

Lattice QCD and flavour physics

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OUTLINE:

- Motivations for flavour physics
- Accuracy of lattice QCD:
 1. the **quenched era** (<2006)
 2. the **precision era**
- The first row unitarity test
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$
- The Unitarity Triangle Analysis
$$V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$
 1. Lattice inputs
 2. Deviations from the SM
- Accuracy of LQCD: 3. the **future**

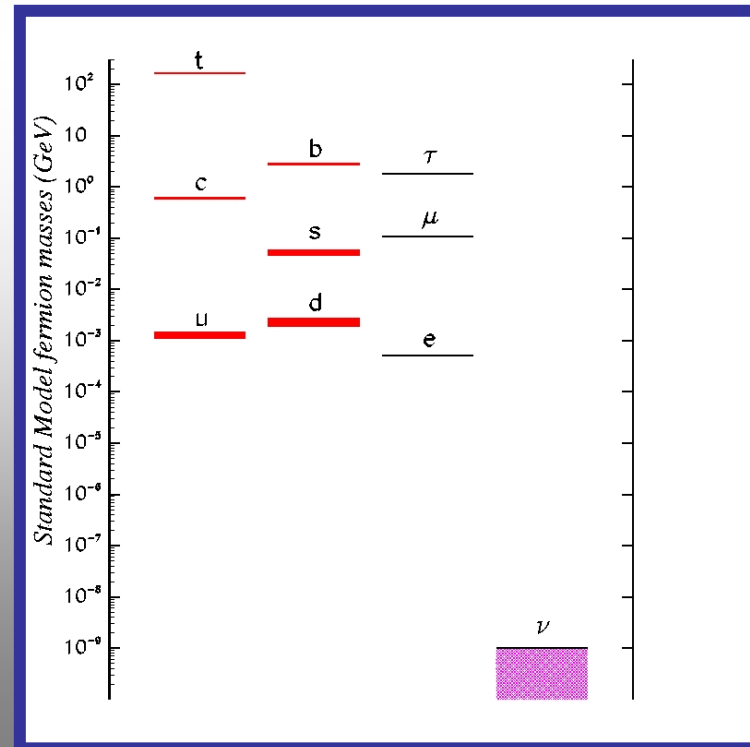
Motivations for flavour physics

1) Flavour physics is (well) described but not explained in the Standard Model

A large number of **free parameters** in the flavor sector:
10 parameters in the quark sector ($6 m_q + 4 \text{ CKM}$),
12 in the lepton sector (with massive neutrinos)

Open questions

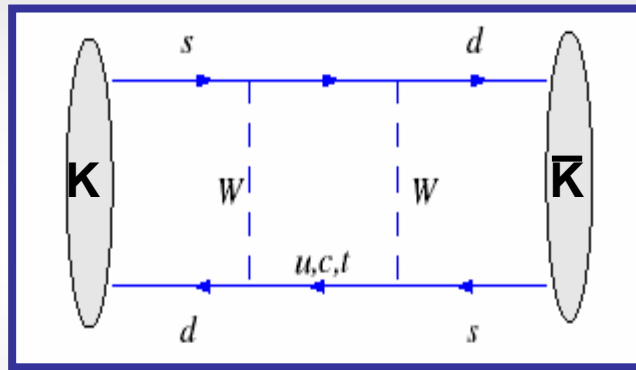
- Why **3 families** with their observed particle content?
- Why the **spectrum** of quarks and charged leptons covers 5 orders of magnitude? ($m_q \sim Y v \sim G_F^{-1/2} \dots$)
- What give rise to the pattern of quark **mixing** and the magnitude of **CP violation**?



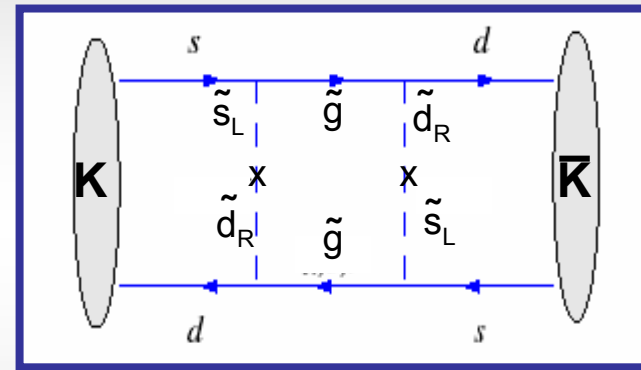
2) Flavour physics plays a crucial role in the indirect searches of new physics

New Physics enters the low-energy processes through quantum loops

➔ Flavor Physics could allow us to discriminate among different New Physics scenarios



Standard Model

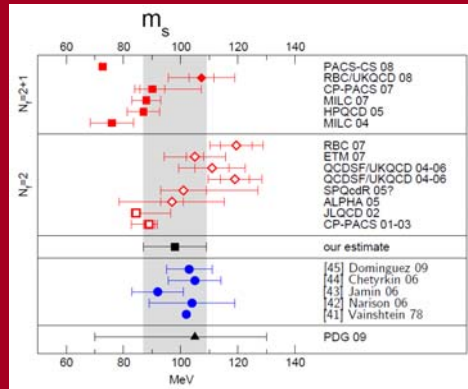
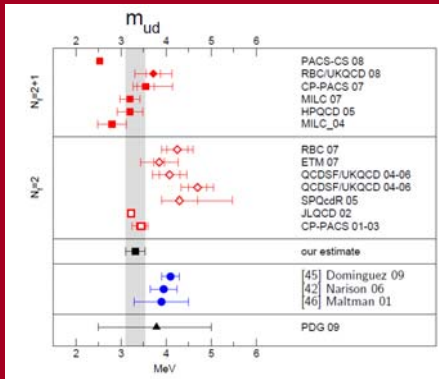


New Physics

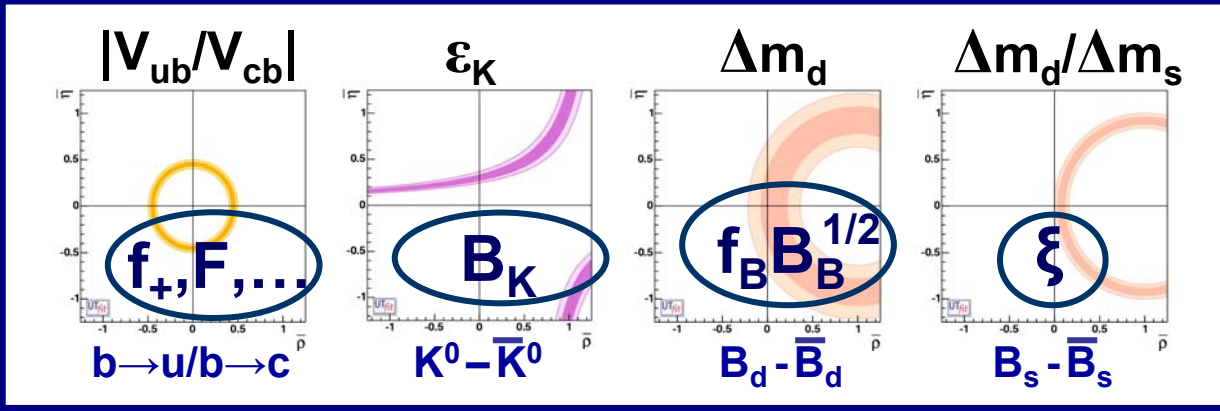
In the past, the existence of the charm quark or the heaviness of the top quark have been predicted from the study of virtual effects long before their experimental observation

No evidence of New Physics from indirect searches has been observed yet: the Standard Model works too well (the "flavour problem")

Lattice QCD and flavour physics



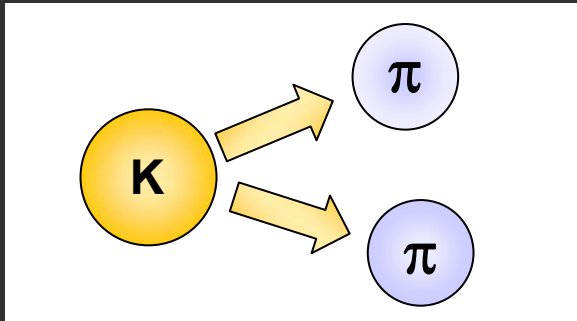
Quark masses



CKM matrix elements

UTA

Beyond SM physics



More difficult problems

Covered in this talk

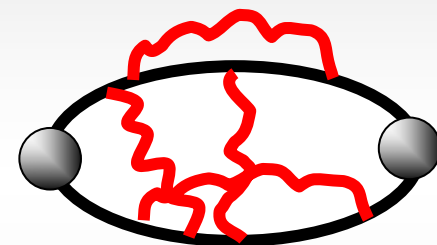
Accuracy of Lattice QCD

1. The “quenched” era

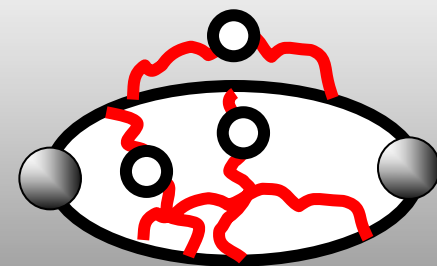
For many years, uncertainties in lattice calculations have been dominated by the quenched approximation

History of lattice errors (before 2006)

	f_B [MeV]	$f_{B_s} \sqrt{B_s}$ [MeV]	ξ
J.Flynn Latt' 96	175(25) 14%	----	----
C.Bernard Latt' 00	200(30) 15%	267(46) 17%	1.16(5) 4%
L.Lellouch Ichep' 02	193(27)(10) 15%	276(38) 14%	1.24(4)(6) 6%
Hashimoto Ichep' 04	189(27) 14%	262(35) 13%	1.23(6) 5%
N.Tantalo CKM' 06	223(15)(19) 11%	246(16)(20) 10%	1.21(2)(5) 4%



QUENCHED



UNQUENCHED

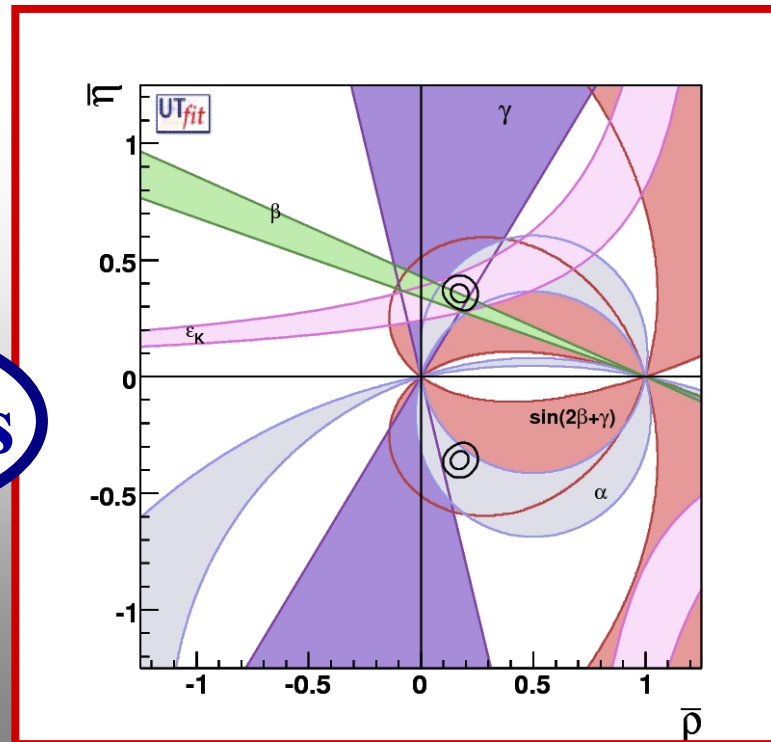
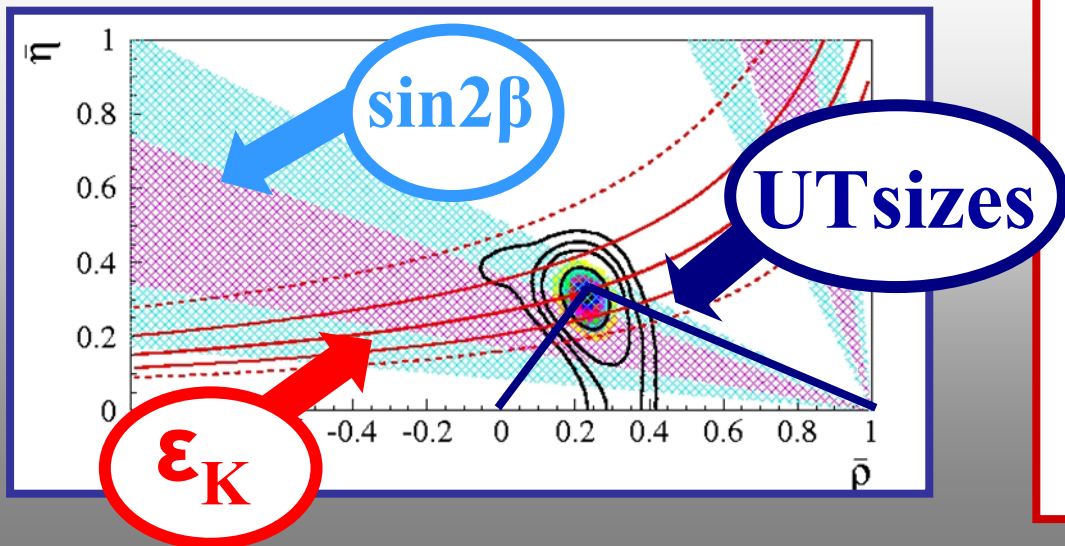
In spite of the relatively large lattice uncertainties, important results for flavour physics have been achieved

