

*An alternative road to LHC physics:  
Improved naturalness with a heavy Higgs*

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Preliminary considerations

The Inert Doublet Model

# Particle Physics in one page

$$\mathcal{L}_{\sim SM} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + i\bar{\psi}D\psi \quad \text{The gauge sector (1)}$$

$$+ \psi_i \lambda_{ij} \psi_j h + h.c. \quad \text{The flavor sector (2)}$$

$$+ |D_\mu h|^2 - V(h) \quad \text{The EWSB sector (3)}$$

$$+ N_i M_{ij} N_j \quad \text{The } \nu\text{-mass sector (4)} \\ \text{(if Majorana)}$$

*(1) : best tested quantitatively*

*(2) + (4) : main developments of last 5 years,  
different in nature, both highly significant*

*(3): the most elusive, so far*

# What will replace current Page 1?

## *1. The best theoretical candidate:*

### ***Unification + supersymmetry***

*(as developed in the 70's/80's)*

Pros

gauge unification  
size of neu-masses

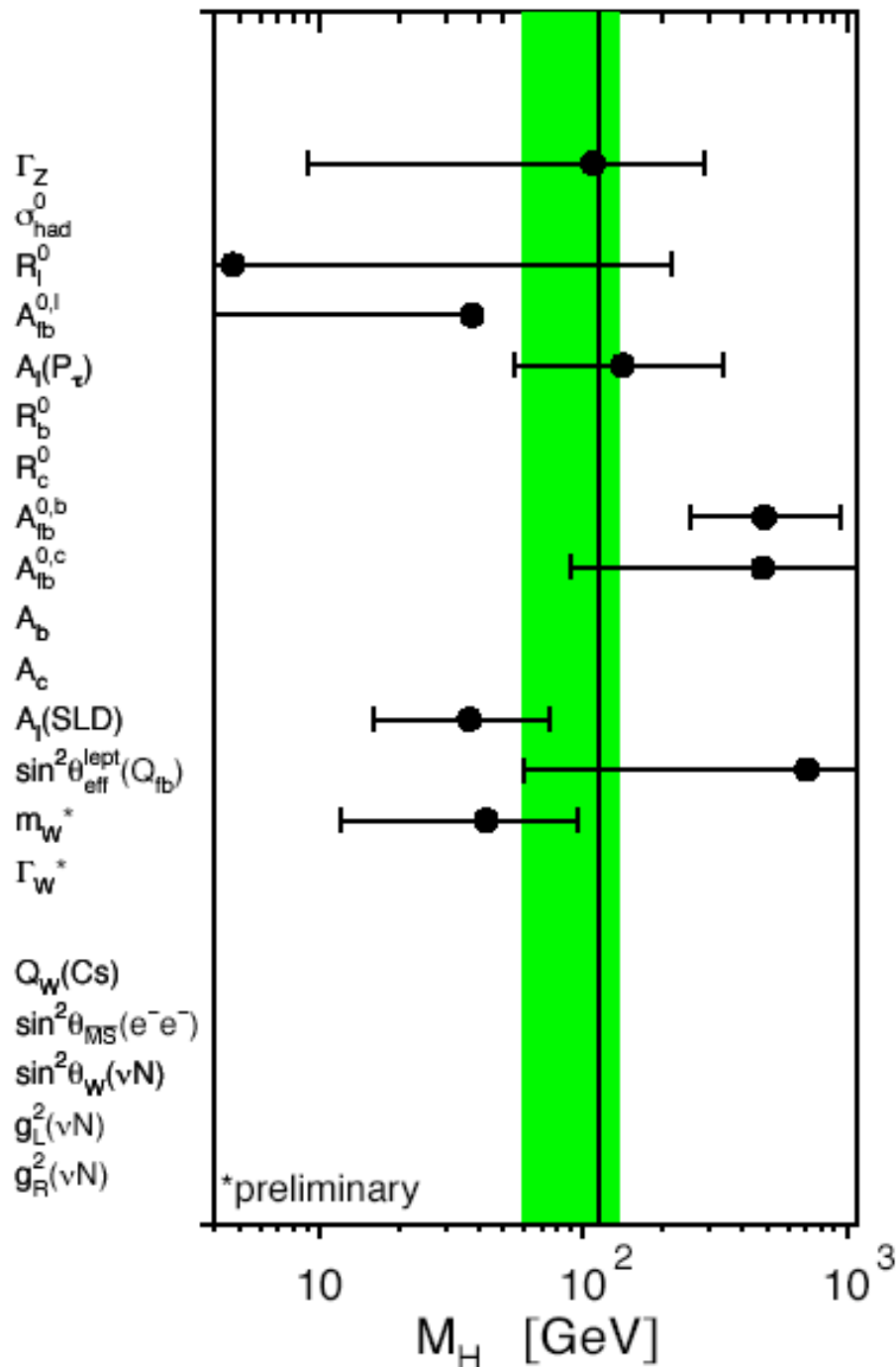
Contras

No susy particles  
No flavour effects  
No proton decay  
No light Higgs

so far!?

