Flavour and CP violation in the Standard Model and Beyond

Luca Silvestrini INFN, Sez. di Roma

Introduction

The Unitarity Triangle in the Standard Model and beyond

Flavour physics beyond the Standard Model:

Minimal Flavour Violation

Extra dimensions

Beyond MFV:

general SUSY models, SUSY GUT's UTfit coll., hep-ph/0605213

UTfit coll., in progress

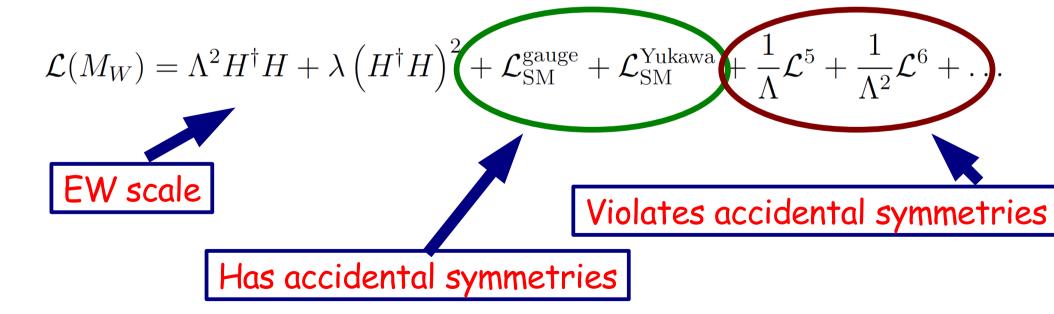
M. Ciuchini et al., in progress

R. Contino & L.S., in progress

Conclusions

INTRODUCTION

The Standard Model works beautifully up to a few hundred GeV's, but it must be an effective theory valid up to a scale $\Lambda \leq M_{planck}$:



THE HIERARCHY PROBLEM

- $m_{EW}(10^2) \leftrightarrow M_{PI}(10^{19}), M_{GUT}(10^{15})$ (in GeV)
 - 1. Supersymmetry: $m_{EW} \sim \Lambda = m_{SUSY} \leftrightarrow M_{PI}$ Bonus: Grand Unification, Dark Matter
 - 2. Warped extra-dims (gauge-Higgs unification): $m_{EW} \sim \Lambda = m_{KK} \leftrightarrow M_{pl}$
- Expect New Physics close to the electroweak scale!

HOW TO PROBE NEW PHYSICS: I. ELECTROWEAK SYMMETRY BREAKING

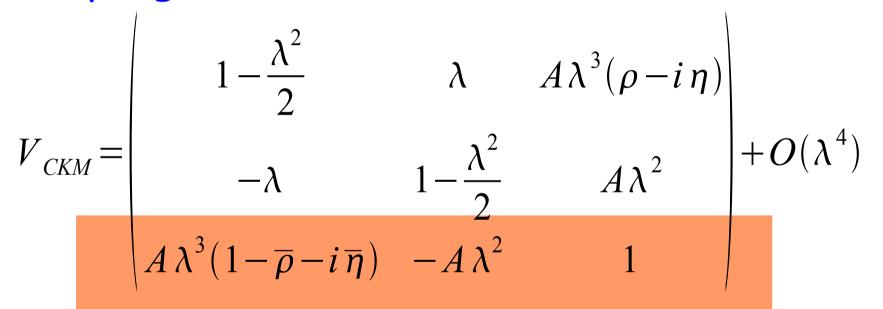
- How can we explore NP with processes involving only SM particles?
- I. Electroweak gauge symmetry spontaneously broken
 - tree-level relations between EW observables (masses, couplings, ...)
 - quantum corrections computable and sensitive to higher-dim operators
 - ⇒ The LEP glorious legacy of precision EW fits:
 ∧ > 2-10 TeV!!

HOW TO PROBE NEW PHYSICS: II. FLAVOUR PHYSICS

- Three flavours of fermions with same gauge quantum numbers but different mass.
- Flavour eigenstates are not weak interaction eigenstates
 - \Rightarrow weak interactions change flavour
- Accidental symmetry of the SM: Neutral current weak interactions conserve flavour!
- quantum corrections computable and sensitive to higher-dim operators

EXPRESS REVIEW OF THE SM

• All flavour violation from charged current coupling: CKM matrix V



• Top quark exchange dominates FCNC loops: third row (V_{tq}) determines FCNC's $\leftrightarrow \bar{\rho}, \bar{\eta}$

Flavour summarized on the $p-\eta$ plane

CC

CC

CC

CC

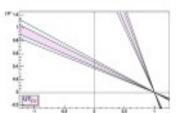
CC

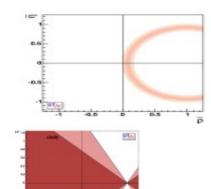
NC

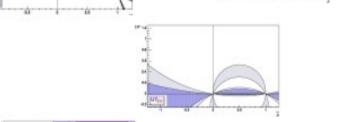
CC/NC

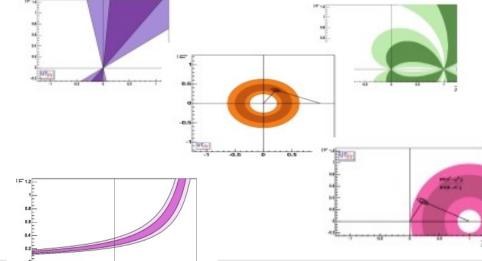
- BR(b \rightarrow clv), BR(B \rightarrow D^(*)lv)
- BR(b \rightarrow ulv), BR(B \rightarrow \pilv)
- Δm_a (B_a-B_a mass diff.) NC
- $A_{CP}(b \rightarrow c\overline{c}s) (J/\psi K, ...)$
- $A_{co}(b \rightarrow s\overline{s}s, dds) (\phi K, \pi K, ...)$ NC
- $A_{CP}(b \rightarrow d\overline{d}d, u\overline{u}d) (\pi\pi, \rho\rho, ...)$
- $BR(b \rightarrow c\overline{u}d, c\overline{u}s)$ (DK, ...)
- $BR(B \rightarrow \tau v)$
- $BR(B \rightarrow \rho \gamma)/BR(B \rightarrow K^* \gamma)$
- NC ε_{μ} (CP violation in K mixing) Napoli, 26/5/20...







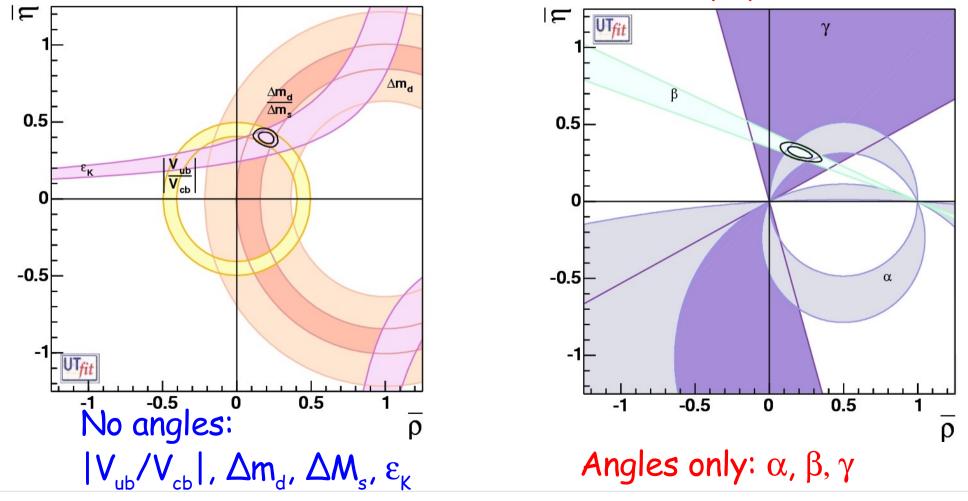




Luca Silvestrini

Progress of the UT analysis

End of parameter determination era, begin of precision test era: redundant determination of the triangle with new measurements from B-factories and Tevatron and test of new physics.



