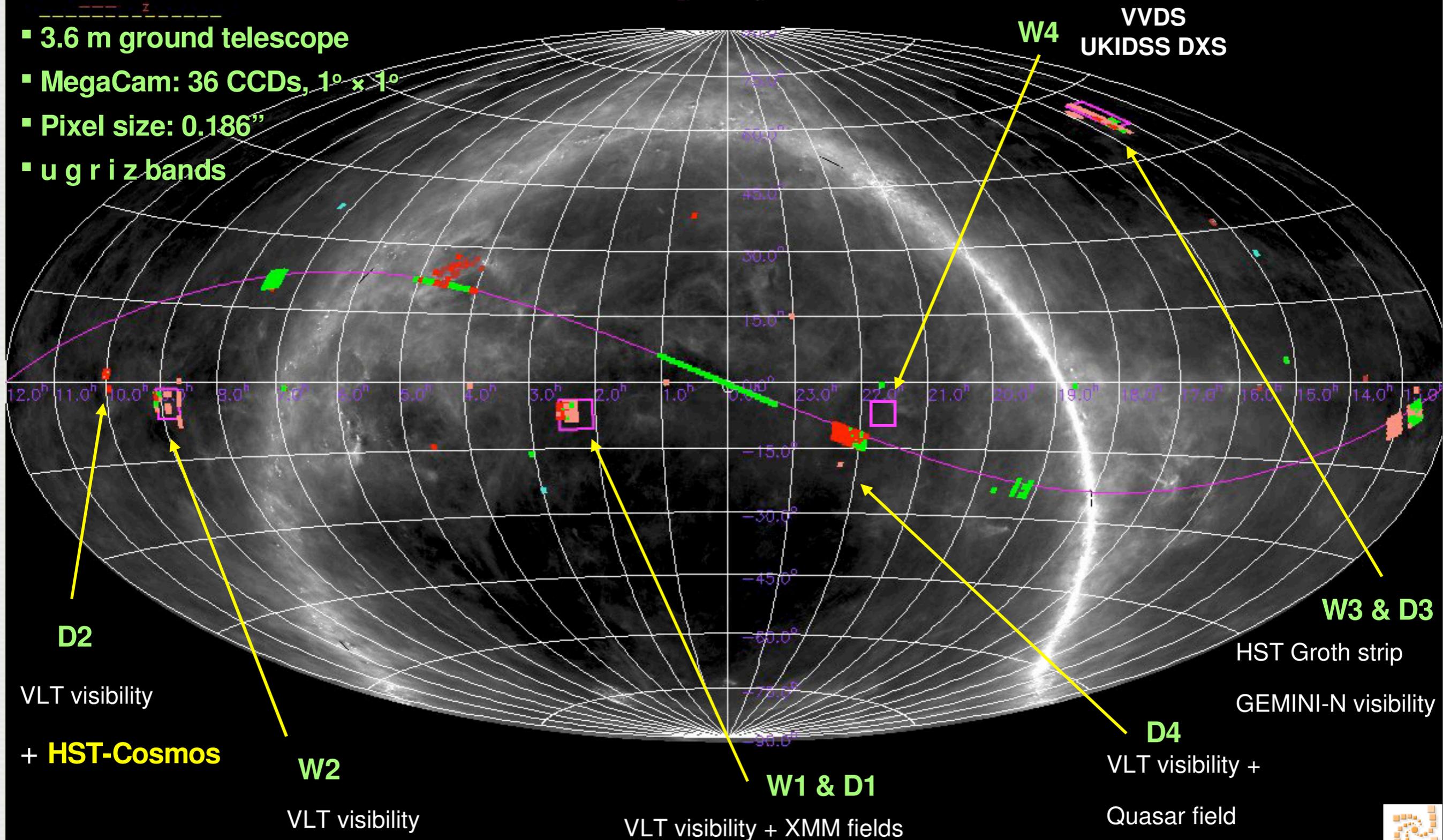
- 4 CFHTLS-Wide ( 170 deg<sup>2</sup> ), 4 CFHTLS-Deep ( 1 deg<sup>2</sup> each )

▪ 3.6 m ground telescope

▪ MegaCam: 36 CCDs, 1° x 1°

▪ Pixel size: 0.186"

▪ u g r i z bands



VVDS  
UKIDSS DXS

W4

W3 & D3

HST Groth strip

GEMINI-N visibility

D4

VLT visibility +

Quasar field

W1 & D1

VLT visibility + XMM fields

W2

VLT visibility

D2

VLT visibility

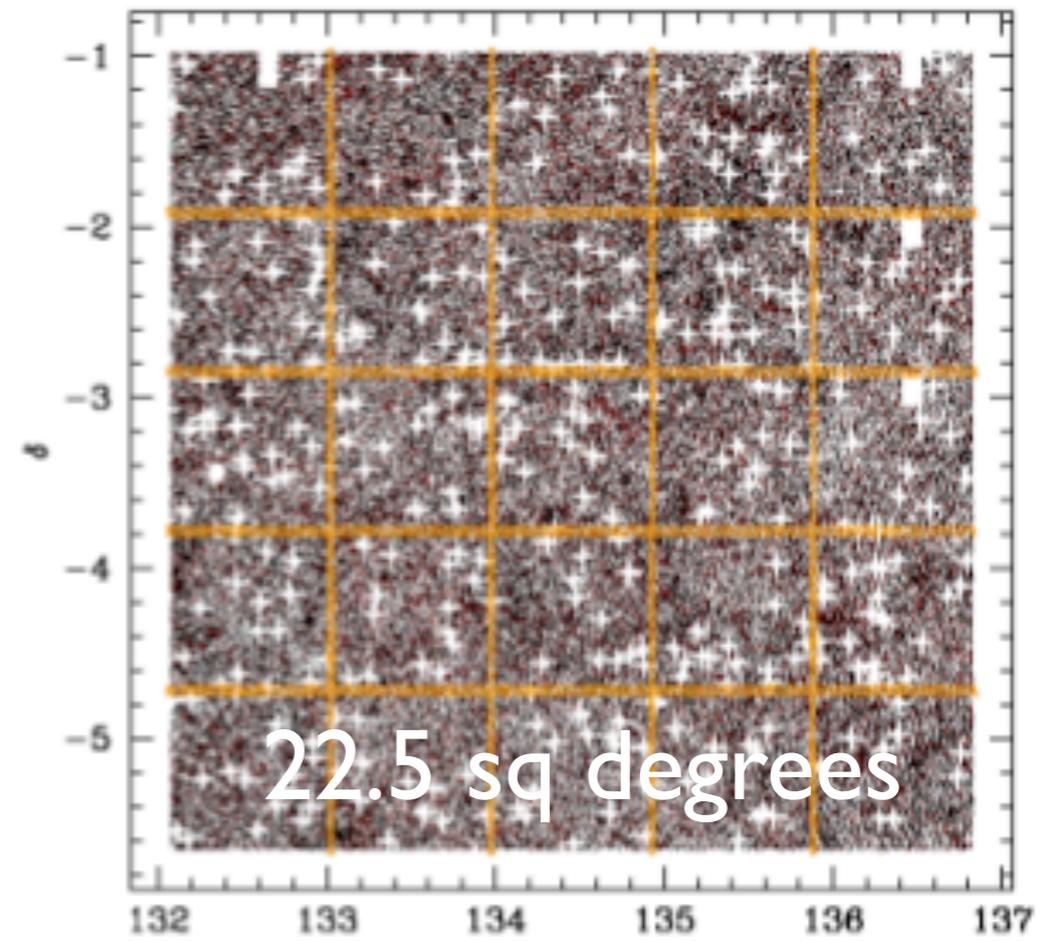
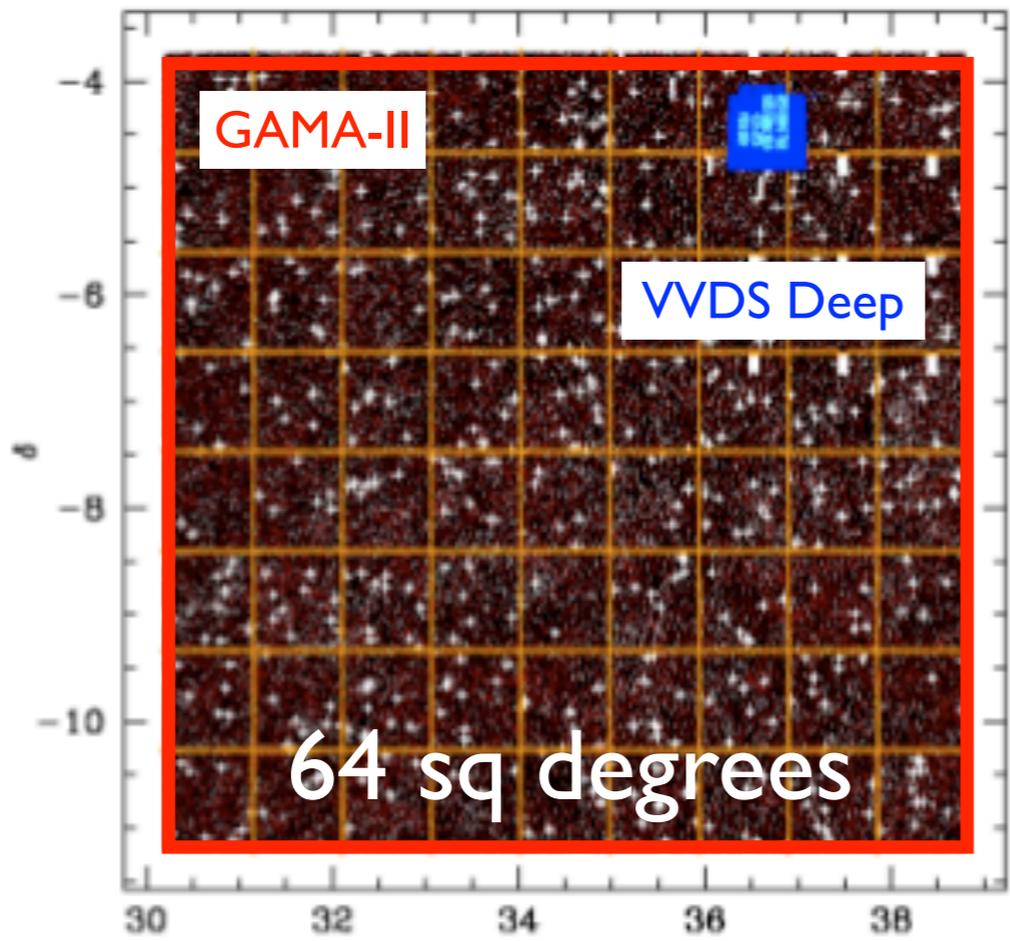
+ HST-Cosmos

VVDS spectro. survey

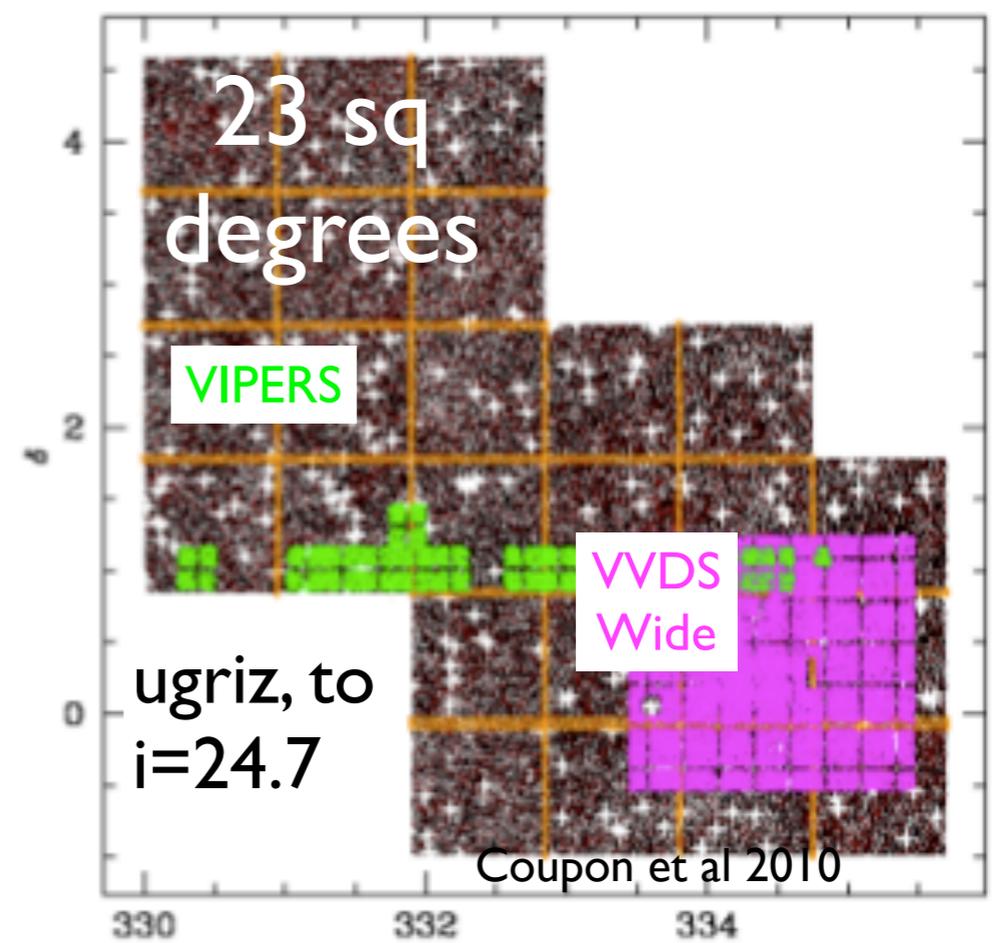
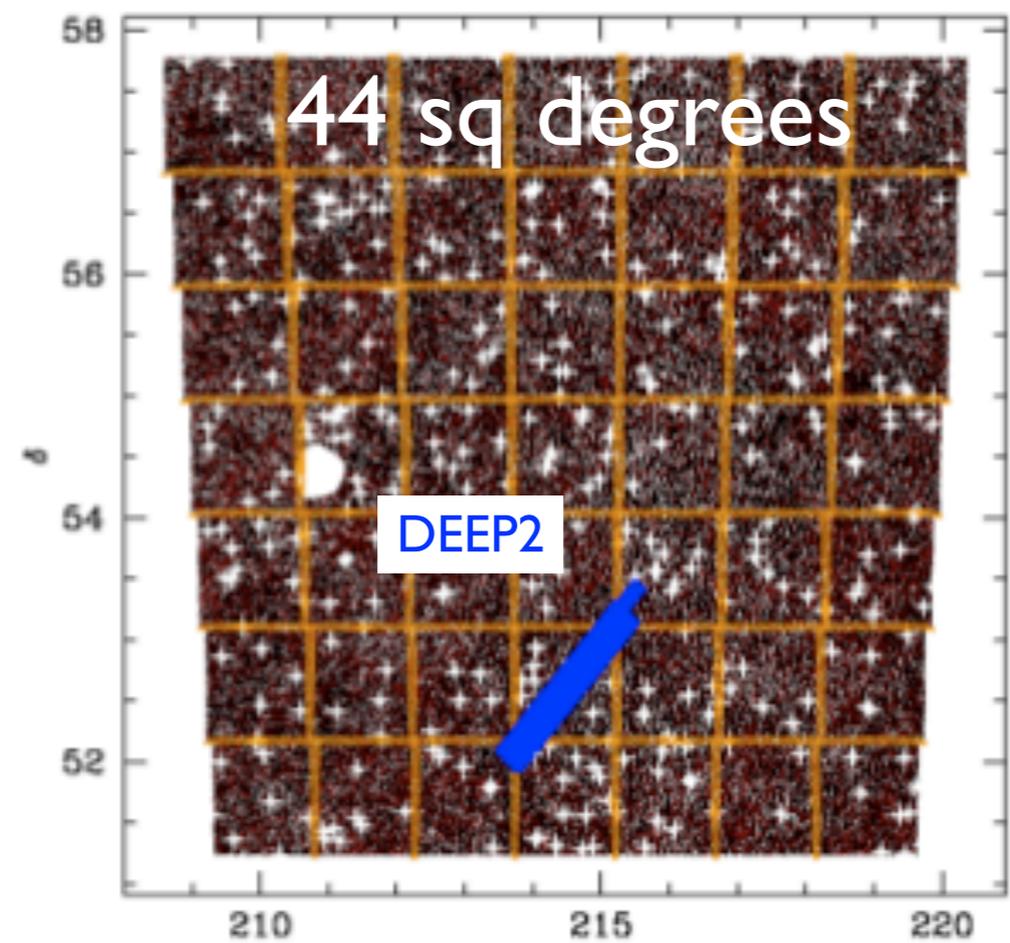
+command line : skywatcher

Terapix/Skywatcher : all data 03A-05A : 20000 Megacam images

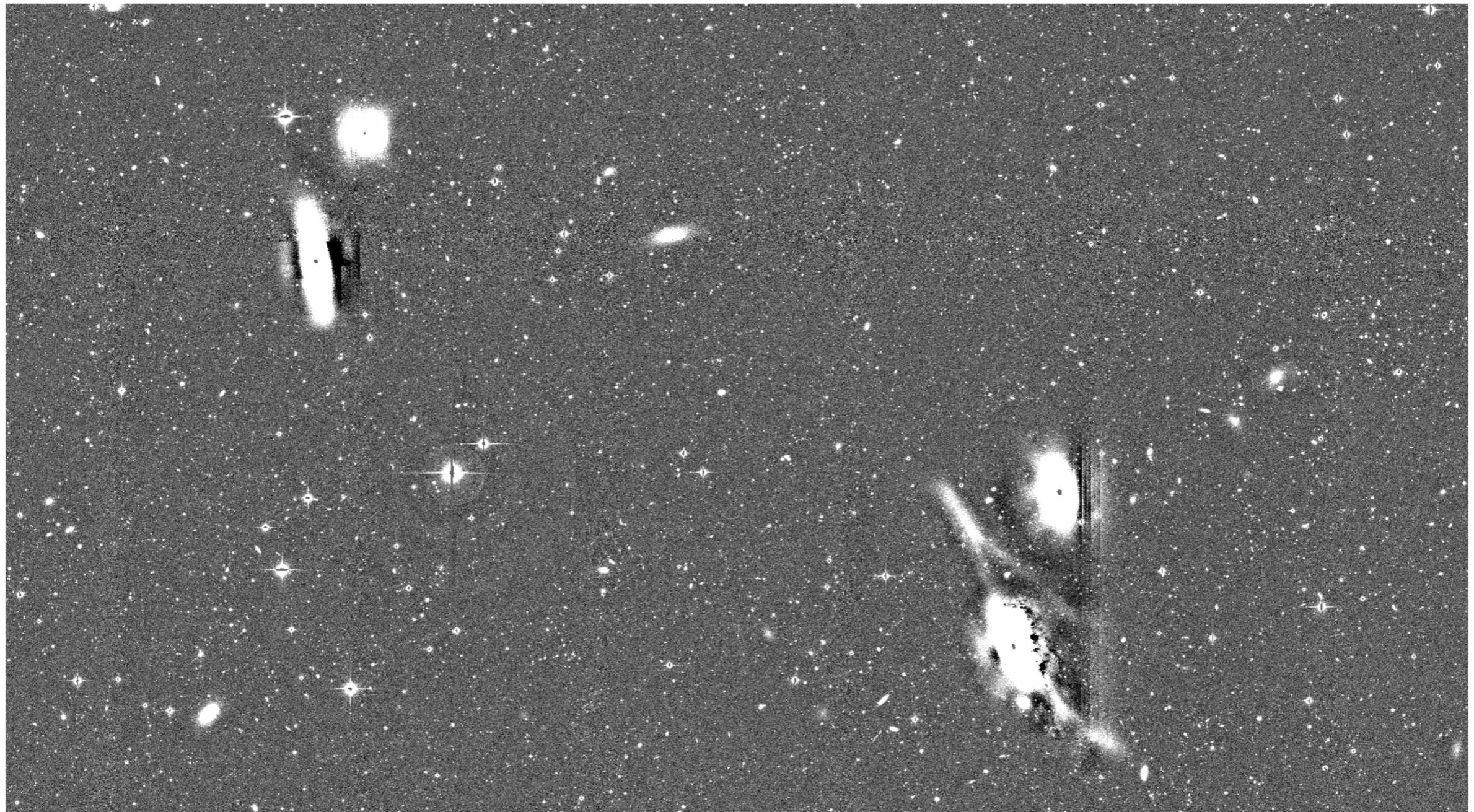




CFHTLS : 155 sq degrees

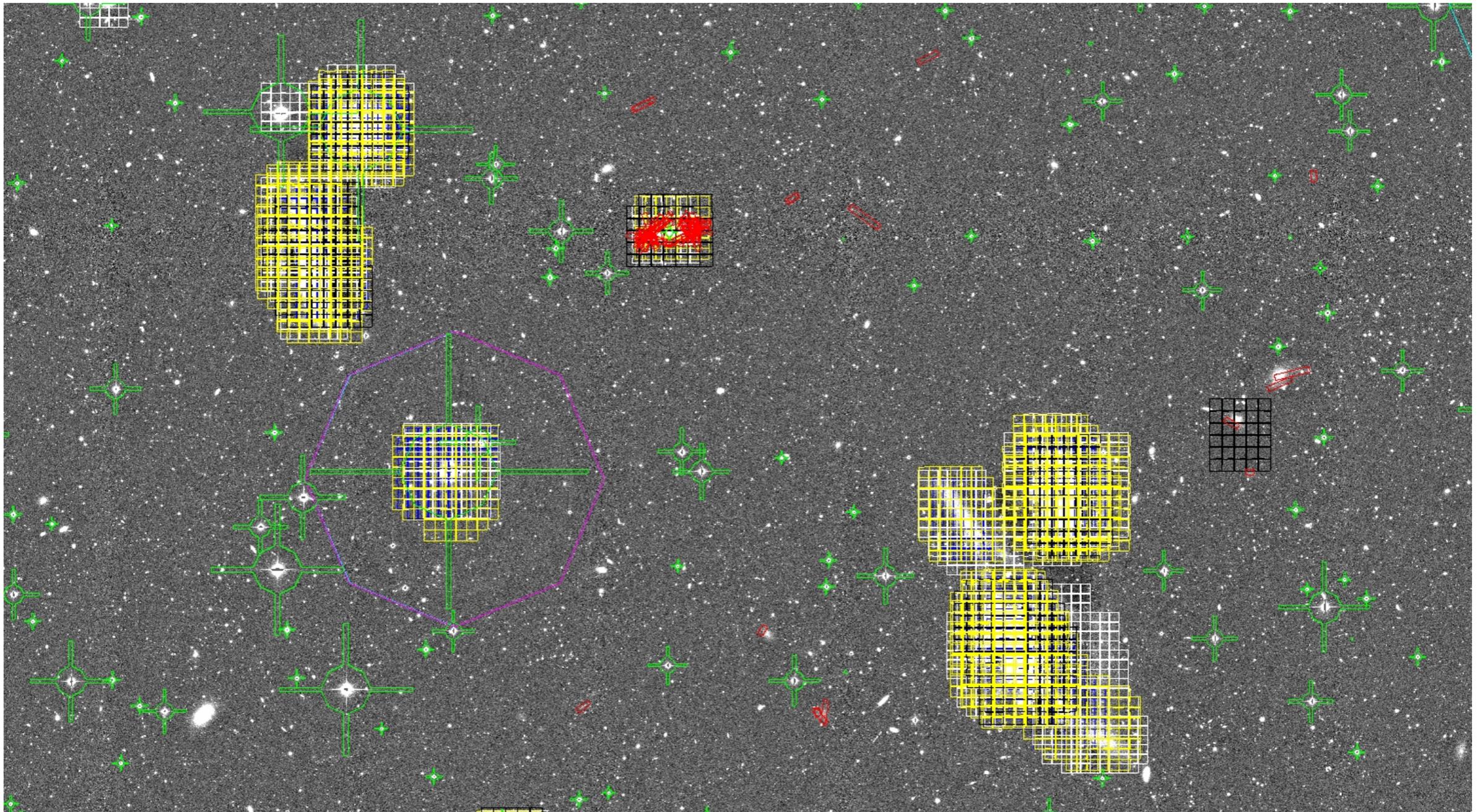


# A MEGACAM@CFHT Image Section



Regions around bright stars and big galaxies need to be excluded from our weak lensing studies.

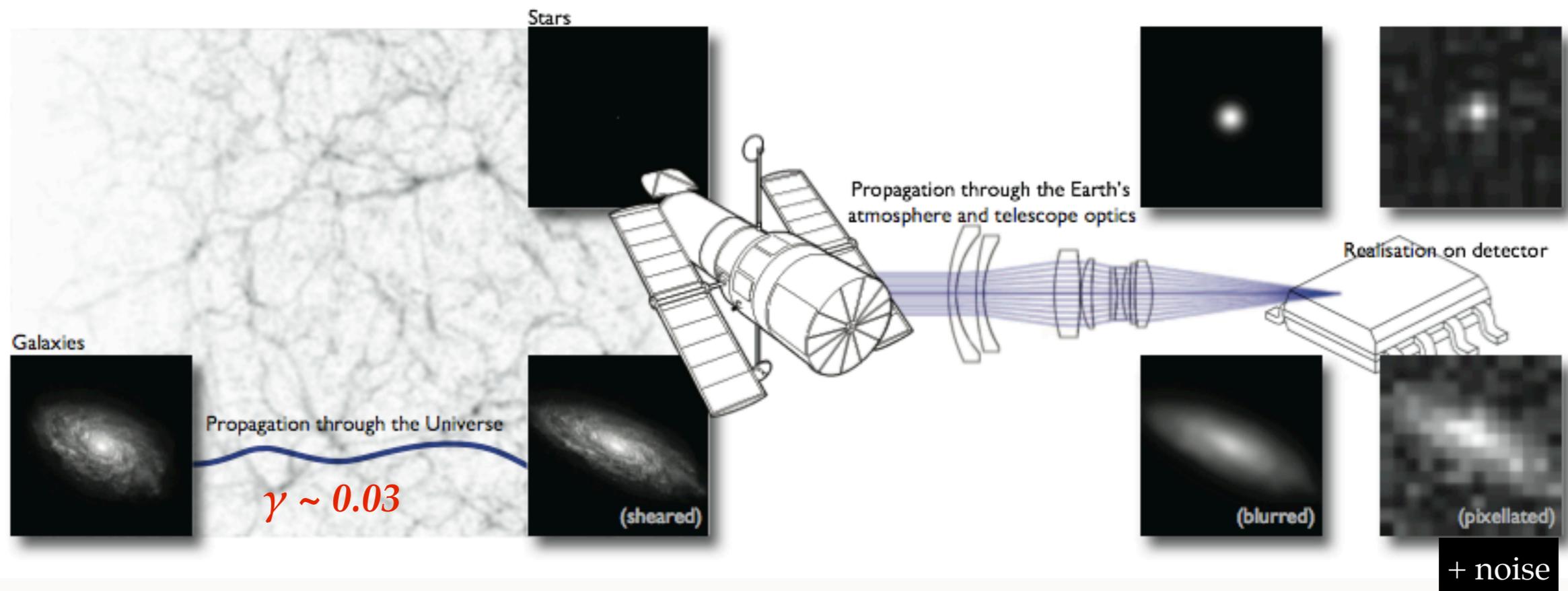
# Semi-Automatic Masking



Moderately bright Stars are masked with template masks; large scale defects produce significant jumps in the object number density

[Erben et al. in 2013]

# SHAPE MEASUREMENT

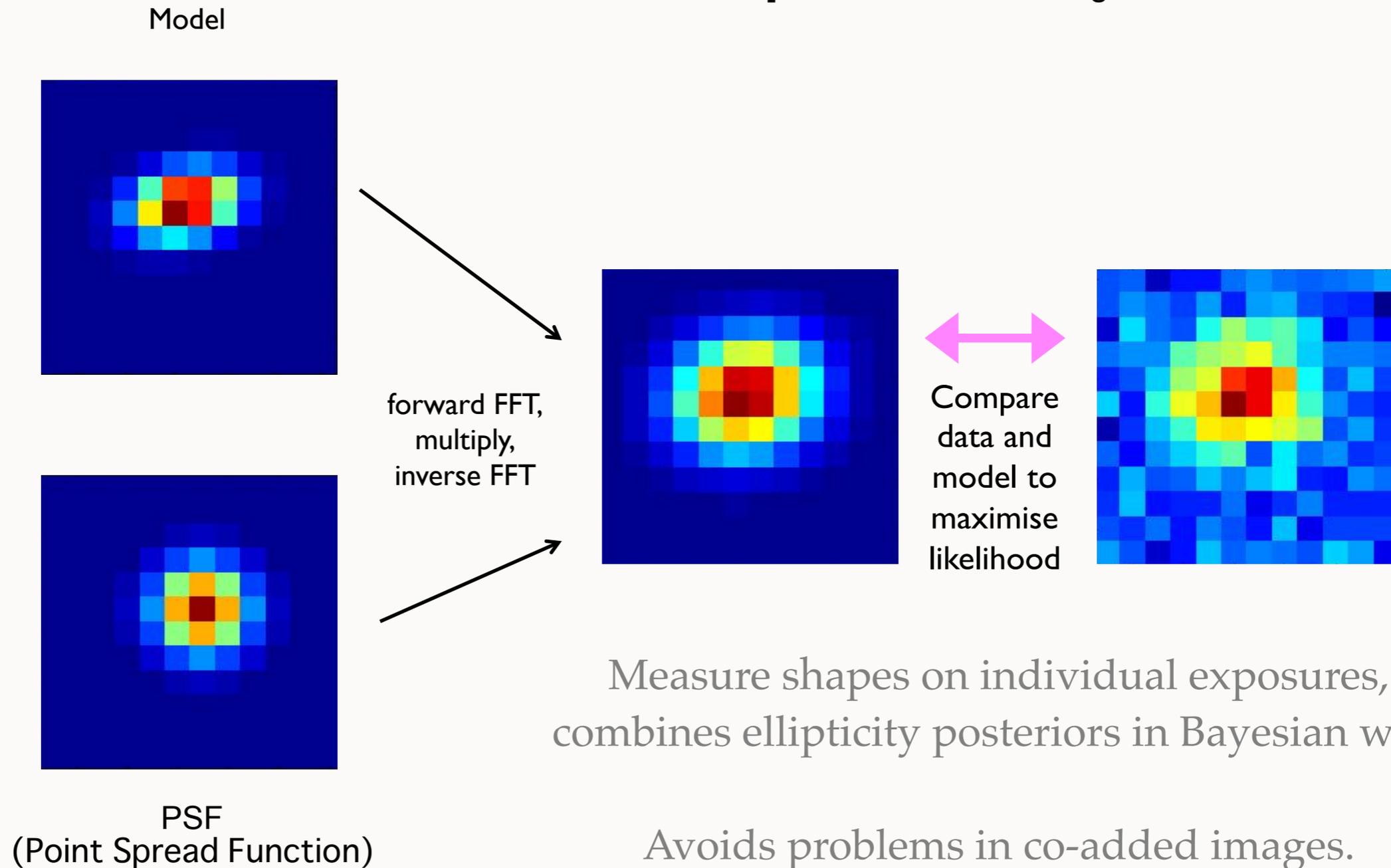


[Bridle et al. 2008, great08 handbook]