CKM PARADIGM OF ~~CP~~

CP-conserving and CP-violating processes determine the same CKM phase

UTfit, today

Ciuchini et al., 2000



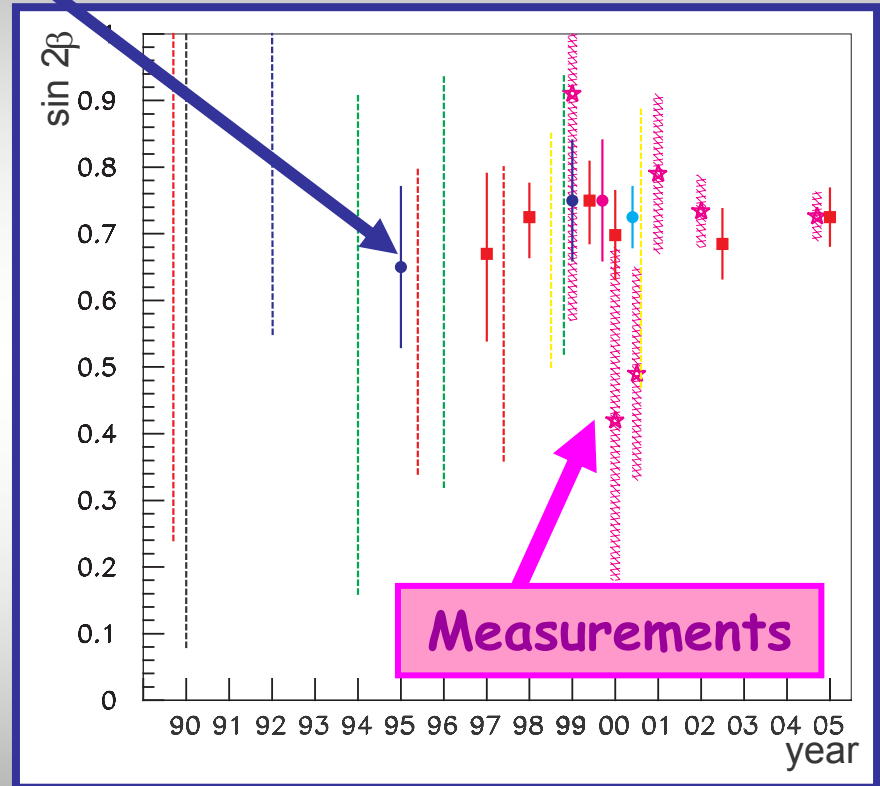
PREDICTION OF $\text{Sin}2\beta$

Ciuchini et al., 1995:
 $\text{Sin}2\beta_{\text{UTA}} = 0.65 \pm 0.12$

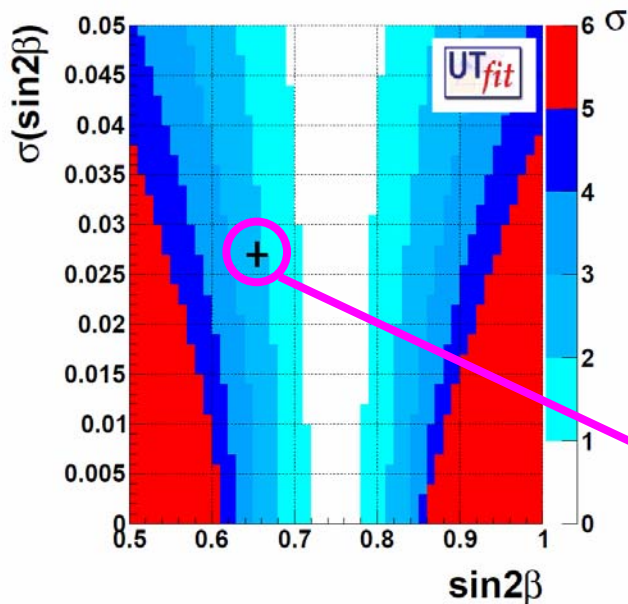
Ciuchini et al., 2000:
 $\text{Sin}2\beta_{\text{UTA}} = 0.698 \pm 0.066$

UTfit today:
 $\text{Sin}2\beta_{\text{UTA}} = 0.751 \pm 0.035$

Predictions exist since 1995



Direct measurement today:
 $\text{Sin}2\beta_{\text{J}/\psi \text{K}0} = 0.655 \pm 0.027$



SM PREDICTION OF Δm_s

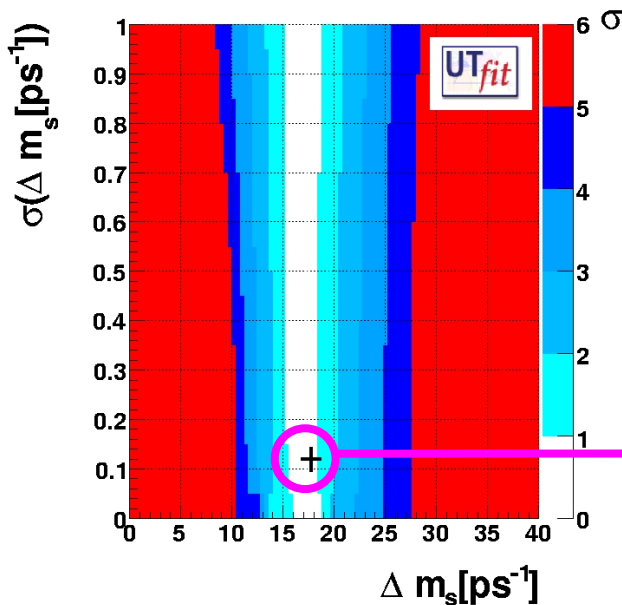
LOOKING FOR NEW PHYSICS EFFECTS

Ciuchini et al., 2000:

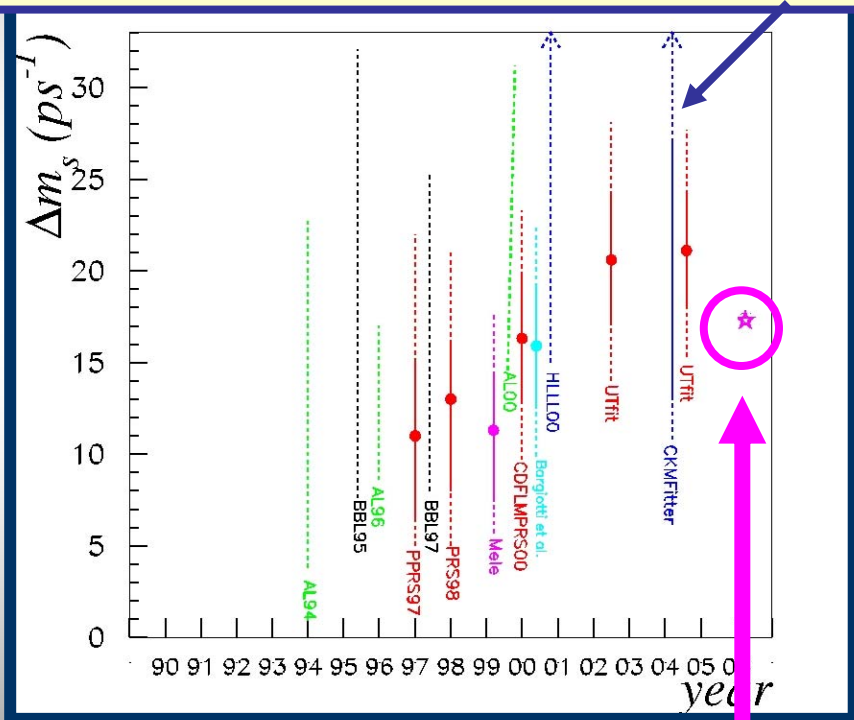
$$\Delta m_s = (16.3 \pm 3.4) \text{ ps}^{-1}$$

UTfit today:

$$\Delta m_s = (16.8 \pm 1.6) \text{ ps}^{-1}$$



The predicted range was very large in the frequentistic CKMFitter approach



Direct measurement today

$$\Delta m_s = (17.77 \pm 0.12) \text{ ps}^{-1}$$

Accuracy of Lattice QCD

2. The “precision” era

PRECISION FLAVOUR PHYSICS

Experiments 2010

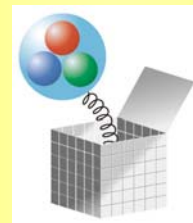
$ V_{us} f_+(0)$	0.21661 ± 0.00047	0.2%
$\frac{ V_{us} F_K}{ V_{ud} F_\pi}$	0.27599 ± 0.00059	0.2%
ϵ_K	$(2.228 \pm 0.011) \times 10^{-3}$	0.5%
Δm_d	$(0.507 \pm 0.005) \text{ ps}^{-1}$	1%
Δm_s	$(17.77 \pm 0.12) \text{ ps}^{-1}$	0.7%
$\text{Sin}2\beta$	0.655 ± 0.027	4%

Lattice 2010

2006

$f_+(0)$	0.5%	0.9%
F_K/F_π	0.9%	1.1%
B_K	5%	11%
$f_B \sqrt{B_B}$	5%	13%
$f_{B_s} \sqrt{B_{B_s}}$	5%	13%
—	—	—

KTEV
Kaons at the Tevatron

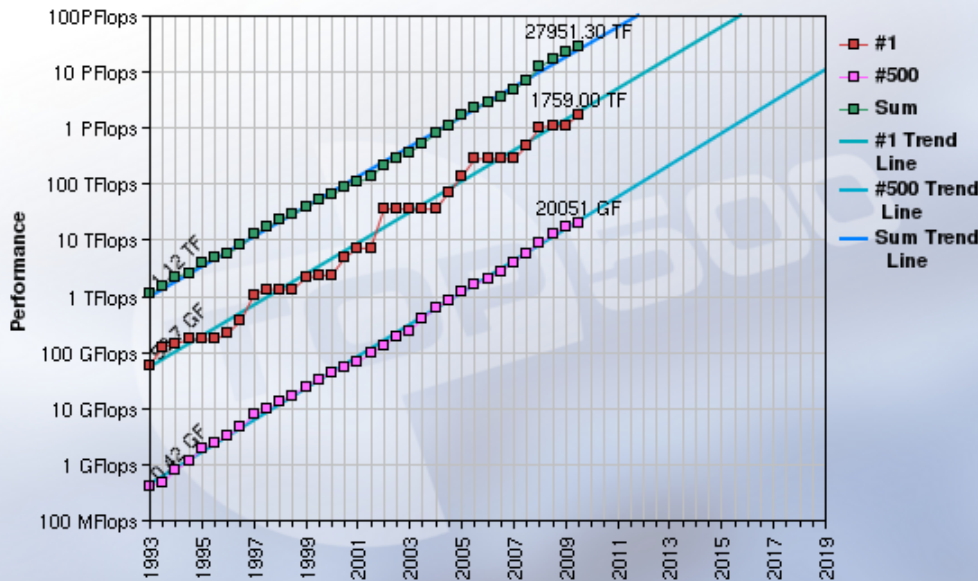
THE "PRECISION ERA" OF LATTICE QCD: WHY NOW

1) Increasing of computational power
→ Unquenched simulations



Projected Performance Development

The Moore's Law



13/11/2009

<http://www.top500.org/>

For Lattice QCD
today: ~ 5-30 TFlops
(like the # 500 in the
TOP500 list)

TeraFlops machines
are required to
perform unquenched
simulations. Available
only since few years.