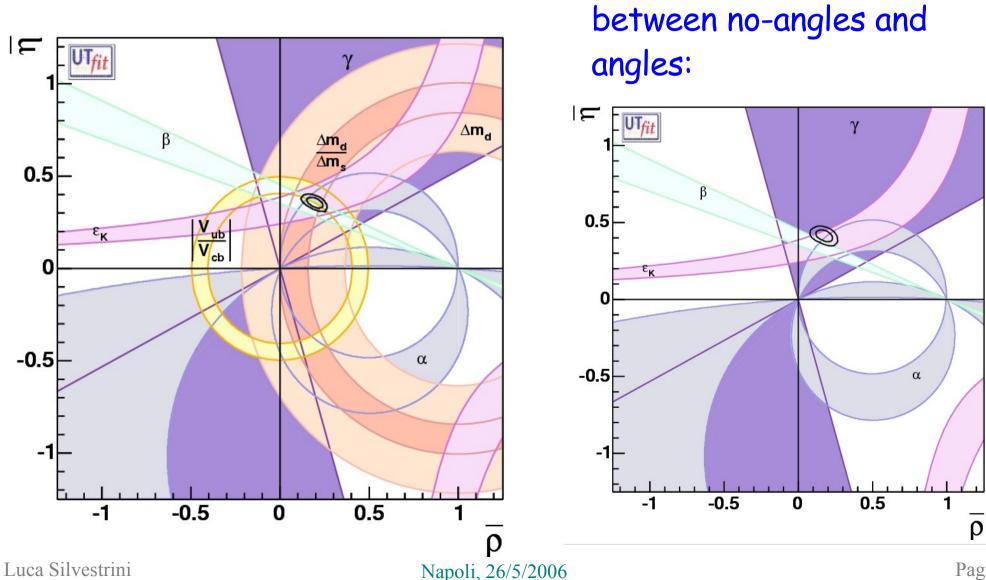
Luca Silvestrini

Napoli, 26/5/2006

Progress of the UT analysis - II

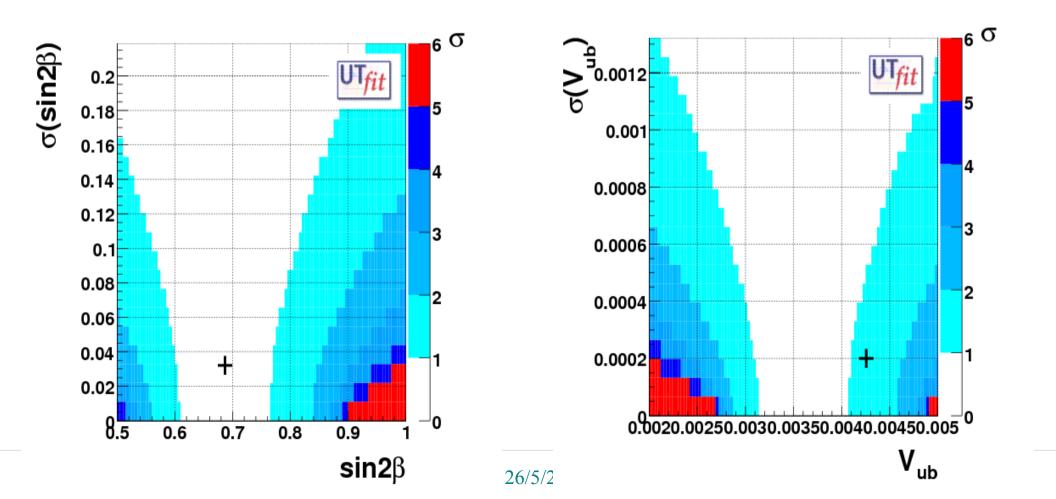
Slight disagreement

Putting it all together:



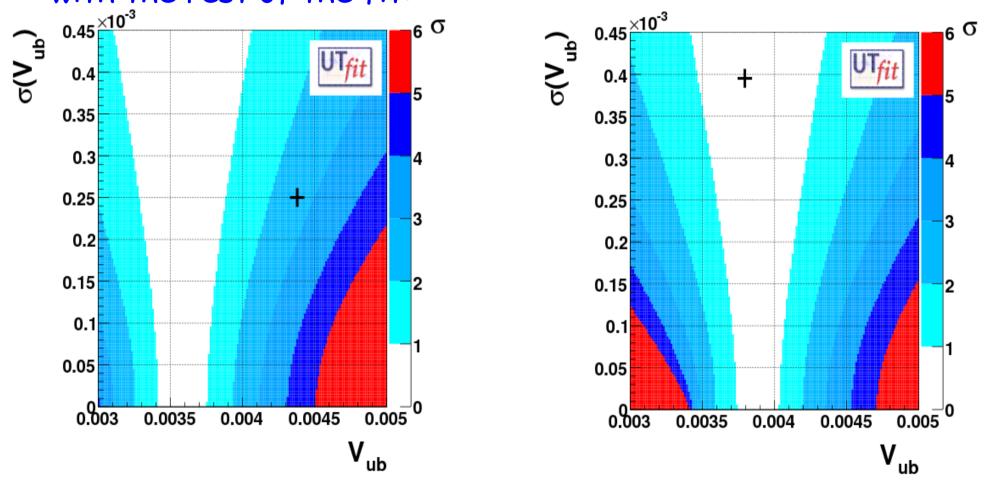
Progress of the UT analysis - III

Where does the difference come from? Test the compatibility of sin2b and Vub with the rest of the fit:



Progress of the UT analysis - IV

Test the compatibility of inclusive Vub and exclusive Vub with the rest of the fit:



A problem with the determination of V_{ub} from inclusive decays?

HOW DOES NP MODIFY FLAVOUR?

- Standard Model:
 - CKM matrix only, loop level only
 - GIM suppression ~ $(m_{qi}^2 m_{qj}^2)/m_W^2$
- Minimal Flavour Violation, Minimal SUGRA:
 - same as above
- General MSSM:
 - New sources of flavour & CPV, loop level only
 - Super-GIM suppression ~ $(m_{sqi}^2 m_{sqj}^2)/m_{gl}^2$
- Extra Dimensions:
 - New sources of flavour & CPV, tree-level
 - Mass suppression ~ m_q/m_{KK}

A strategy for New Physics:

- 1. Add most general NP to all sectors
- 2. Use all available info
- 3. Constrain simultaneously ρ,η and NP contributions

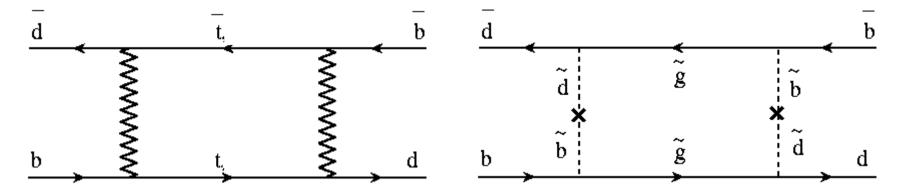
Only possible thanks to the new measurements of CKM angles Recent info on Δm_s , $\Delta \Gamma_s / \Gamma_s$, leptonic asymmetries allows to

constrain NP in b \rightarrow s transitions

Will become the standard fit in the near future!

Utfit coll., hep-ph/0605213. See also Ligeti et al., hep-ph/0604112; Grossman et al, hep-ph/0605028. Previous attempts: Ciuchini et al., hep-ph/0307195; CKMfitter group, hep-ph/0406184; Ligeti, hep-ph/0408267; Botella et al., hep-ph/0502133; Agashe et al., hep-ph/0509117; UTfit coll., hep-ph/0509219.