- Use stars to correct for instrumental and atmospheric distortions
- An individual galaxy shape cannot be well estimated, but need to measure the ensemble free from systematic bias

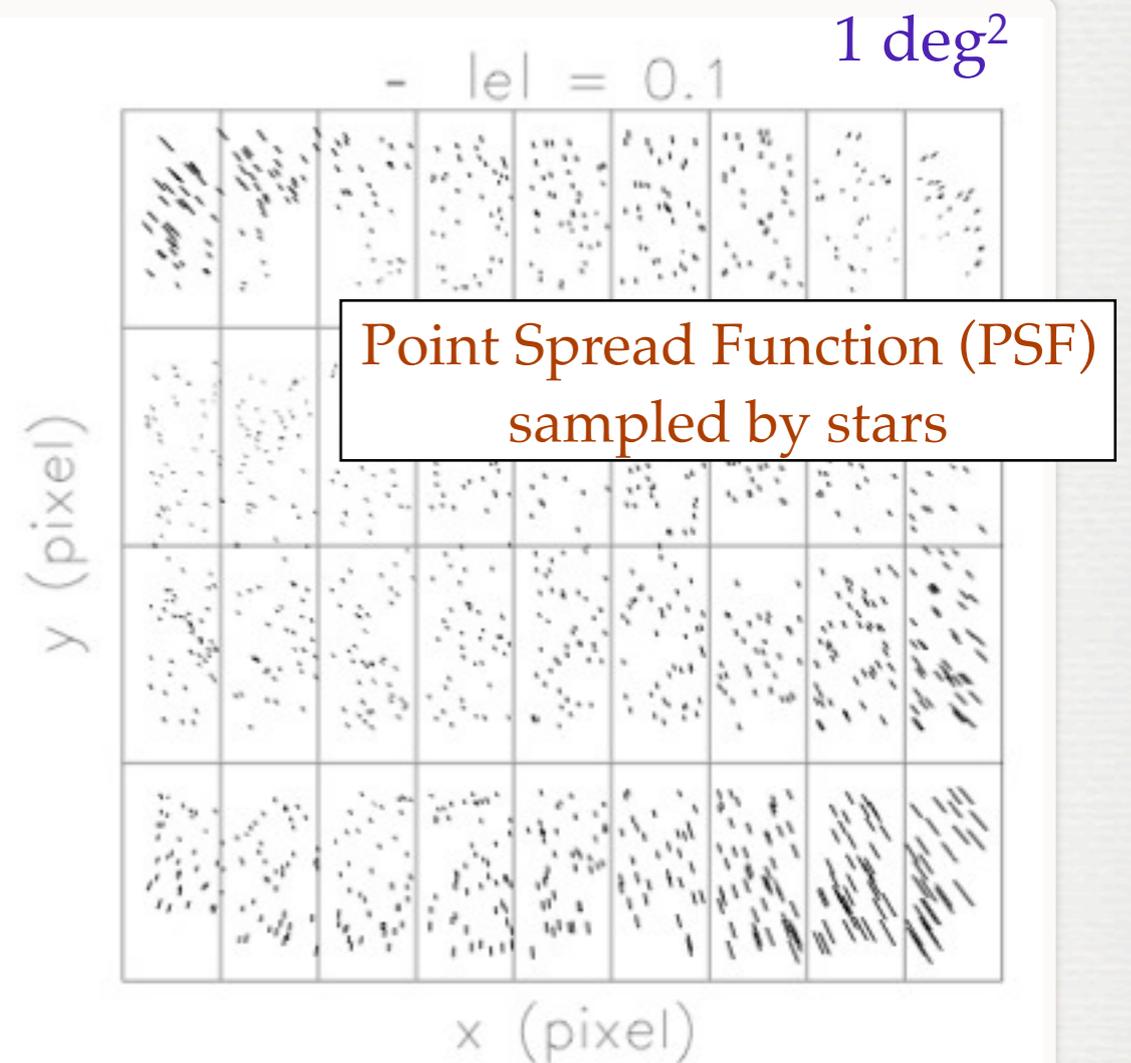
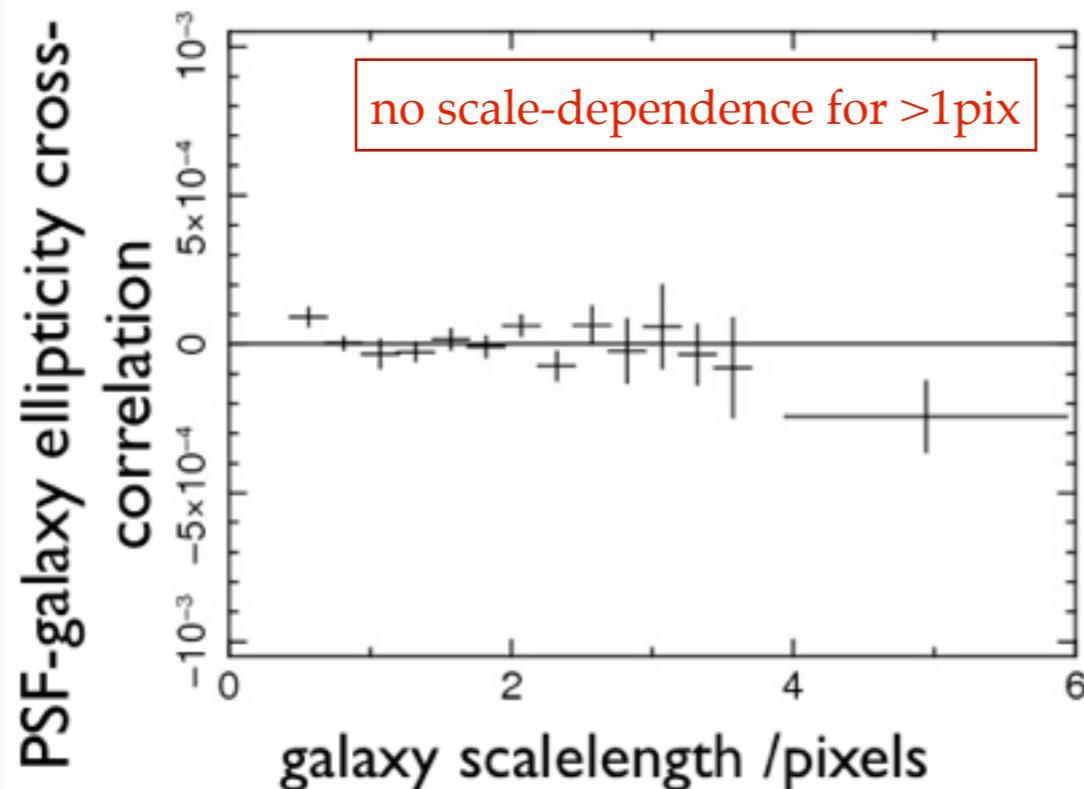
# SHAPE MEASUREMENT: LENSFIT

[Miller et al 2007, Kitching et al 2008, Miller et al. 2013]



# SHEAR MEASUREMENT: SYSTEMATICS

- Correlation between
  - galaxy shapes (after correction)
  - star shapes (uncorrected)non-zero  $\Leftrightarrow$  PSF residuals
- Compare to noise simulations (incl. LSS)

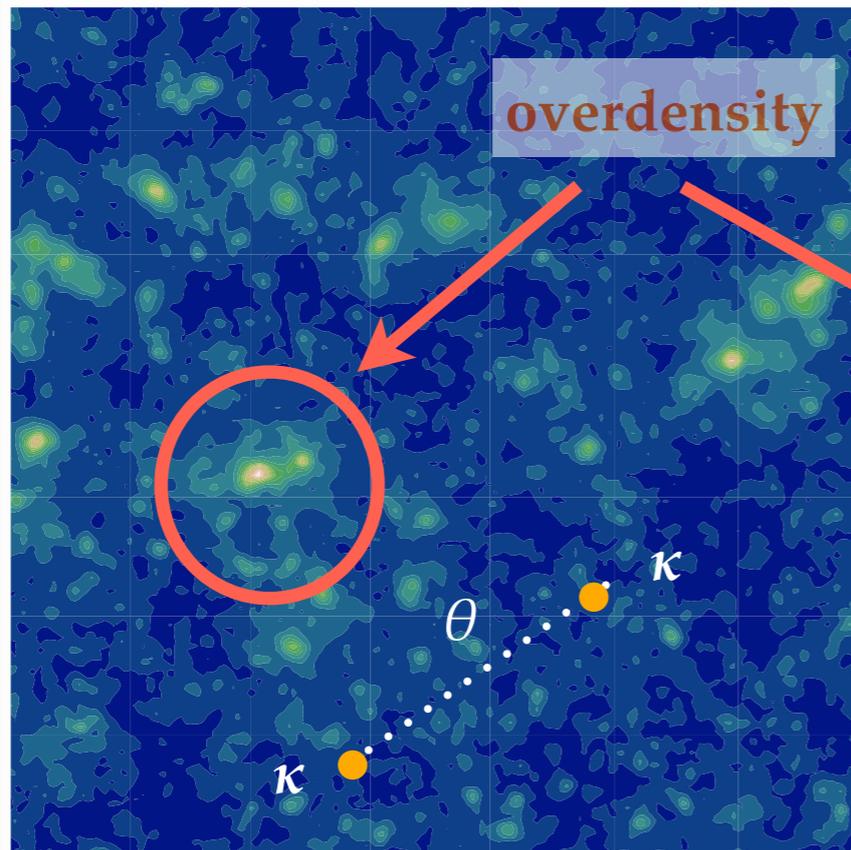
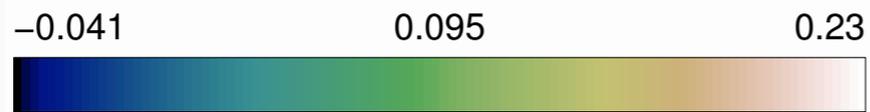


- **Cosmology-blind**
- 80% of data pass

# MASS AND SHEAR

Projected matter density

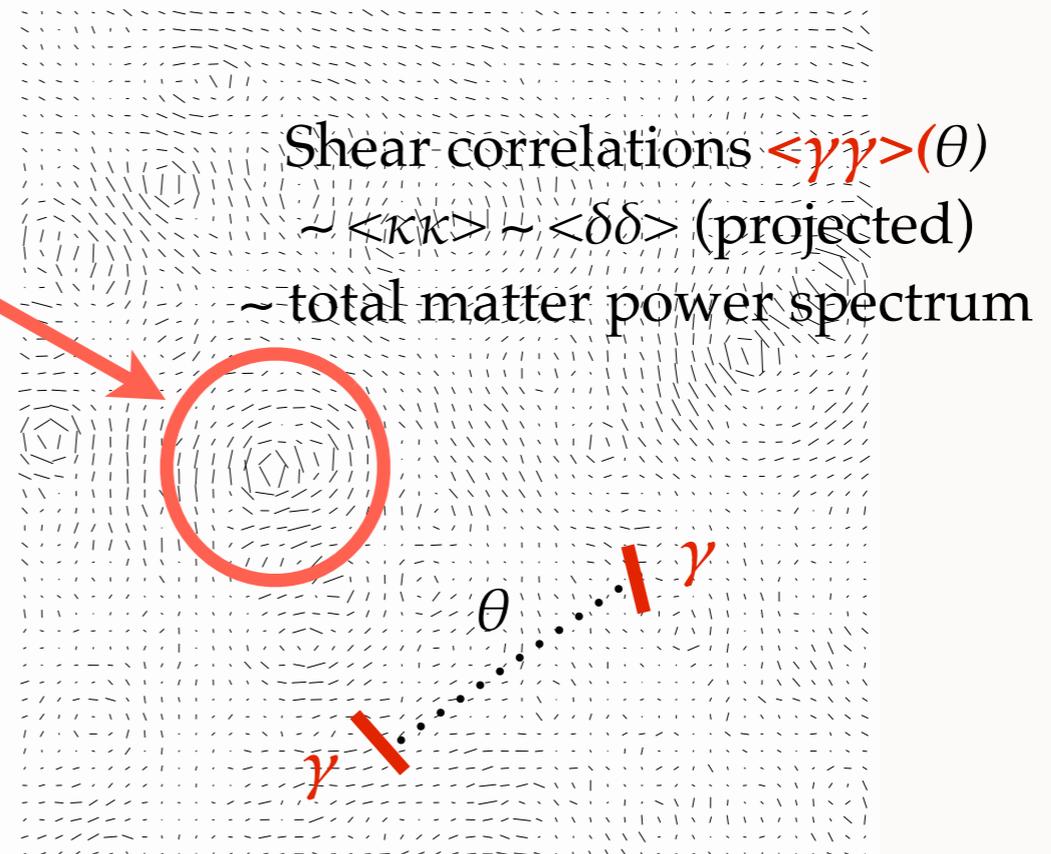
convergence  $\kappa$



Distortion field

shear  $\gamma$

tangential distortions around mass peaks



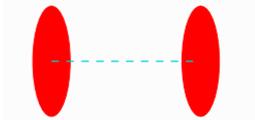
Source galaxies at  $z = 1$ , ray-tracing simulations by T. Hamana

# SHEAR CORRELATION

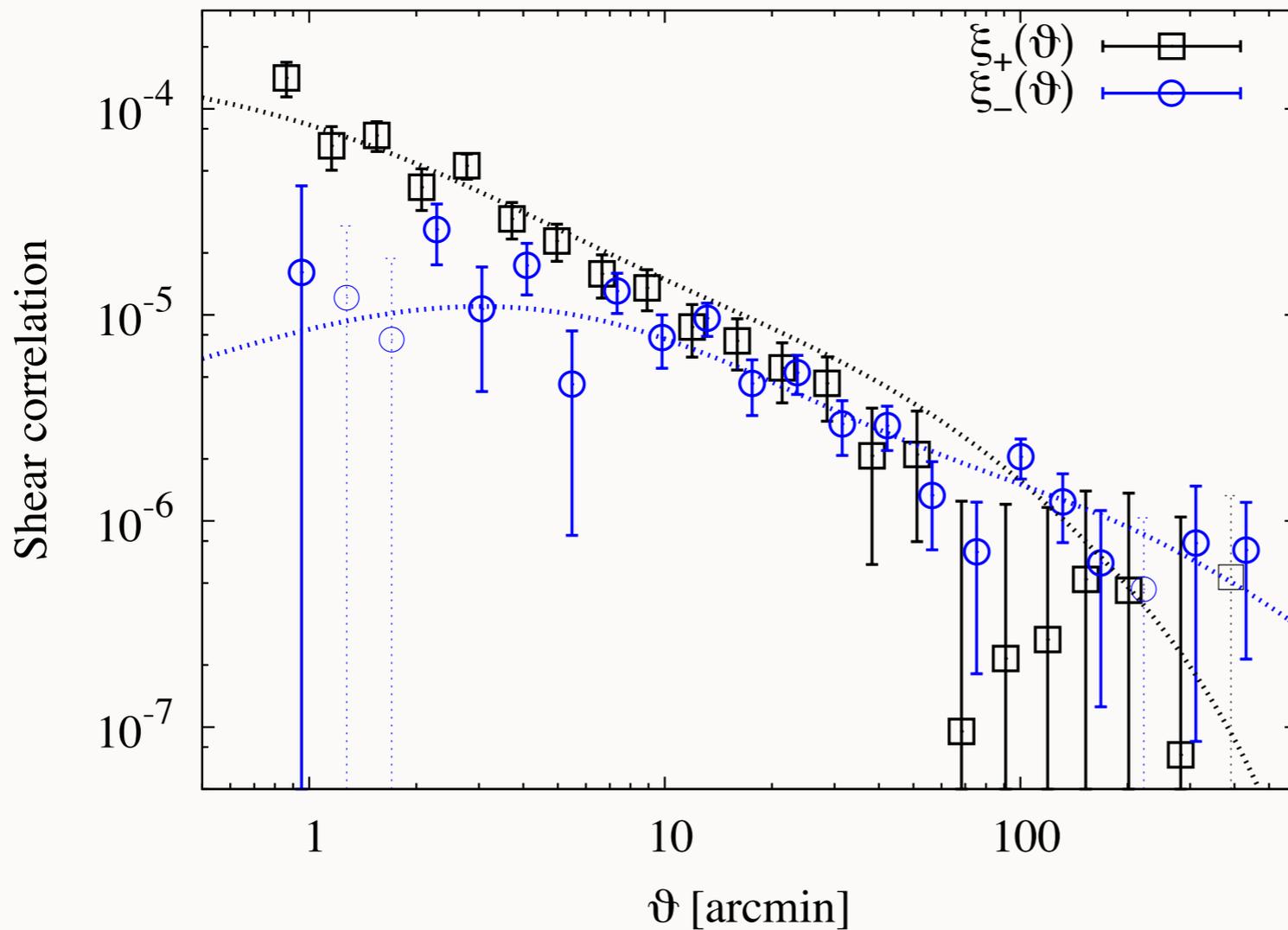
$$\xi_+(\vartheta) = \langle \gamma_t \gamma_t \rangle (\vartheta) + \langle \gamma_x \gamma_x \rangle (\vartheta)$$

$$\xi_-(\vartheta) = \langle \gamma_t \gamma_t \rangle (\vartheta) - \langle \gamma_x \gamma_x \rangle (\vartheta)$$

$\langle \gamma_t \gamma_t \rangle$



$\langle \gamma_x \gamma_x \rangle$



[Kilbinger et al. 2013]

Prediction  
(WMAP7 cosmology):

Flat Universe

$$\Omega_m = 0.27$$

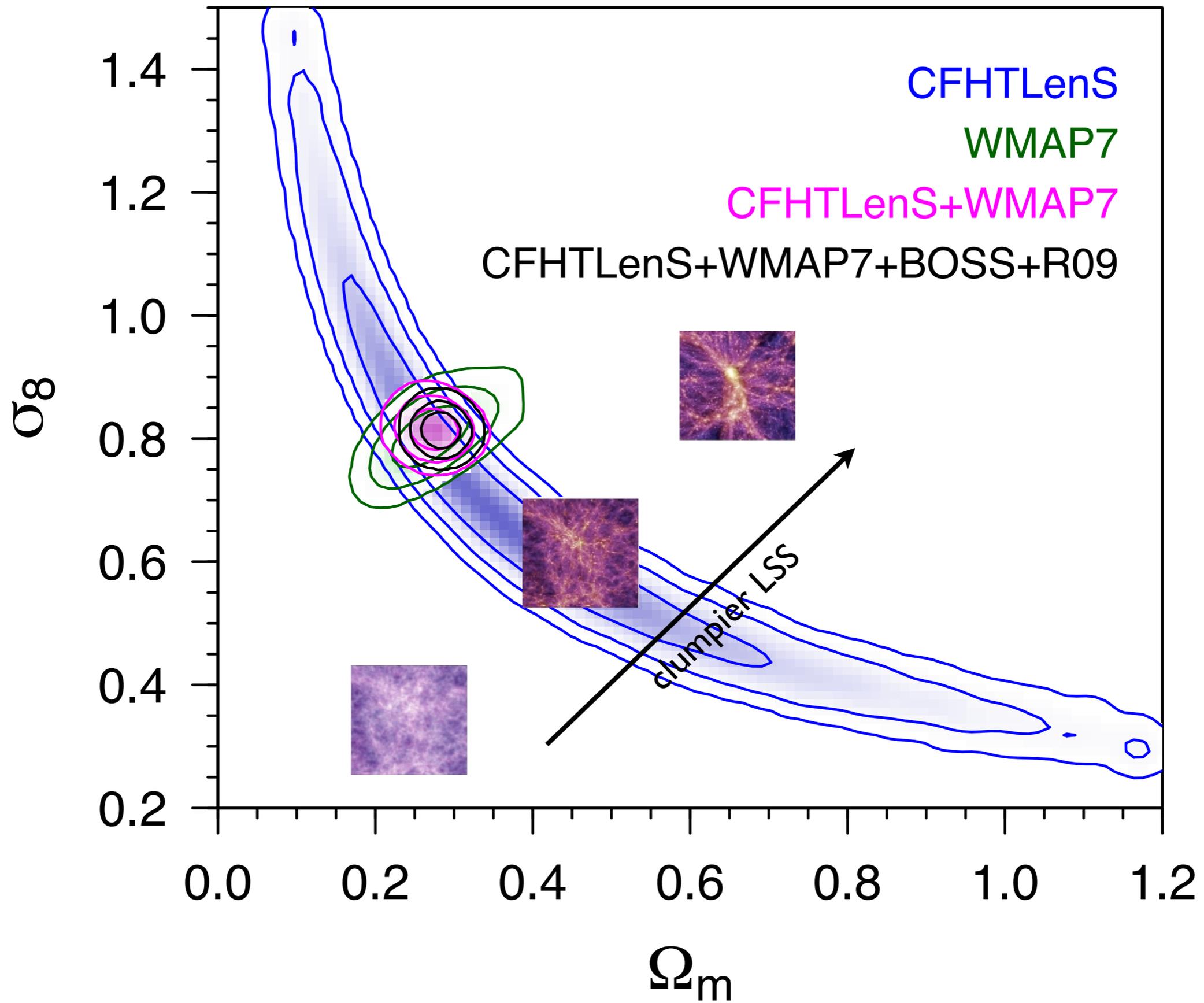
$$\sigma_8 = 0.8$$

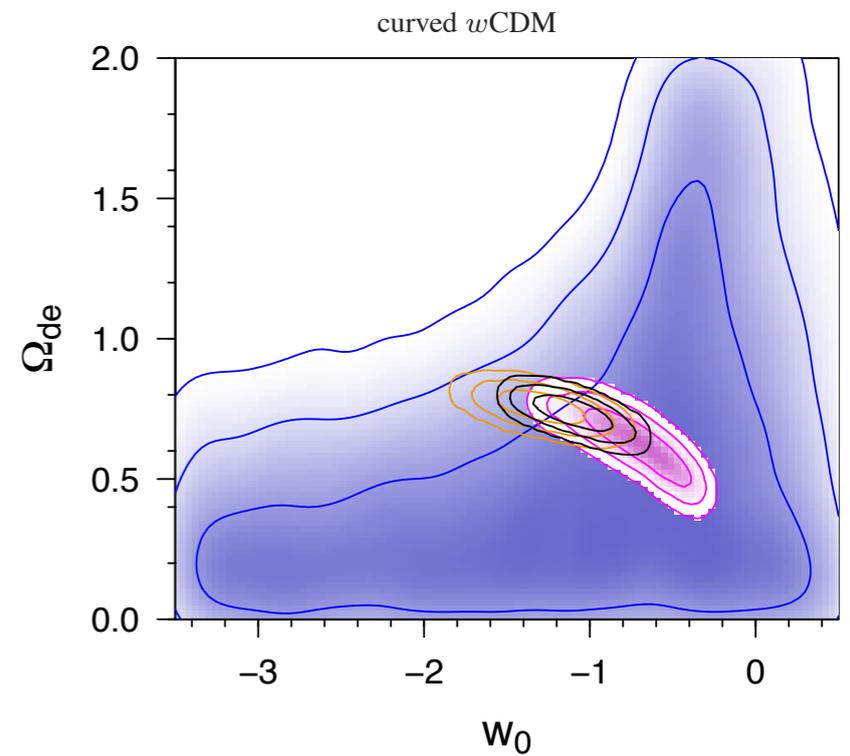
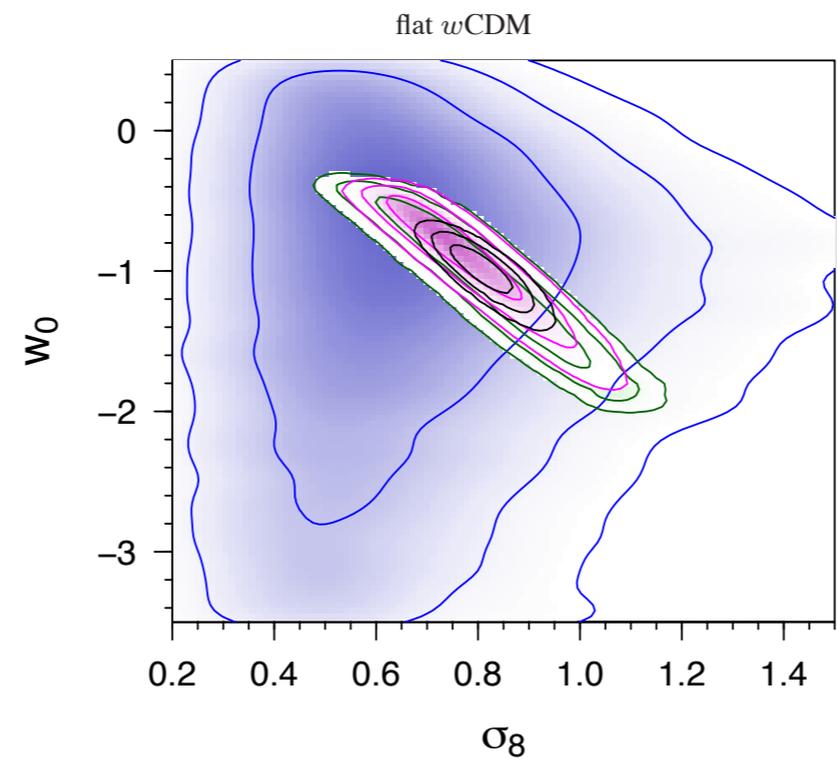
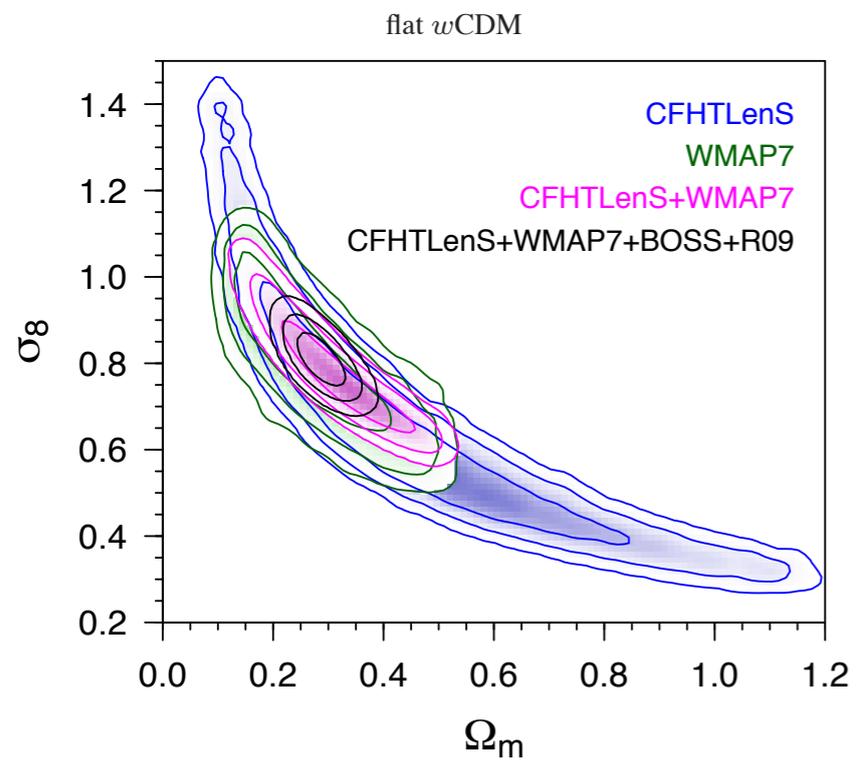
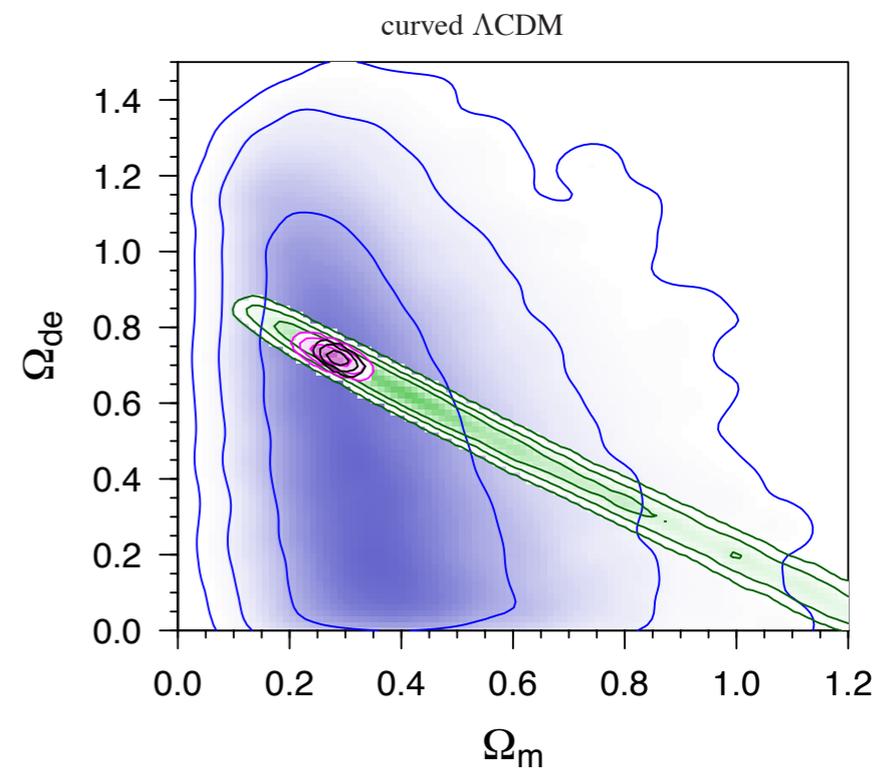
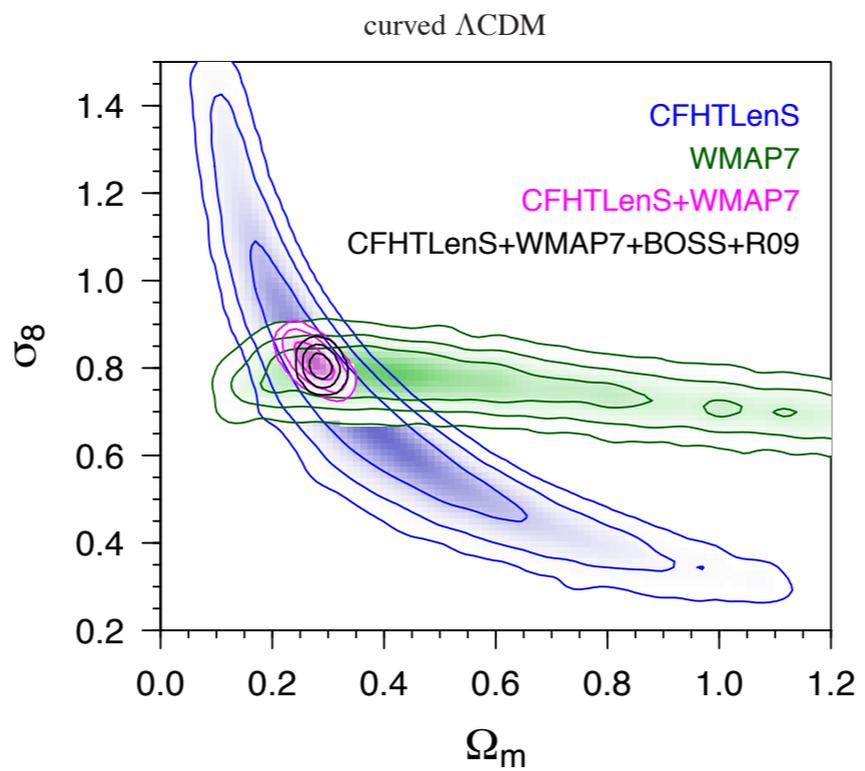
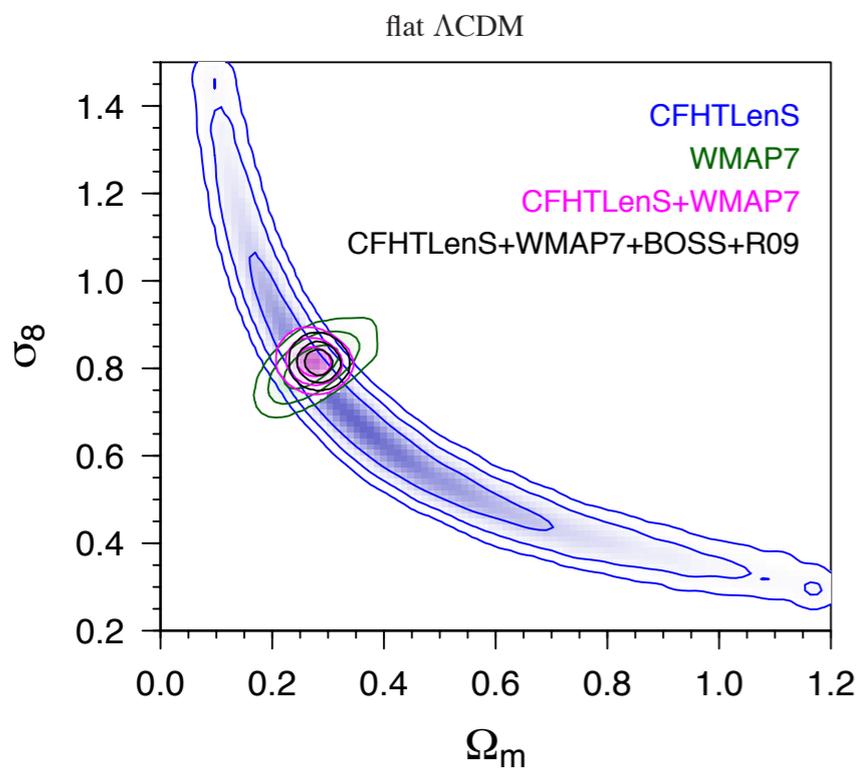
$$w = -1$$