## *2. Experiments should tell, with LHC playing not the least role*

# The physics of Electroweak breaking



A  $\Rightarrow$  a light Higgs

B from the top loop correction to the Higgs potential

$$m_h^2 = \frac{3\lambda_t^2}{4\pi^2} \Lambda_t^2 \pm m_0^2$$

$$\Lambda_t \approx 400 \text{ GeV} \left( \frac{m_h}{115 \text{ GeV}} \right) D_t^{1/2}$$

What is the related, apparently necessary, new physics?

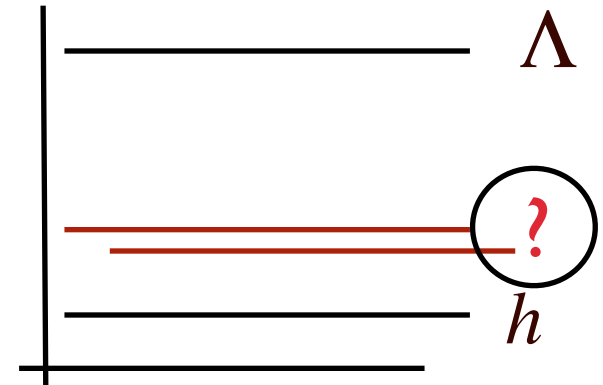
How can  $\Lambda_t$  be so low without disturbing agreement with exps?

the “LEP paradox”

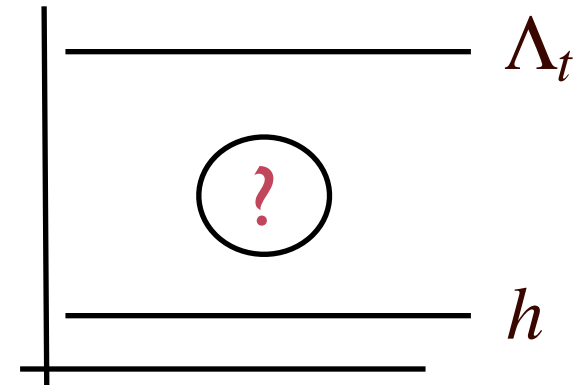
the “little hierarchy problem”

2 (or 3) different ways to go  
(crucially different for the LHC)

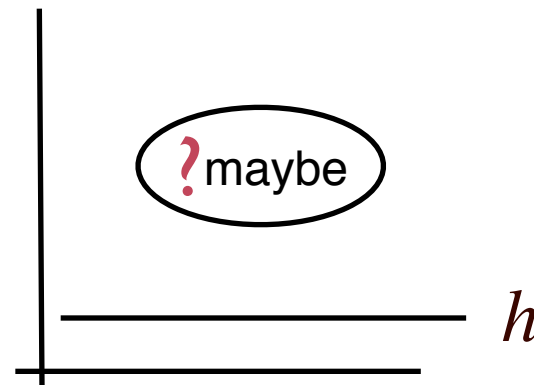
What cancels the top-loop  
divergence?



Can one raise  $\Lambda_t$  ?



The “landscape”



# The Standard Model again

## 1. Naturalness

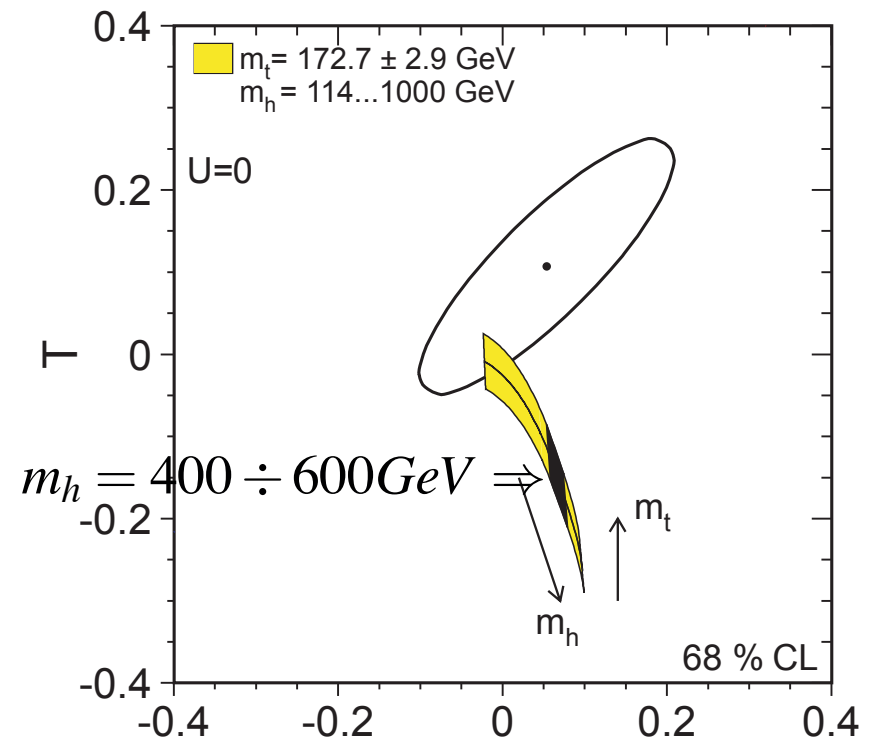
$$\delta m_h^2 = \alpha_t \Lambda_t^2 + \alpha_g \Lambda_g^2 + \alpha_h \Lambda_h^2$$