General parametrization of the mixing amplitudes



Mixing amplitude = SM contribution + NP contribution

$$A_q^{\text{full}} = A_q^{\text{SM}} e^{2i\phi_q^{\text{SM}}} + A_q^{\text{NP}} e^{2i(\phi_q^{\text{SM}} + \phi_q^{\text{NP}})} = C_{B_q} e^{2i(\phi_q^{\text{SM}} + \phi_{B_q})} A_q^{\text{SM}}$$

$$(\Delta m_q) = |A_q^{\text{full}}| = C_{B_q} (\Delta m_q)^{\text{SM}} \qquad \frac{\Delta \Gamma_q}{\Delta m_q} = \text{Re} \left(\frac{\Gamma_{12}^q}{A_q^{\text{full}}}\right)$$

$$A_{CP} (J/\Psi K_S) = \sin \arg(A_d^{\text{full}}) = \sin 2(\beta + \phi_{B_d})$$

$$A_{CP} (J/\Psi \phi) = -\sin \arg(A_s^{\text{full}}) = \sin 2(\beta_s - \phi_{B_s})$$

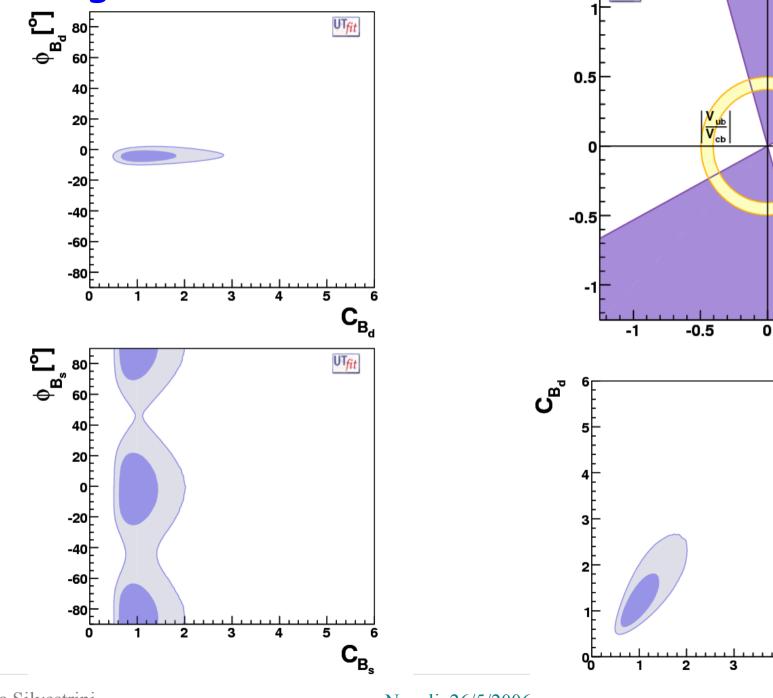
$$A_{\text{SL}} = \frac{\Gamma(\bar{B}^0 \to \ell^+ X) - \Gamma(B^0 \to \ell^- X)}{\Gamma(\bar{B}^0 \to \ell^- X)} = \text{Im} \left(\frac{\Gamma_{12}^d}{A_d^{\text{full}}}\right) \qquad A_{\text{CH}} \equiv \frac{N(\ell^+ \ell^+) - N(\ell^- \ell^-)}{N(\ell^+ \ell^+) + N(\ell^- \ell^-)}$$

Napoli, 26/5/2006

NP parameters & exp constraints

- Angle measurements determine ρ,η and ϕ_d up to an ambiguity of 180°
- $\Delta m_{d} \& \Delta m_{s} fix C_{Bd} \& C_{Bs}, \varepsilon$ determines C_{ε}
- $\Delta \Gamma_s / \Gamma_s$ constrains ϕ_s
- A_{_{SL}} and A_{_{CH}} suppress the "wrong" solution in the $\rho-\eta$ plane
- $\Delta\Gamma_{\rm d}/\Gamma_{\rm d}$ improves the constraint on $\phi_{\rm d}$

•Using all constraints:



Luca Silvestrini

Napoli, 26/5/2006

ľ

UT_{fit}

γ

0.5

UTfit

 $\mathbf{C}_{\mathbf{B}_{\mathbf{s}}}$

5

4

1

p

summary of constraints

Parameter	Output	Parameter	Output
C_{B_d}	1.17 ± 0.39	$\phi_{B_d}[^\circ]$	-4.2 ± 2.1
C_{B_s}	0.97 ± 0.27	$\phi_{B_s}[^\circ]$	$(-2 \pm 15) \cup (93 \pm 15)$
C_{ϵ_K}	0.95 ± 0.18		
$\overline{\rho}$	0.24 ± 0.06	$\overline{\eta}$	0.37 ± 0.04
$\alpha[^{\circ}]$	96 ± 9	$\beta[^\circ]$	26 ± 2
$\gamma[^{\circ}]$	57 ± 9	$\mathrm{Im}\lambda_{\mathrm{t}}[10^{-5}]$	14.9 ± 1.6
$V_{ub}[10^{-3}]$	4.27 ± 0.20	$V_{cb}[10^{-2}]$	4.15 ± 0.07
$V_{td}[10^{-3}]$	7.9 ± 0.6	$\left V_{td}/V_{ts}\right $	0.194 ± 0.016
R_b	0.44 ± 0.02	R_t	0.85 ± 0.07
$\sin 2\beta$	0.788 ± 0.035	$\sin 2\beta_s$	0.040 ± 0.004

 $\phi_{Bd} \neq 0 @ 2 \sigma$ because of the tension in the SM fit. Need more statistics + check of incl V_{ub}

THE LESSON OF THE UT ANALYSIS

New Physics in $\Delta B=2$ and $\Delta S=2$ can be up to ~50% of the SM only if NP has the same phase of the SM, otherwise it has to be at most ~ 20%. **This is a completely general result.** In the following, we will see what is the implication of this statement for various new physics models.

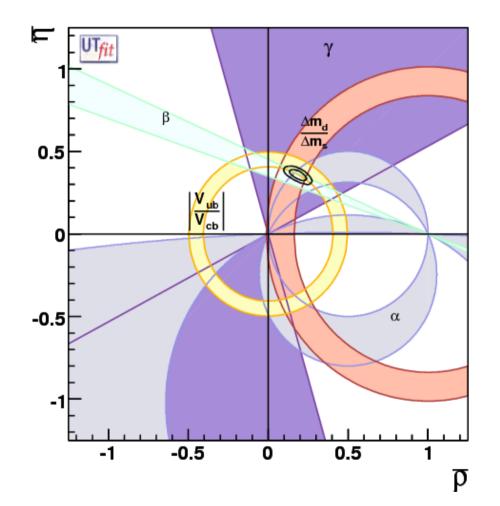
MINIMAL FLAVOUR VIOLATION

Gabrielli, Giudice, NPB433; Buras et al., PLB500; D'Ambrosio et al., NPB 645; Bobeth et al., hep-ph/0505110

 No new source of flavour and CP violation NP contributions also governed by Yukawas NP only modifies SM top contribution to FCNC & CPV
 One Higgs or small/moderate tanβ No new operators, full correlations among K & B decays
 Large tanβ New operators, less correlations among K & B decays

The Universal Unitarity Triangle

Buras et al., PLB500 Angle measurements + $\Delta M_d / \Delta M_s$ unaffected by NP in MFV



valid in any MFV model for any value of $tan\beta$

CONSTRAINTS ON MFV SCALE A

D'Ambrosio et al., NPB645

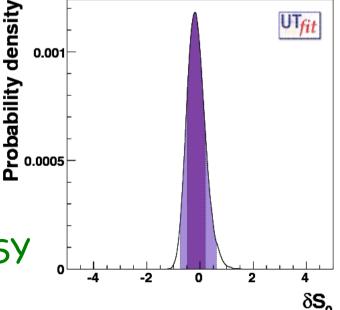
MFV models with one Higgs doublet or 2HD @ low/moderate tanß: Universal NP effect in the ΔF =2 Inami-Lim function of the top

$$\begin{aligned} \mathcal{H}_{\text{eff}}^{\Delta F=2} &= \mathcal{H}_{\text{SM}} + \mathcal{H}_{\text{NP}} = \left(V_{tq} V_{tq'}^* \right)^2 \left(\frac{S_0(x_t)}{\Lambda_0^2} + \frac{a_{\text{NP}}}{\Lambda^2} \right) \left(\bar{q}' q \right)_{(V-A)} \left(\bar{q}' q \right)_{(V-A)} \\ S_0(x_t) &\to S_0(x_t) + \delta S_0, \quad \left| \delta S_0 \right| = O\left(4 \frac{\Lambda_0^2}{\Lambda^2} \right), \quad \Lambda_0 = \frac{\pi Y_t}{\sqrt{2}G_F M_W} \sim 2.4 \text{ TeV} \end{aligned}$$