CPU cost for $N_f=2$ Wilson fermions:

[Del Debbio et al. 2006]

$$\text{TFlops-years} \approx 0.15 \left(\frac{N_{\text{conf}}}{100} \right) \left(\frac{L_s}{3 \text{ fm}} \right)^5 \left(\frac{L_t}{2L_s} \right) \left(\frac{0.15}{\hat{m}/m_s} \right) \left(\frac{0.08 \text{ fm}}{a} \right)^6$$

2) Algorithmic improvements: → Light quark masses in the ChPT regime

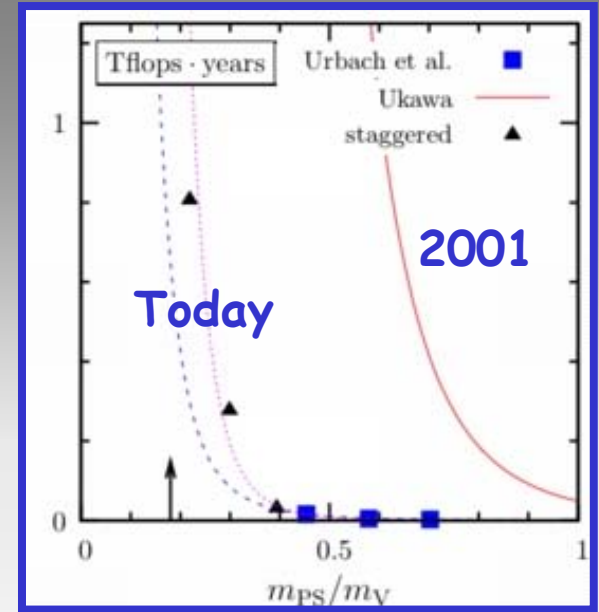
CPU cost (for $N_f=2$ Wilson fermions):

Ukawa 2001 (The Berlin wall):

$$\text{TFlops-years} \approx 3.1 \left(\frac{N_{\text{conf}}}{100} \right) \left(\frac{L_s}{3 \text{ fm}} \right)^5 \left(\frac{L_t}{2L_s} \right) \left(\frac{0.2}{\hat{m} / m_s} \right)^3 \left(\frac{0.1 \text{ fm}}{a} \right)^7$$

Del Debbio et al. 2006:

$$\text{TFlops-years} \approx 0.03 \left(\frac{N_{\text{conf}}}{100} \right) \left(\frac{L_s}{3 \text{ fm}} \right)^5 \left(\frac{L_t}{2L_s} \right) \left(\frac{0.2}{\hat{m} / m_s} \right) \left(\frac{0.1 \text{ fm}}{a} \right)^6$$



Today: $M_{\pi}^{\text{latt}} \approx 200 - 300 \text{ MeV}$ ($\hat{m}_{ud}^{\text{latt}} / m_s \approx 1/6 - 1/12$) **ChPT**

Few years ago: $M_{\pi}^{\text{latt}} \approx 500 \text{ MeV}$ ($\hat{m}_{ud}^{\text{latt}} / m_s \approx 1/2$)

KAON AND B PHYSICS ON THE LATTICE

Collaboration	Quark action	Nf	a [fm]	$(M_\pi)^{\min}$ [MeV]	Observables
MILC + FNAL, HPQCD,...	Improved staggered	2+1	≥ 0.045	230	$f_K, B_K, f_B, B_B,$ $B \rightarrow D/\pi \ell \nu$
PACS-CS	Clover (NP)	2+1	0.09	156	f_K
RBC/UKQCD	DWF	2+1	≥ 0.08	290	$f_+(0), f_K, B_K,$ $K \rightarrow \pi\pi$
BMW	Clover smeared	2+1	≥ 0.07	190	f_K
JLQCD	Overlap	2 [2+1]	0.12	290	B_K
ETMC	Twisted mass	2 [2+1+1]	≥ 0.07	260	$f_+(0), f_K, B_K,$ f_B
QCDSF	Clover (NP)	2	≥ 0.06	300	$f_+(0), f_K$

THE FIRST ROW UNITARITY TEST

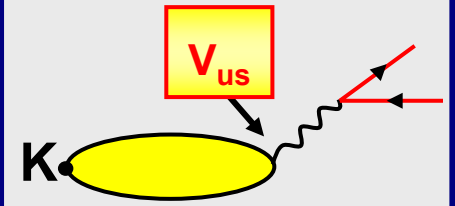
$$|V_{ud}|^2 + |V_{us}|^2 + \cancel{|V_{ub}|^2} = 1$$

The most stringent unitarity test

V_{us}/V_{ud} from $K\mu 2/\pi\mu 2$ decays

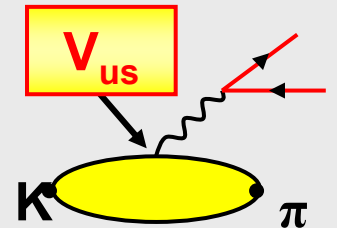
$$\frac{\Gamma(K \rightarrow \mu \bar{\nu}_\mu (\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}_\mu (\gamma))} = \frac{|V_{us}|^2}{|V_{ud}|^2} \left(\frac{f_K}{f_\pi} \right)^2 \frac{m_K (1 - \frac{m_\mu^2}{m_K^2})}{m_\pi (1 - \frac{m_\mu^2}{m_\pi^2})} \times 0.9930(35)$$

[Marciano 04]



V_{us} from $Kl3$ decays

$$\Gamma_{K \rightarrow \pi l \nu} = C_K^2 \frac{G_F^2 m_K^5}{192 \pi^2} |S_{EW}| [1 + \Delta_{SU(2)} + 2\Delta_{EM}] \times |V_{us}|^2 |f_+^{K\pi}(0)|^2$$

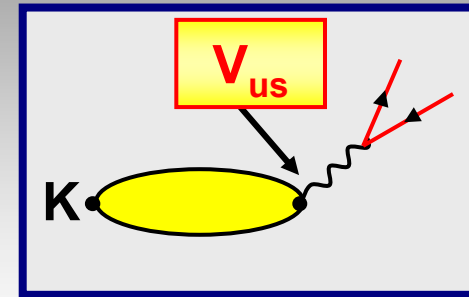
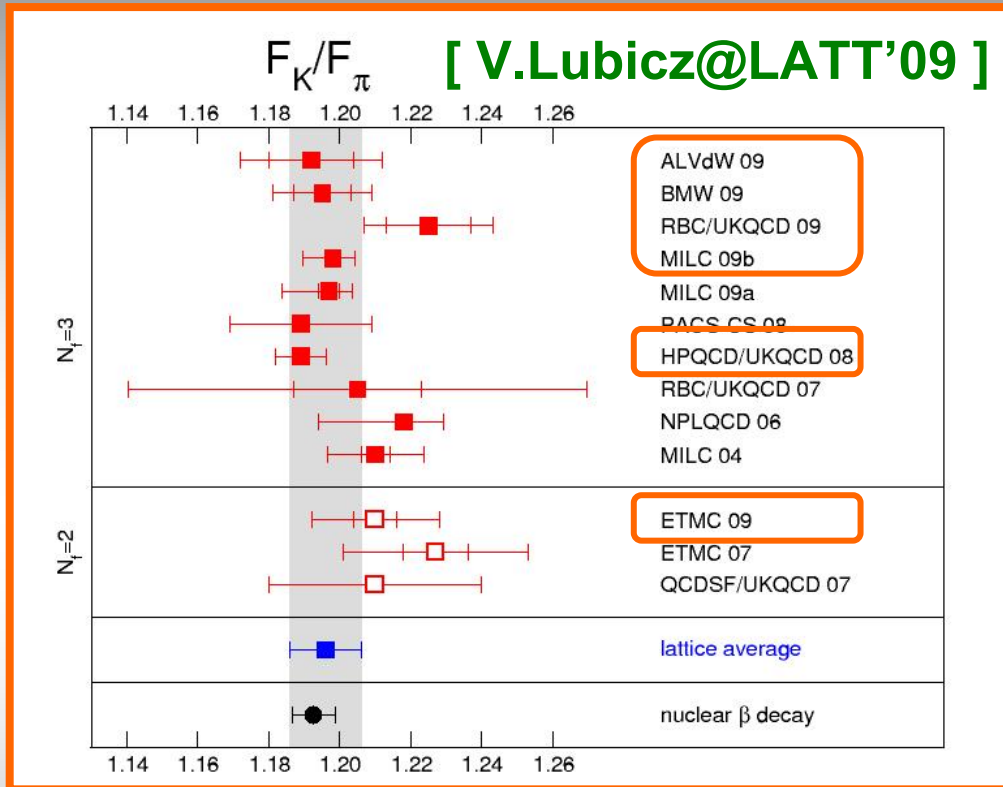


$$\frac{|V_{us}|}{|V_{ud}|} \frac{f_K}{f_\pi} = 0.27599(59)$$

Flavi
net **A**
Kaon WG

$$|V_{us}| f_+(0) = 0.21661(47)$$

V_{us}/V_{ud} from leptonic K decays: f_K/f_π



$$\frac{\Gamma(K \rightarrow \mu \bar{\nu}_\mu (\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}_\mu (\gamma))} = \frac{|V_{us}|^2 \left(\frac{f_K}{f_\pi}\right)^2 m_K \left(1 - \frac{m_\mu^2}{m_K^2}\right)}{|V_{ud}|^2 \left(\frac{f_\pi}{f_K}\right)^2 m_\pi \left(1 - \frac{m_\mu^2}{m_\pi^2}\right)} \times 0.9930(35) \quad [\text{Marciano 04}]$$

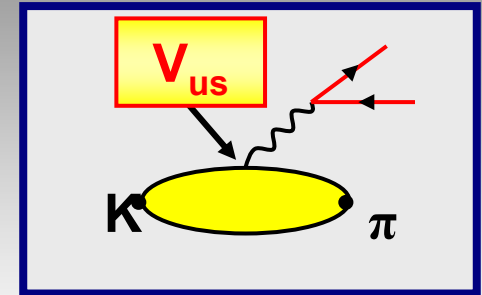
$$f_K/f_\pi = 1.196(1)(10) \quad 0.8\%$$

The accuracy is comparable to the one reached on $f_+(0)$ [0.5%]

- $|V_{us}|_{KI2} = 0.2248(19)$
- $|V_{us}| = 0.2255(10)$
Using unitarity and $|V_{ud}|$ from nuclear β decays

V_{us} from semileptonic K decays: $f_+^{K\pi}(0)$

$$\Gamma_{K \rightarrow \pi l \nu} = C_K^2 \frac{G_F^2 m_K^5}{192 \pi^2} |S_{EW}| [1 + \Delta_{SU(2)} + 2\Delta_{EM}] \times |V_{us}|^2 |f_+^{K\pi}(0)|^2$$



Ademollo-Gatto: $f_+(0) = 1 - O(m_s - m_u)^2 \leftarrow O(1\%)$. But represents the largest theoret. uncertainty