Smith et al. (2003)

non-linear power spectrum

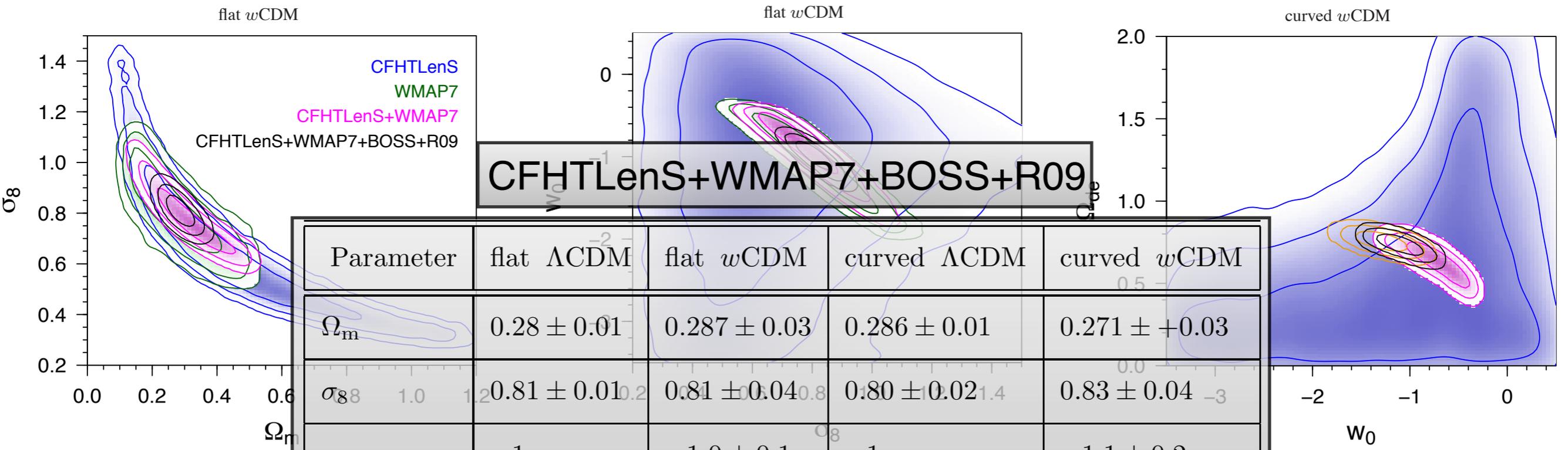
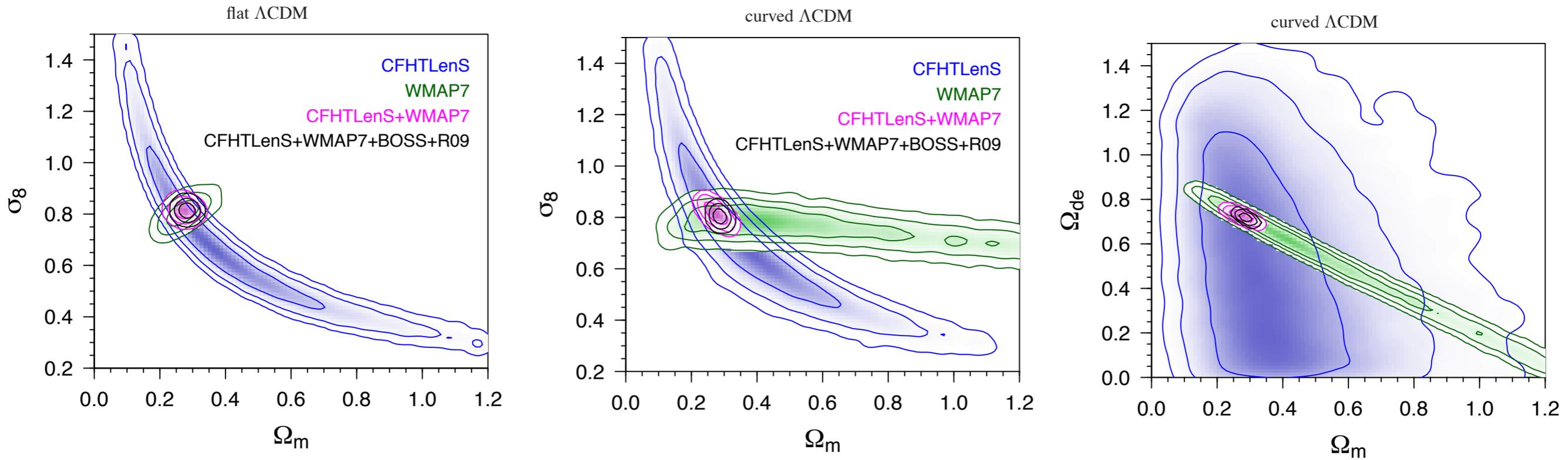
flat  $\Lambda$ CDM





[Kilbinger et al. in 2013]

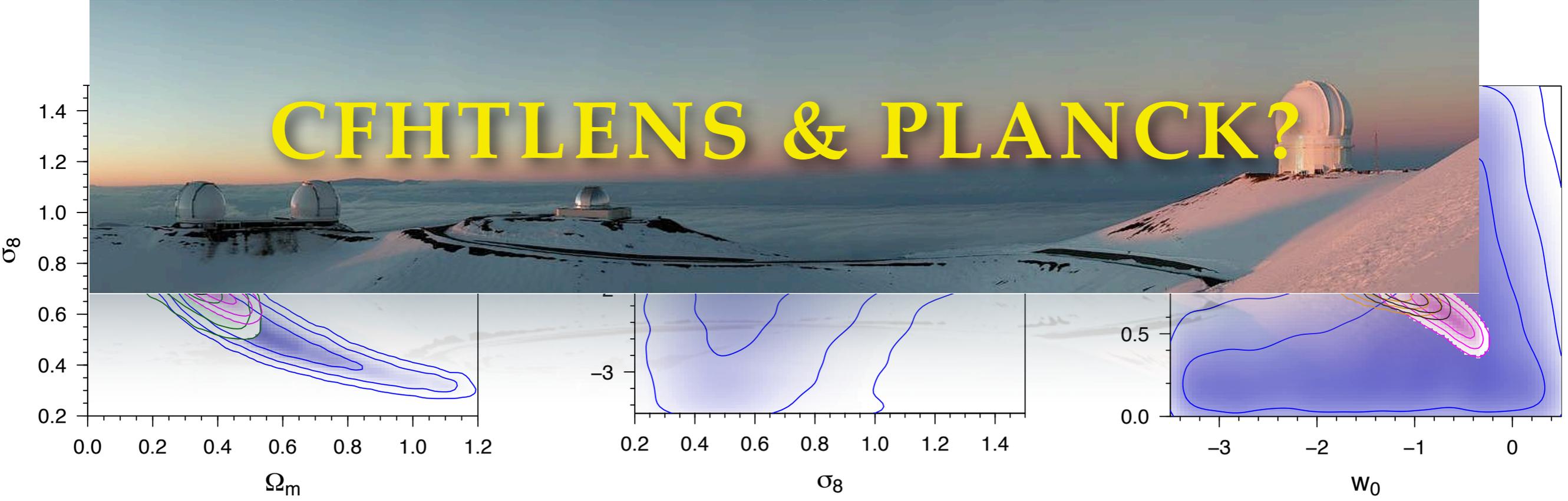
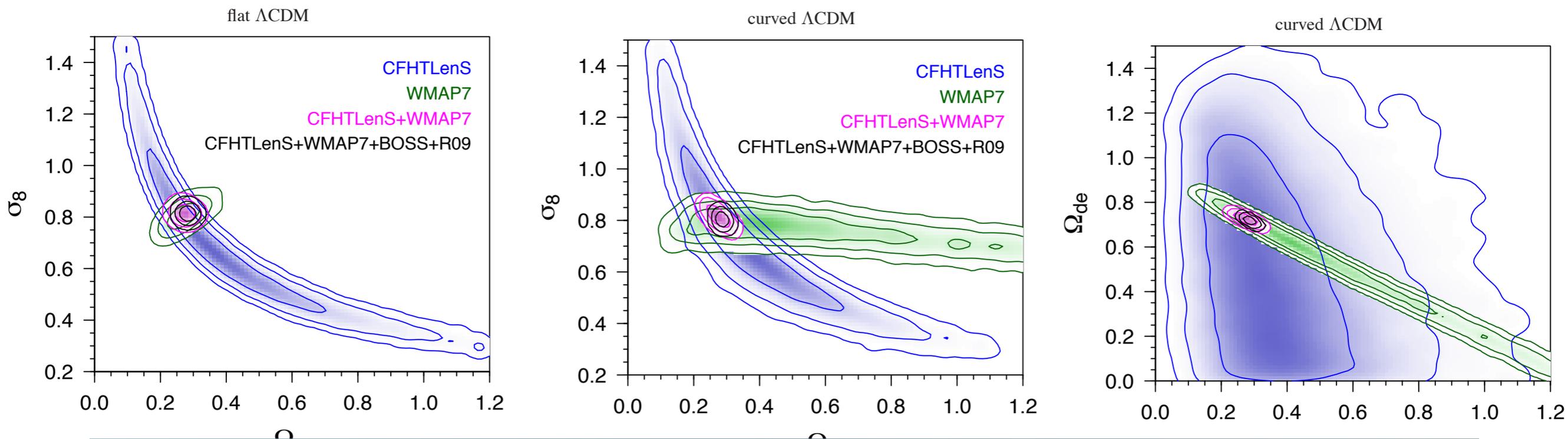
2d cosmic shear,  
no tomography



**CFHTLenS+WMAP7+BOSS+R09**

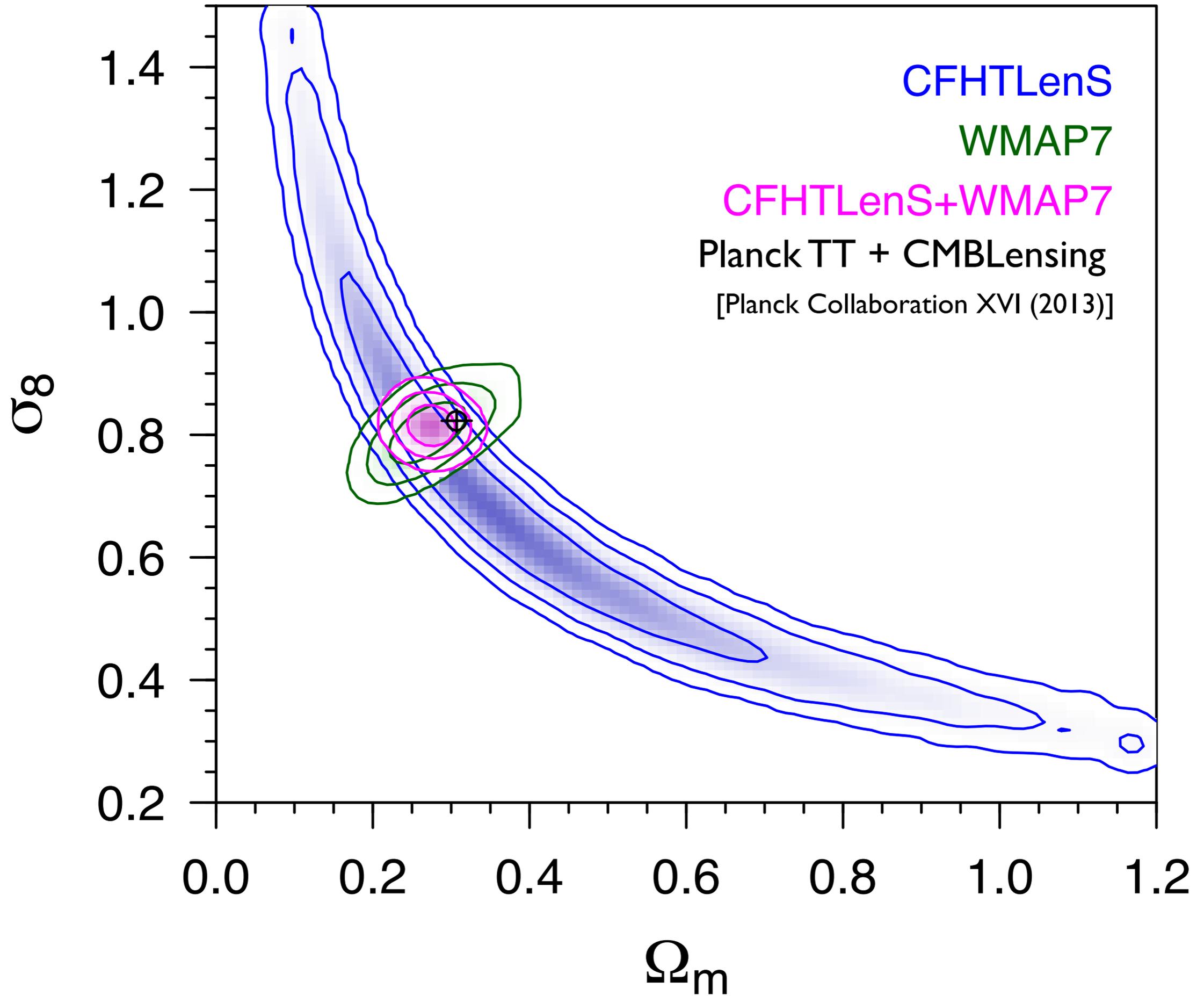
Parameter	flat $\Lambda$ CDM	flat $w$ CDM	curved $\Lambda$ CDM	curved $w$ CDM
$\Omega_m$	$0.28 \pm 0.01$	$0.287 \pm 0.03$	$0.286 \pm 0.01$	$0.271 \pm 0.03$
$\sigma_{88}$	$0.81 \pm 0.01$	$0.81 \pm 0.04$	$0.80 \pm 0.02$	$0.83 \pm 0.04$
$w_0$	-1	$-1.0 \pm 0.1$	-1	$-1.1 \pm 0.2$
$\Omega_{de}$	$1 - \Omega_m$	$1 - \Omega_m$	$0.72 \pm 0.01$	$0.74 \pm 0.03$
$\Omega_K$	0	0	$-0.005 \pm 0.005$	$-0.006^{+0.006}_{-0.005}$