We can bound NP effective scale Λ :

 Λ > 5.7 TeV @95% prob. for positive δS_0

Notice: strong int. $\Rightarrow \Lambda \sim M$ (mass of new particles), weak int. $\Rightarrow \Lambda >> M ! Ex. SM, SUSY$



UPPER BOUNDS ON RARE DECAYS IN MFV

Bobeth et al., NPB726

Branching Ratios	MFV (95%)	SM (68%)	SM (95%)	exp
$Br(K^+ \to \pi^+ \nu \bar{\nu}) \times 10^{11}$	< 11.9	8.3 ± 1.2	[6.1, 10.9]	$(14.7^{+13.0}_{-8.9})$ [19]
$Br(K_{\rm L} \to \pi^0 \nu \bar{\nu}) \times 10^{11}$	< 4.59	3.08 ± 0.56	[2.03, 4.26]	$< 5.9 \cdot 10^4 \; [37]$
$Br(K_{\rm L} \to \mu^+ \mu^-)_{\rm SD} \times 10^9$	< 1.36	0.87 ± 0.13	[0.63, 1.15]	-
$Br(B \to X_s \nu \bar{\nu}) \times 10^5$	< 5.17	3.66 ± 0.21	[3.25, 4.09]	< 64 [38]
$Br(B \to X_d \nu \bar{\nu}) \times 10^6$	< 2.17	1.50 ± 0.19	[1.12, 1.91]	-
$Br(B_s \to \mu^+ \mu^-) \times 10^9$	< 7.42	3.67 ± 1.01	[1.91, 5.91]	$< 2.7 \cdot 10^2$ [39]
$Br(B_d \to \mu^+ \mu^-) \times 10^{10}$	< 2.20	1.04 ± 0.34	[0.47, 1.81]	$< 1.5 \cdot 10^3 \ [39]$

In MFV models (at low/moderate tan β) rare decays can be only slightly enhanced w.r.t the SM. Strong suppressions still possible at present.

THE MSSM

- In the MSSM, two classes of contributions to FCNC's:
 - Supersymmetrization of SM contributions $(W \rightarrow \tilde{w}, t \rightarrow \tilde{t}) + H^{\pm}$: also present in MFV
 - pure SUSY contributions: g̃ q̃: requires new sources of flavour violation in squark mass matrices

Hall, Kostelecky & Raby; Gabbiani et al.

THE MSSM W. MFV @ LARGE tanß

Isidori & Paradisi, hep-ph/0605012

- Consider the MSSM with MFV at very large tanß and squark masses at the TeV scale
- Only relevant contribution to FCNC from Higgs exchange
- Main effects: small suppression of Δm_s and of BR(B $\rightarrow \tau v$), enhancement of BR(B_s $\rightarrow \mu \mu$)
- Interesting scenario, need more data...

THE GENERAL MSSM

Ciuchini et al., in progress, Preliminary

- We consider a MSSM with generic soft SUSY-breaking terms, but
 - dominant gluino contributions only
 - mass insertion approximation

Think of δ 's as SUSY equivalent of CKM mixing

four insertions AB=LL, LR, RL, RR

CONSTRAINTS ON δ 's

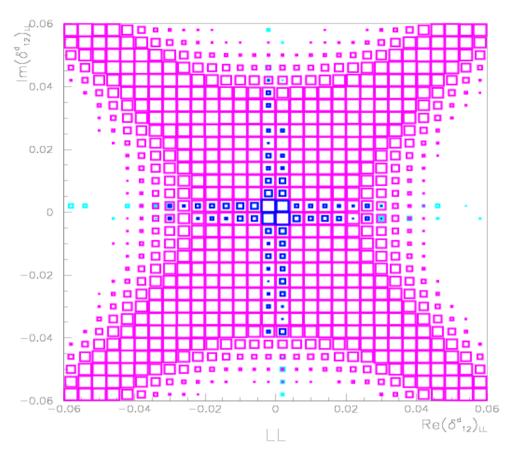
• $\binom{d_{12}}{\Delta B}_{AB}$ constraints from Δm_{k} & ε_{k} • $\binom{d_{13}}{AB}$ contribute to B mixing: AB constraints from $\Delta m_{\rm B}$ & sin2 β • $\binom{d}{\delta^{23}}_{ABb}$ - s decays:

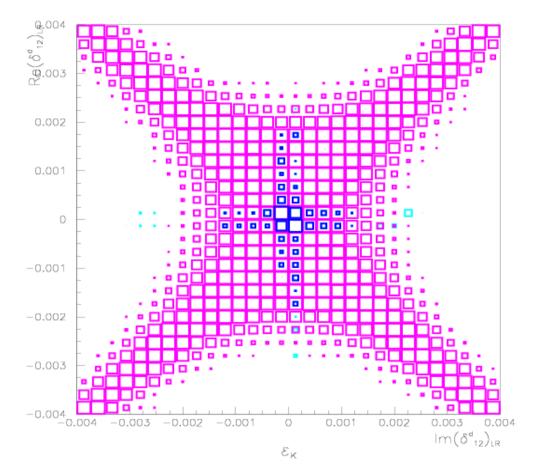
constraints from $\Delta m_{_{Bs}}$, b $\rightarrow s\gamma$, b $\rightarrow sl^+l^-$

• for reference, choose $m_{al} = m_{sq} = 350 \text{ GeV}$

Re $(\delta^{d}_{12})_{LL,RR}$ vs Im $(\delta^{d}_{12})_{LL,RR}$

Re $(\delta^{d}_{12})_{LR,RL}$ vs Im $(\delta^{d}_{12})_{LR,RL}$



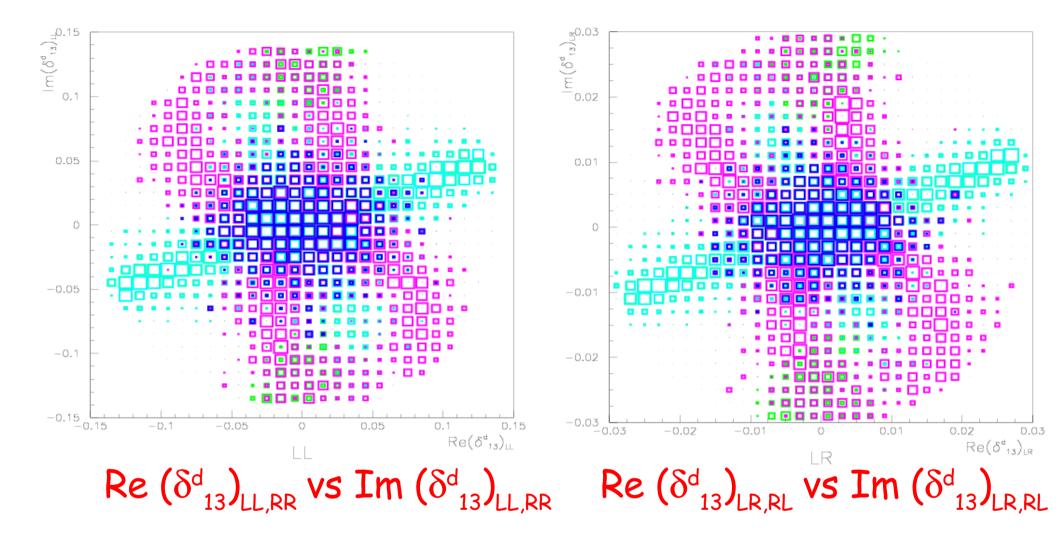


 Δm_{k} only ϵ_{k} only Δm_{k} and ϵ_{k}

Full NLO analysis, including recently computed NLO corrections to the matching (Ciuchini et al., to appear soon)