SU(3)-ChPT

$$f_+(0) = 1 + f_2 + f_4 + O(p^8)$$

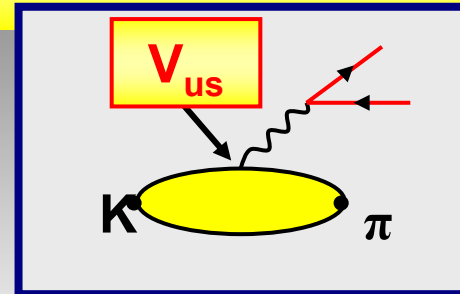
Vector Current Conservation

$f_2 = -0.023$
Independent of L_i
(Ademollo-Gatto)

THE LARGEST UNCERTAINTY

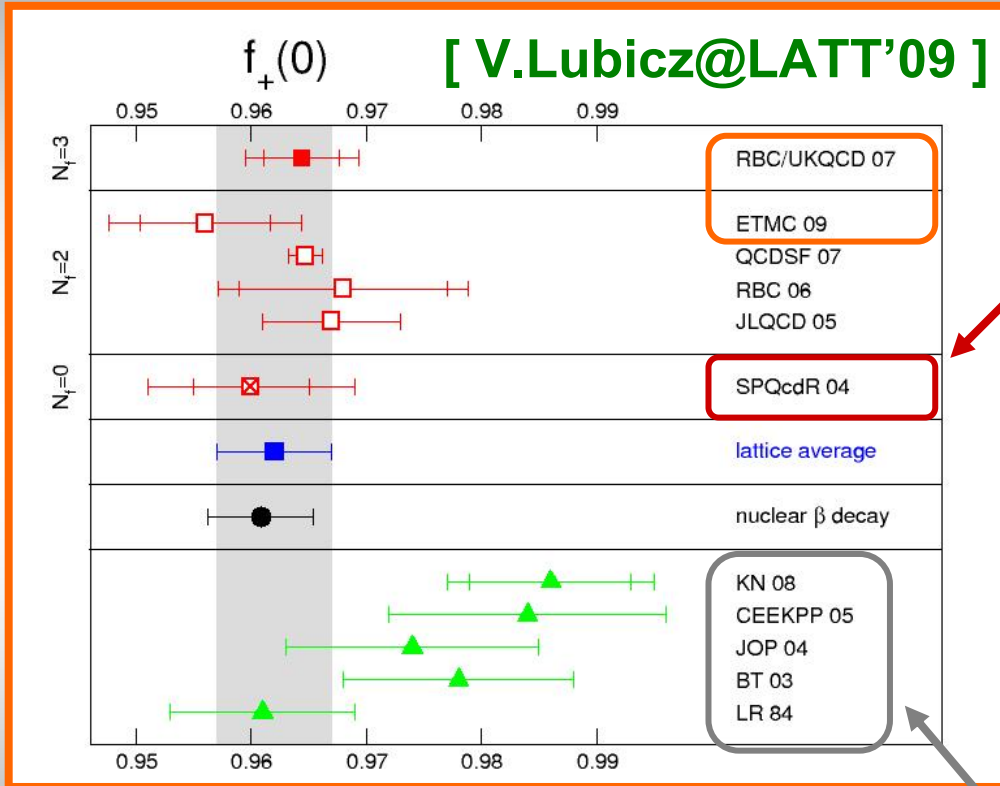
Old standard estimate:
Leutwyler, Roos (1984)
(QUARK MODEL)
 $f_4 = -0.016 \pm 0.008$

V_{us} from semileptonic K decays: $f_+^{K\pi}(0)$



Double ratio method:
the achieved accuracy is $O(1\%)$

The first lattice calculation, 2004



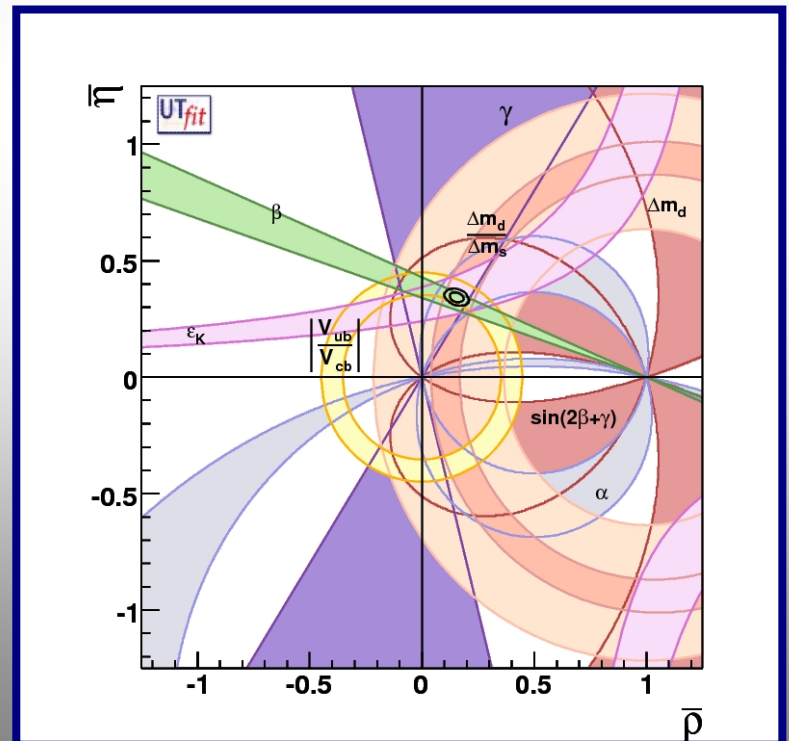
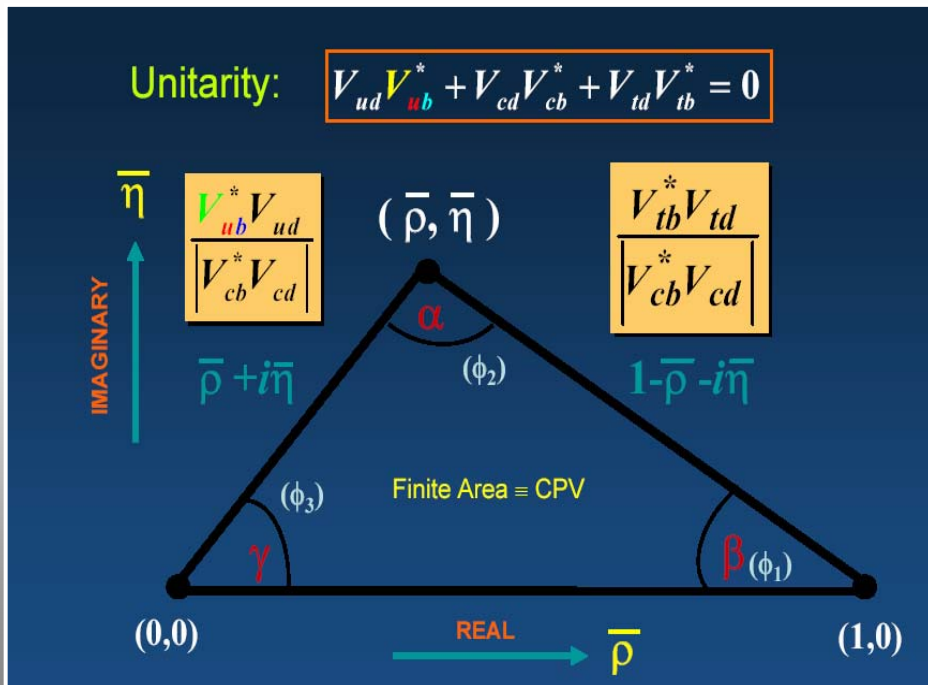
- $|V_{us}|_{Kl3} = 0.2252(13)$
- $|V_{us}|_{Kl2} = 0.2248(19)$
- $|V_{us}| = 0.2255(10)$
Using unitarity and $|V_{ud}|$ from nuclear β decays

$f_+(0) = 0.962(3)(4)$ **0.5%**

Analytical model calculations tends to give larger predictions than lattice results

THE UNITARITY TRIANGLE ANALYSIS

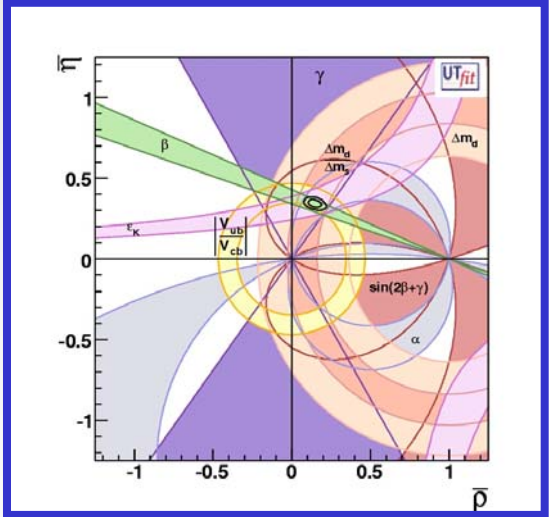
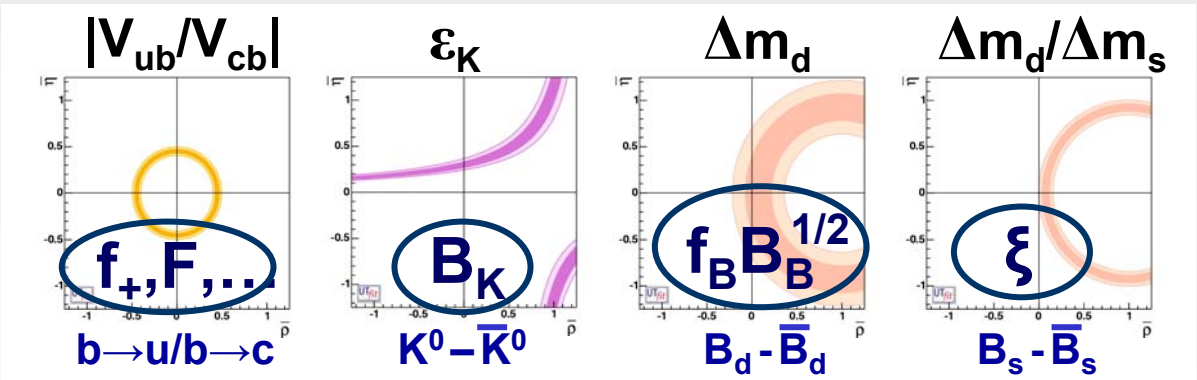
1. Lattice inputs



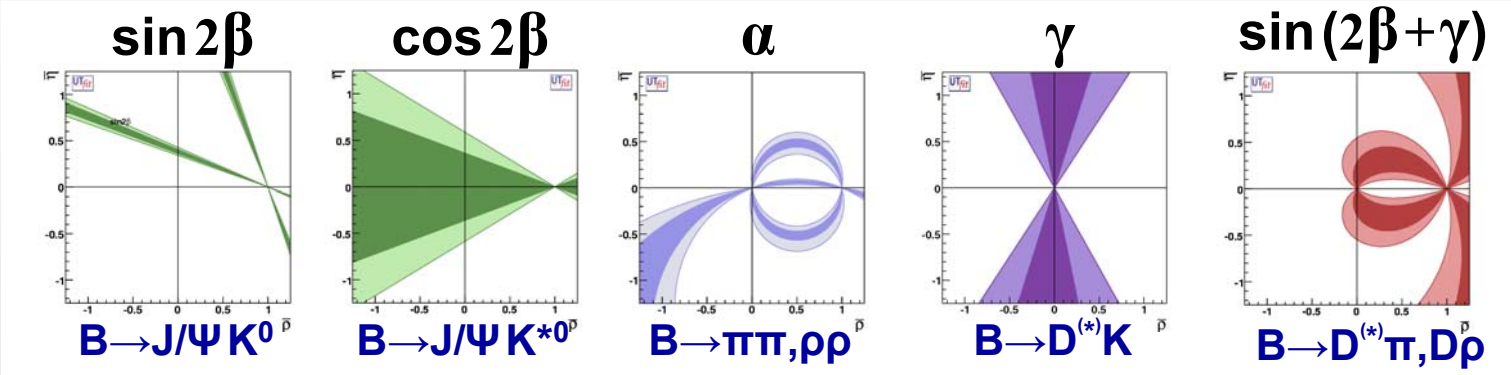
THE UTA CONSTRAINTS



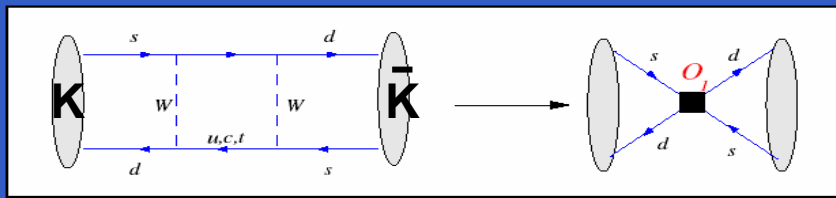
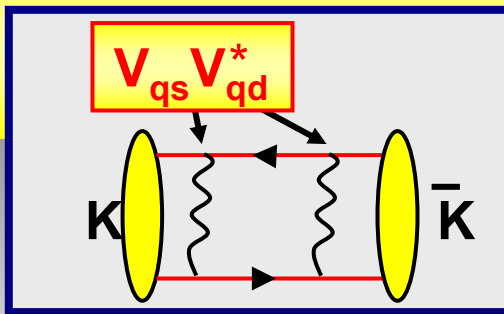
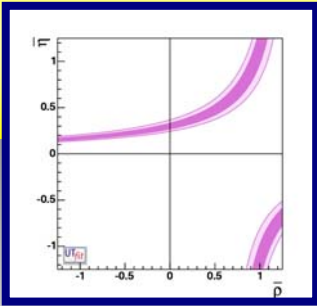
UT-LATTICE