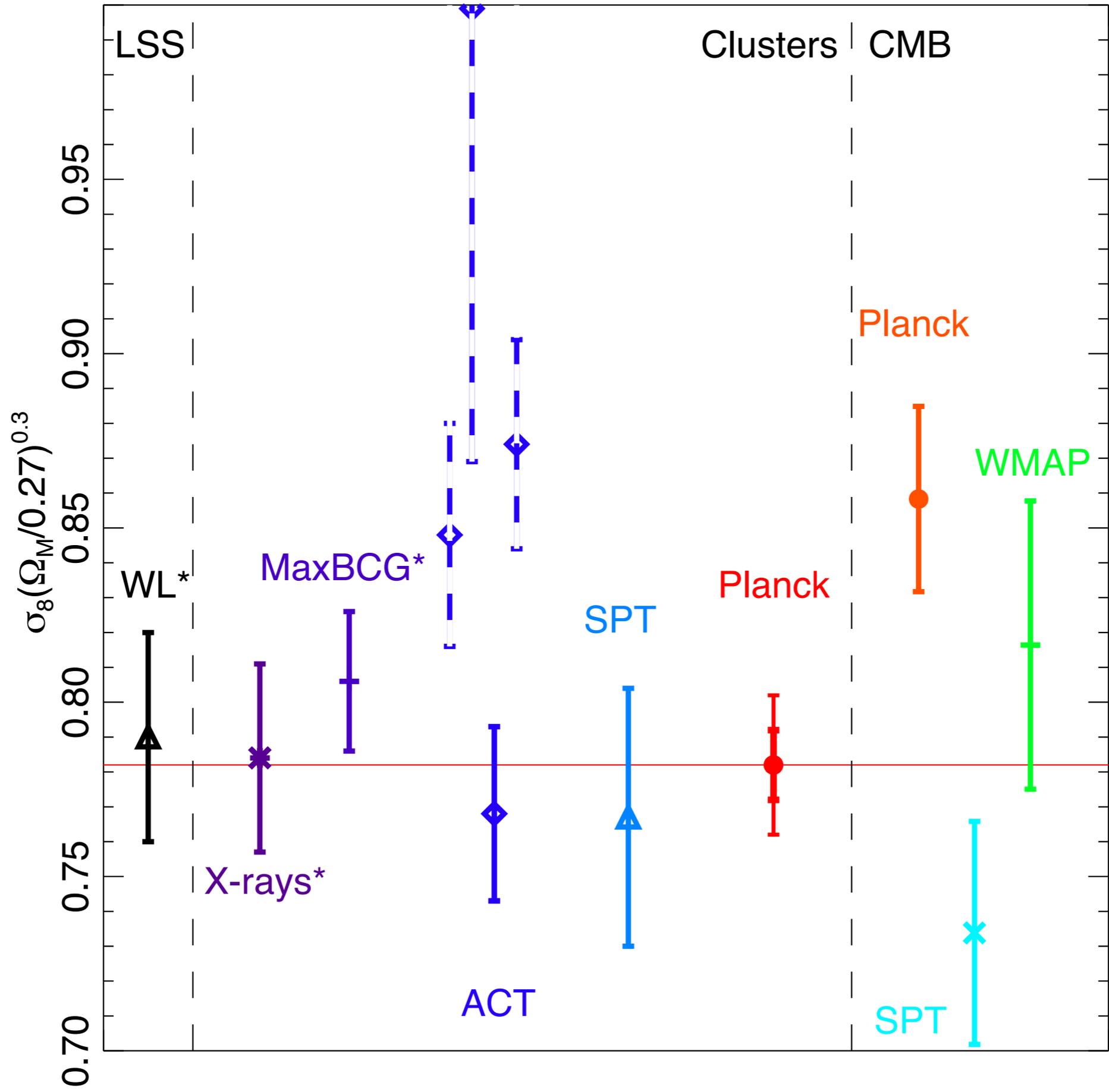
**2d cosmic shear,  
no tomography**



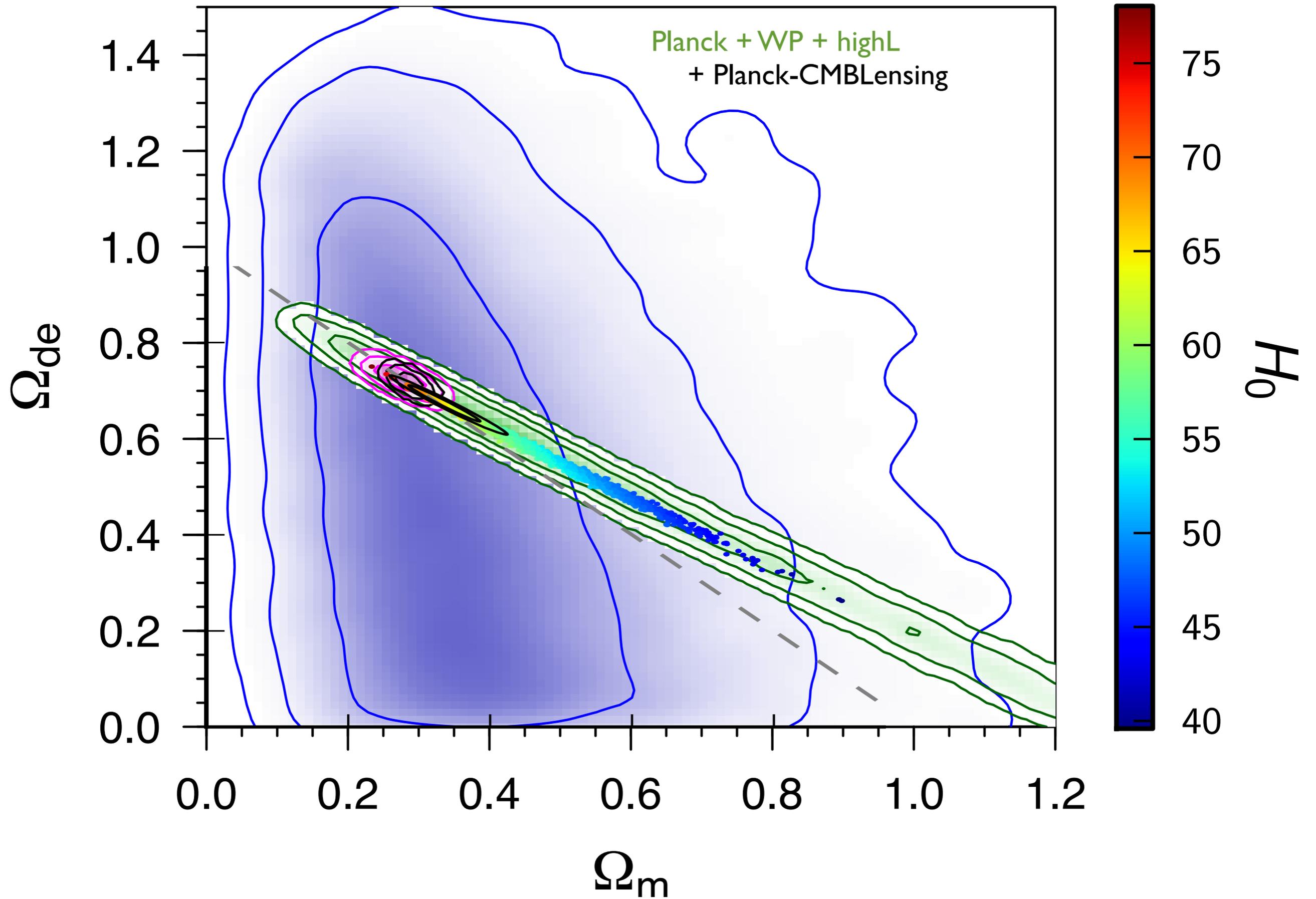
2d cosmic shear,  
no tomography

flat  $\Lambda$ CDM

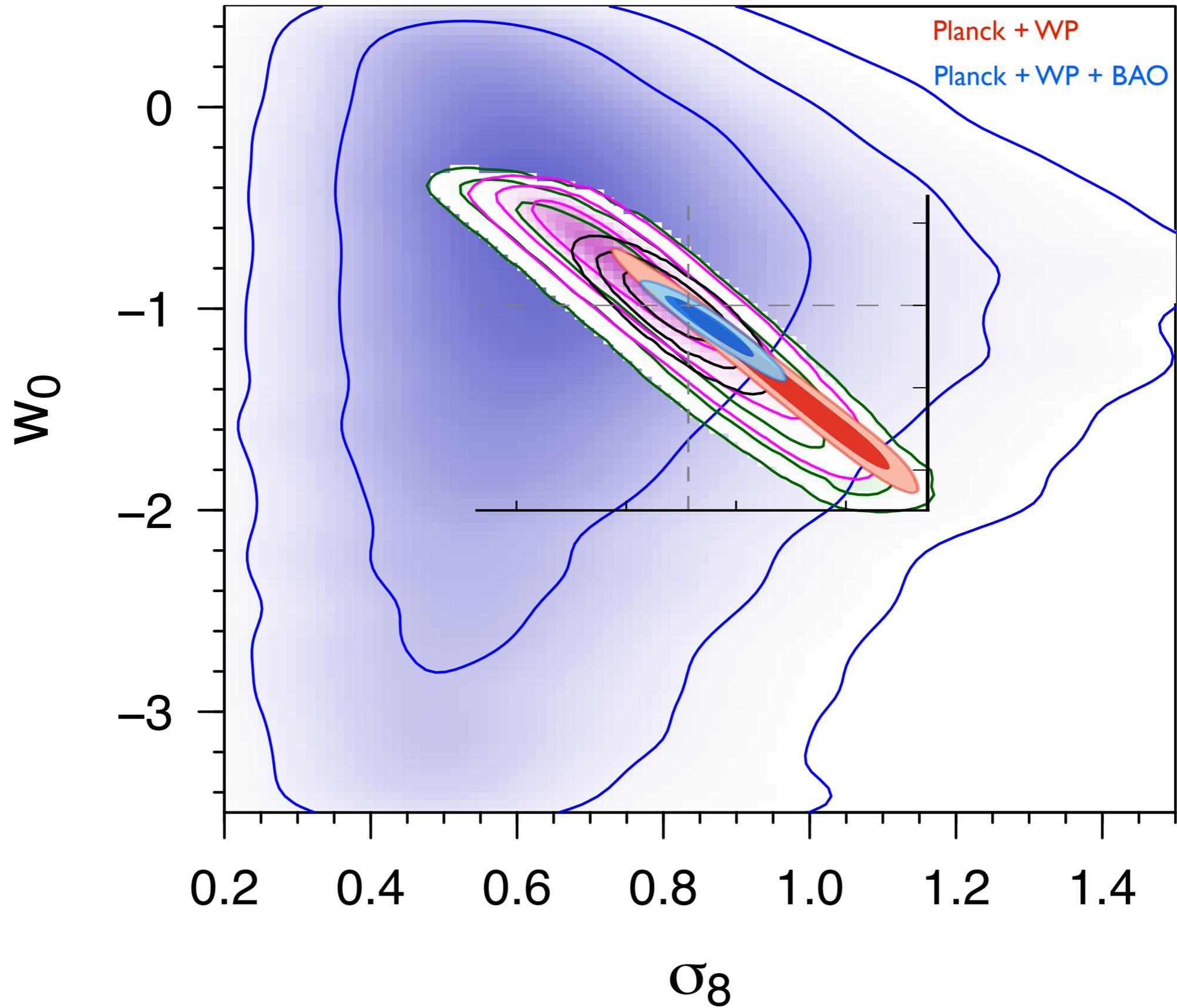


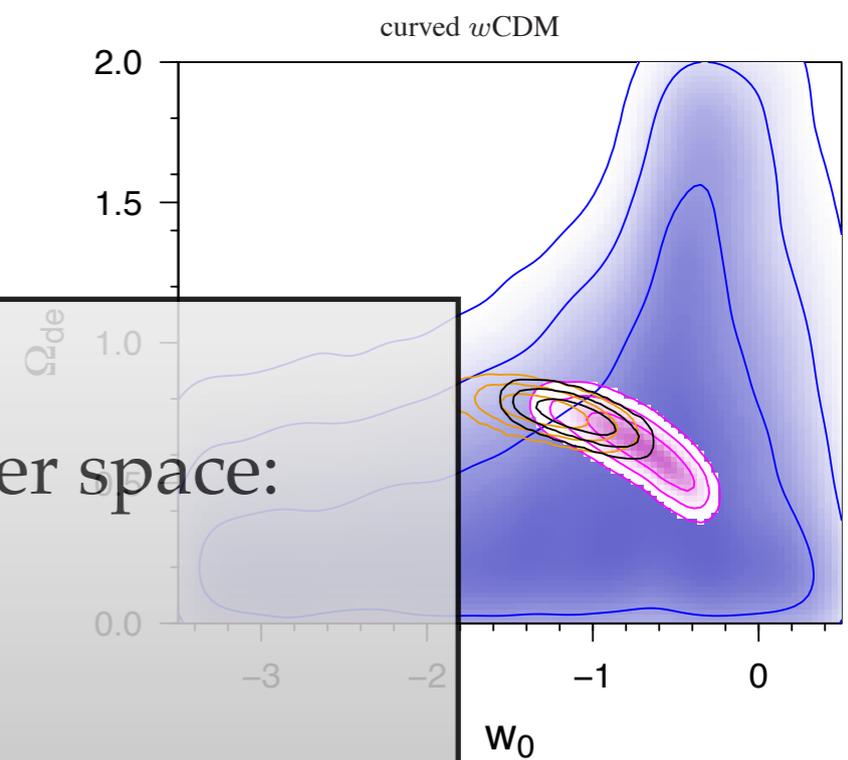
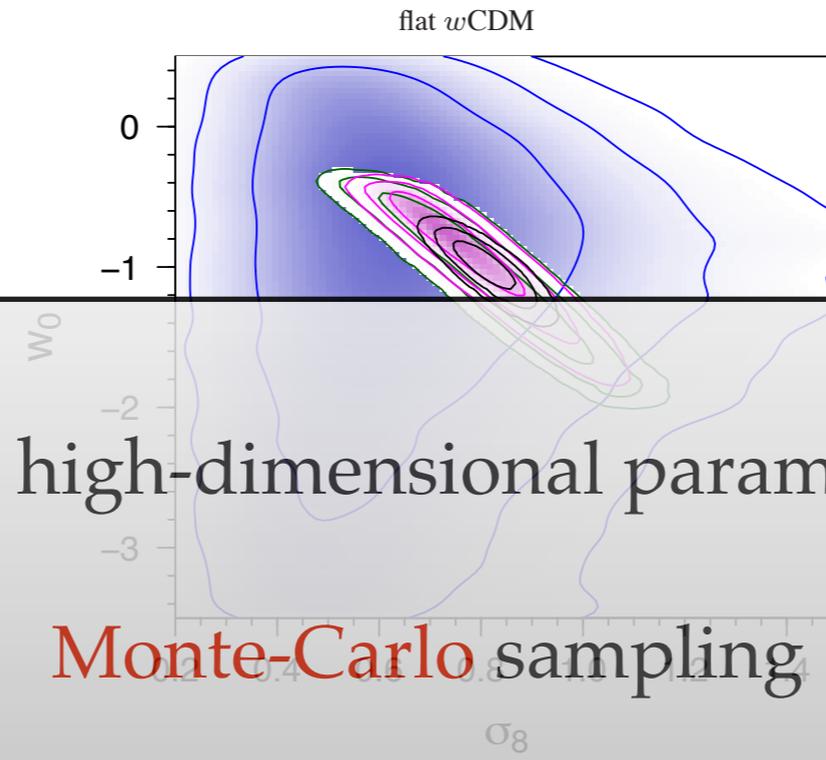
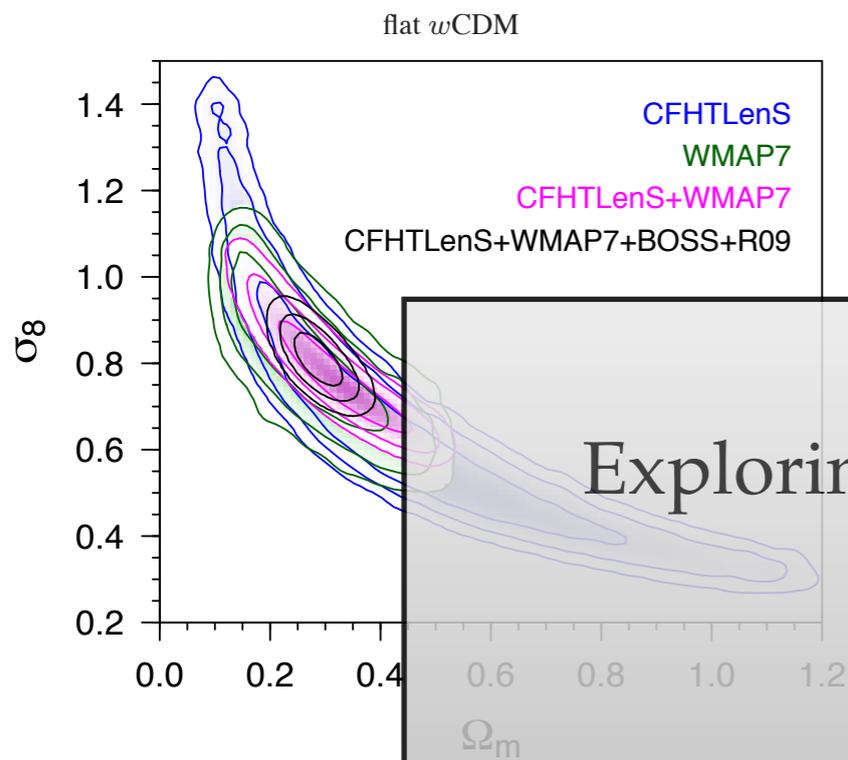
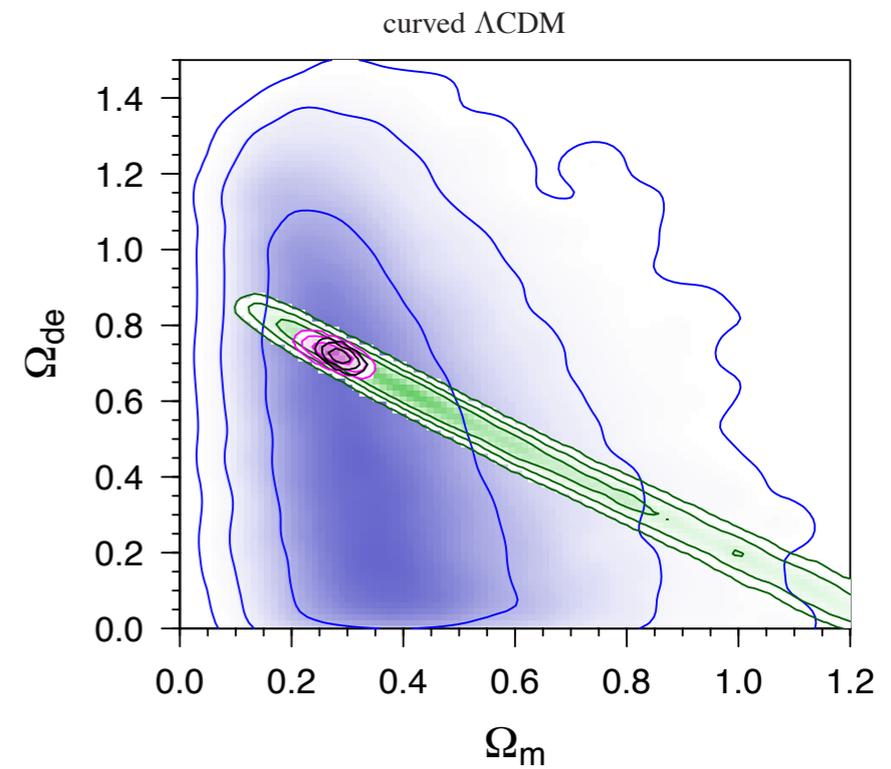
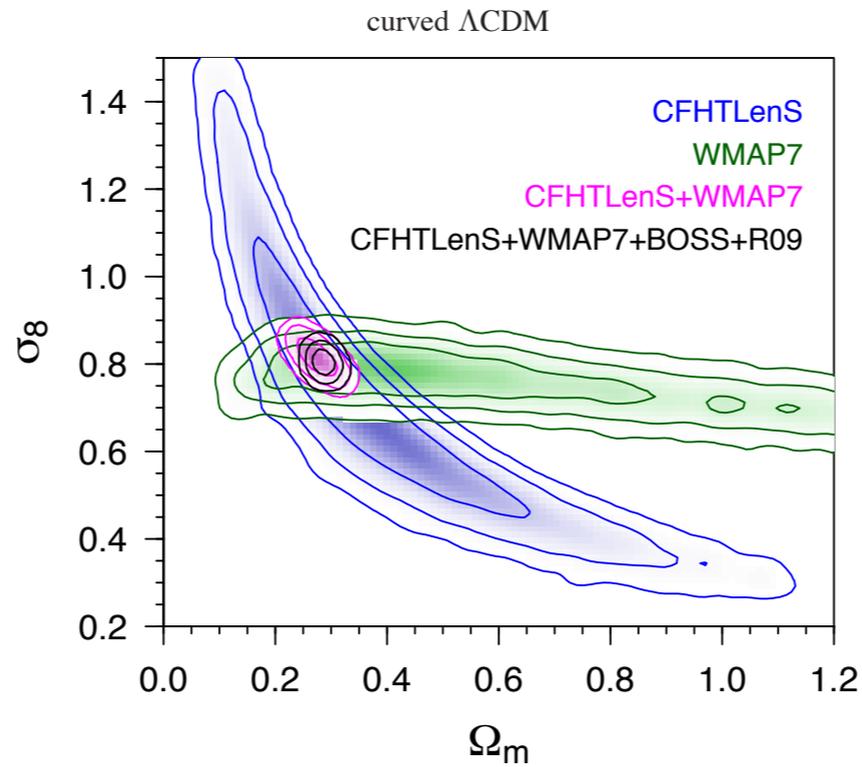
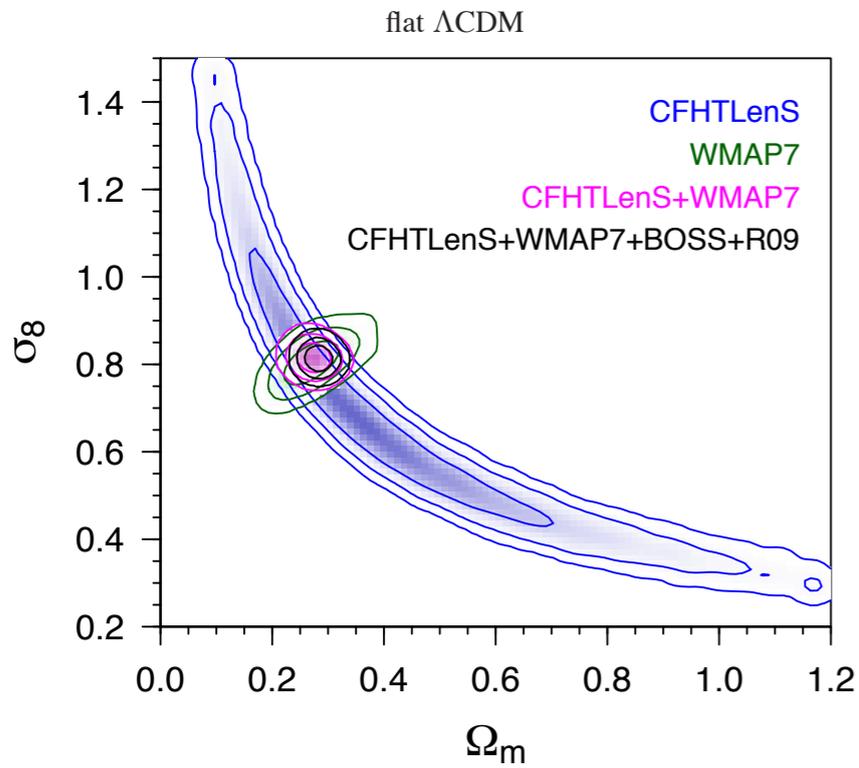


curved  $\Lambda$ CDM



flat  $w$ CDM





Exploring high-dimensional parameter space:

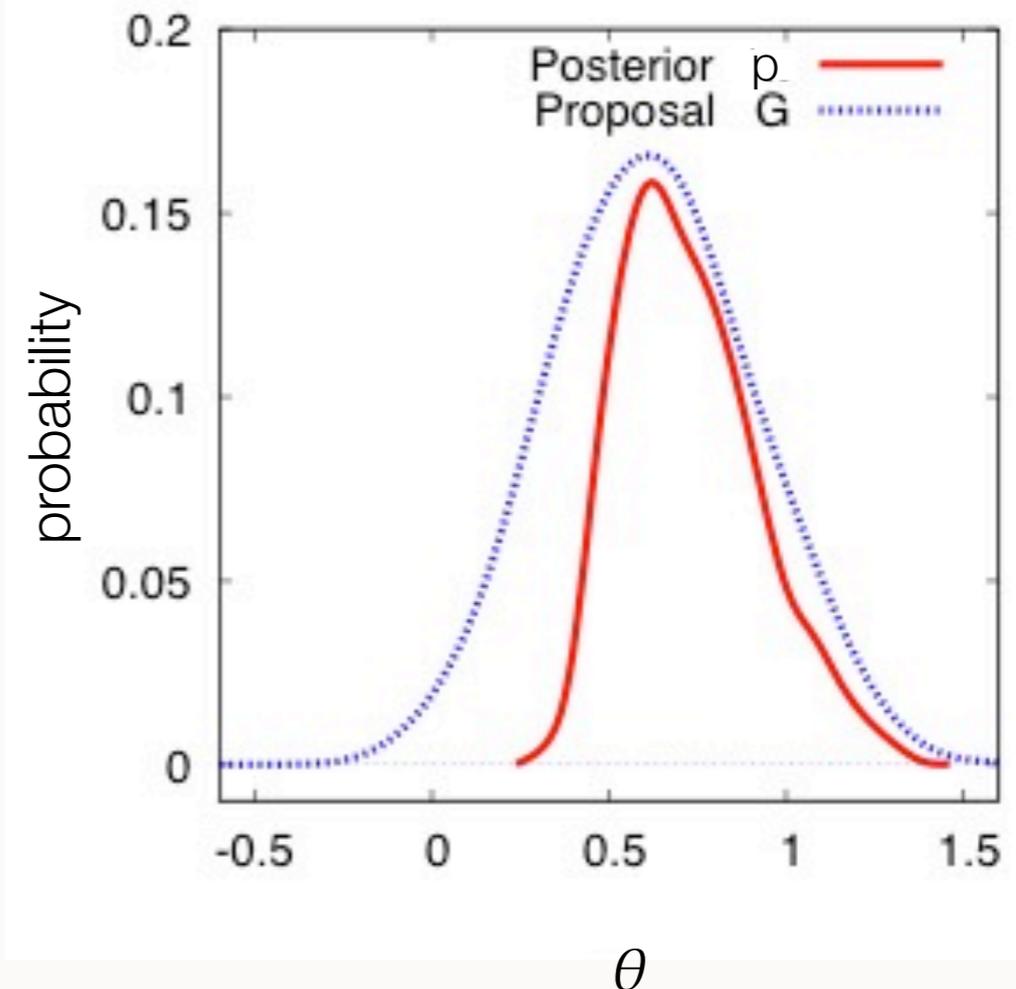
Monte-Carlo sampling

Population Monte Carlo (PMC): Alternative to MCMC

2d cosmic shear,  
no tomography

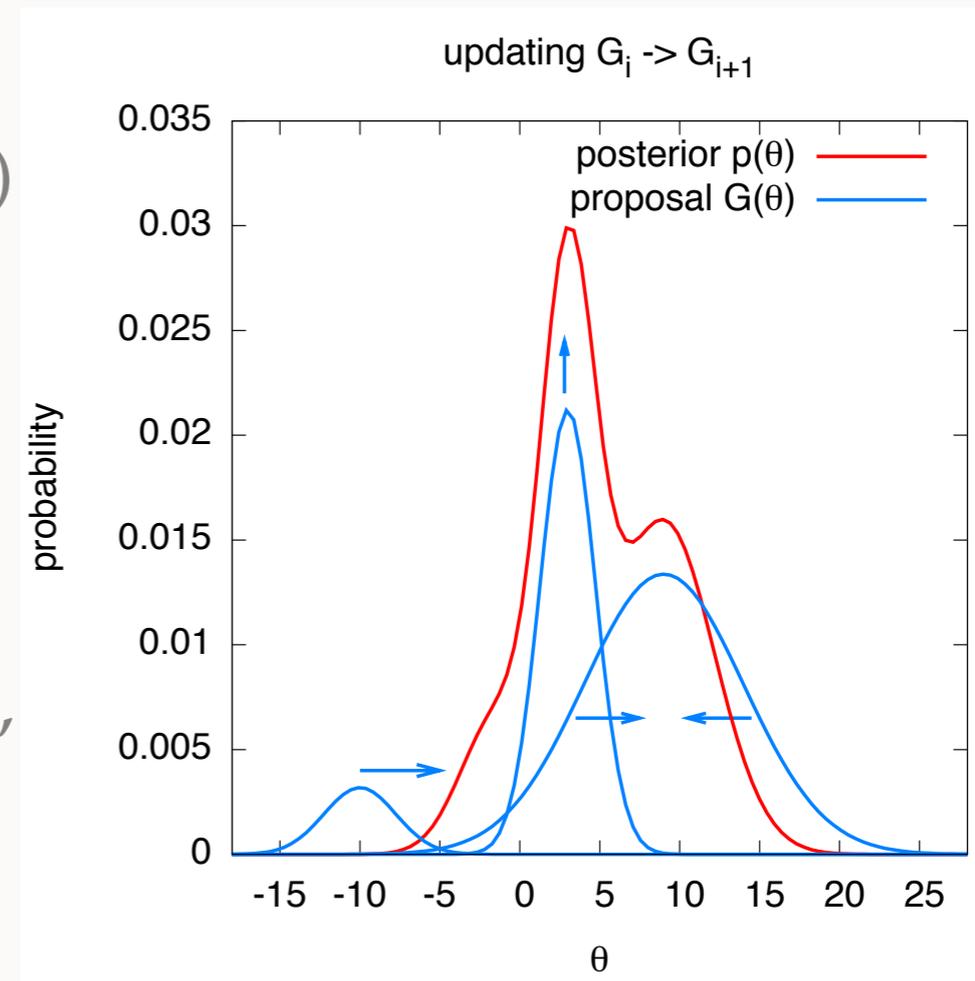
# IMPORTANCE SAMPLING

- Sample from proposal distribution  $G$  (importance function). E.g. mixture of Gaussians
- Weigh each sample point  $\theta$  by ratio (importance weight)  
 $w = p(\theta) / G(\theta)$
- Evaluation of posterior  $p$  (likelihood x prior) can be done in parallel
- Poor performance if proposal far from posterior



# POPULATION MONTE CARLO (PMC)

- Solution: Create adaptive importance samples (“populations”) [Cappé et al. 2004, 2007]
- Iteration  $G_i \rightarrow G_{i+1}$ : Update mean, covariance and component weights
- Stop when proposal  $p$  ‘close enough’
- PMC sample engine and cosmology modules, public code, [www.cosmopmc.info](http://www.cosmopmc.info), [Kilbinger et al. 2010, arXiv:1101.0950]

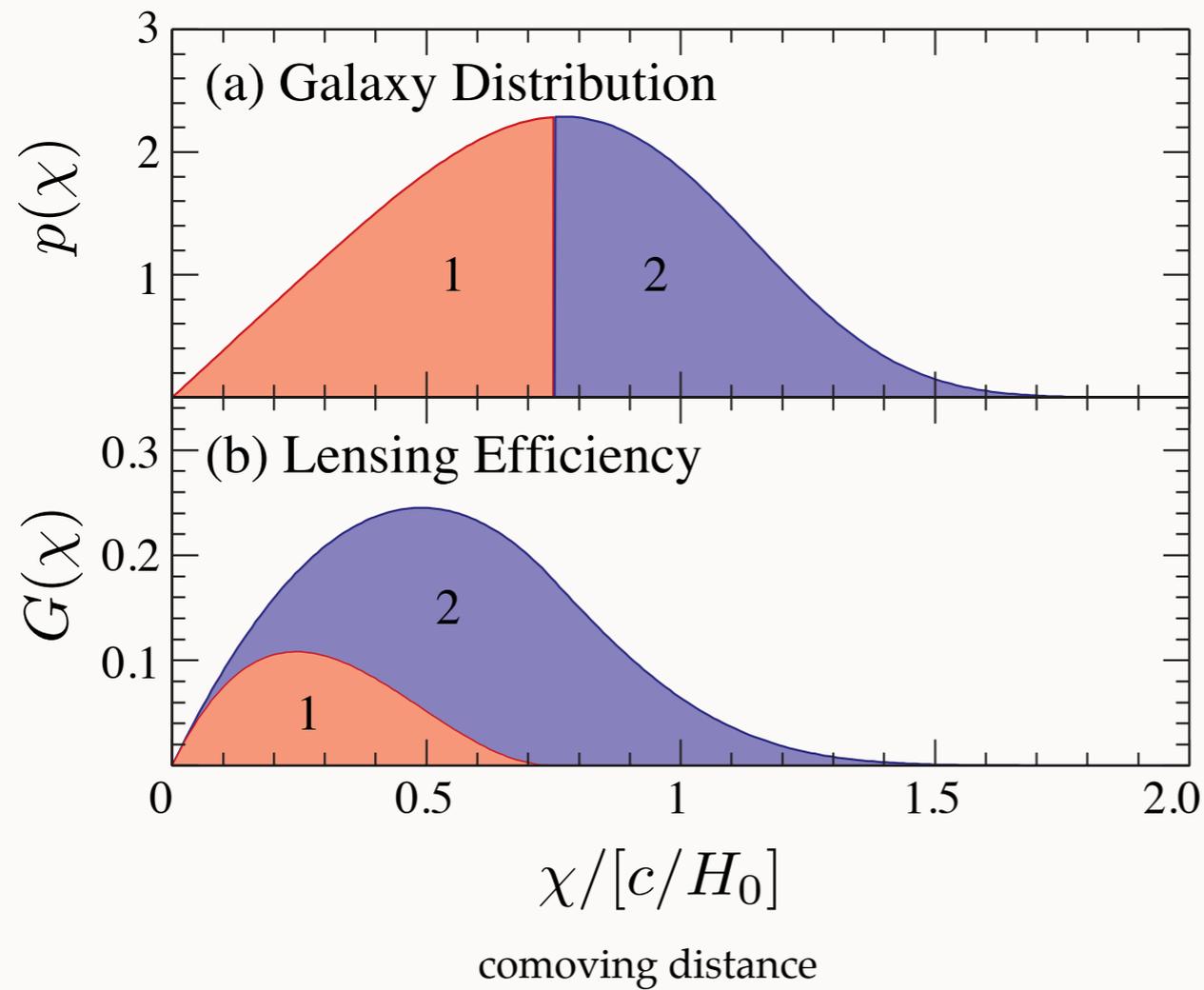


# LENSING TOMOGRAPHY

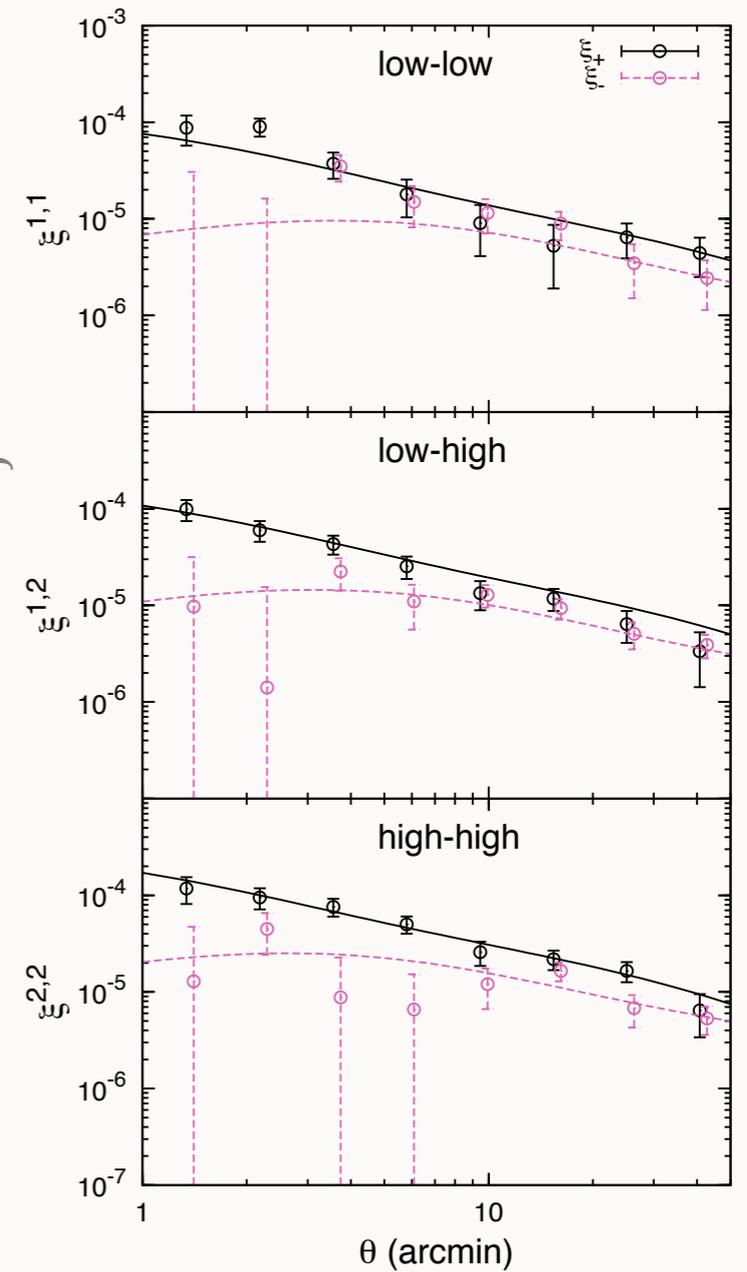
3d cosmic shear:

low:  $z = [0.5; 0.85]$

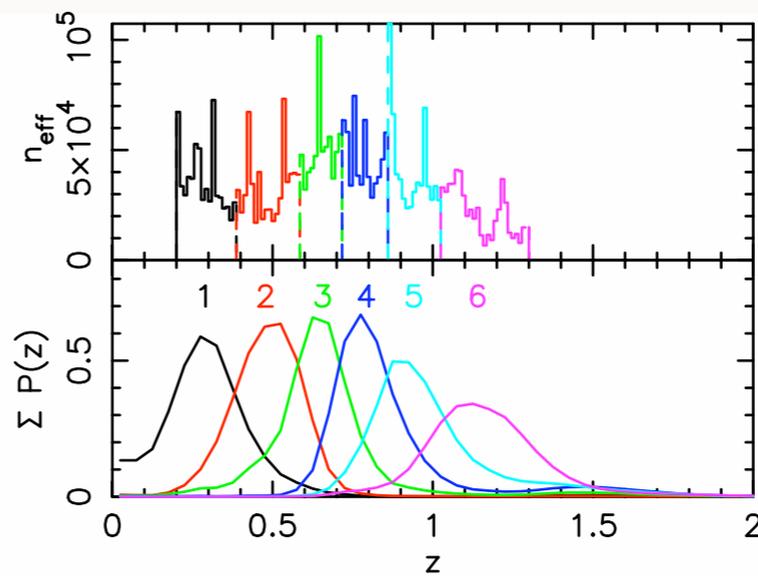
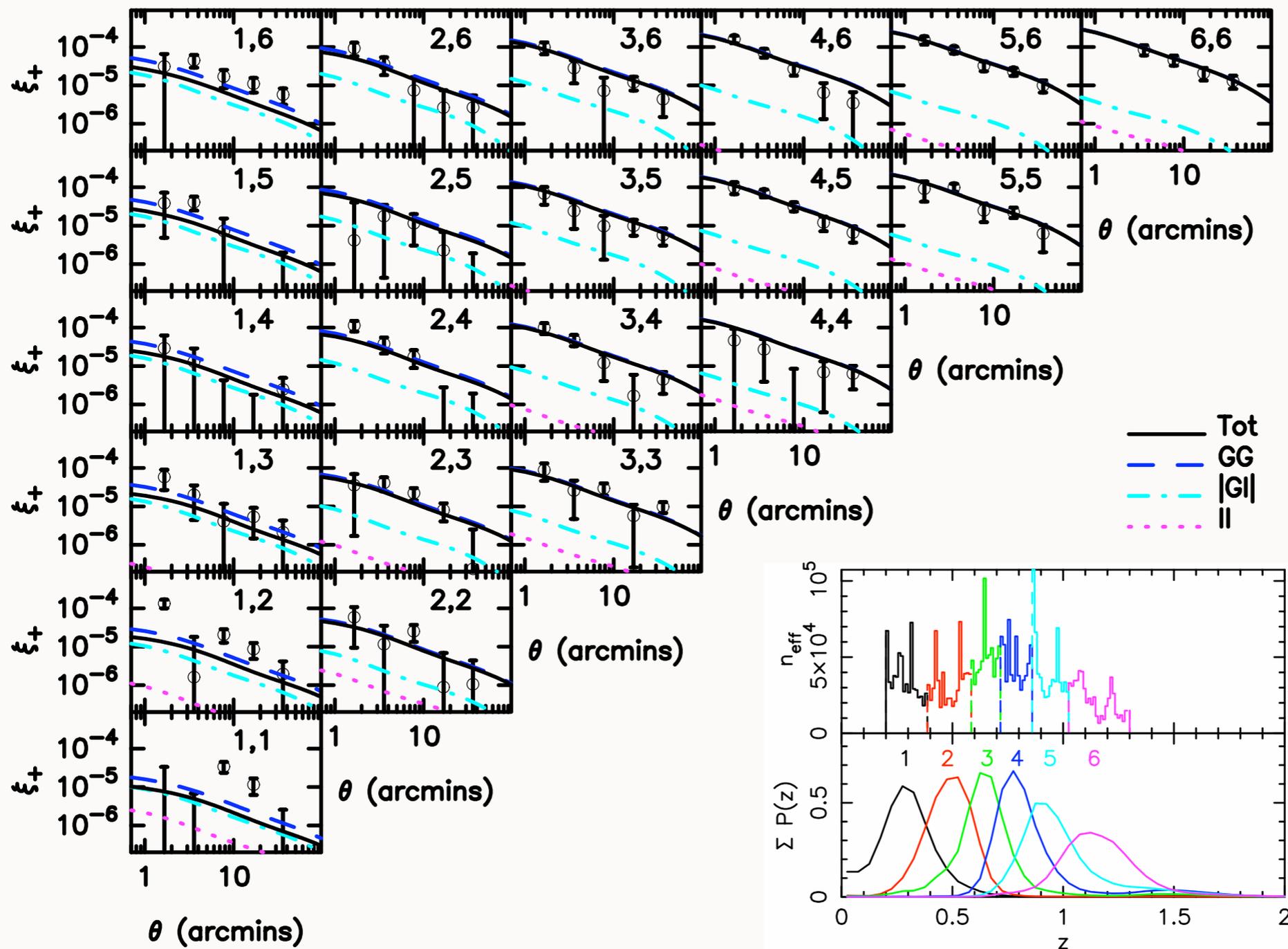
high:  $z = [0.85; 1.3]$