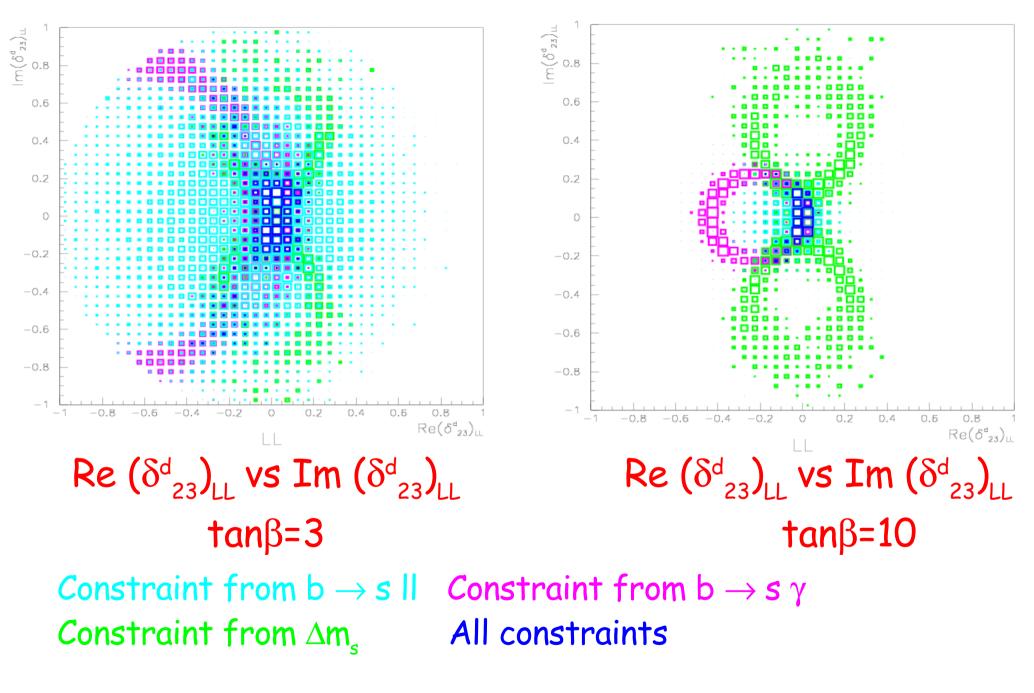
Luca Silvestrini

Napoli, 26/5/2006

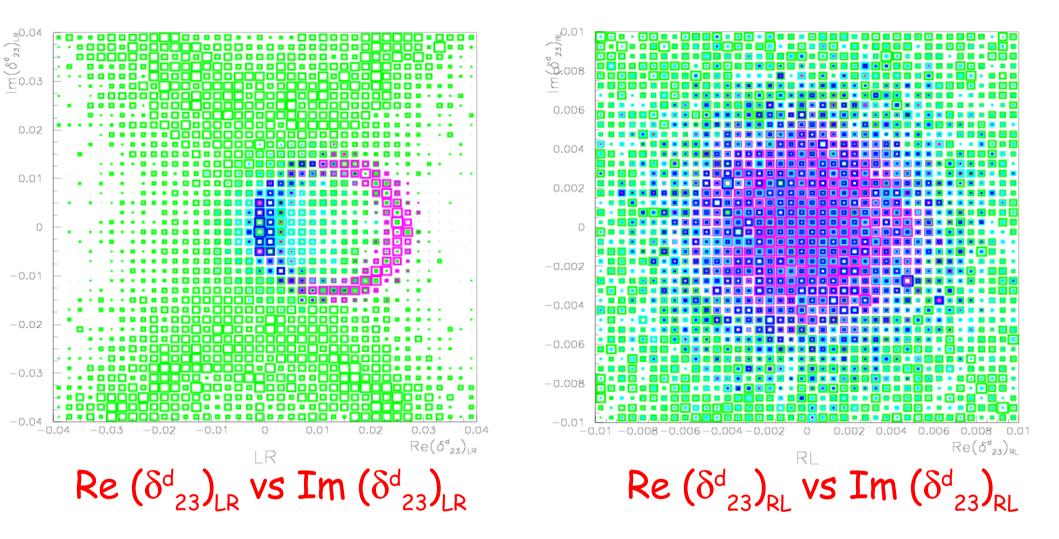


 Δm_{B} only sin 2 β only

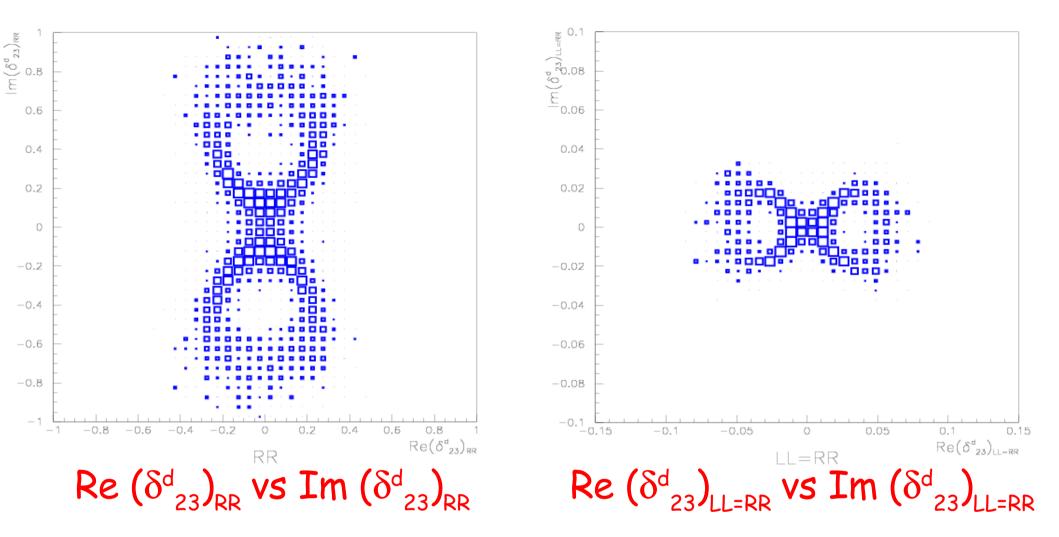
sin 2β and cos 2β All constraints



Contribution to $b \rightarrow s$ decays grows with tan β



LR & RL dominated by BR(b \rightarrow s γ) & BR(b \rightarrow s I⁺I⁻) RL does not interfere with the SM



LL & LL=RR dominated by CDF measurement of Δm_s

THE SUSY FLAVOUR PROBLEM

$\left(\delta^d_{12}\right)$	LL,RR	$\left(\delta^d_{12}\right)$	LR,RL	$\left(\delta^d_{13}\right)$	LL,RR	$\left(\delta^d_{13}\right)_I$	LR,RL
${\rm Re}$	Im	${\rm Re}$	Im	${\rm Re}$	Im	${\rm Re}$	Im
410^{-2}	410^{-2}	210^{-3}	210^{-3}	10^{-1}	510^{-2}	210^{-2}	10^{-2}
$\left(\delta^d_{23}\right)$	$\left(LL \right)_{LL}$	$\left(\delta^d_{23}\right)$	$\Big)_{RR}$	$\left(\delta^d_{23}\right)$	$\left(\right)_{LR}$	$\left(\delta^d_{23}\right)$	$\Big)_{RL}$
$\frac{\left(\delta^d_{23}\right)}{\text{Re}}$	$\left(\int_{LL} \right)_{LL}$	$\frac{\left(\delta^d_{23}\right)}{\text{Re}}$	$\Big)_{RR}$ Im	$\left(\delta^d_{23} \right)$ Re	$\left(\int_{LR} \right)_{LR}$	$\frac{\left(\delta^d_{23}\right)}{\text{Re}}$	$\Big)_{_{RL}}$ Im