UT-ANGLES



$K^0 - \bar{K}^0$ mixing: B_K



$$\langle \bar{K}^0 | Q(\mu) | K^0 \rangle = \frac{8}{3} f_K^2 m_K^2 B_K(\mu)$$

Pre-history

QCD SR, Pich, De Rafael, **1985**:

$$\hat{B}_K = 0.33 \pm 0.09$$

LQCD, Gavela et al., **1987**:

$$\hat{B}_K = 0.90 \pm 0.20$$

History

Quench. error

$$\hat{B}_K = 0.90 \pm 0.03 \pm 0.15$$

S. Sharpe@Latt'96 17%

$$\hat{B}_K = 0.86 \pm 0.05 \pm 0.14$$

L. Lellouch@Latt'00 17%

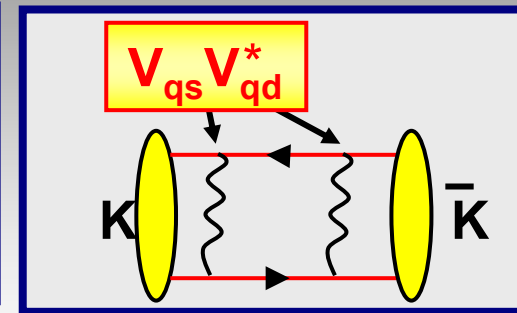
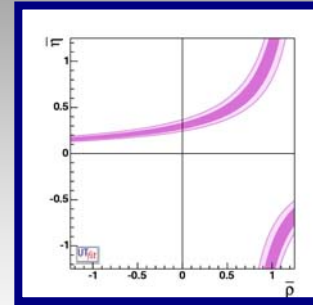
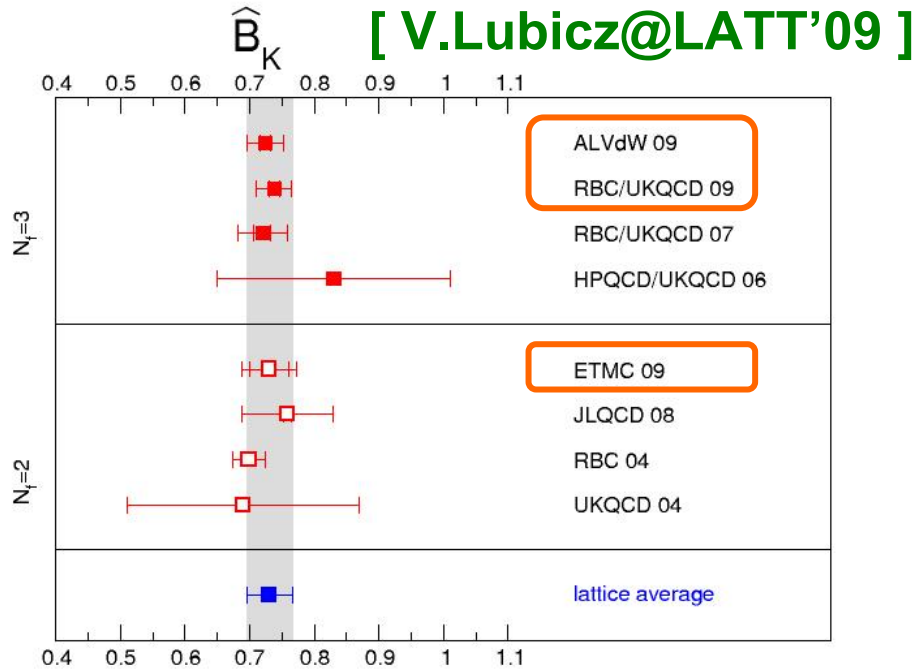
$$\hat{B}_K = 0.79 \pm 0.04 \pm 0.08$$

C. Dawson@Latt'05 11%

$$\hat{B}_K = 0.731 \pm 0.036$$

V. Lubicz@Latt'09 5%

$K^0 - \bar{K}^0$ mixing: B_K



From the UT fit, assuming the Standard Model

$$\hat{B}_K = 0.87(8)$$

UT fit

with $K\epsilon = 0.94(2)$,

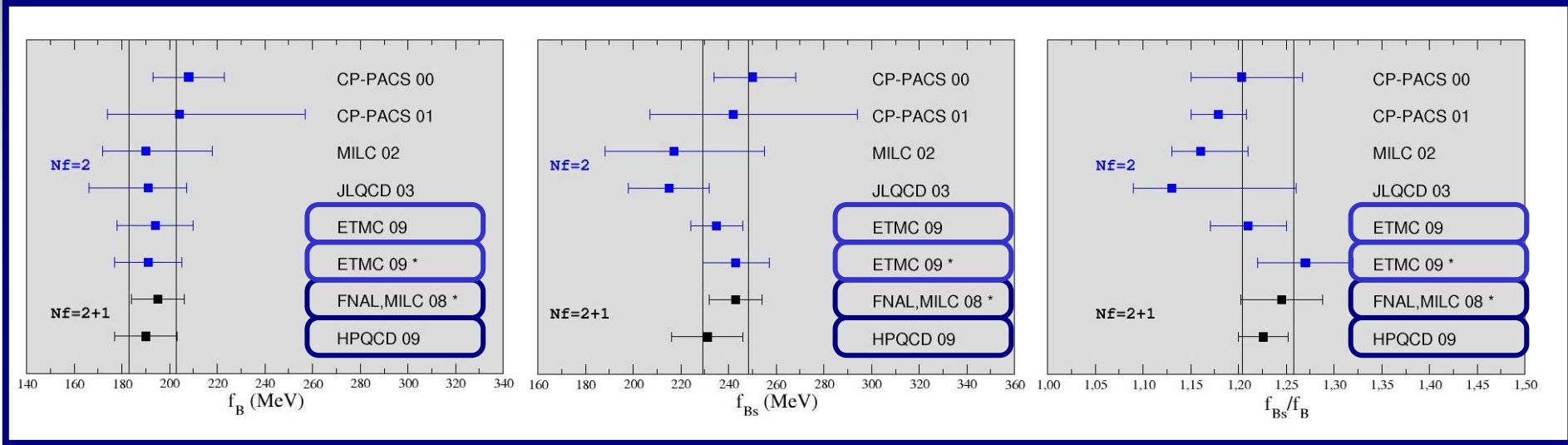
A.Buras, D.Guadagnoli, G.Isidori,
arXiv:1002.3612

$$\hat{B}_K = 0.731(7)(35) \quad 5\%$$

Error in 2006: 11%

B-mesons decay constants: f_B, f_{B_s}

Lattice inputs for $\Delta m_{d/s}$ and $B \rightarrow \tau \nu$



Averages from J.Laiho, E.Lunghi, R.Van de Water, 0910.2928

$f_{B_s} = 238.8 \pm 9.5 \text{ MeV}$
 $f_B = 192.8 \pm 9.9 \text{ MeV}$

4-5%

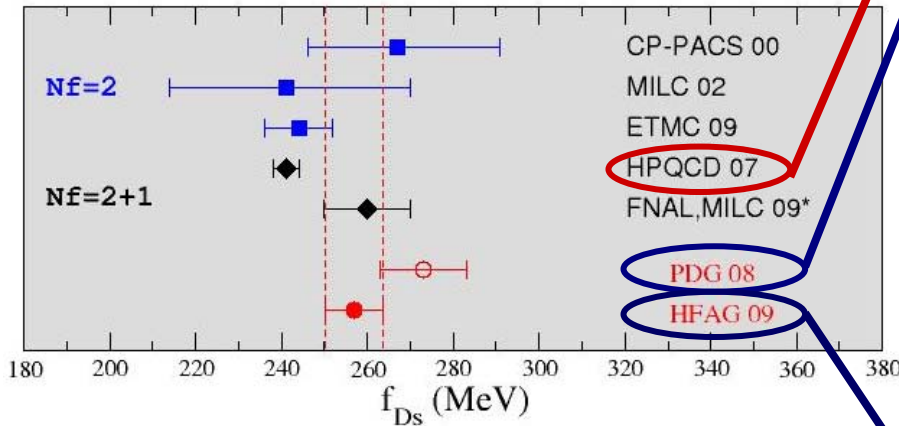
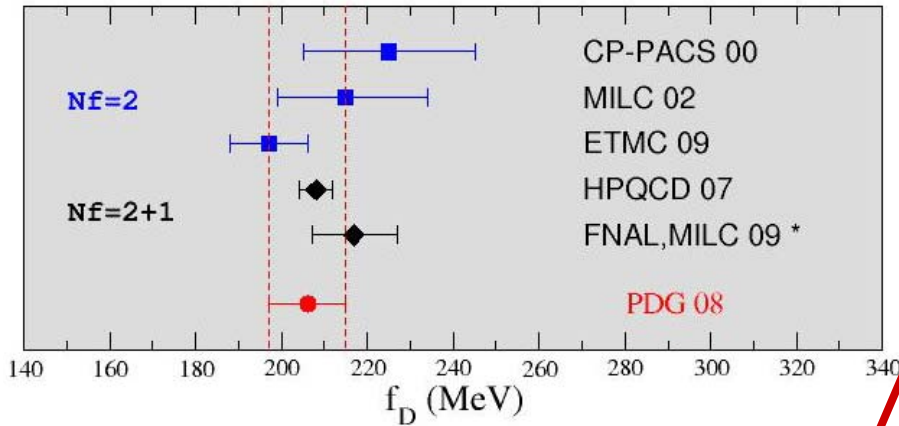
$f_{B_s}/f_B = 1.231 \pm 0.027$

2%

Error in 2006: 14%

Error in 2006: 5%

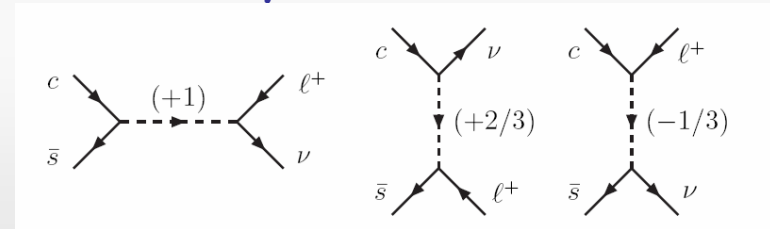
Is there an " f_{D_s} puzzle" ?