Benjamin et al. 2013



# LENSING TOMOGRAPHY

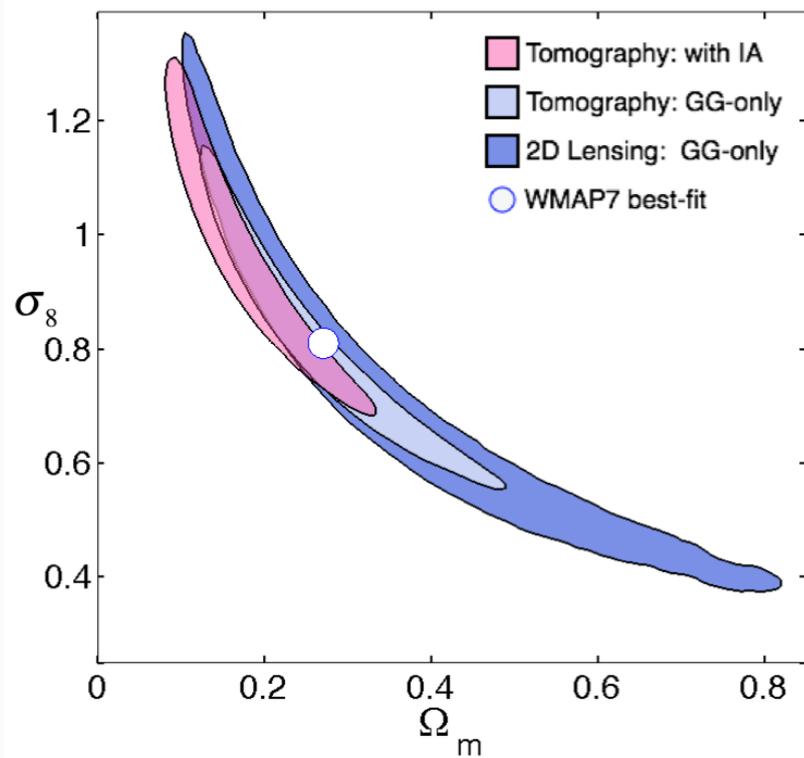


Bin	$z_{\text{BPZ}}$	$z_m$	$\bar{z}$
1	0.20 – 0.39	0.28	0.36
2	0.39 – 0.58	0.48	0.50
3	0.58 – 0.72	0.62	0.68
4	0.72 – 0.86	0.82	0.87
5	0.86 – 1.02	0.93	1.00
6	1.02 – 1.30	1.12	1.16

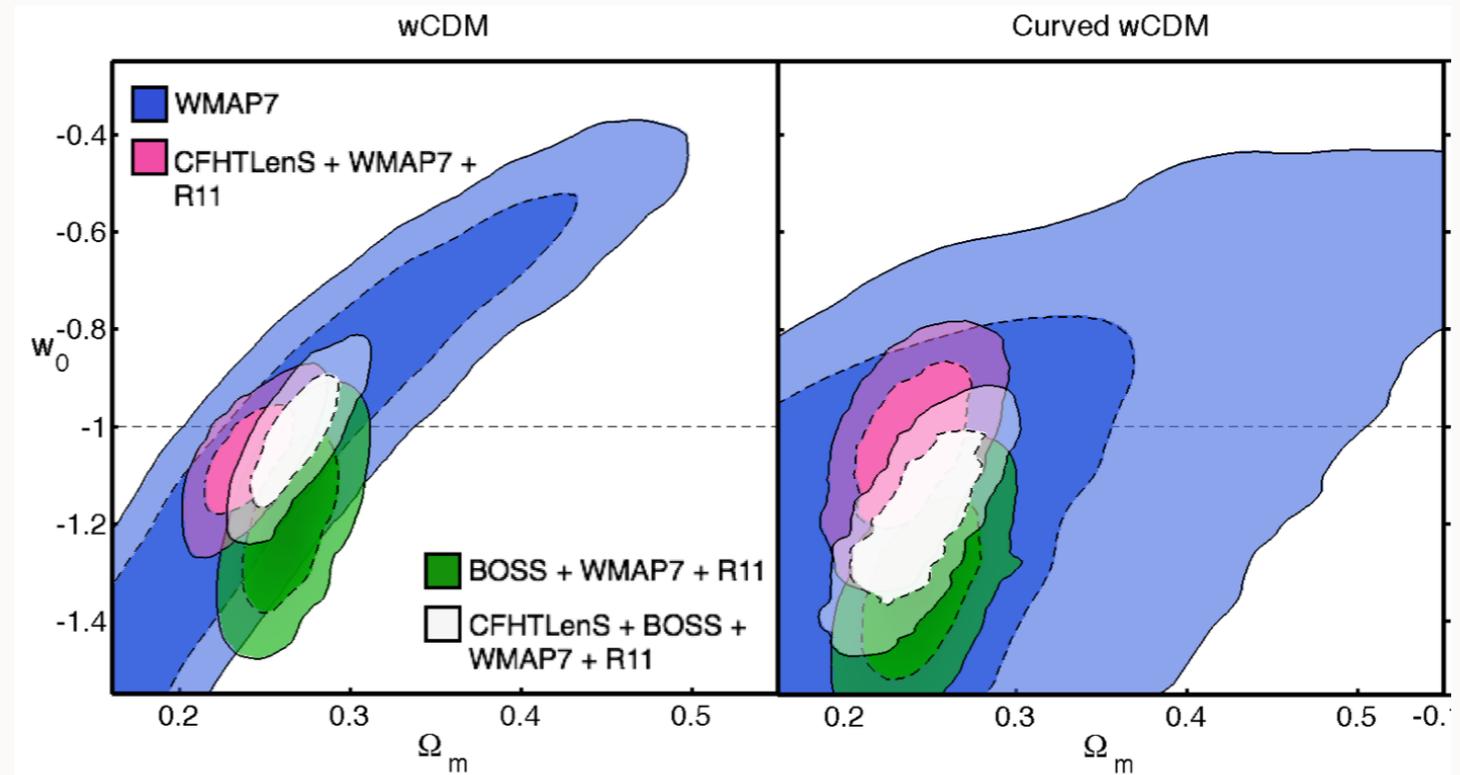
[Heymans et al. 2013]

# LENSING TOMOGRAPHY

[Heymans et al. 2013]



Tomography helps lifting the  $\Omega_m - \sigma_8$  degeneracy of 2D lensing.



CFHTLenS + WMAP7 + R11 + BOSS

flat  $w$ CDM

curved  $w$ CDM

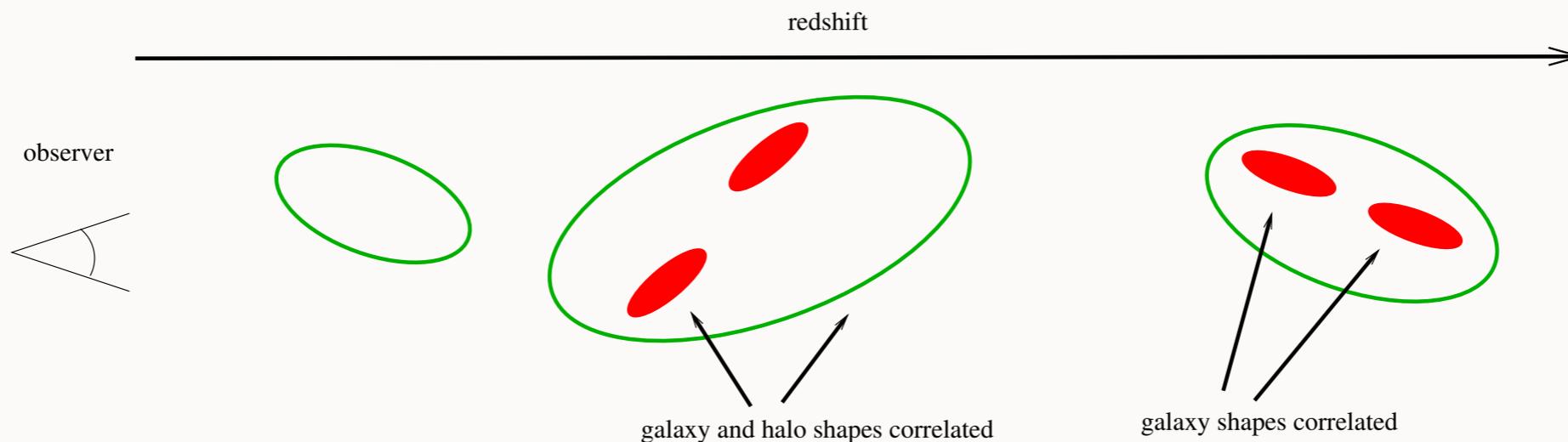
$w_0$

$-1.02^{+0.09}_{-0.09}$

$-1.19^{+0.14}_{-0.11}$

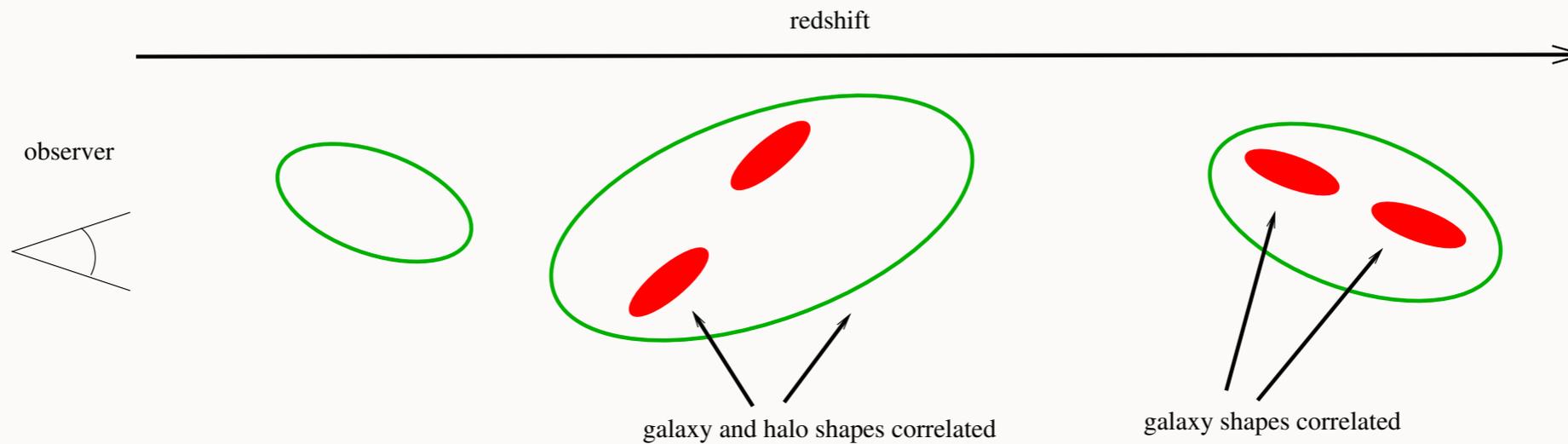
# INTRINSIC ALIGNMENT

- Galaxy shapes correlated with environment, e.g. dm halo shape



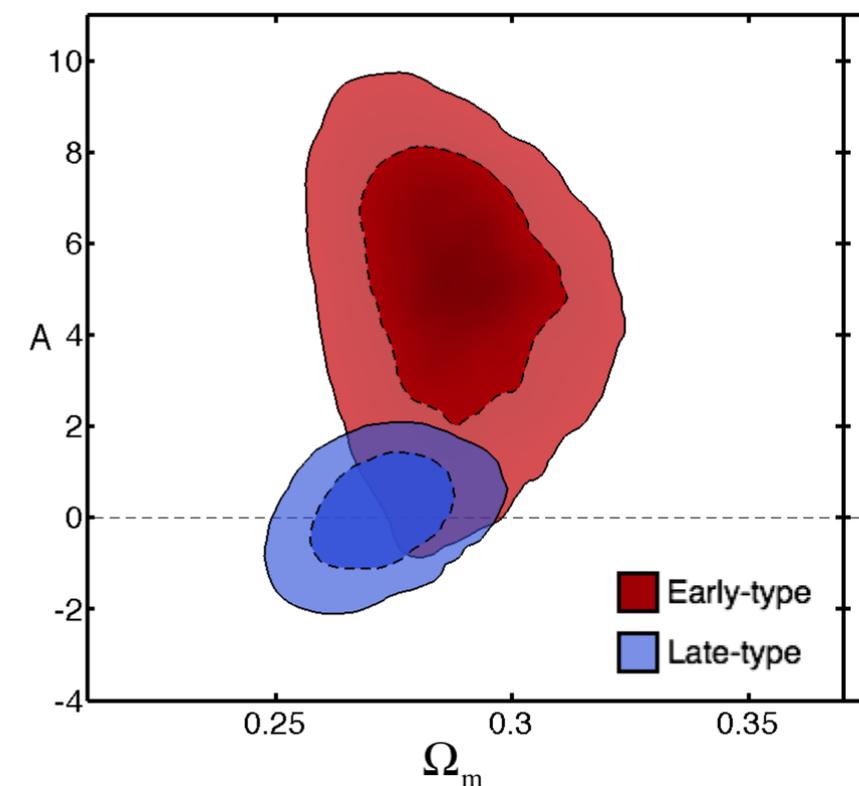
- Galaxies at same  $z$ : remove from analysis
- Galaxies @ different  $z$ :
  - Nulling (model-independent): scan through  $z$  (Benjamini, Schneider)
  - Fitting shear + alignment models: many parameters (Bridle, King, Kirk)

# INTRINSIC ALIGNMENT



Simple intrinsic alignment model:  
Galaxy ellipticity linearly related to tidal field  
[Hirata & Seljak 2004, Bridle & King 2007].

One free amplitude parameter  $A$ , fixed  $z$ -dependence.



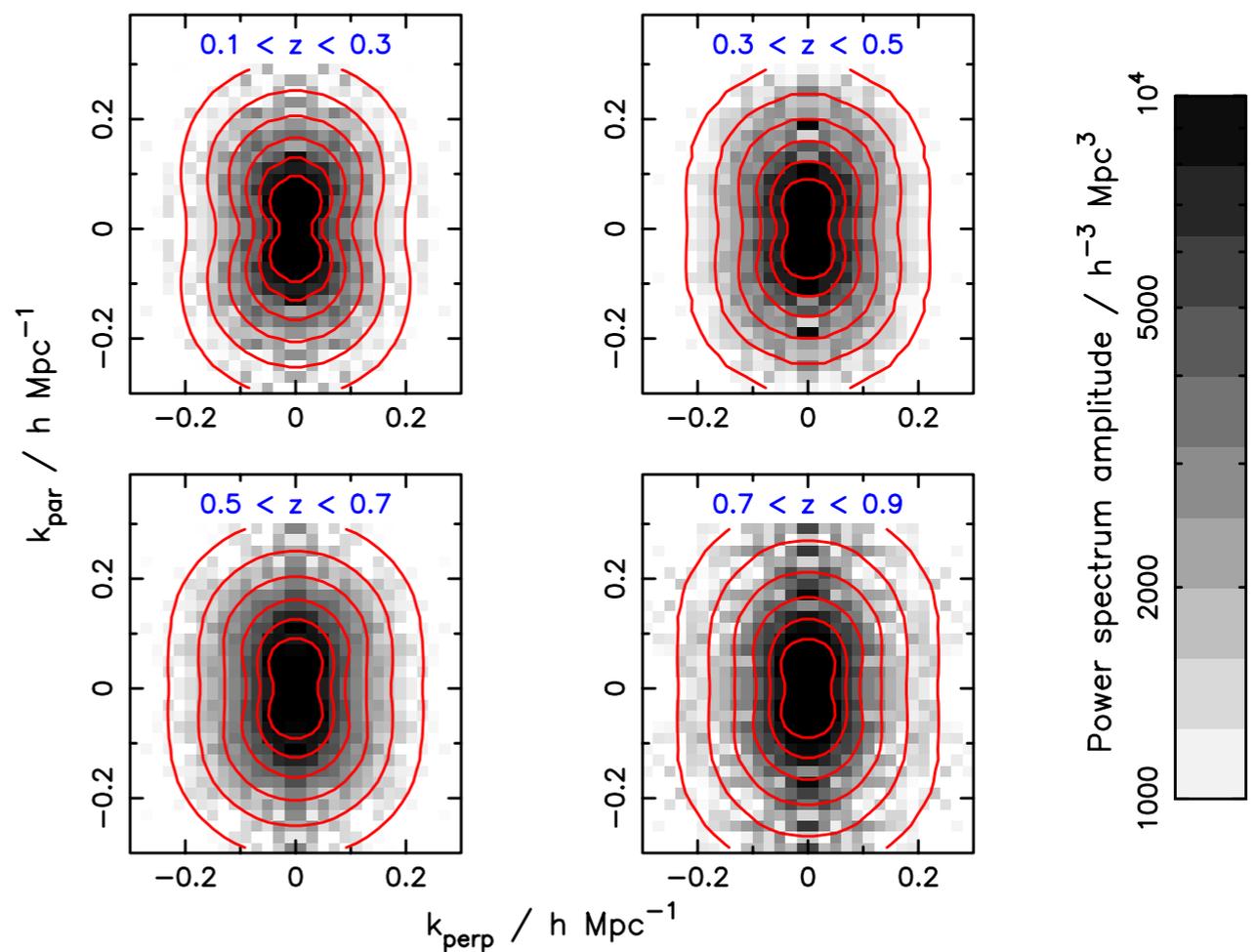
[Heymans et al. 2013]

# MODIFIED GRAVITY



# WIGGLE-Z DATA

- CFHTLenS Cosmic Shear
  - Two redshift bins;  $1 < \theta < 100$  arcmin
- WiggleZ Redshift Space Distortions (Blake et al. 2011)
- Auxiliary Data
  - WMAP7 ( $l > 100$ )
  - $H_0 = 73.8 \pm 0.024 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (Riess et al. 2011)
- Utilise CosmoPMC, MGCAMB, WMAP Likelihood, CosmoloGUI



Blake et al 2011

- non-constant Sigma, mu: only late-time effect. Time-dependence like DE. CMB would dominate constraint on const S, m

# METRISATION

$$ds^2 = -(1 + 2\varphi)dt^2 + (1 - 2\phi)a^2 dx^{\Gamma 2}$$

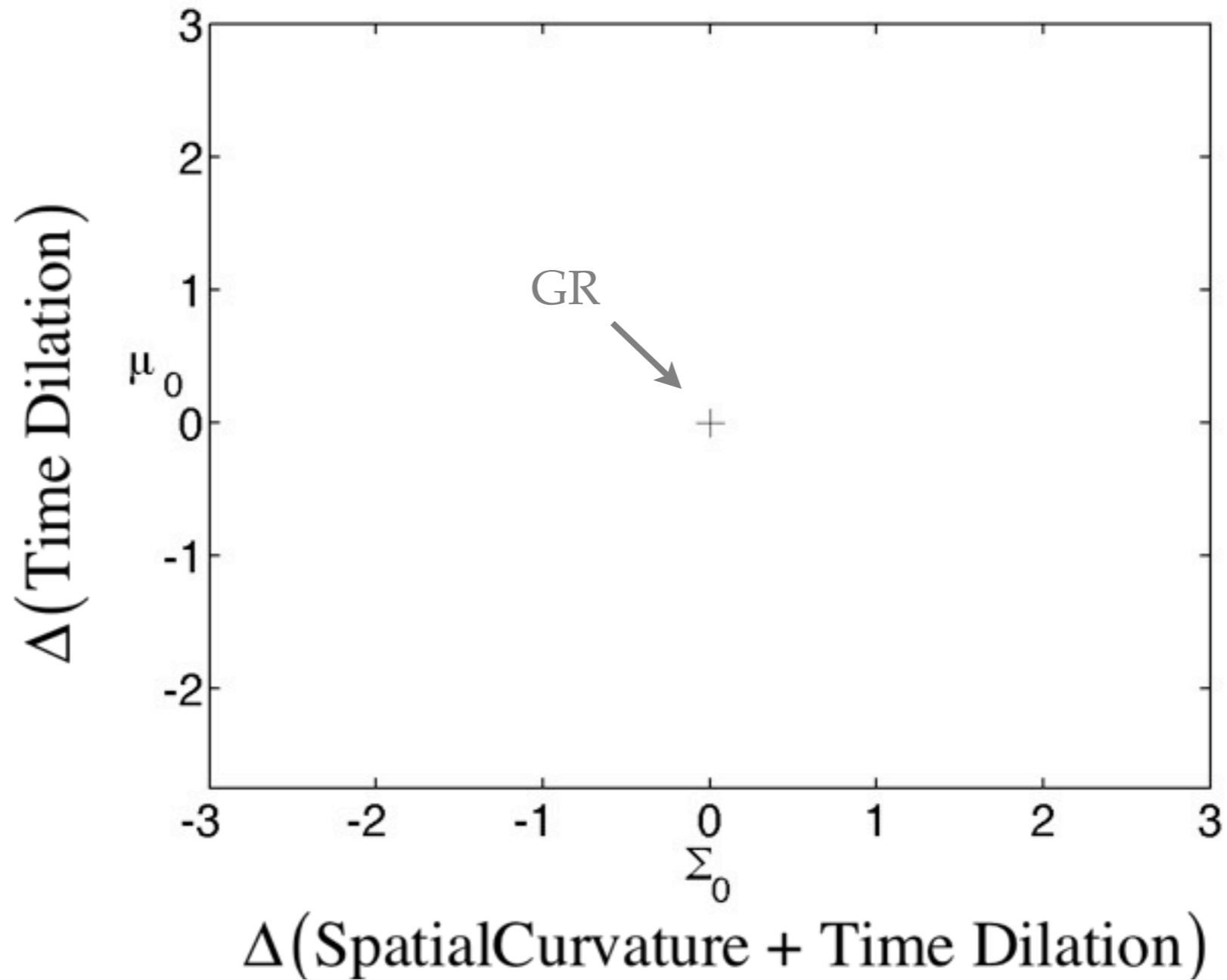
▣ Gravitational potential as experienced by galaxies:

$$\nabla^2 \varphi = 4\pi G a^2 \bar{\rho} \delta [1 + \mu] \quad \mu(a) \propto \Omega_{\Lambda}(a)$$

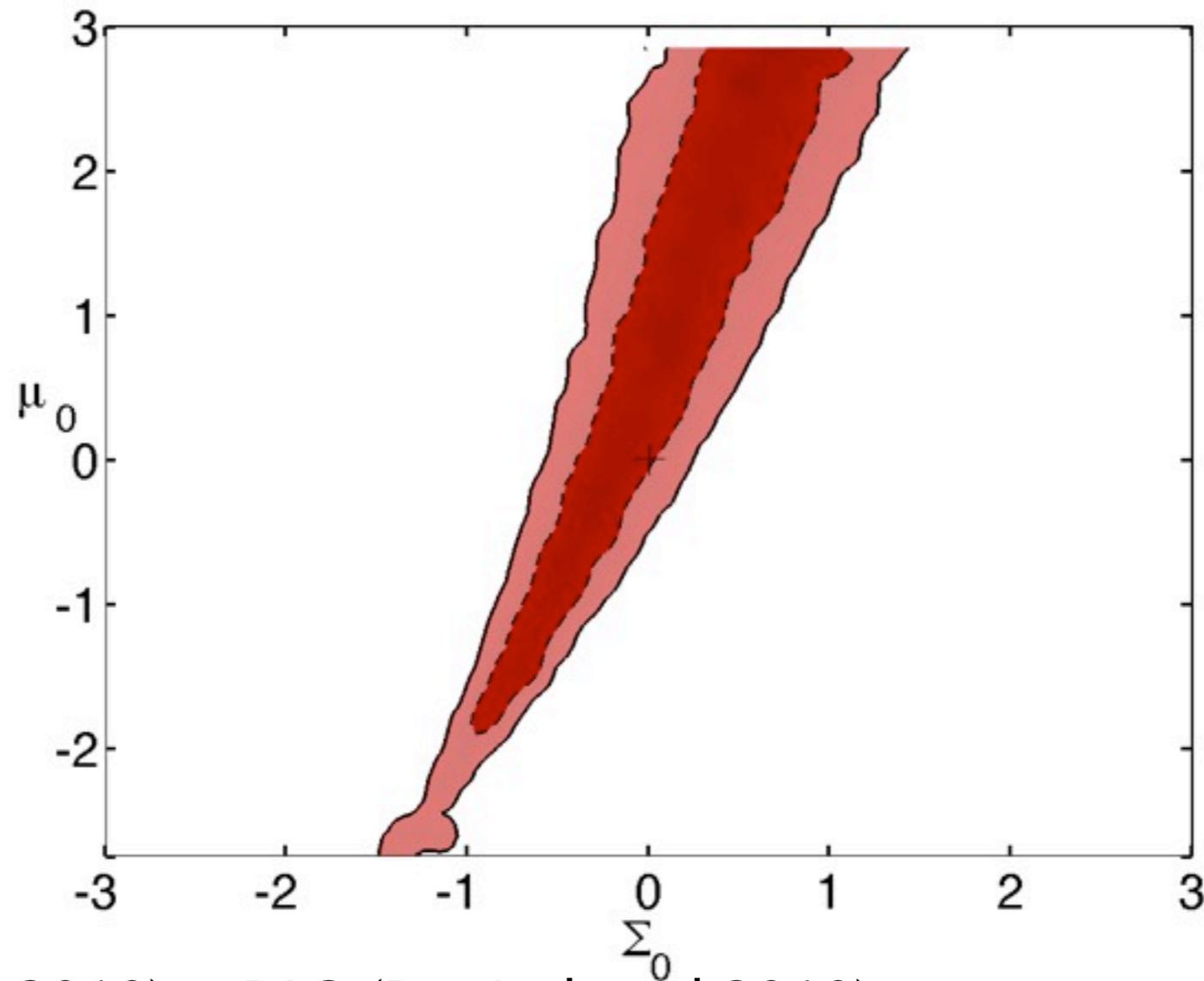
▣ Gravitational potential as experienced by photons:

$$\nabla^2 (\varphi + \phi) = 8\pi G a^2 \bar{\rho} \delta [1 + \Sigma] \quad \Sigma(a) \propto \Omega_{\Lambda}(a)$$

# PARAMETRISATION



# PREVIOUS CONSTRAINTS

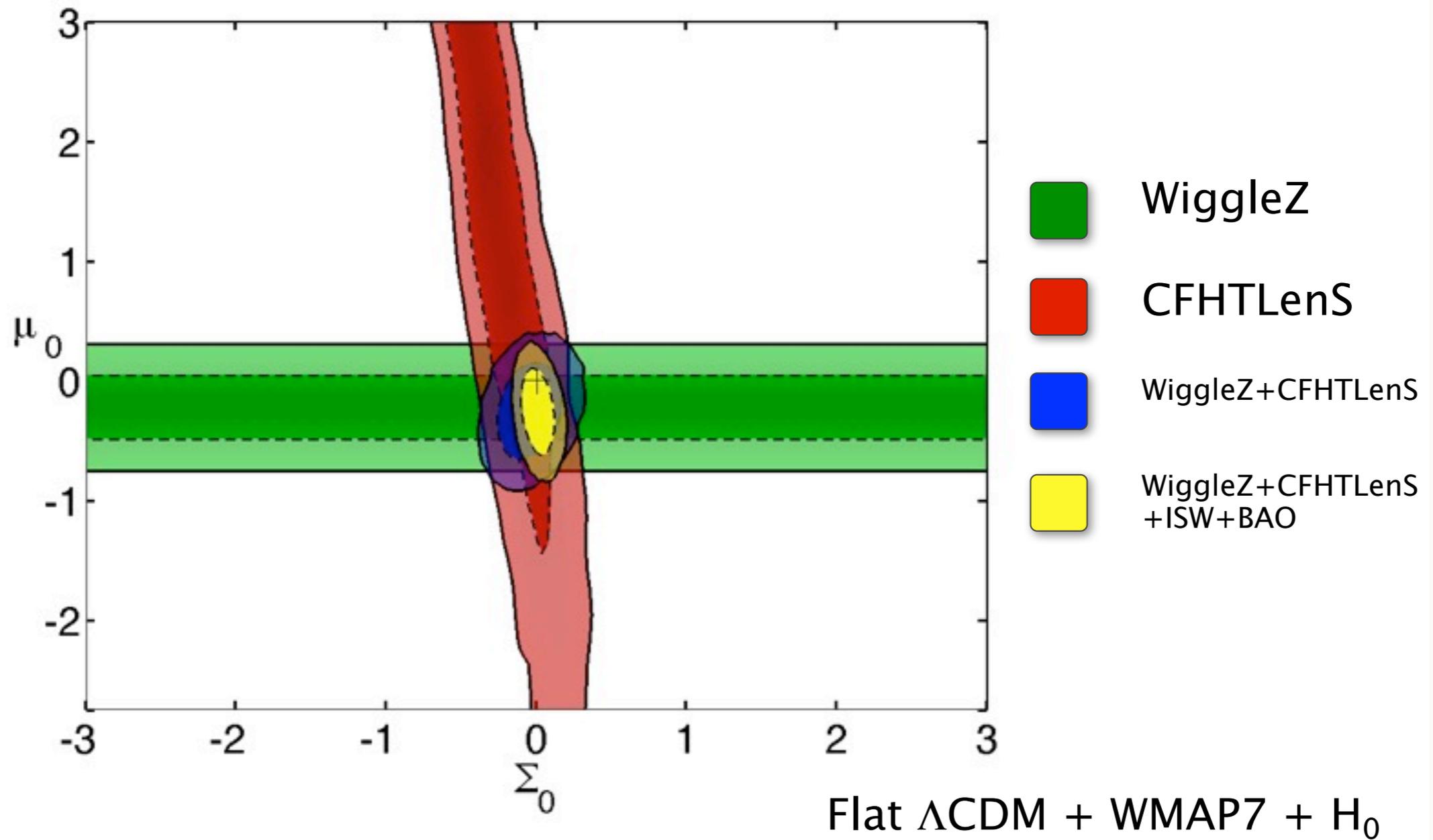


$E_G$  (Reyes et al 2010) + BAO (Percival et al 2010)