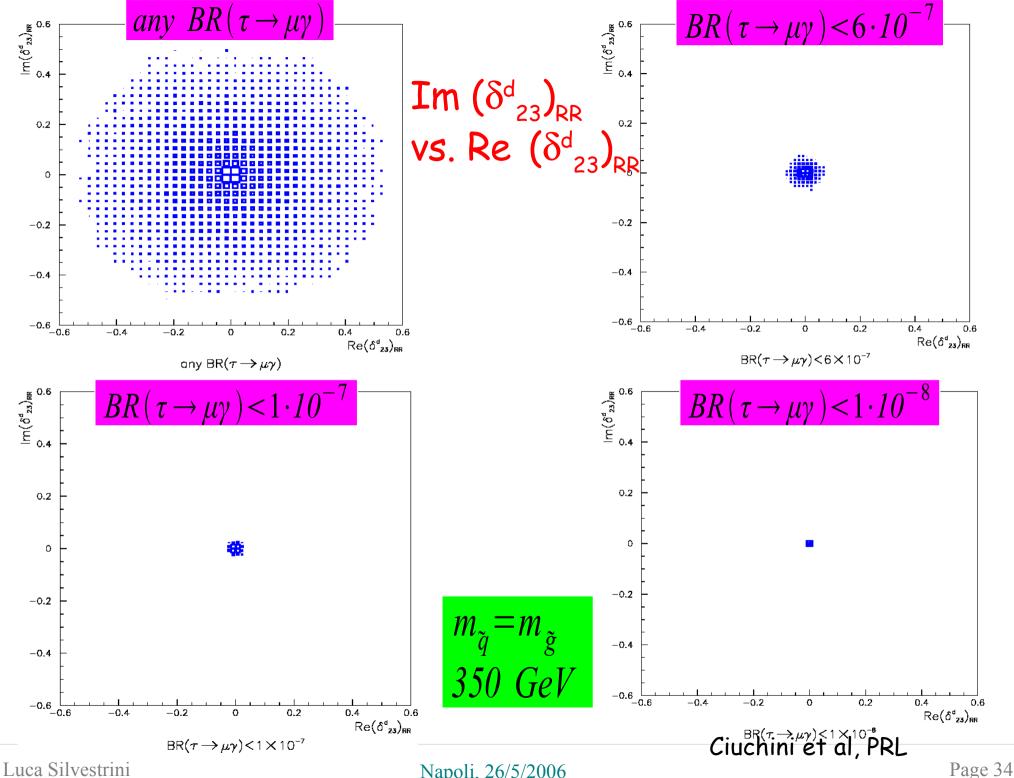
- Strong constraints on SUSY breaking mechanism:
 - -Flavour-universal breaking?
 - -Flavour symmetry?

SUSY-GUTs

- In an SU(5)-like GUT, quark and leptons are unified, so also squark and sleptons.
- After running down to weak scale, one has:

	Relations at weak scale	Additional Conditions at M_{GUT}
(1)	$(\delta^{u}_{ij})_{RR} \approx (m^{2}_{e^{c}}/m^{2}_{u^{c}}) \; (\delta^{l}_{ij})_{RR}$	$m_{u^c}^2(0) = m_{e^c}^2(0)$
(2)	$(\delta^q_{ij})_{LL} \approx (m_{e^c}^2/m_Q^2) \ (\delta^l_{ij})_{RR}$	$m_Q^2(0) = m_{e^c}^2(0)$
(3)	$(\delta^d_{ij})_{RR} \approx (m_L^2/m_{d^c}^2) \; (\delta^l_{ij})_{LL}$	$m_{d^c}^2(0) \ = \ m_L^2(0)$
(4)	$(\delta^d_{ij})_{LR} \approx (m^2_{L_{avg}}/m^2_{Q_{avg}}) (m_b/m_{\tau}) (\delta^l_{ij})^{\star}_{LR}$	$A^e_{ij} = A^d_{ji}$

Correlations between quark & lepton FCNC!



Napoli, 26/5/2006

EXTRA DIMENSIONS

- Combine two ideas:
 - Gauge-Higgs unification: $h = A_5$
 - 5D gauge invariance protects the Higgs mass
 - Higgs interactions are (5D) gauge interactions
 - Higgs mass is calculable Manton; Hosotani; Czacki et al; Scrucca et al.
 - Warped spacetime
 - Planck scale gets redshifted to the TeV: solution to the hierarchy problem
 Randall-Sundrum; Agashe et al.

FERMION MASSES

Scrucca, Serone & LS; Agashe, Contino & Pomarol; ...

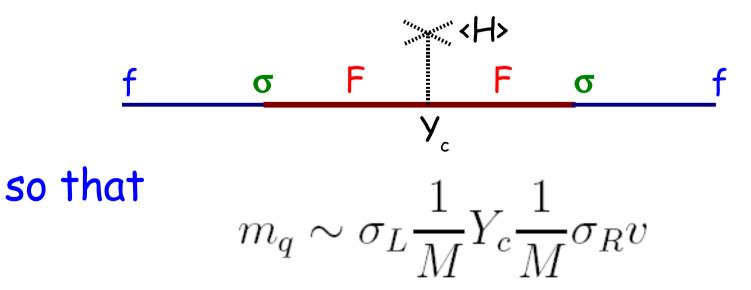
- In Gauge-Higgs unification, fermion masses come from gauge interactions in the bulk
- To obtain flavour structure, flavours must have different wave functions:
- In 5D language: Light fermions localized, heavy fermions in bulk
- In effective theory language: Light fermions elementary, heavy fermions composite

A GENERAL LAGRANGIAN

 Fermion interactions in extra-dim(-like) models:

$$\mathcal{L}_{\text{ferm}} = \bar{f}\sigma F + M\bar{F}F + Y_c\bar{F}HF + g_c\bar{F}GF$$

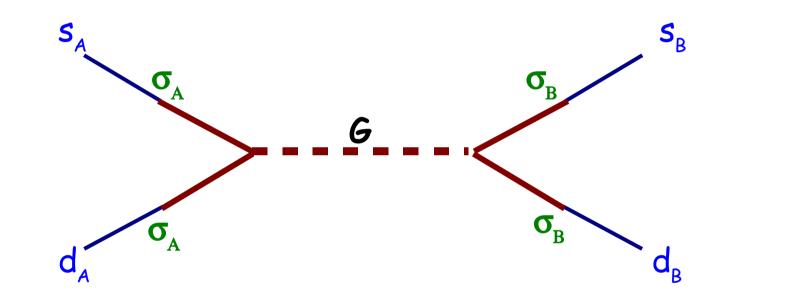
SM fermion masses are given by



$\Delta F=2 PROCESSES$

Contino & L.S., in progress - Preliminary

• The relevant Feynman diagram is



$$\mathcal{H}_{\text{eff}} \sim \left(\bar{s}_A \sigma_A \frac{1}{M} g_c T^A \gamma_\mu \frac{1}{M} \sigma_A d_A\right) \left(\bar{s}_B \sigma_B \frac{1}{M} g_c T^A \gamma^\mu \frac{1}{M} \sigma_B d_B\right) \frac{1}{m_{KK}^2}$$

$\Delta F=2 PROCESSES: RESULTS$

• Expressing the unknown couplings and masses in terms of quark masses and mixing angles, we obtain, for A=L and B=R,

$$\varepsilon_K \sim 14 \varepsilon_K^{\exp} \left(\frac{g_c}{Y_c}\right)^2 \left(\frac{3 \text{TeV}}{m_{KK}}\right)^2$$

assuming that CP violating phases are of O(1) All other Δ F=2 processes are below 20% $\varepsilon_{\rm K}$ requires m_{KK} ~ 10 TeV and/or $g_c/Y_c \sim 1/3$ stronger than precision EW constraints

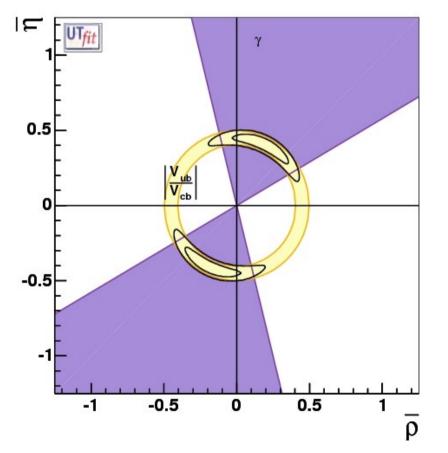
CONCLUSIONS

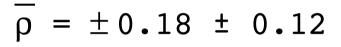
- Flavour physics is a powerful probe of new physics
- Sensitive to scales much higher than m_{FW}:
 - -mechanism of SUSY breaking
 - -grand unification structure
- Very constraining also for extra dimensions
- LHC-flavour complementarity to explore NP in the near future