A lattice result by **HPQCD**, which claims a 1.2% precision on f_{D_s} , shows a **discrepancy of about 3σ** with the PDG'08 average:

- $f_{D_s} = 241 \pm 3 \text{ MeV}$ HPQCD 07
- $f_{D_s} = 273 \pm 10 \text{ MeV}$ PDG 08

B. Dobrescu, A. Kronfeld, 0803.0512
 "Evidence for nonstandard leptonic decays of D_s mesons"

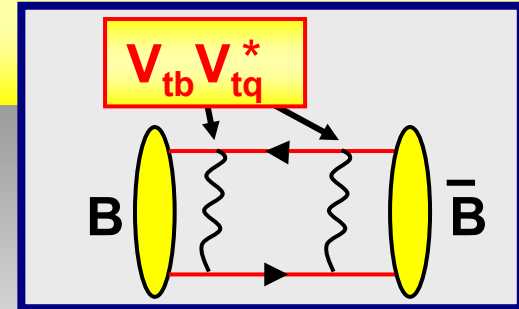
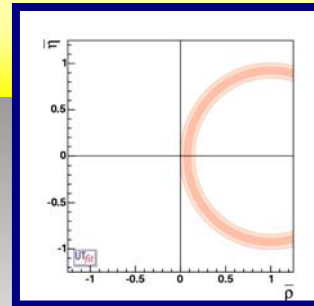


This year, after a **new CLEO-c result**, the tension is reduced at the **2σ level**:

- $f_{D_s} = 256.9 \pm 6.8 \text{ MeV}$ HFAG 09

B- \bar{B} mixing: $B_{Bd/s}$

$$\langle \bar{B} | Q(\mu) | B \rangle = \frac{8}{3} m_B^2 f_B^2 B_B(\mu)$$



Only one modern calculation
HPQCD [0902.1815]

$$\hat{B}_{Bd} = 1.26 \pm 0.11$$

$$\hat{B}_{Bs} = 1.33 \pm 0.06$$

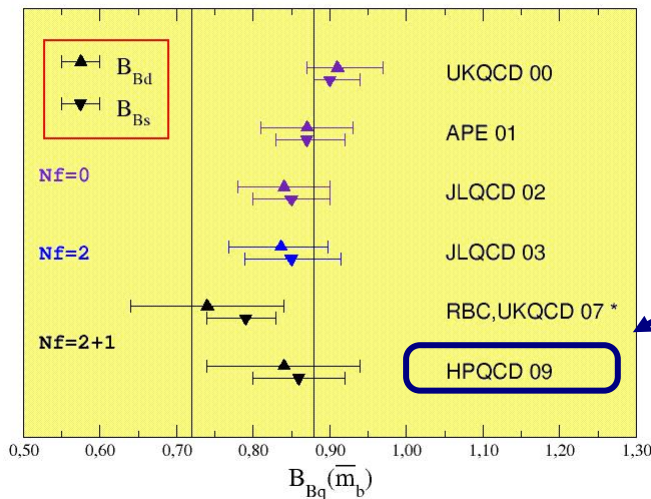
Combining with f_B and f_{Bs} :

$$f_{Bs} \sqrt{\hat{B}_{Bs}} = 275 \pm 13 \text{ MeV} \quad 5\%$$

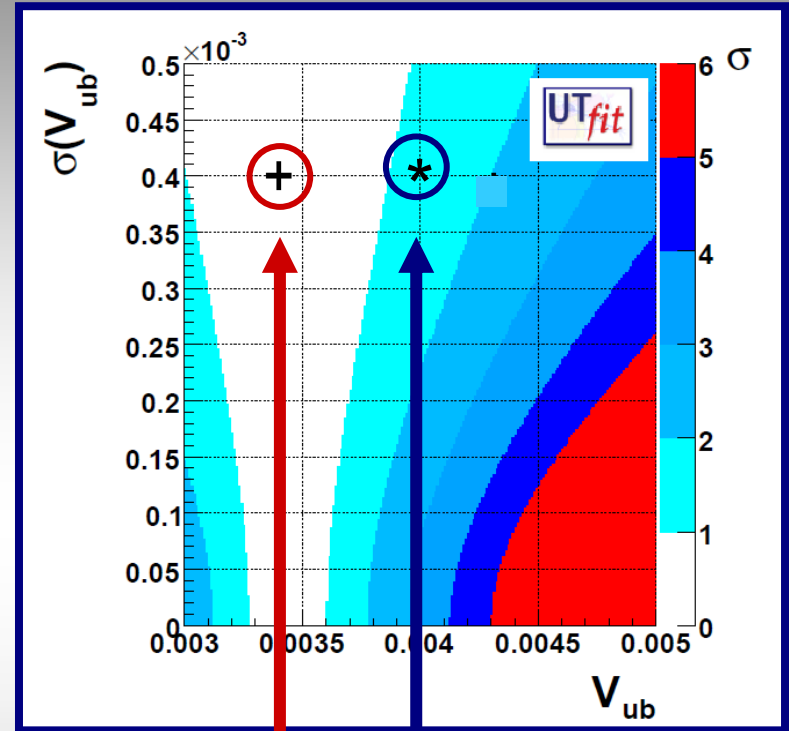
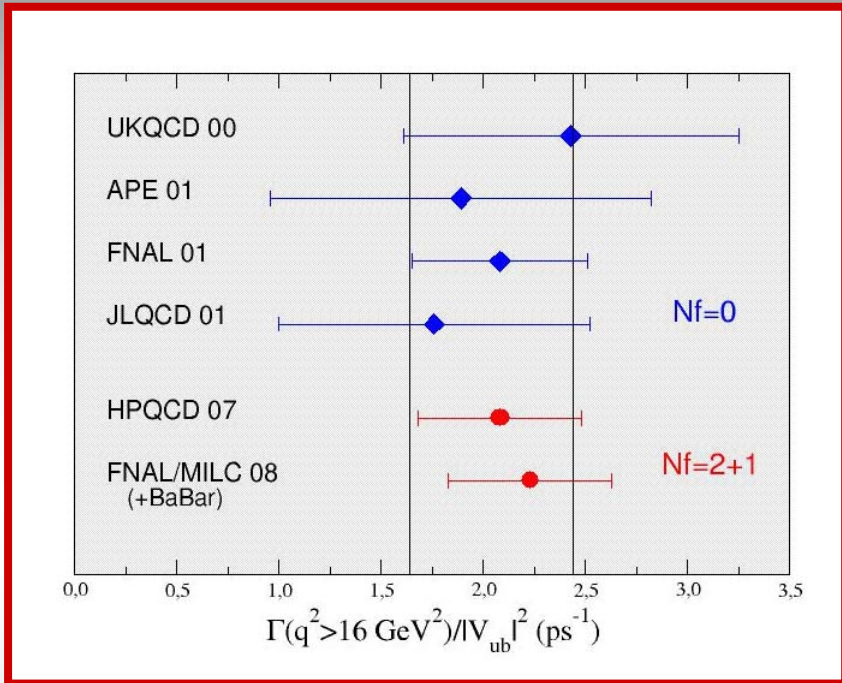
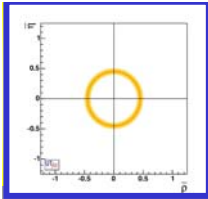
$$\xi = 1.243 \pm 0.028 \quad 2\%$$

Error in 2006: 13%

Error in 2006: 5%



Exclusive V_{ub} - $B \rightarrow \pi l \nu$



$$|V_{ub}|_{\text{excl.}} = (35.0 \pm 4.0) 10^{-4}$$

11%

Error in 2006: 11%

MORE LATTICE CALCULATIONS REQUIRED

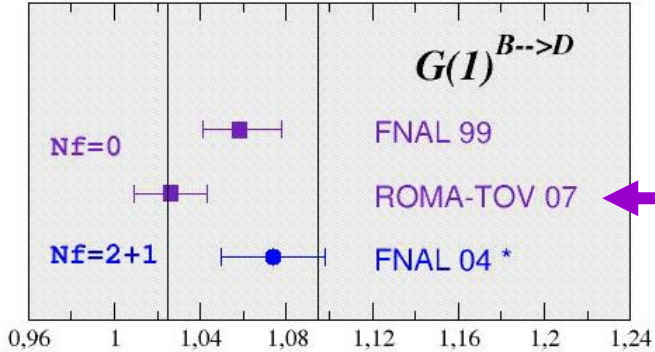
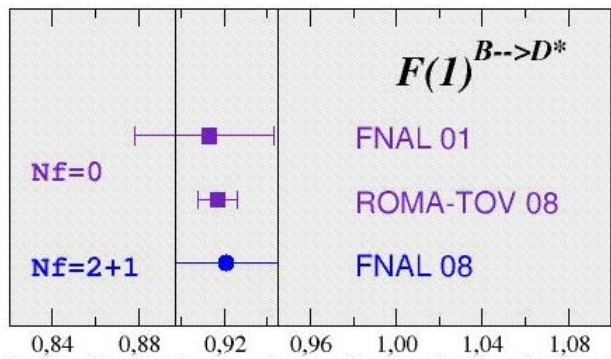
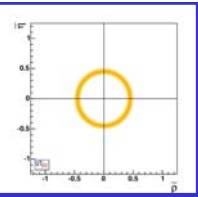
$$V_{ub}^{\text{excl.}} = (3.5 \pm 0.4) 10^{-3}$$

From LQCD and QCDSR

$$V_{ub}^{\text{incl.}} = (4.0 \pm 0.4) 10^{-3}$$

Model dependent
BLNP, DGE, GGOU, ADFR, BLL

Exclusive V_{cb} - $B \rightarrow D/D^* l \nu$



TWO DIFFERENT APPROACHES:

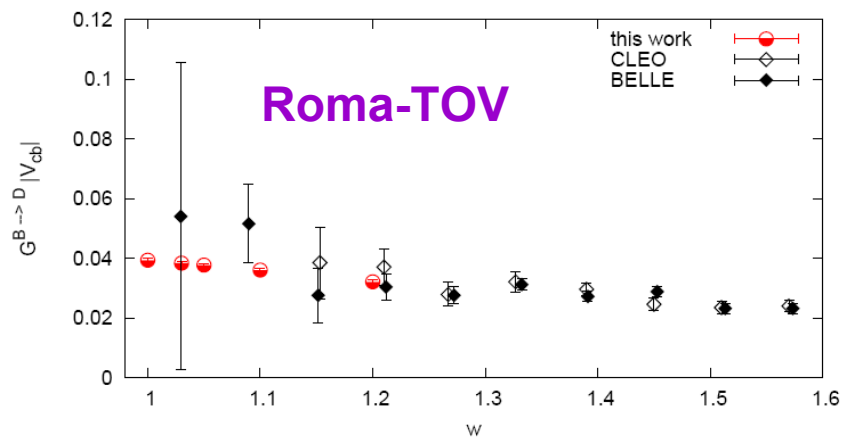
- "double ratios" (FNAL)
- "step scaling" (TOV)

Remarkable agreement

Averages from
VL, C. Tarantino 0807.4605

$F(1) = 0.924 \pm 0.022$ **2%**

$G(1) = 1.060 \pm 0.035$ **3%**



Error in 2006: 4%

THE UNITARITY TRIANGLE ANALYSIS

2. Deviations from the Standard Model

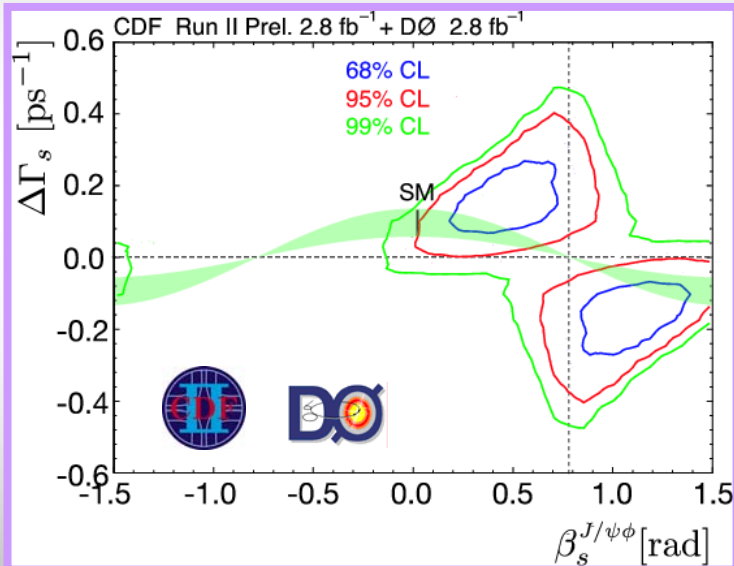
Overall, flavour data are in excellent agreement with the SM expectation at the present level of accuracy.