Flat  $\Lambda$ CDM

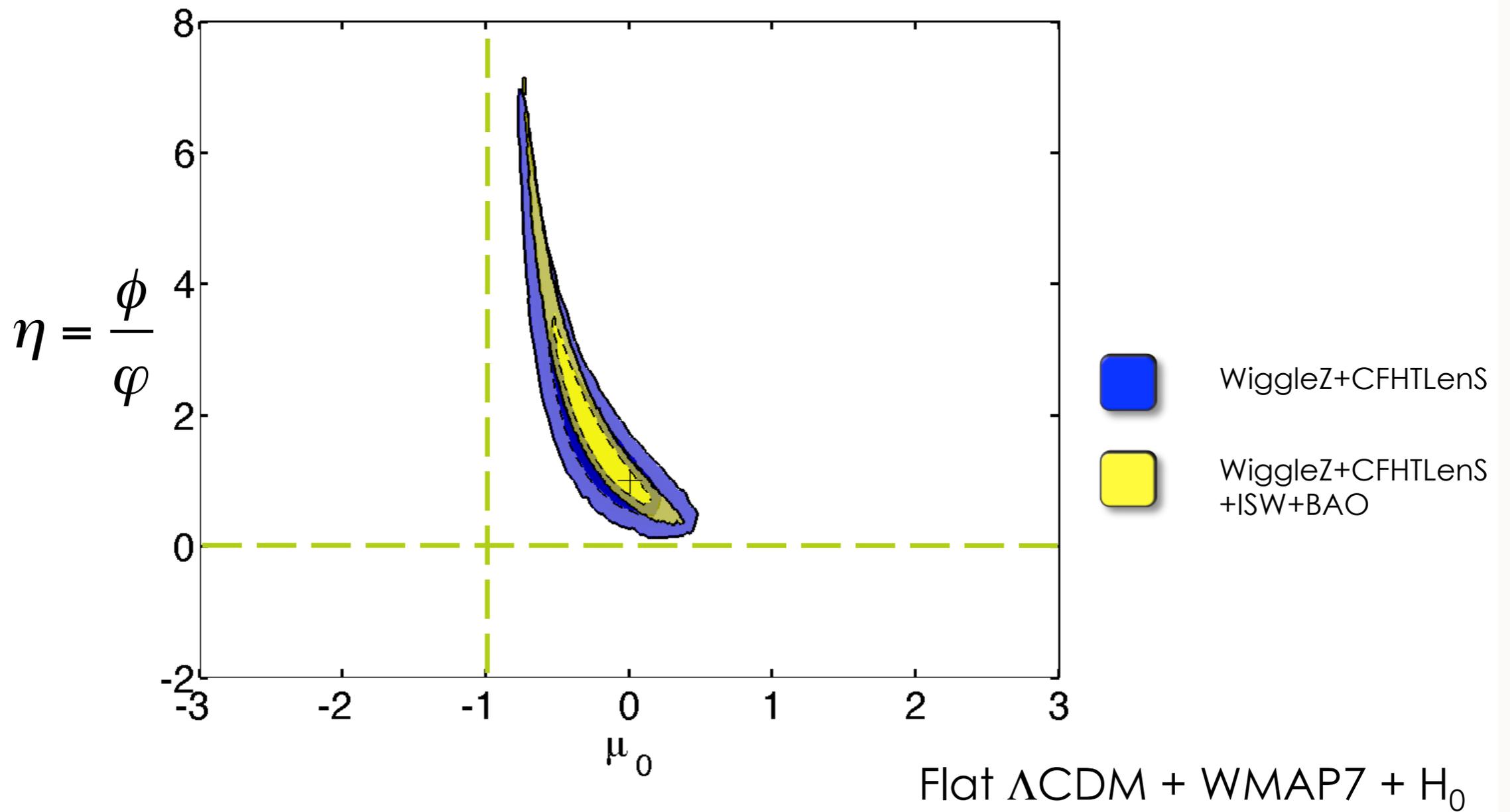
# CFHTLENS CONSTRAINTS

Simpson et al. 2013



# GRAVITATIONAL SLIP

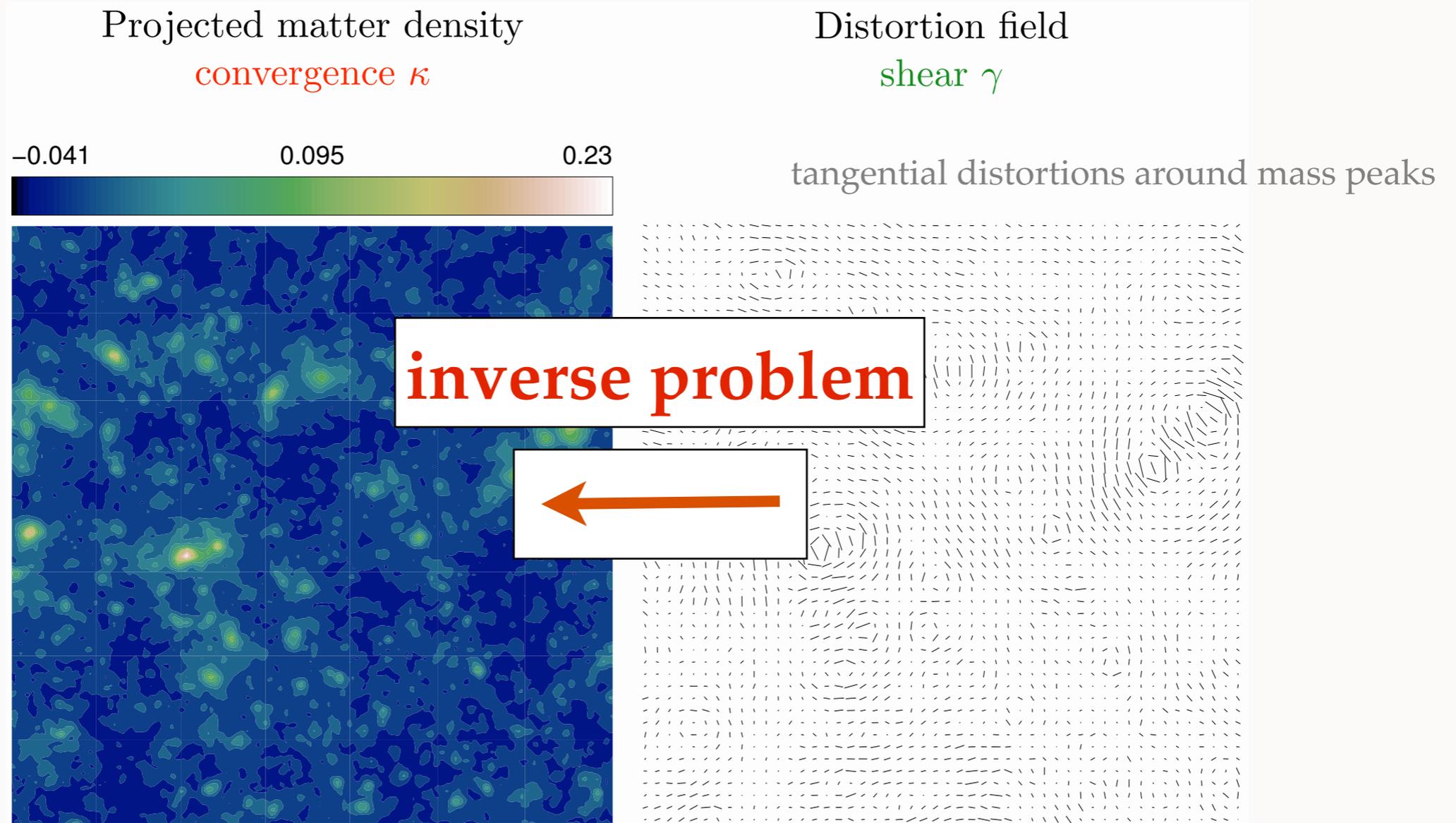
[Simpson et al. 2013]



# MASS MAPS



# LENSING MASS MAPS



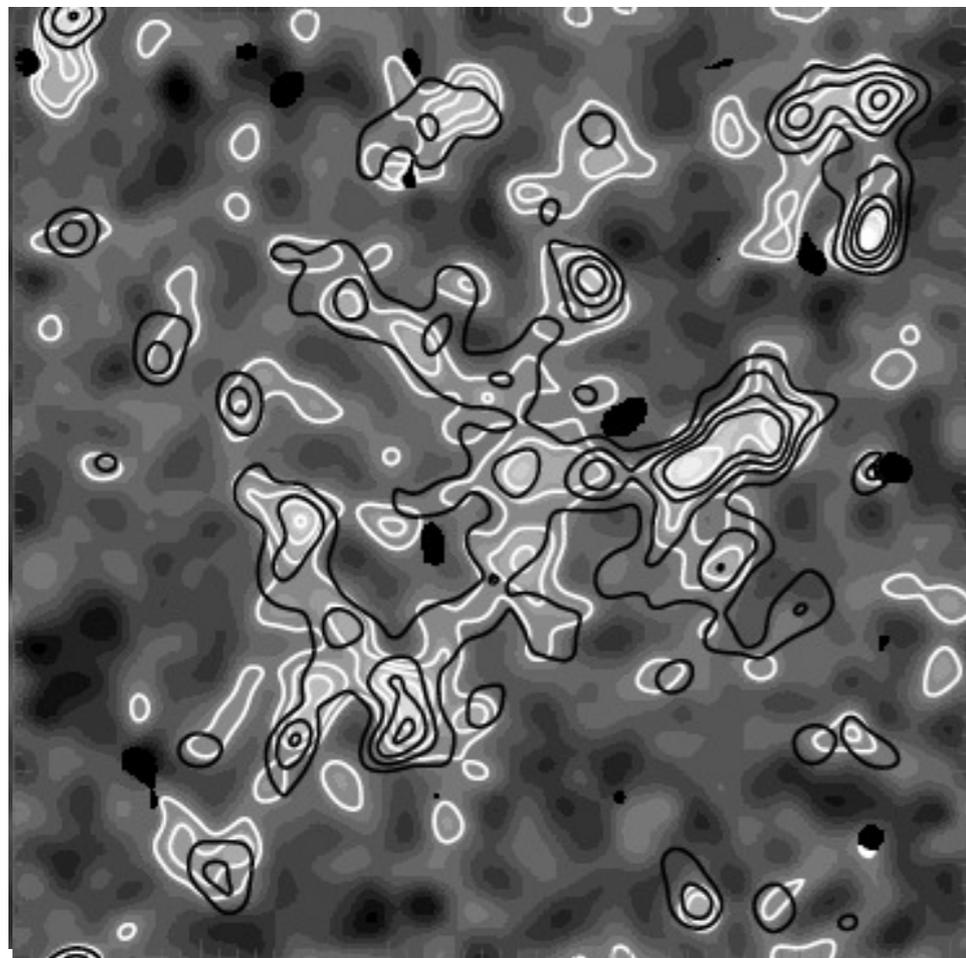
Source galaxies at  $z = 1$ , ray-tracing simulations by T. Hamana



# LENSING MASS MAPS

[van Waerbeke et al. 2013]

- Map dark-matter structures. Compare to optical (galaxies), X-ray (hot gas), SZ (gas)
- High-density regions trace non-linear structures
- Higher-order correlations, non-linear evolution of LSS
- 3D mass reconstruction, evolution of cosmic structures



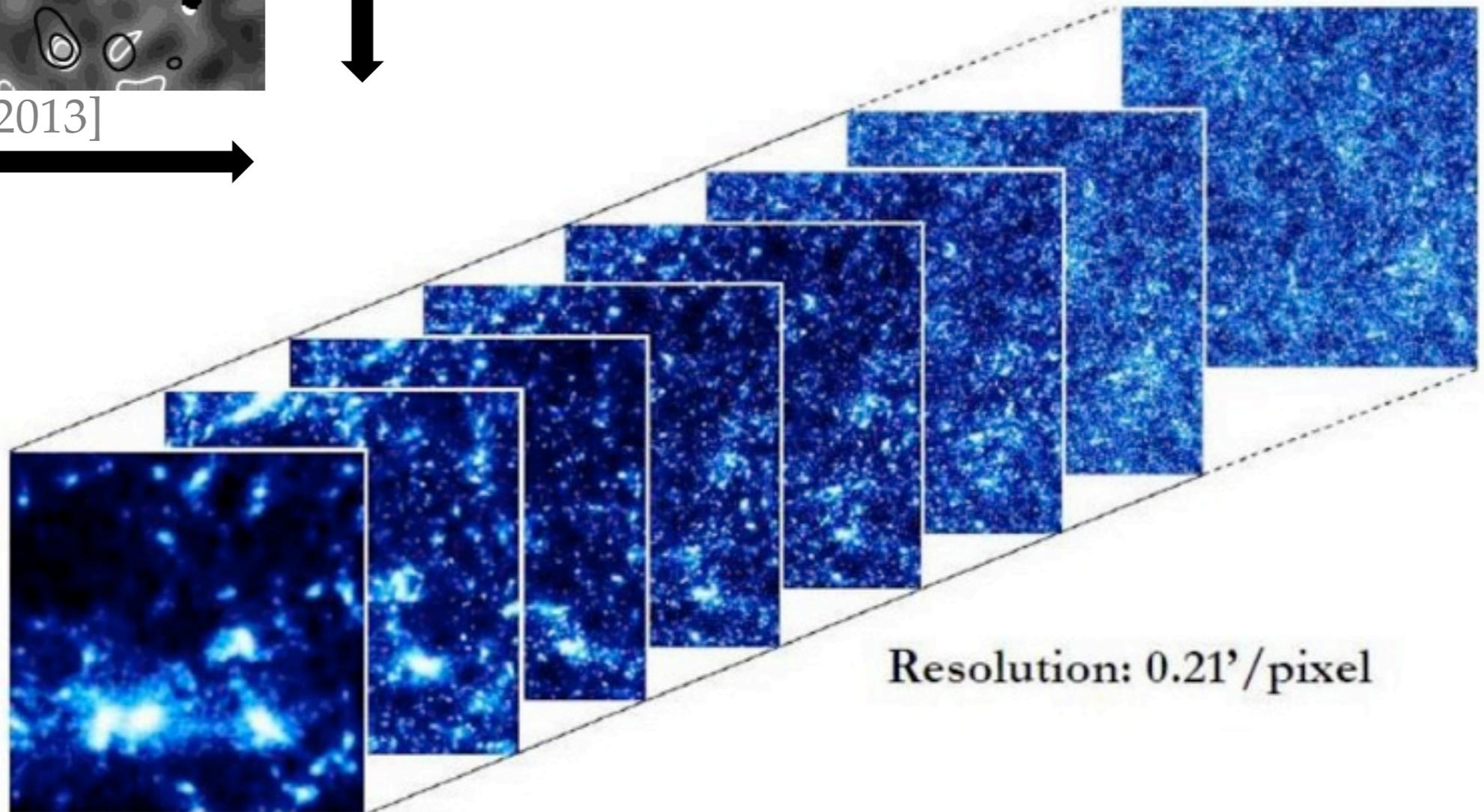
[van Waerbeke et al. 2013]



3.4 degrees

Ray-tracing simulations  
[Harnois-Deraps, Vafaei & van Waerbeke 2012]

$z=3$



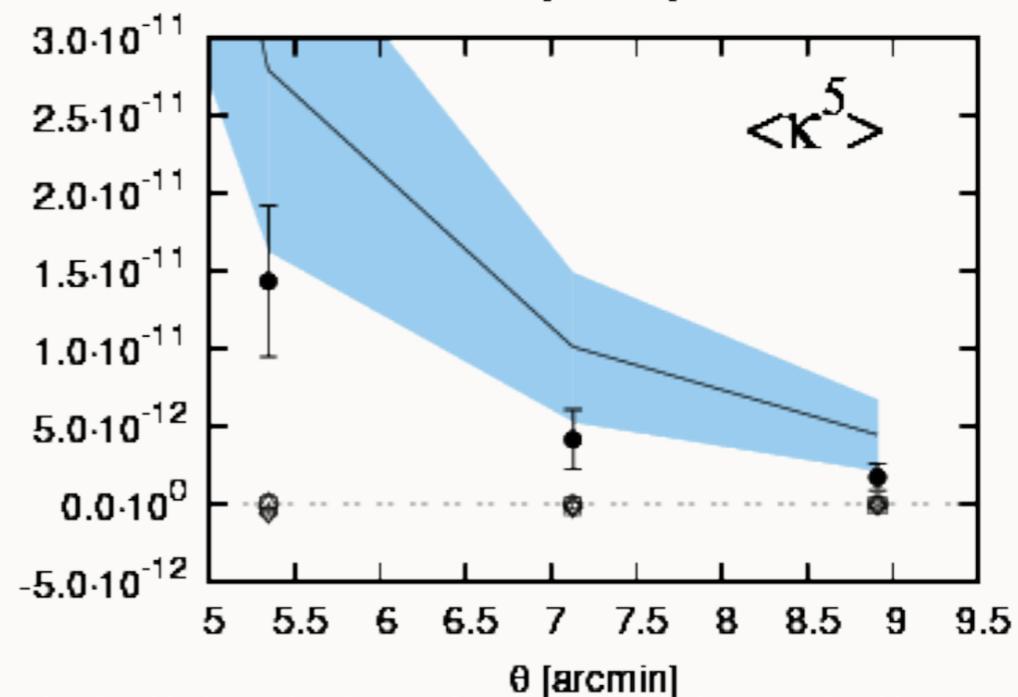
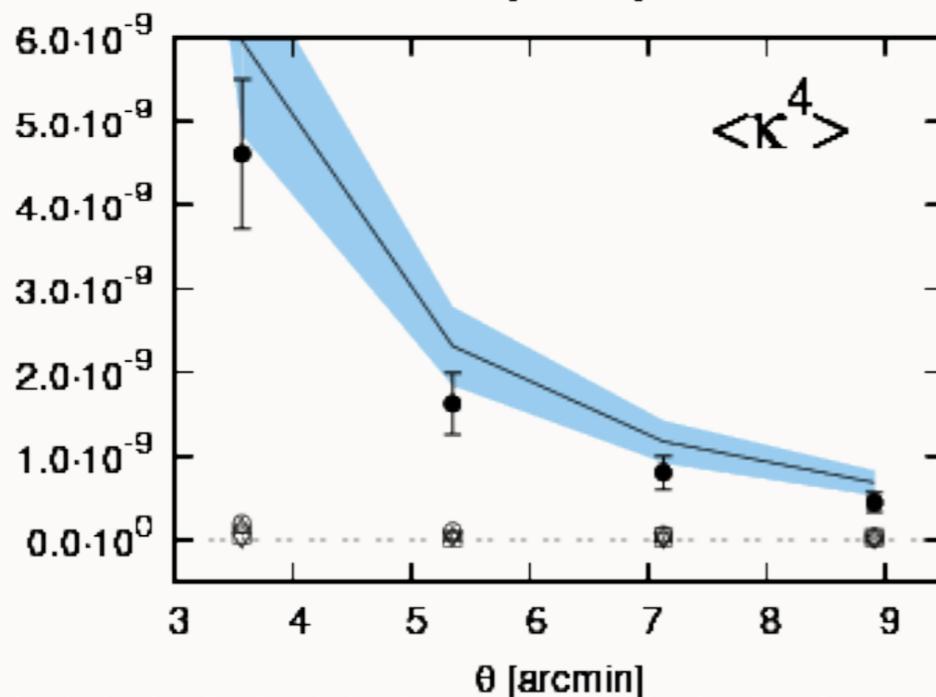
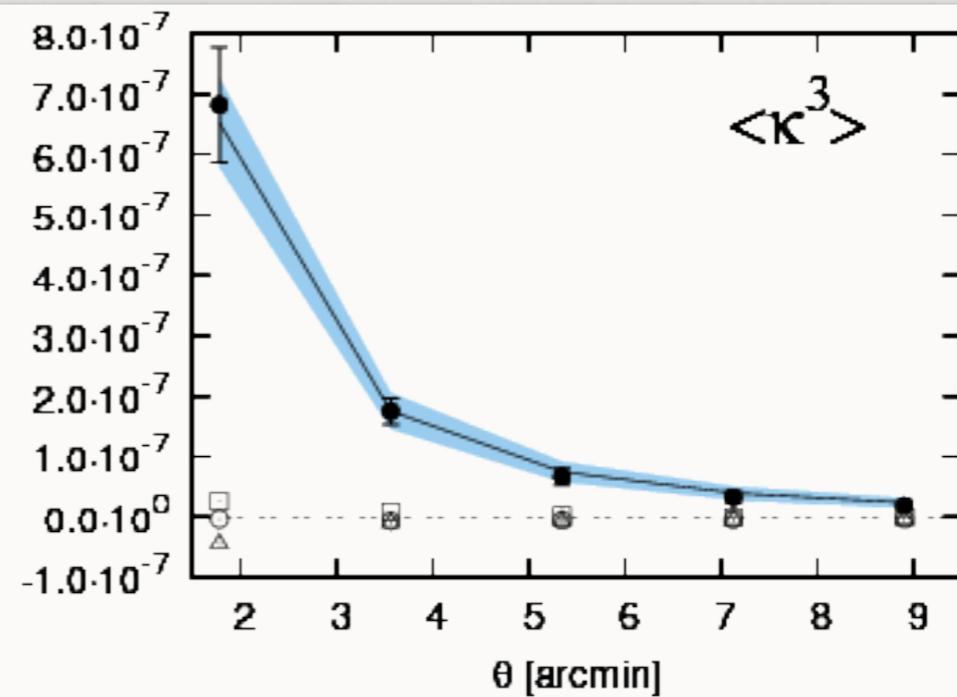
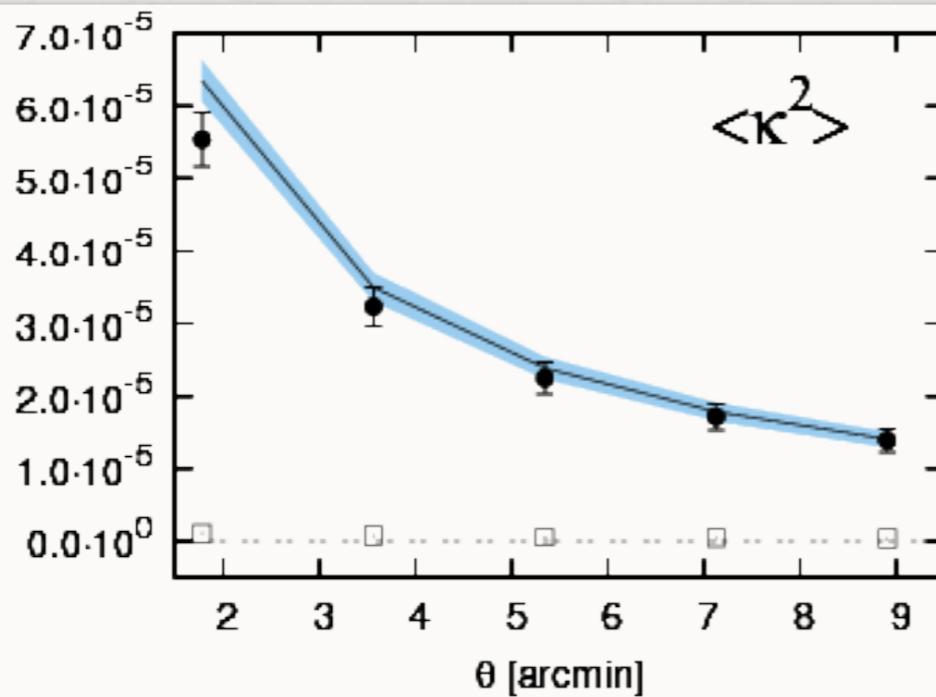
$z=0.03$

Resolution: 0.21' / pixel

Black contours: Input

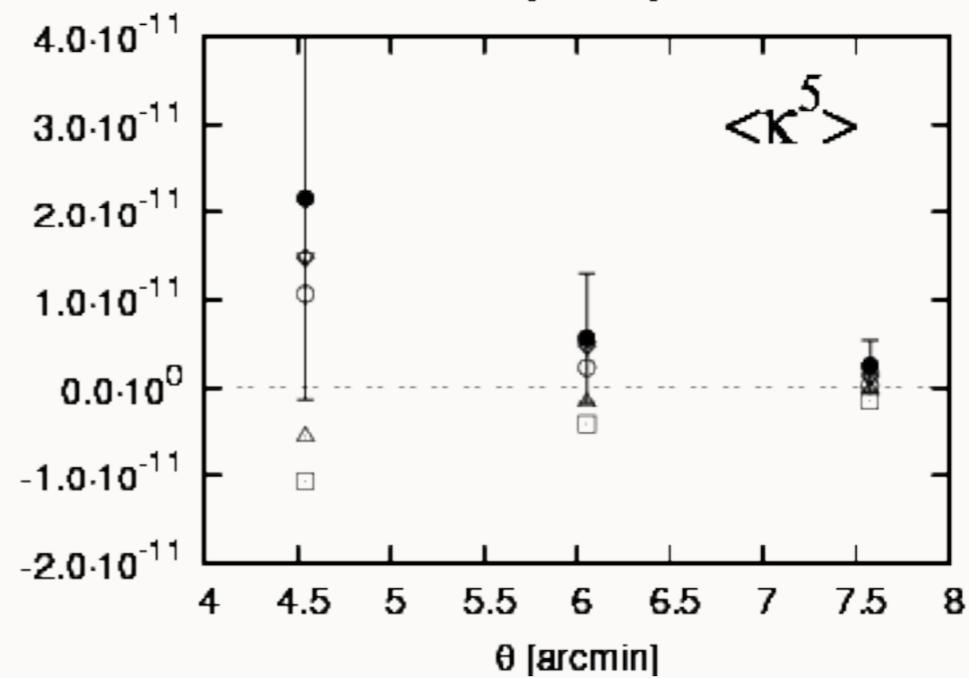
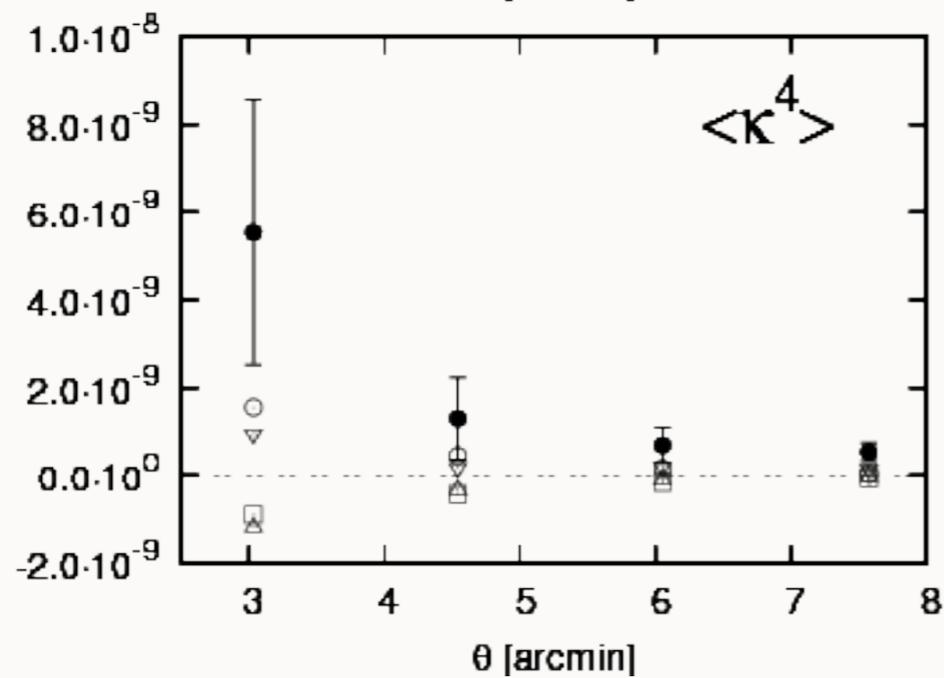
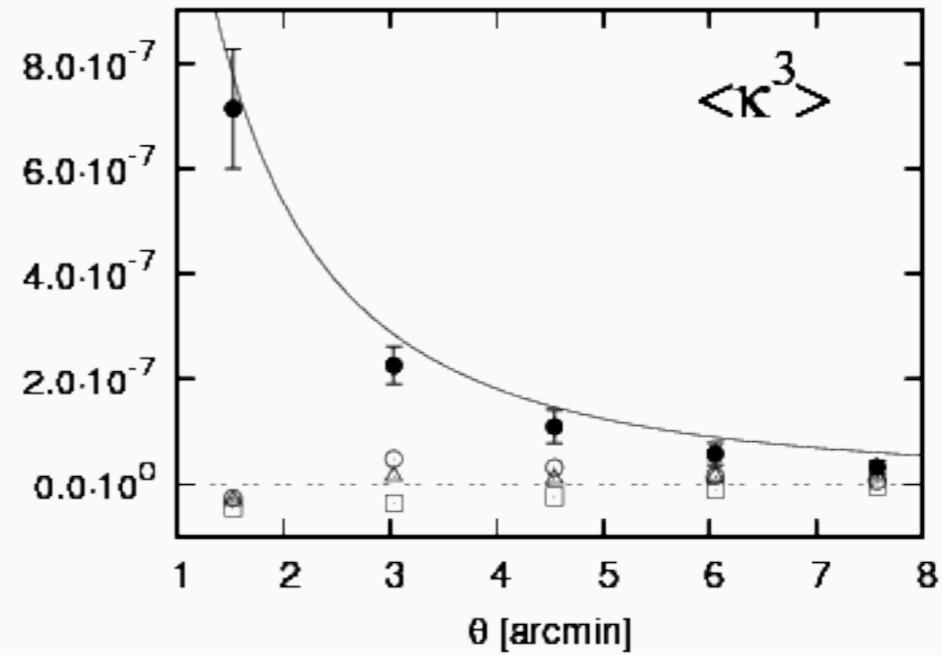
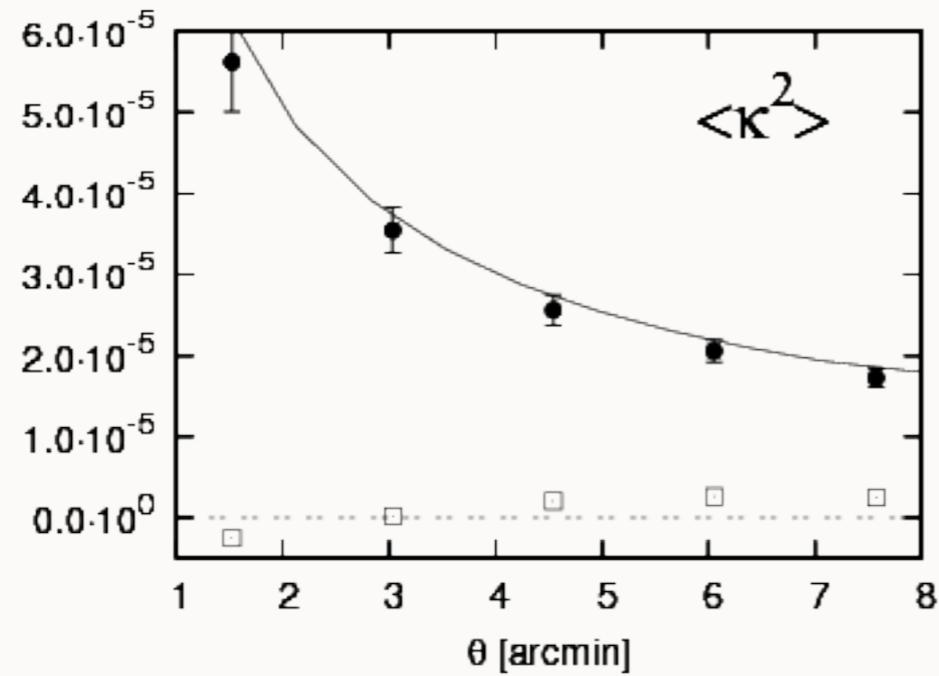
White contours +  
background map:  
Reconstruction