BACKUP SLIDES

THE REFERENCE UT

Assumptions: (1) 3-generations unitarity (2) no new physics in tree-level processes Using only tree-level: γ and $|V_{ub}/V_{cb}|$. Results:





$$\overline{\eta}$$
 = ±0.41 ± 0.05

 $sin2\beta = 0.782 \pm 0.065$ -0.641 ± 0.087

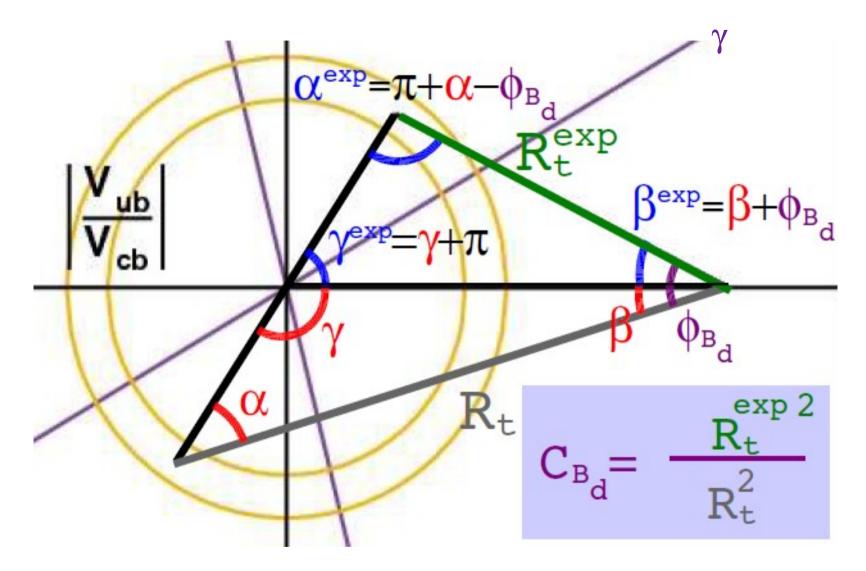
$$\gamma = (65\pm18)^{\circ} \text{ U} (-115\pm18)^{\circ}$$

 $\alpha = (87\pm15)^{\circ} U (-46\pm15)^{\circ}$

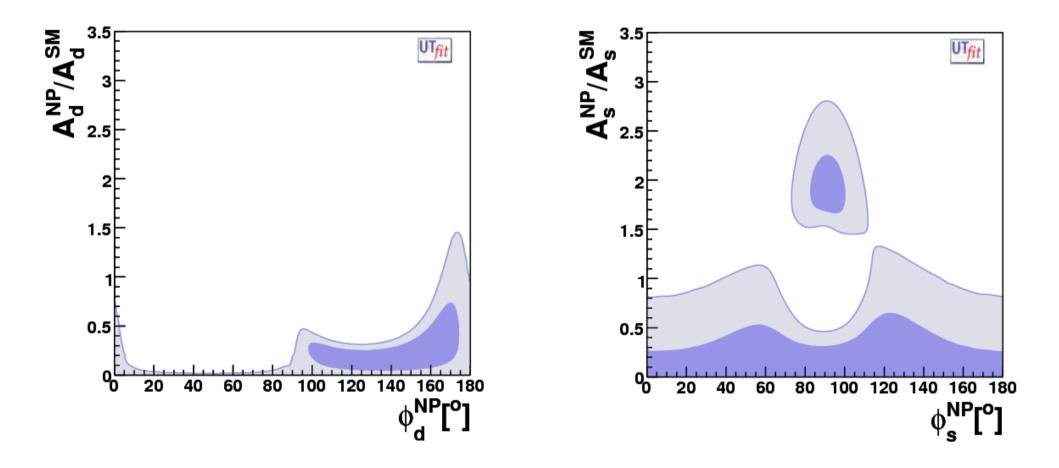
Any model of new physics must satisfy these constraints

UTfit coll., hep-ph/0501199; Botella et al., hep-ph/0502133

UT constraints in the presence of NP

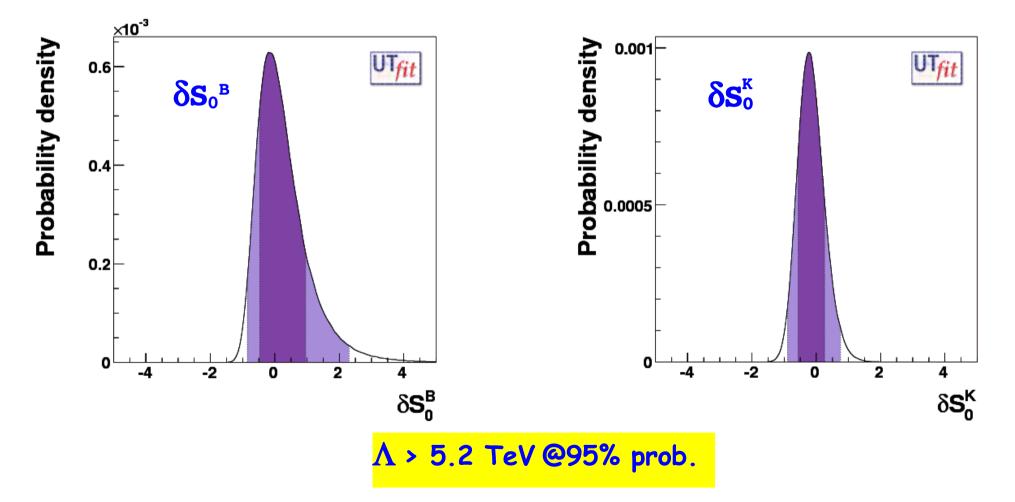


Another look at NP in B_q mixing



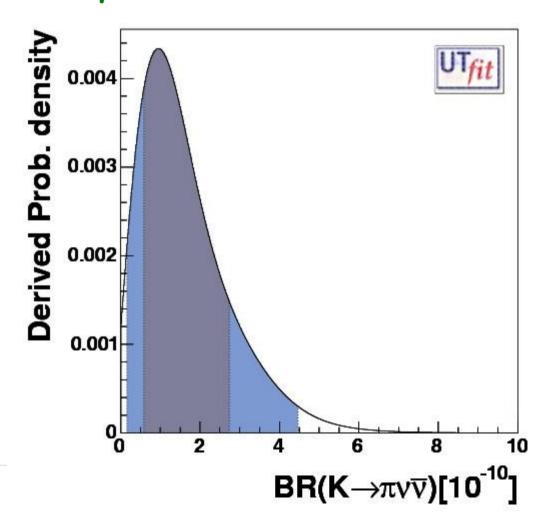
 $2H + large \tan\beta$: terms proportional to the bottom Yukawa coupling are enhanced and cannot be neglected any more

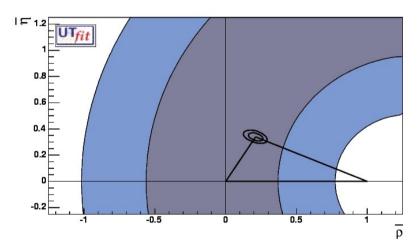
$$\delta S_0^B \neq \delta S_0^K$$



A COMMENT ON BR(K⁺ $\rightarrow \pi^+ \nu \nu$)

The experimental pdf is peaked at the SM prediction:





SM prediction (not using exp): $(8.3 \pm 1.2) 10^{-11}$

RARE DECAYS IN MFV

- What are the constraints on MFV from rare decays?
- What are the predictions for yet unmeasured rare decays? Where could we see effects of MFV? How can we test MFV?