Yet there are few processes showing 2-3 σ deviations...

1) THE PHASE OF B_s MIXING

update from UTfit Coll., PMC Physics A 2009, 3:6 [arXiv:0803.0659]

The time-dependent CP asymmetry in $B_s \rightarrow J/\psi\phi$ has been measured at Tevatron

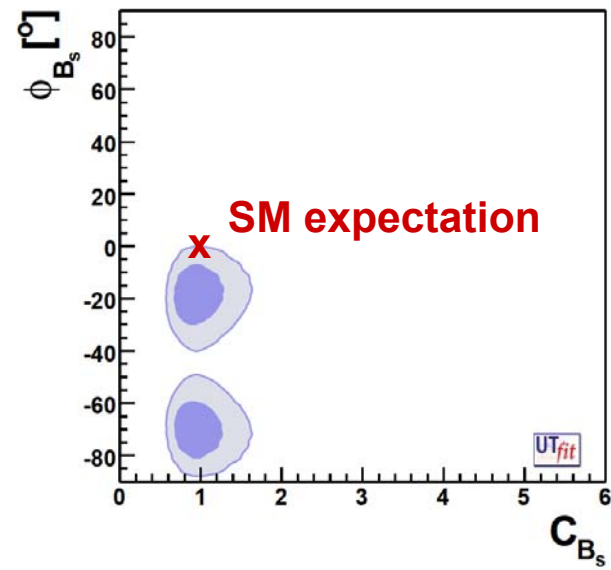


2.12 σ from the SM

NB: A 5 σ measurement could be possible at the Tevatron

From a global fit

$$C_{B_s} e^{2i\phi_{B_s}} = \frac{\langle B_s^0 | H_{\text{eff}}^{\text{full}} | \bar{B}_s^0 \rangle}{\langle B_s^0 | H_{\text{eff}}^{\text{SM}} | \bar{B}_s^0 \rangle}$$



2.5 σ from the SM



2) $Br(B \rightarrow \tau \nu)$

UTfit Coll., arXiv:0908.3470

$$BR(B \rightarrow \tau \nu)_{\text{exp}} = (1.73 \pm 0.34) \times 10^{-4}$$

$$BR(B \rightarrow \tau \nu)_{\text{no-fit}} = (0.98 \pm 0.24) \times 10^{-4}$$

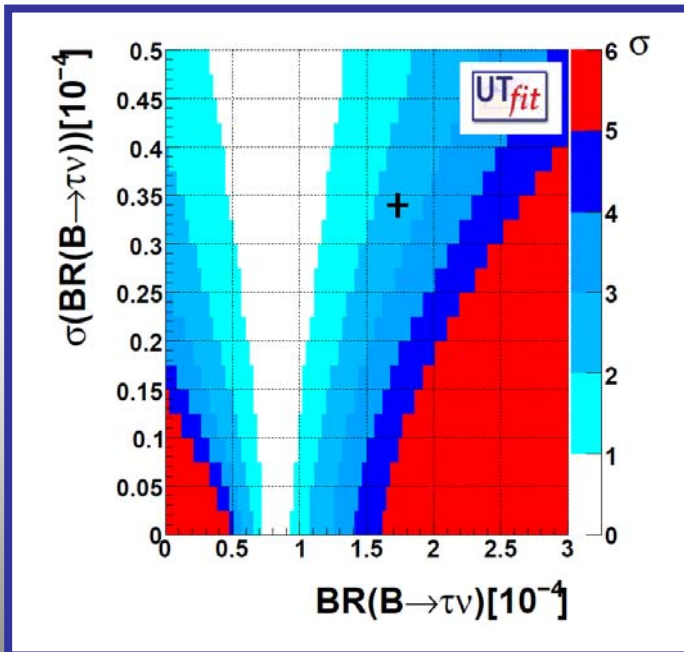
$$BR(B \rightarrow \tau \nu)_{\text{UT}} = (0.84 \pm 0.11) \times 10^{-4}$$

$$BR(B \rightarrow \tau \nu) = \frac{G_F^2 m_B m_\tau^2}{8\pi} \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

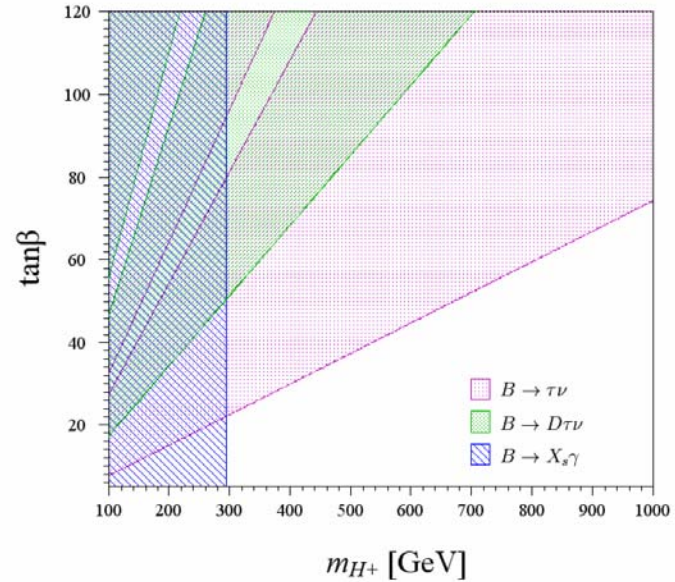
1.8 σ

2.5 σ

2HDM-II



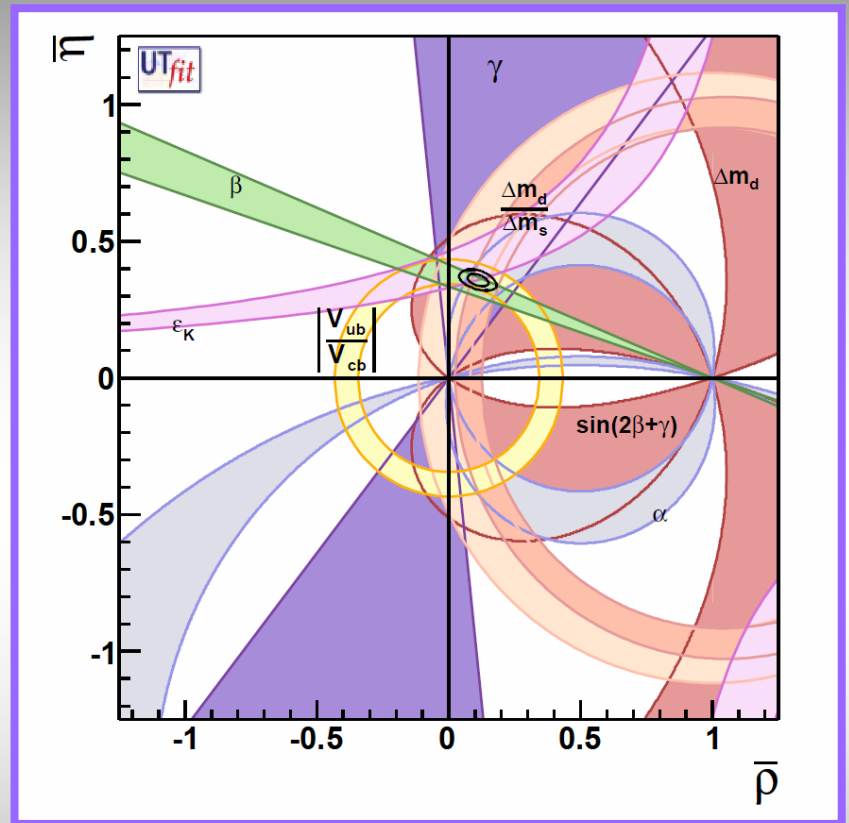
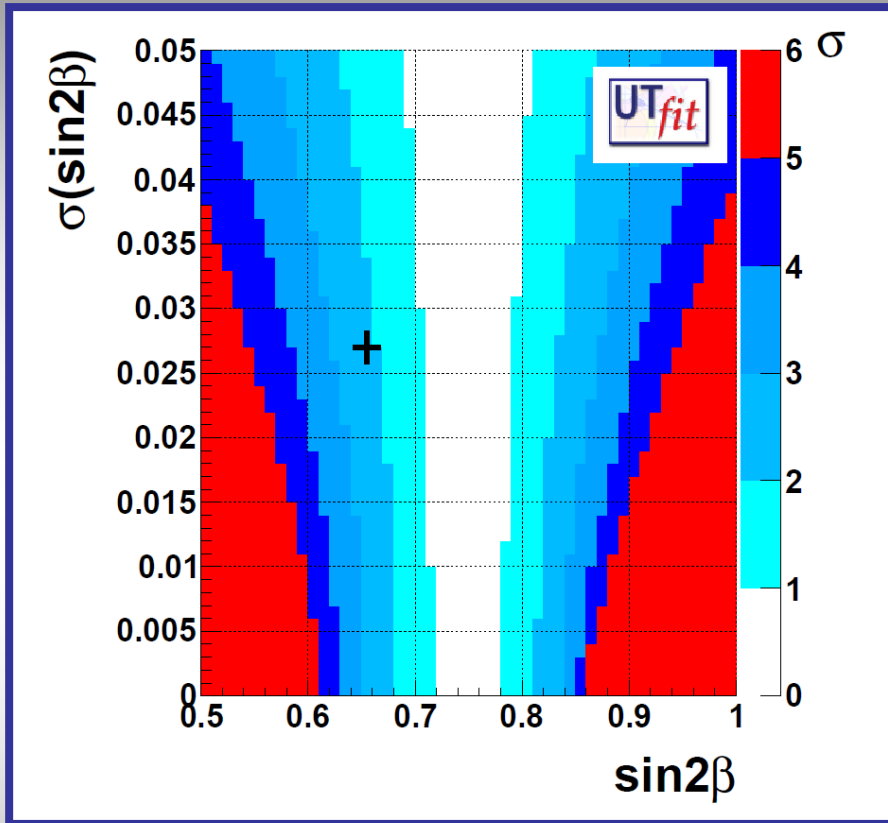
2.5 σ from the SM



$$BR(B \rightarrow \tau \nu) = BR(B \rightarrow \tau \nu)_{\text{SM}} \left(1 - \tan^2 \beta \frac{m_B^2}{m_{H^+}^2}\right)^2$$

$$\tan \beta < 7.4 \frac{m_{H^+}}{100 \text{ GeV}} \quad @ 95\%$$

3) TENSION IN THE SM FIT



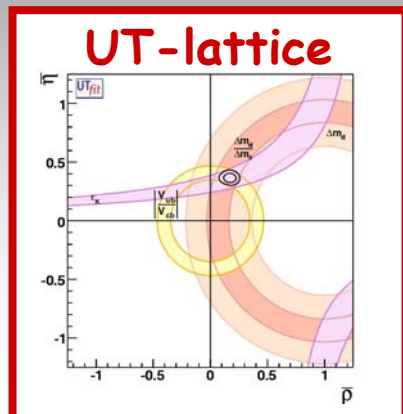
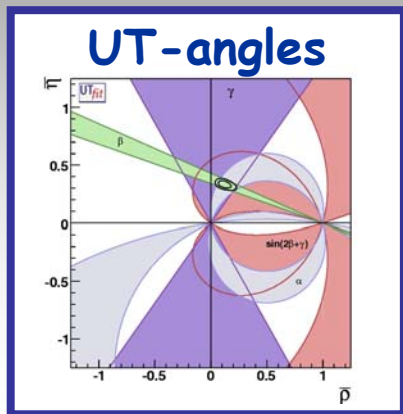
$$\text{Sin}2\beta_{J/\psi K^0} = 0.655 \pm 0.027$$

$$\text{Sin}2\beta_{\text{UTA}} = 0.751 \pm 0.035$$

$\sim 2.2\sigma$ from the SM



OF LATTICE PARAMETERS



Assuming the validity of the **Standard Model** one can perform a fit of the hadronic parameters:

Tension in the fit

2%! from Δm_s

	B_K	$f_{B_s} \sqrt{B_{B_s}}$ (MeV)	ξ
UTA	0.87 ± 0.08	265 ± 4	1.25 ± 0.06
Lattice	0.73 ± 0.04	275 ± 13	1.24 ± 0.03

Lattice inputs are less relevant today for the SM analysis. But they are crucial when looking for new physics effects

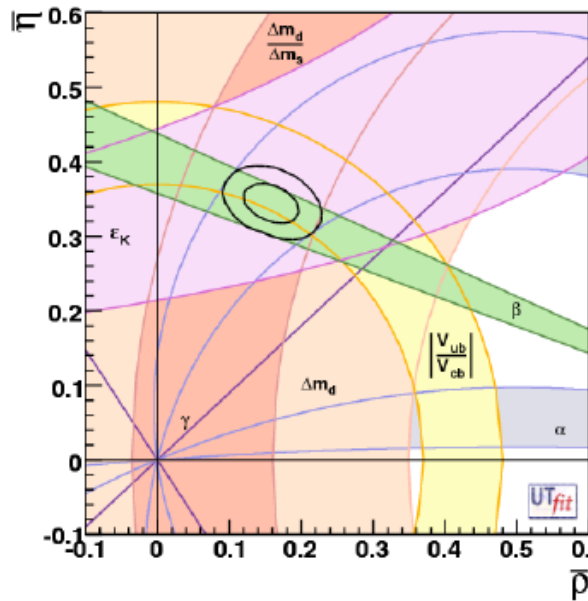
Accuracy of Lattice QCD

3. The future

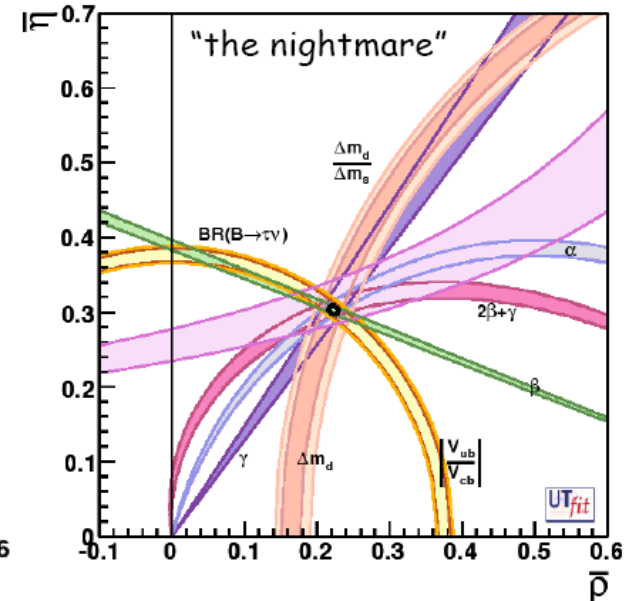
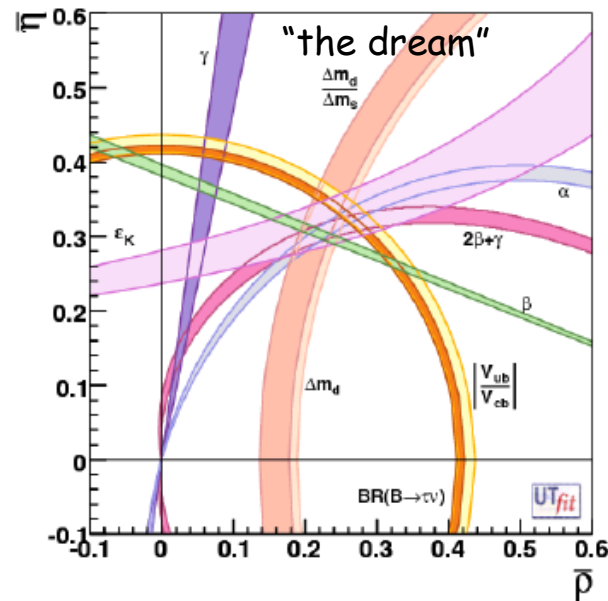
The goal of the **SuperB factory** is precision flavour physics for **indirect New Physics searches**

For example: testing the CKM paradigm at the 1% level

Today



With a SuperB in 2015



The theoretical accuracy must compete with the experimental one.

Can we reach the 1% accuracy in Lattice QCD ??

Cost of the "SuperB" lattice simulation

Simulation parameters

Nconf = 120

$a = 0.033$ fm
[$1/a = 6.0$ GeV]

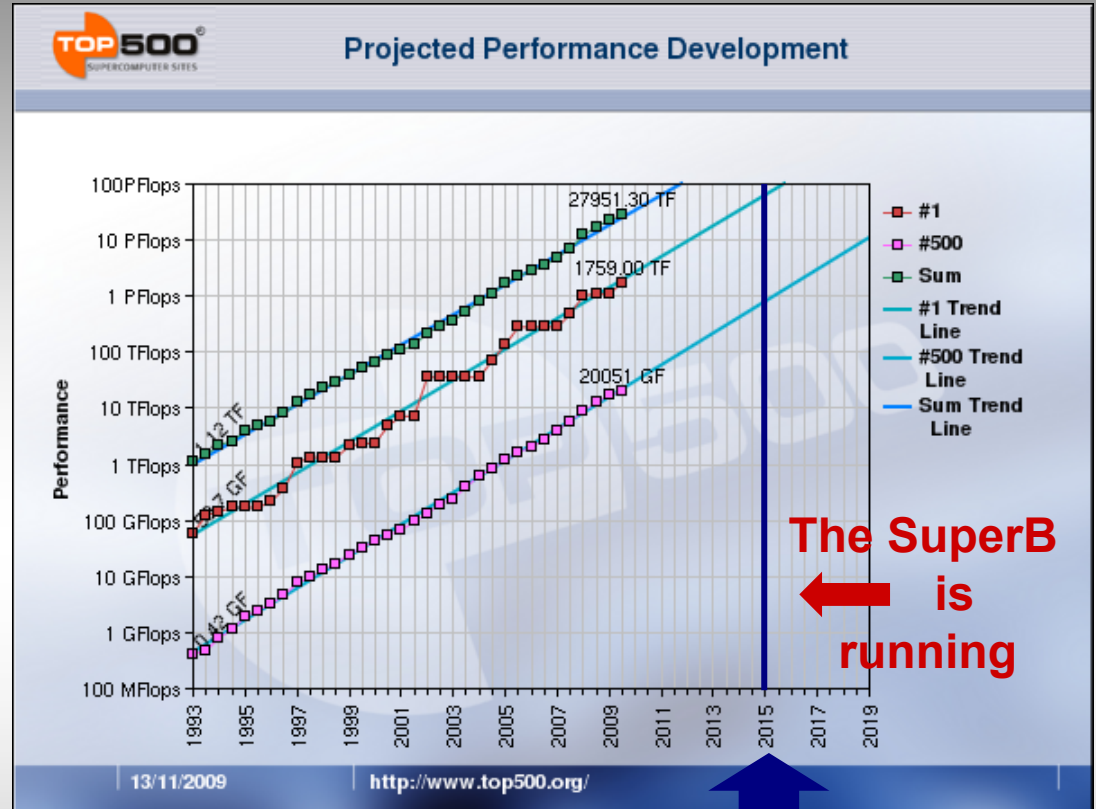
$\hat{m}/m_s = 1/12$

[$M_\pi = 200$ MeV]

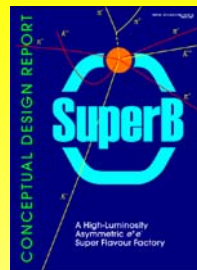
$L_s = 4.5$ fm
[$V = 136^3 \times 270$]

~ 3 PFlop-years

VL @ SuperB IV



Affordable with
1-10 PFlops available
for Lattice QCD in 2015!

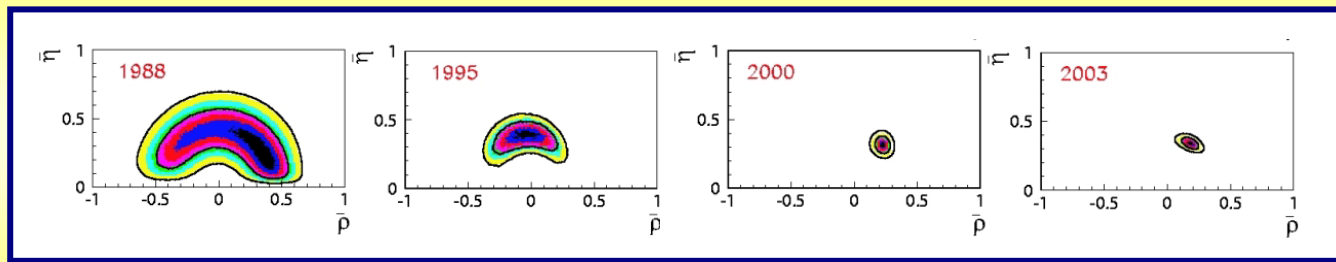



V.Lubicz @
Villa Mondragone
Monte Porzio Catone - Italy
13 - 15 November 2006

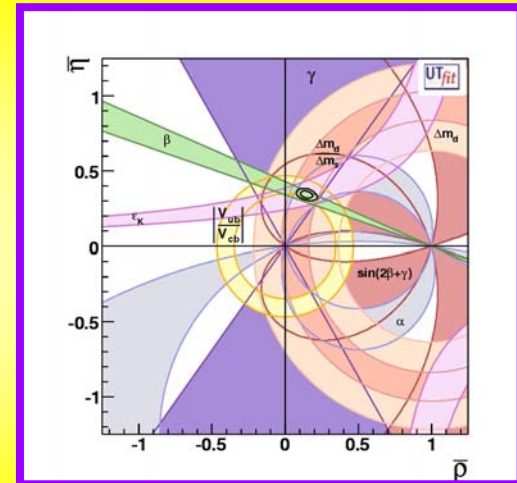
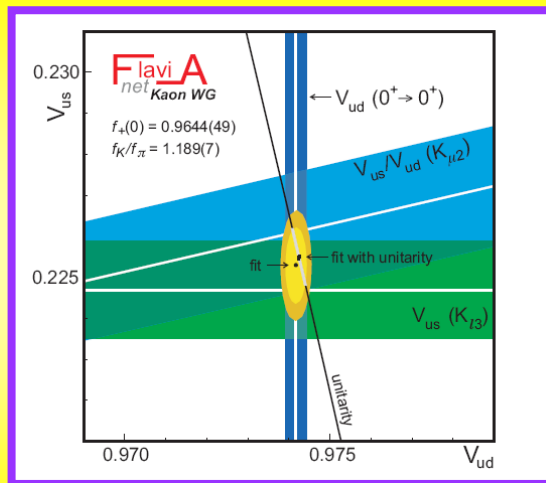


Hadronic matrix element	Lattice error in 2006	Lattice error in 2009	6 TFlop Year [2009]	60 TFlop Year [2011 LHCb]	1-10 PFlop Year [2015 SuperB]
$f_+^{K\pi}(0)$	0.9%	0.5%	0.7%	0.4%	< 0.1%
\hat{B}_K	11%	5%	5%	3%	1%
f_B	14%	5%	3.5 - 4.5%	2.5 - 4.0%	1 - 1.5%
$f_{B_s} B_{B_s}^{1/2}$	13%	5%	4 - 5%	3 - 4%	1 - 1.5%
ξ	5%	2%	3%	1.5 - 2 %	0.5 - 0.8 %
$\mathcal{F}_{B \rightarrow D/D^*lv}$	4%	2%	2%	1.2%	0.5%
$f_+^{B\pi}, \dots$	11%	11%	5.5 - 6.5%	4 - 5%	2 - 3%
$T_1^{B \rightarrow K^*/\rho}$	13%	13%	----	----	3 - 4%

The past



the present



and the future