# MOMENTS: SIMULATIONS



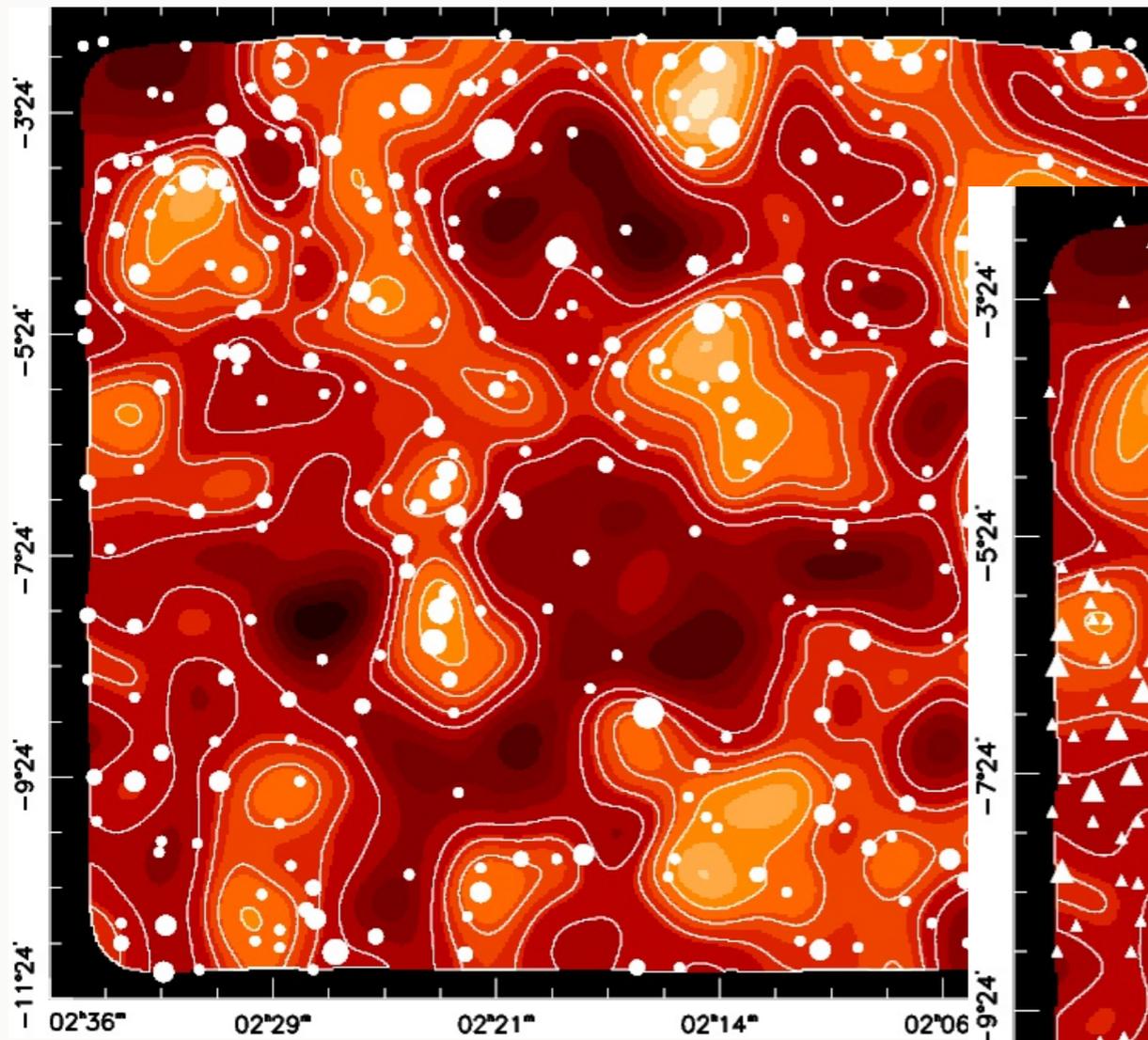
[van Waerbeke et al. 2013]

# MOMENTS: CFHTLENS



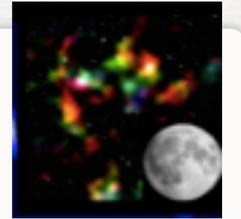
[van Waerbeke et al. 2013]

# LOOKING FOR PEAKS

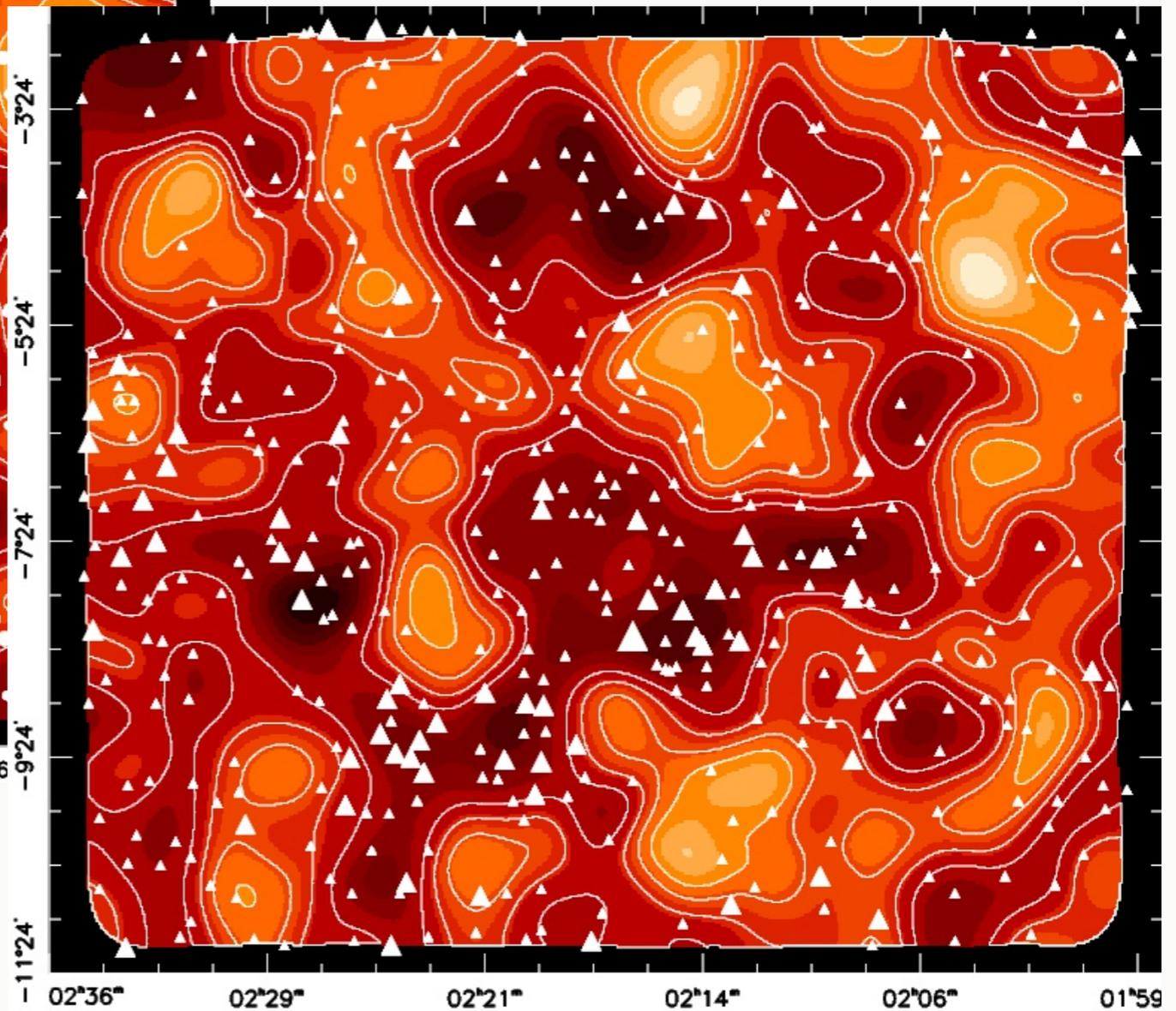


positive peaks

negative peaks



CFHTLenS WI  
[van Waerbeke et al. 2013]



# OUTLOOK





# TIMELINE TO EUCLID

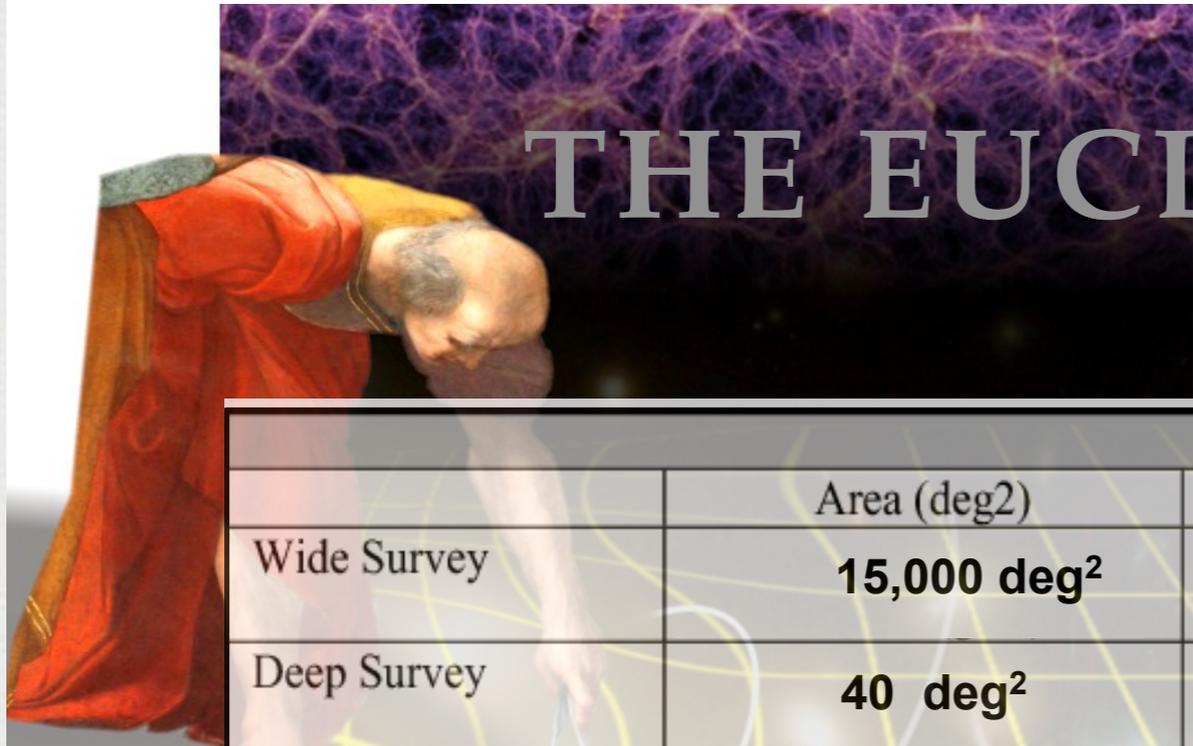
- **CTIO** 75 deg<sup>2</sup>, **DLS** 25 deg<sup>2</sup>, **SDSS stripe-82** 168 deg<sup>2</sup>
- **COSMOS**. 2003 - 2005  
1.64 deg<sup>2</sup>, ACS/HST  
Excellent photometric redshifts (30 bands from UV to IR), very deep. Space-based.
- **CFHTLS**. 2003 - 2009  
155 deg<sup>2</sup>, MegCam/CFHT  
Science papers are being submitted and accepted. Catalogues have been made public on **Nov 1, 2012**. See [www.cfhtlens.org](http://www.cfhtlens.org) .



# TIMELINE TO EUCLID

- **KiDS.** 2011 -  
1,500 deg<sup>2</sup>, OmegaCam/VST  
Excellent image quality and seeing. Deep IR coverage (VISTA) + u-band
- **DES.** 2012 -  
5,000 deg<sup>2</sup>, DECam/CTIO  
Large area, IR coverage. Large spectro-follow up planned (DESPEC)
- **HSC survey.** ≥ 2013 -  
1,200 deg<sup>2</sup>, HyperSuprimeCam/Subaru.  
Excellent image quality and seeing, very deep (8m telescope!). Deep and Ultra-deep field
- **LSST.** ≥ 2018 -  
20,000 deg<sup>2</sup>
- **Euclid.** ≥ 2019 -  
15,000 deg<sup>2</sup>  
Very stable PSF, space-based.

# THE EUCLID MISSION



## SURVEYS In ~5.5 years

	Area (deg <sup>2</sup> )	Description
Wide Survey	<b>15,000 deg<sup>2</sup></b>	Step and stare with 4 dither pointings per step.
Deep Survey	<b>40 deg<sup>2</sup></b>	In at least 2 patches of > 10 deg <sup>2</sup> 2 magnitudes deeper than wide survey

## PAYLOAD

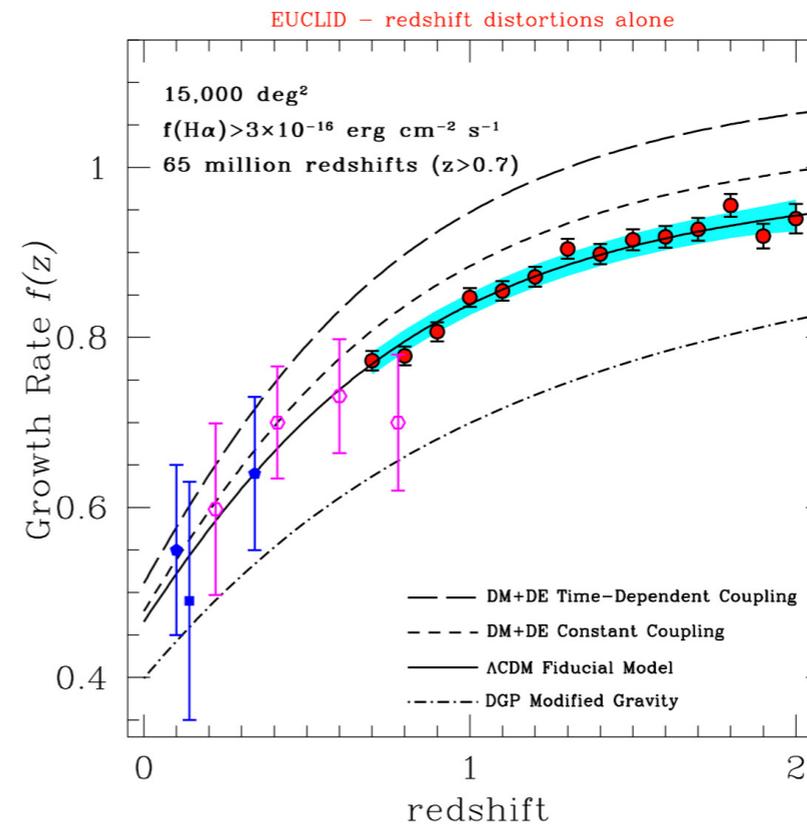
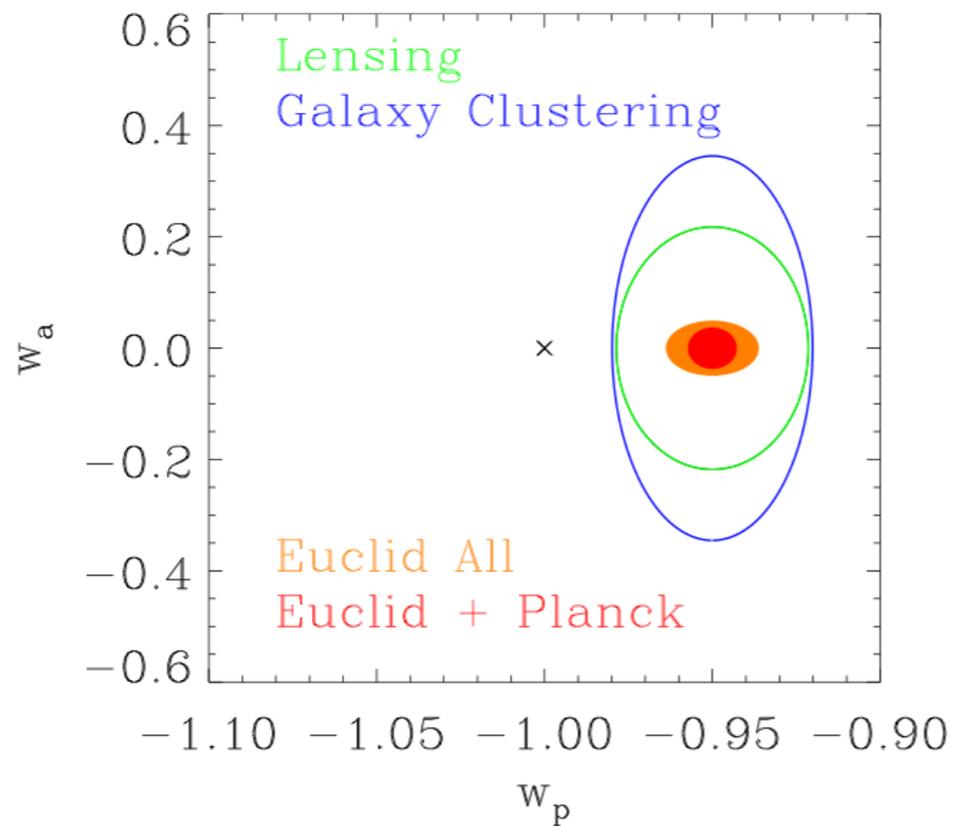
Telescope	1.2 m Korsch, 3 mirror anastigmat, f=24.5 m				
Instrument	VIS		NISP		
Field-of-View	0.787×0.709 deg <sup>2</sup>		0.763×0.722 deg <sup>2</sup>		
Capability	Visual Imaging		NIR Imaging Photometry		NIR Spectroscopy
Wavelength range	550– 900 nm	Y (920-1146nm),	J (1146-1372 nm)	H (1372-2000nm)	1100-2000 nm
Sensitivity	24.5 mag 10σ extended source	24 mag 5σ point source	24 mag 5σ point source	24 mag 5σ point source	3 10 <sup>-16</sup> erg cm <sup>-2</sup> s <sup>-1</sup> 3.5σ unresolved line flux
	Shapes + Photo-z of $n = 1.5 \times 10^9$ galaxies ?			z of $n=5 \times 10^7$ galaxies	
Detector Technology	36 arrays 4k×4k CCD		16 arrays 2k×2k NIR sensitive HgCdTe detectors		
Pixel Size	0.1 arcsec		0.3 arcsec		0.3 arcsec
Spectral resolution					R=250

Possibility to propose other surveys: SN and/or  $\mu$ -lens surveys, Milky Way ?

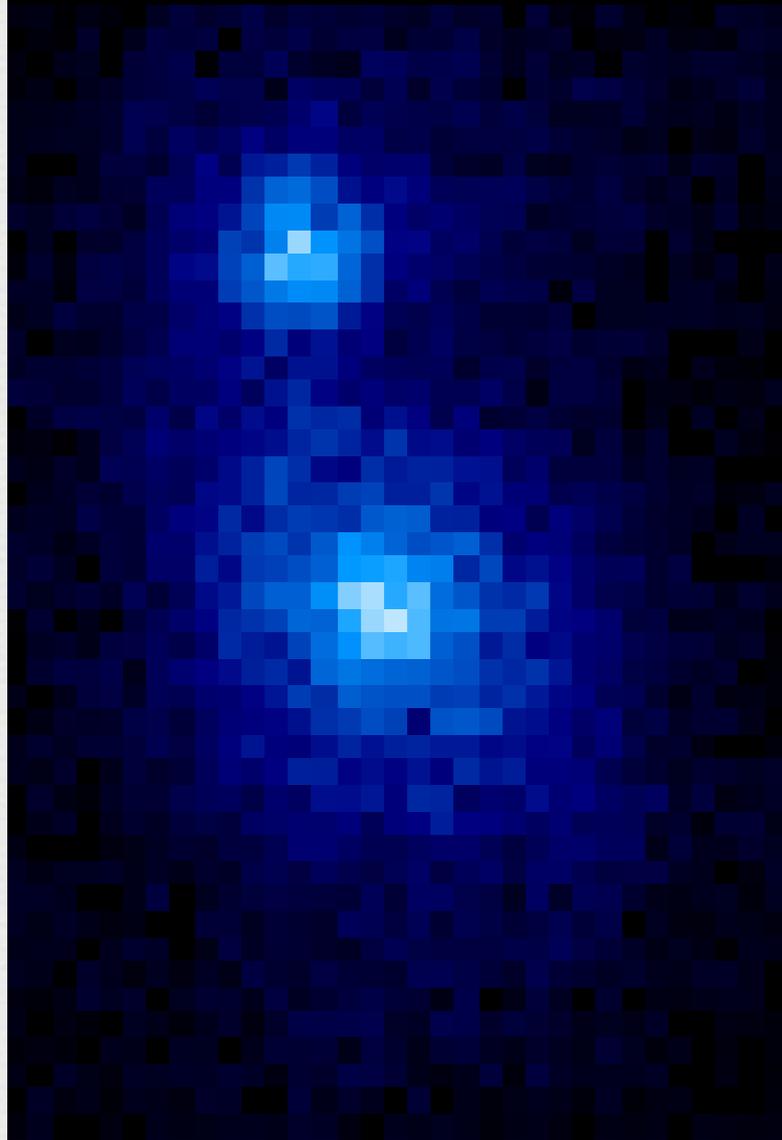
# EUCLID FORECASTS

	Modified Gravity	Dark Matter	Initial Conditions	Dark Energy		
Parameter	$\gamma$	$m_\nu/eV$	$f_{NL}$	$w_p$	$w_a$	$FoM$
Euclid Primary	0.010	0.027	5.5	0.015	0.150	430
Euclid All	0.009	0.020	2.0	0.013	0.048	1540
Euclid+Planck	0.007	0.019	2.0	0.007	0.035	4020
Current	0.200	0.580	100	0.100	1.500	~10
<b>Improvement Factor</b>	<b>30</b>	<b>30</b>	<b>50</b>	<b>&gt;10</b>	<b>&gt;50</b>	<b>&gt;300</b>

CFHTLenS + WiggleZ  
+ WMAP5 + H0:  
 $\gamma = 0.52 \pm 0.09$



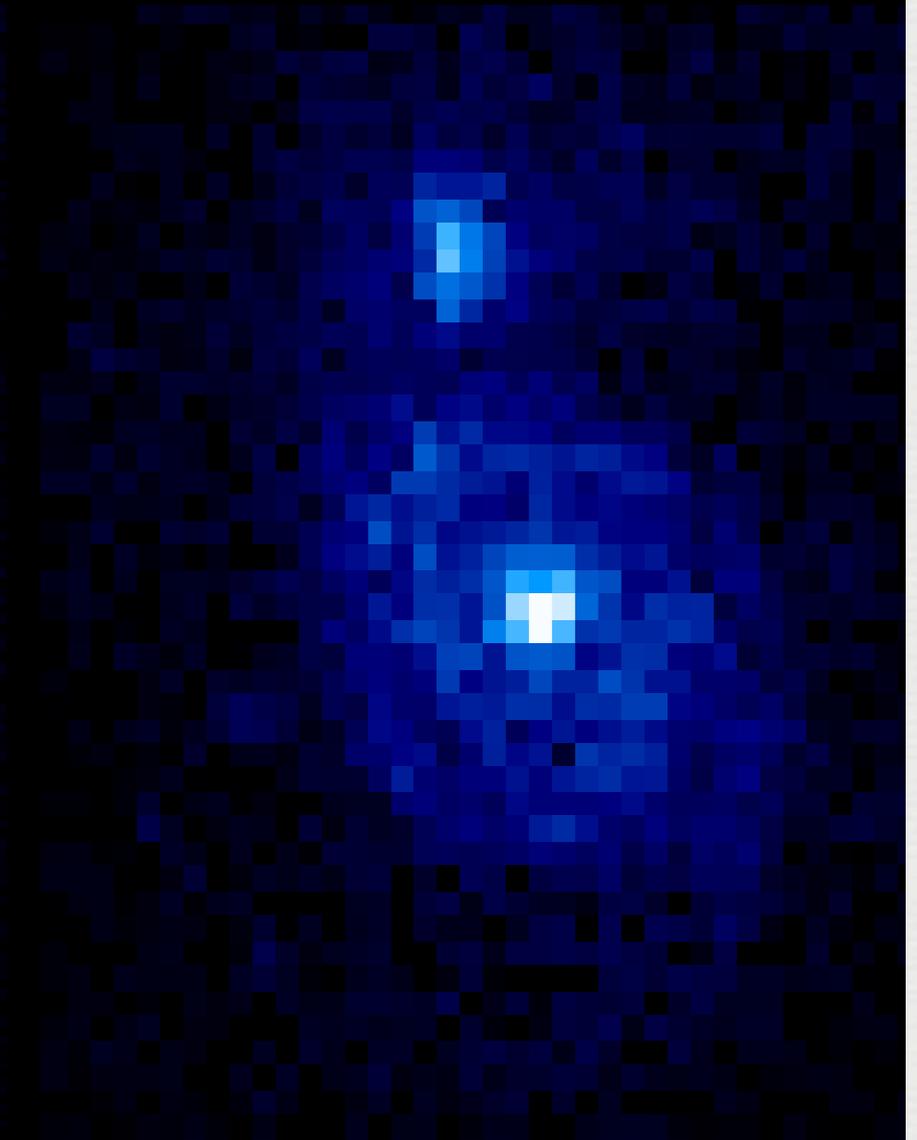
# M51



SDSS @  $z=0.1$



Euclid @  $z=0.1$



Euclid @  $z=0.7$

- Euclid images of  $z\sim 1$  galaxies: same resolution as SDSS images at  $z\sim 0.05$  and at least 3 magnitudes deeper.
- Space imaging of Euclid will outperform any other surveys of weak lensing.