Identify leading NP contributions:

1) dimension 4 operators: FCNC effective Z vertex

$$\Rightarrow C = C_{SM} + \Delta C$$

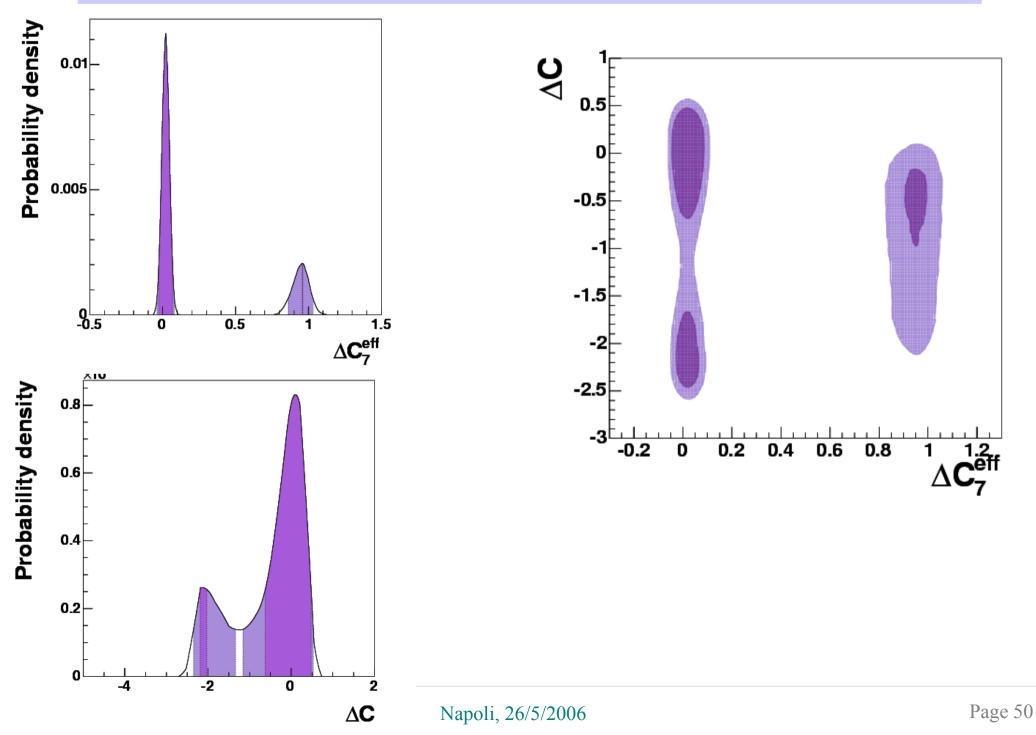
2) dimension 5 operators: (chromo)magnetic penguin $\Rightarrow C_7^{eff} = (C_7^{eff})_{SM} + \Delta C_7^{eff}$

3) dimension 6 operators: penguins, boxes \Rightarrow subleading NP contributions to rare decays Rare decays \Leftrightarrow SM functions(m_t) + ΔC , ΔC_7^{eff} Model-independent analysis in terms of ΔC , ΔC_7^{eff} Can be refined in specific MFV models (ex. CMSSM)

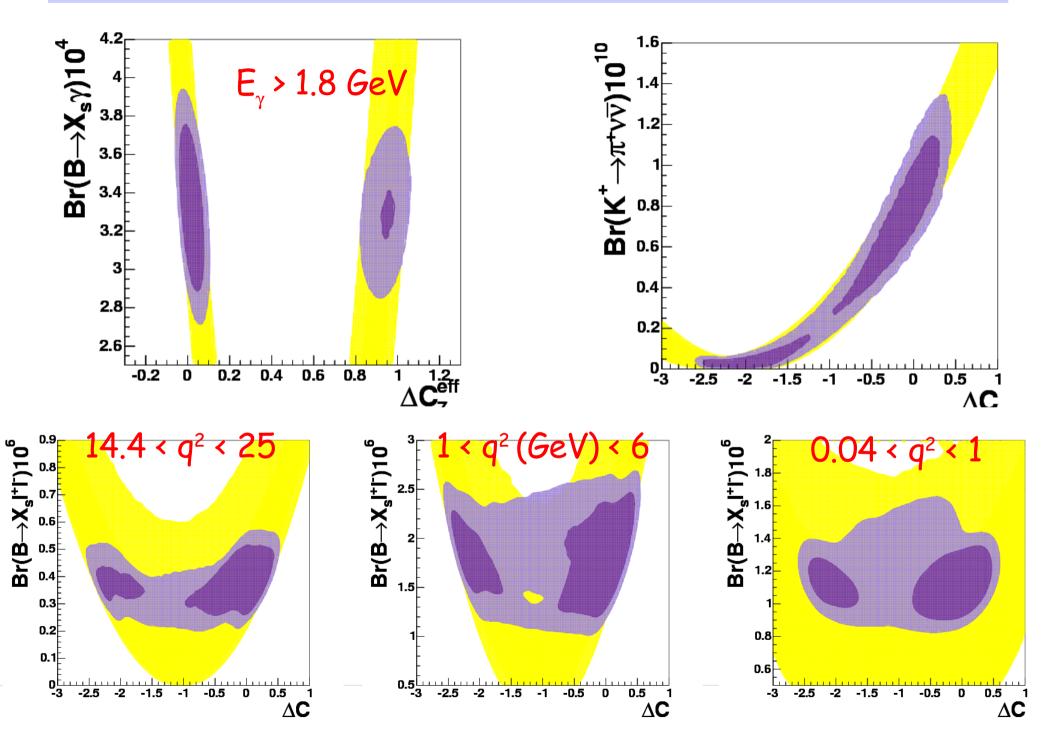
MFV GENERAL ANALYSIS

- ρ,η from the UUT analysis
- ΔC_7^{eff} can be constrained using BR(B $\rightarrow X_s \gamma$)
- ΔC can be constrained using BR(B $\rightarrow X_s l^+ l^-$) and BR(K⁺ $\rightarrow \pi^+ vv$)
- Get predictions for all other rare decays

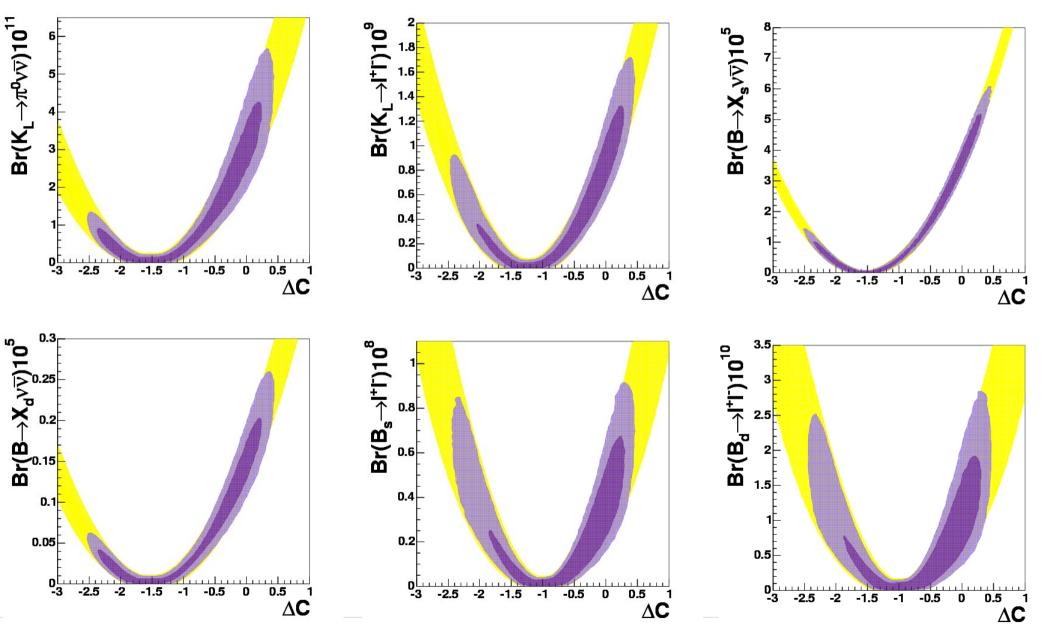
CONSTRAINTS ON NP



NP CONTRIBUTIONS vs EXP CONSTRAINTS



PREDICTIONS FOR RARE DECAYS



Luca Silvestrini

Napoli, 26/5/2006