# FUTURE LENSING SURVEYS

- Order of magnitude more area → dominated by systematic errors!
- No current shape measurement method accurate enough for future surveys
- Space-based weak lensing challenges (CTI, PSF undersampling, color gradients)
- No show-stopper for weak lensing found yet

# LIKELIHOOD FUNCTION

$$L(\mathbf{d}^{\text{obs}}; \boldsymbol{\theta}) = \frac{1}{\sqrt{(2\pi)^n \det C}} \exp[-\chi^2(\mathbf{d}^{\text{obs}}; \boldsymbol{\theta})/2]$$
$$\chi^2(\mathbf{d}^{\text{obs}}; \boldsymbol{\theta}) = \left(\mathbf{d}(\boldsymbol{\theta}) - \mathbf{d}^{\text{obs}}\right)^t C^{-1} \left(\mathbf{d}(\boldsymbol{\theta}) - \mathbf{d}^{\text{obs}}\right)$$

$\mathbf{d}^{\text{obs}}$  : data vector of ellipticity correlations, e.g.  $d_i = \xi(\vartheta_{j(i)}, z_{k(i)})$

$\mathbf{d}(\boldsymbol{\theta})$ : model vector

$\boldsymbol{\theta}$  : vector of cosmological parameters, e.g.  $\Omega_m, \sigma_8, h, w \dots$

$C$  : covariance matrix,  $C = \langle dd^t \rangle - \langle d \rangle \langle d^t \rangle$

We need integrals  
over the likelihood:

mean of parameter vector

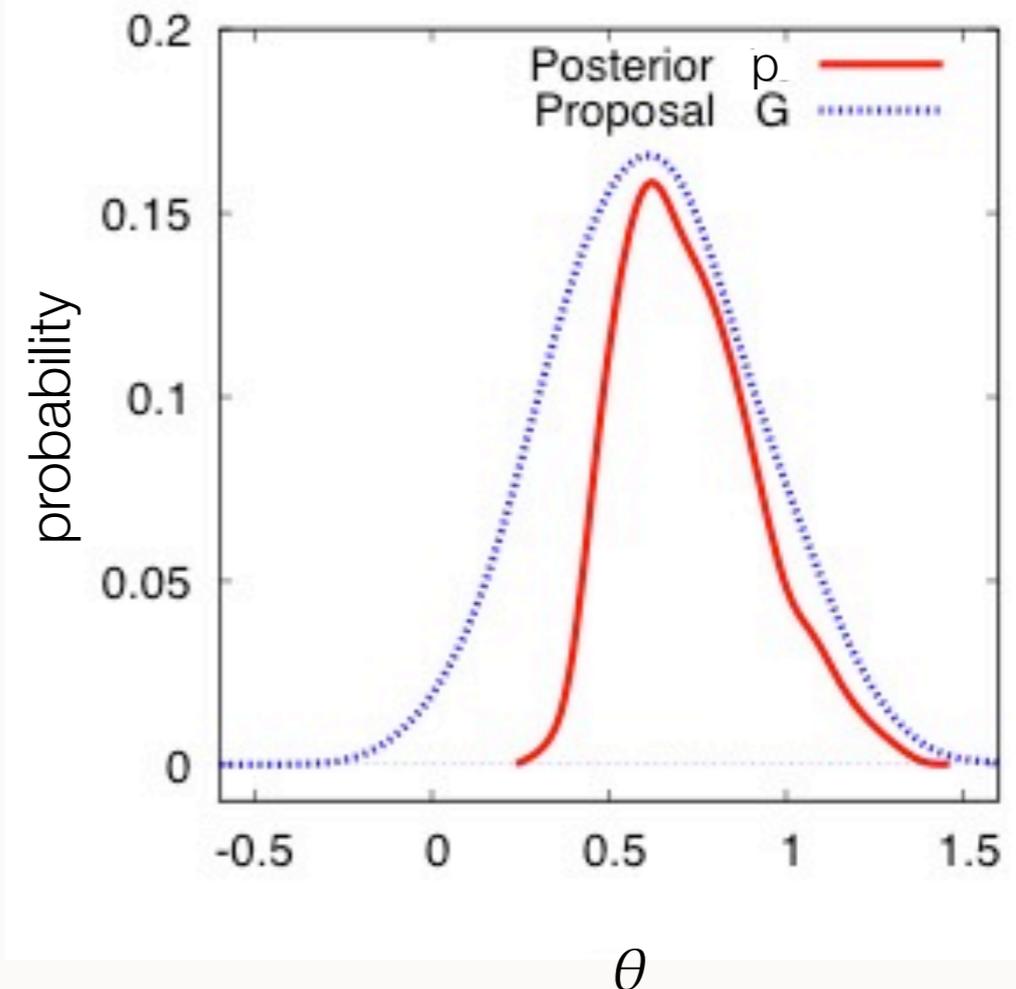
$$\int d^n \theta \boldsymbol{\theta} L(\boldsymbol{\theta}) \pi(\boldsymbol{\theta})$$

68% confidence region

$$\int d^n \theta 1_{68\%} L(\boldsymbol{\theta}) \pi(\boldsymbol{\theta})$$

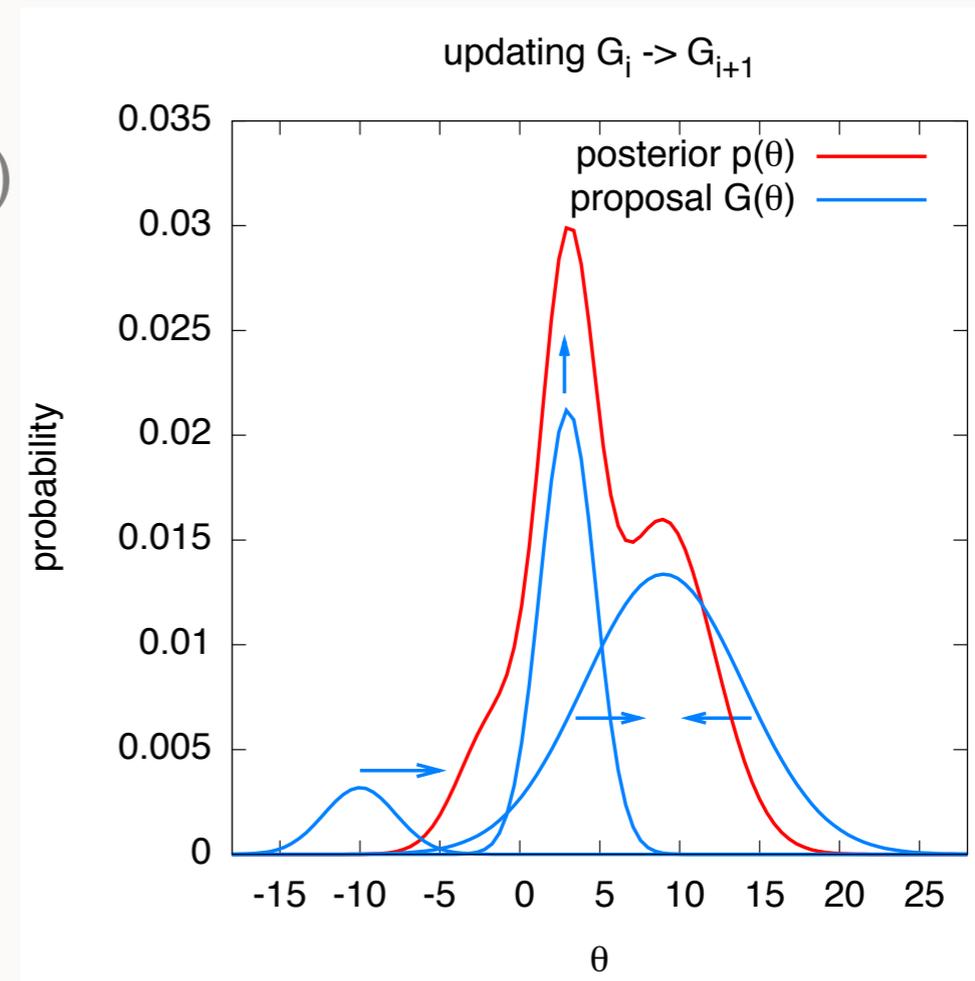
# IMPORTANCE SAMPLING

- Sample from proposal distribution  $G$  (importance function). E.g. mixture of Gaussians
- Weigh each sample point  $\theta$  by ratio (importance weight)  
 $w = p(\theta) / G(\theta)$
- Evaluation of posterior  $p$  (likelihood x prior) can be done in parallel
- Poor performance if proposal far from posterior



# POPULATION MONTE CARLO (PMC)

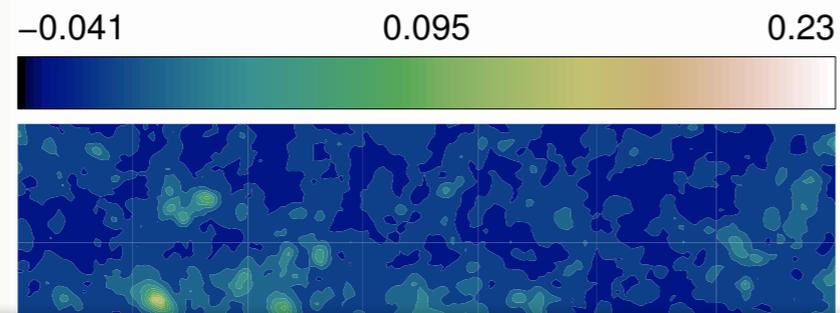
- Solution: Create adaptive importance samples (“populations”) [Cappé et al. 2004, 2007]
- Iteration  $G_i \rightarrow G_{i+1}$ : Update mean, covariance and component weights
- PMC sample engine and cosmology modules, public code, [www.cosmopmc.info](http://www.cosmopmc.info), [Kilbinger et al. 2010, arXiv:1101.0950]
- Stop when proposal  $p$  ‘close enough’ to posterior  $G$



# E- AND B-MODE

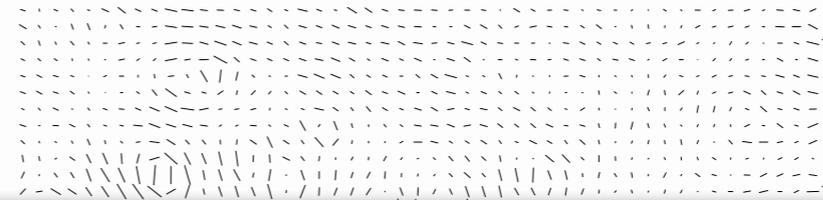
Projected matter density

convergence  $\kappa$



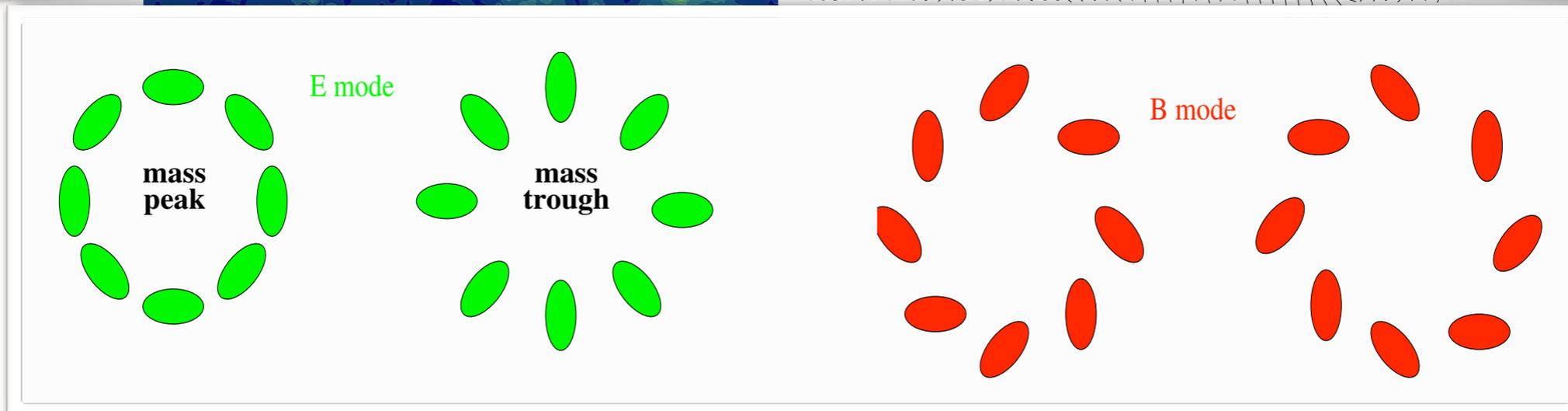
Distortion field

shear  $\gamma$



mass peaks

Gravitational lensing only produces E-mode pattern (to first order)



B-mode detected → hint for systematics in data

# E- AND B-MODES

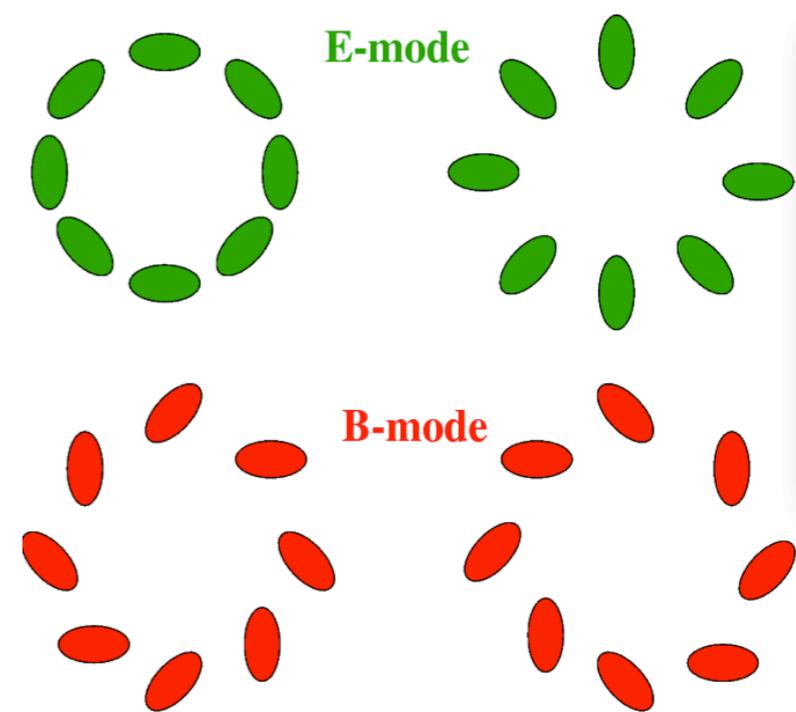
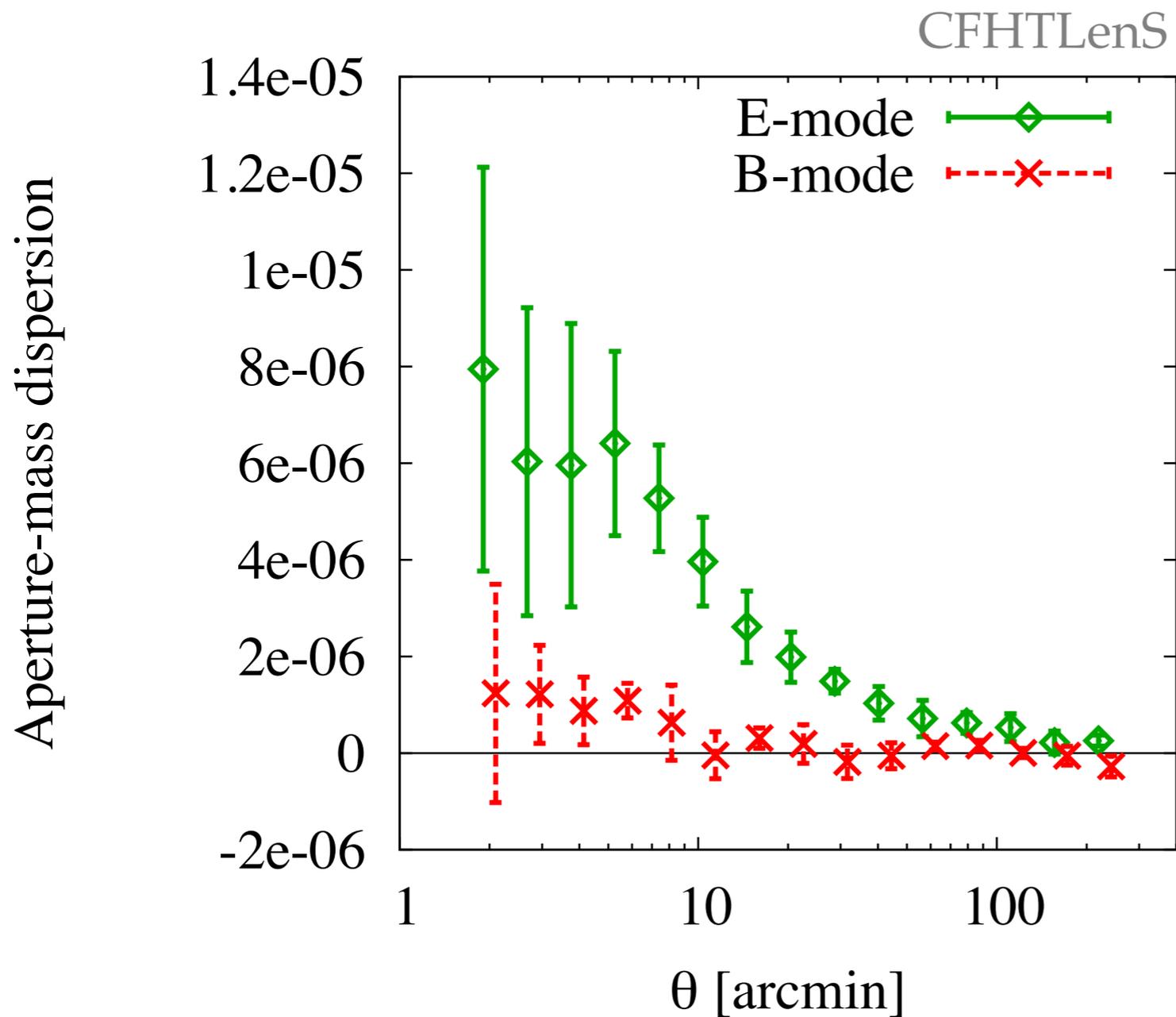


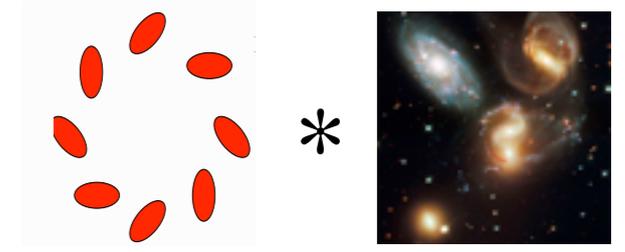
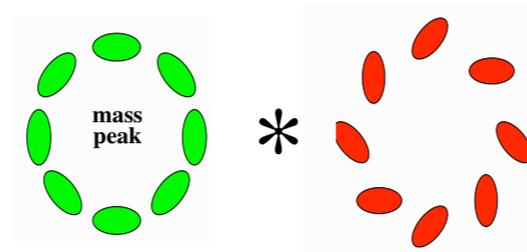
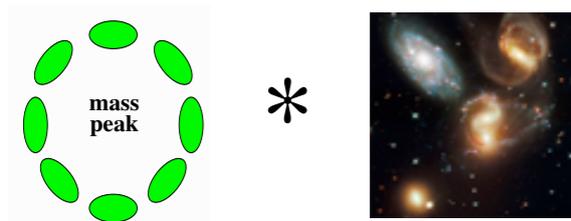
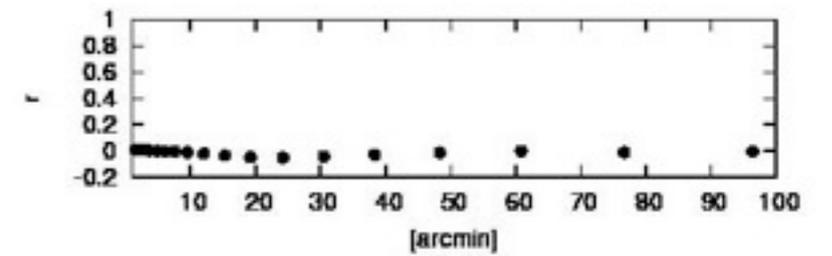
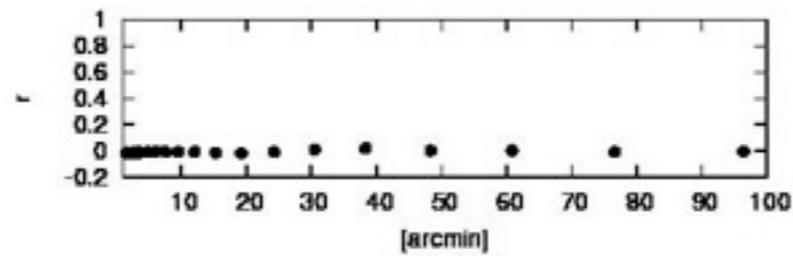
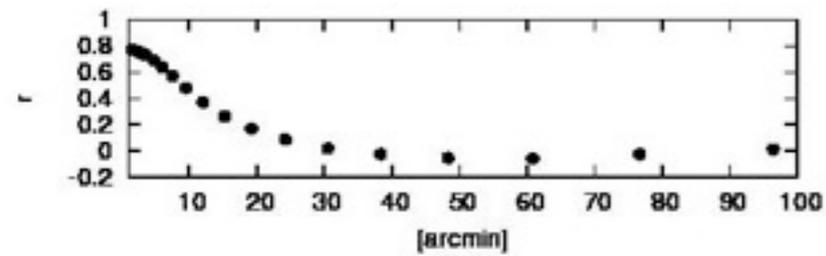
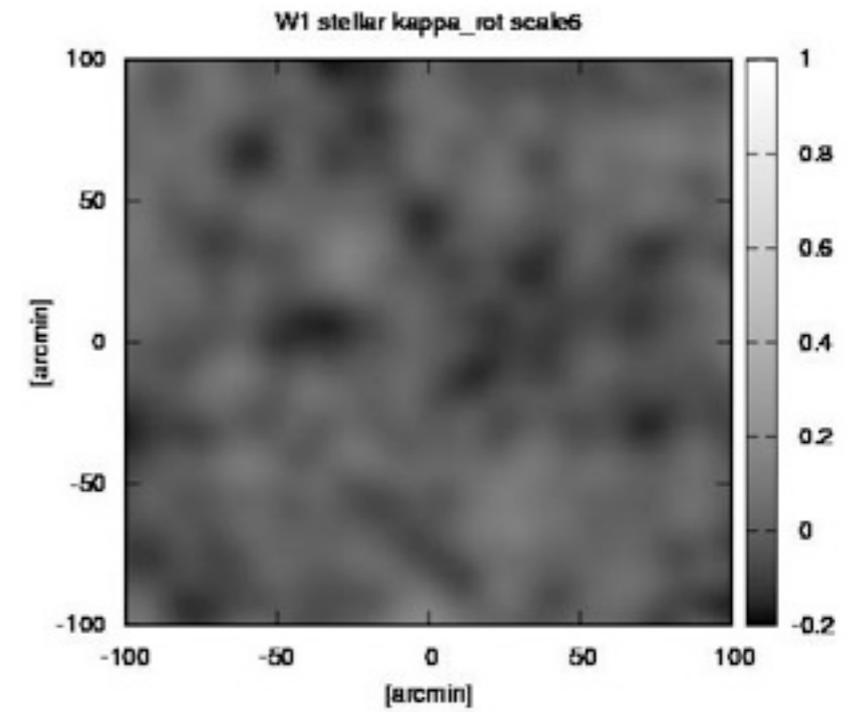
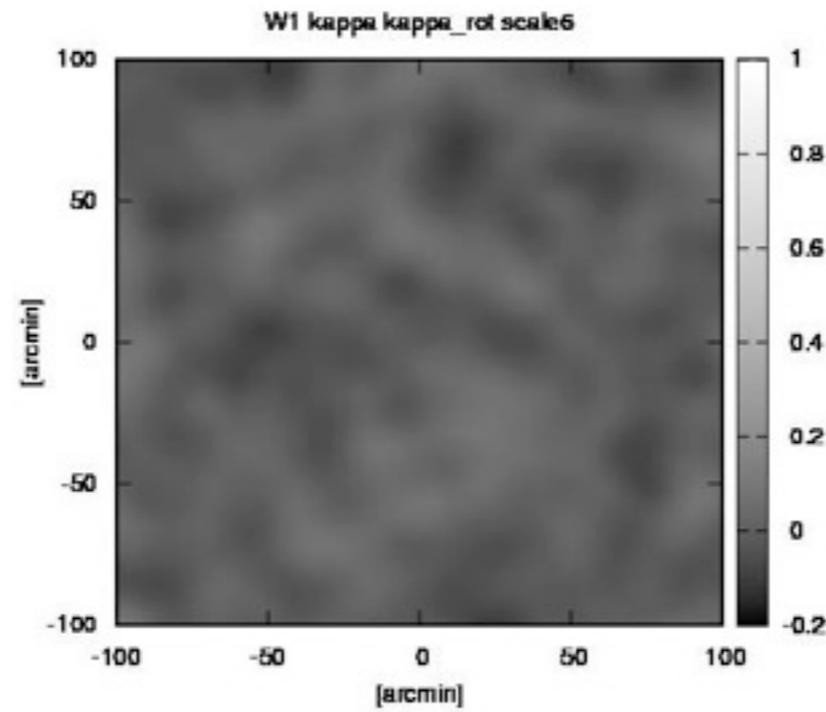
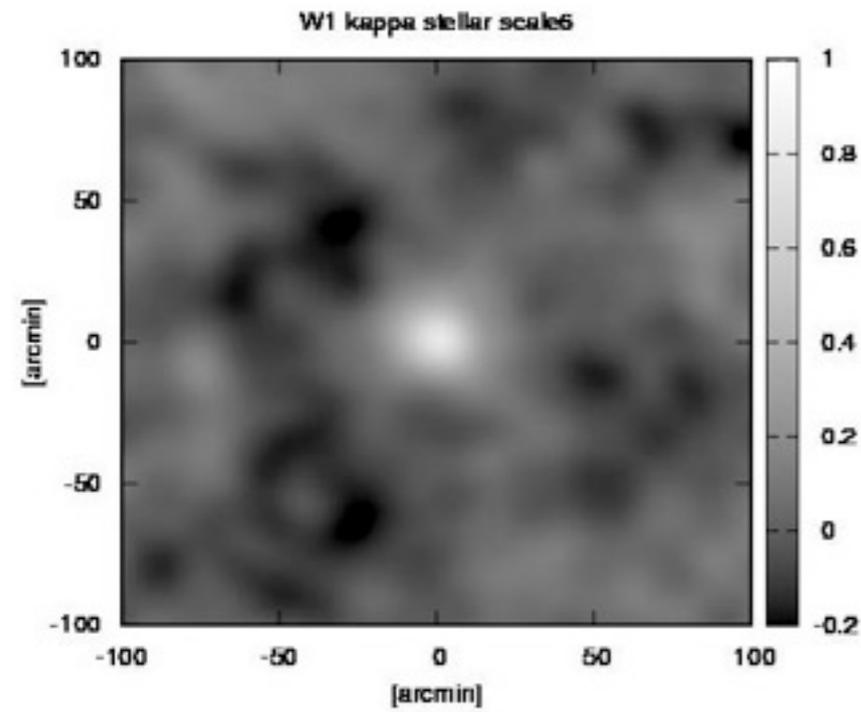
Fig.1. *Left:* E- and B-modes measured in CFHTLenS. *Right:* typical E- and B-mode shear patterns.

# W1 cross-correlation analysis

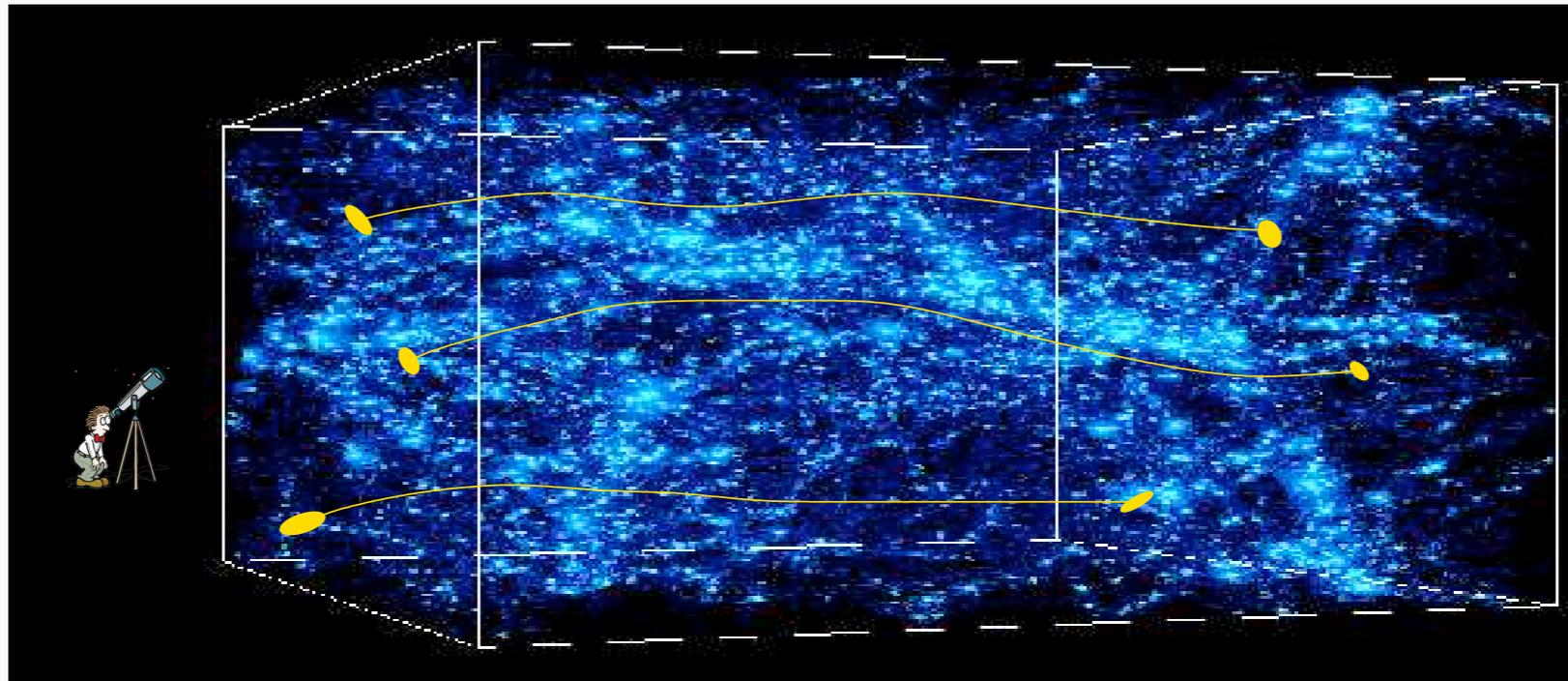
$\langle \kappa_{\text{mass}} \kappa_{\text{galaxies}} \rangle$

$\langle \kappa_{\text{mass}} \kappa_{\text{rot}} \rangle$

$\langle \kappa_{\text{rot}} \kappa_{\text{galaxies}} \rangle$



# WEAK LENSING SUMMARY



- Galaxy shape correlations measure 'lumpiness' of large-scale structure (LSS)
- Sensitive to both geometry and growth,  $z = 0.2 \dots 1$ , acceleration epoch; dark energy, modified gravity
- Weak lensing regime: need huge number of galaxies to measure statistically & excellent image quality