$$\Rightarrow \begin{aligned} \Lambda_t &\approx 3.5 m_h \\ \Lambda_g &\approx 9 m_h > \Lambda_t \\ \Lambda_h &\approx 1.3 \text{ TeV} \end{aligned}$$

## 2. Perturbativity

$m_h, \text{GeV}$	$\Lambda_P, \text{TeV}$	$\Lambda_L, \text{TeV}$
400	2.4	80
500	1.8	16
600	1.6	7.5

## 3. EWPT



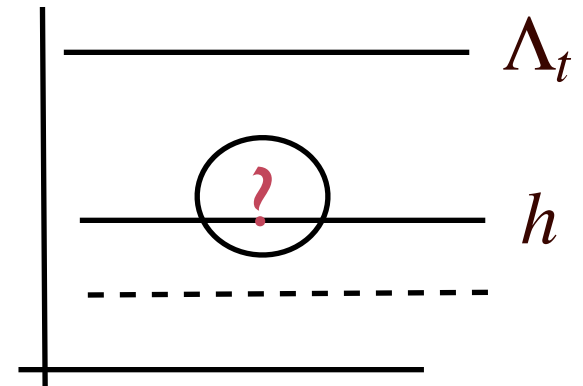
## A simple (provisional) conclusion

A Higgs boson in the mass range of 400-600 GeV, if it were consistent with the EWPT, would allow to raise the cutoff to  $\sim 1.5$  TeV without any cancellation and remaining fully perturbative

Can one raise  $\Lambda_t$  ?



What allows to raise  $m_h$  ?



# The Inert Doublet Model

Consider the most general 2H doublet model invariant under  $H_2 \Rightarrow -H_2$  to get natural flavour conservation (i.e., only  $H_1$  couples to matter)

$$V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^\dagger H_2|^2 + \frac{\lambda_5}{2} [(H_1^\dagger H_2)^2 + \text{h.c.}]$$

$\lambda_4, \lambda_5 \Rightarrow$  custodial symmetry

$\lambda_5 \Rightarrow$  PQ symmetry

Take  $\mu_1^2 < 0, \mu_2^2 > 0$  so that

$$H_1 = \begin{pmatrix} \phi^+ \\ v + (h + i\chi)/\sqrt{2} \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ (S + iA)/\sqrt{2} \end{pmatrix}$$



# The Inert Doublet Model (continued)

Parameter space:

$$\mu_1^2, \lambda_1 \Rightarrow v(M_Z), m_h \quad (\text{in the usual way})$$

$$\lambda_2 \quad (\text{not relevant to the spectrum})$$

$$\mu_2^2, \lambda_{3,4,5} \Rightarrow m_L, m_{NL}, m_H; \lambda_L$$

$$m_H^2 = \mu_2^2 + \lambda_3 v^2$$

$$m_S^2 = \mu_2^2 + (\lambda_3 + \lambda_4 + \lambda_5) v^2$$

$$m_A^2 = \mu_2^2 + (\lambda_3 + \lambda_4 - \lambda_5) v^2$$

custodial symm. limit:  $m_H = m_S = m_A$

PQ symmetry limit:  $m_S = m_A$

absolute minimum:

$$\lambda_{1,2} > 0 \quad \lambda_3, \lambda_L \equiv \lambda_3 + \lambda_4 - |\lambda_5| > -2(\lambda_1 \lambda_2)^{1/2}$$

# Naturalness, perturbativity, EWPT in the IDM

## 1. Naturalness

$$\delta m_h^2 = \alpha_t \Lambda_t^2 + \alpha_g \Lambda_g^2 + \alpha_{11} \Lambda_{H_1}^2 + \alpha_{12} \Lambda_{H_2}^2$$
$$\delta \mu_2^2 = -\frac{1}{2} (\alpha_g \Lambda_g^2 + \alpha_{22} \Lambda_{H_2}^2 + \alpha_{21} \Lambda_{H_1}^2)$$

## 2. Perturbativity

$$16\pi^2 \frac{d\lambda_i}{d \log \Lambda} = \beta_i(\lambda)$$

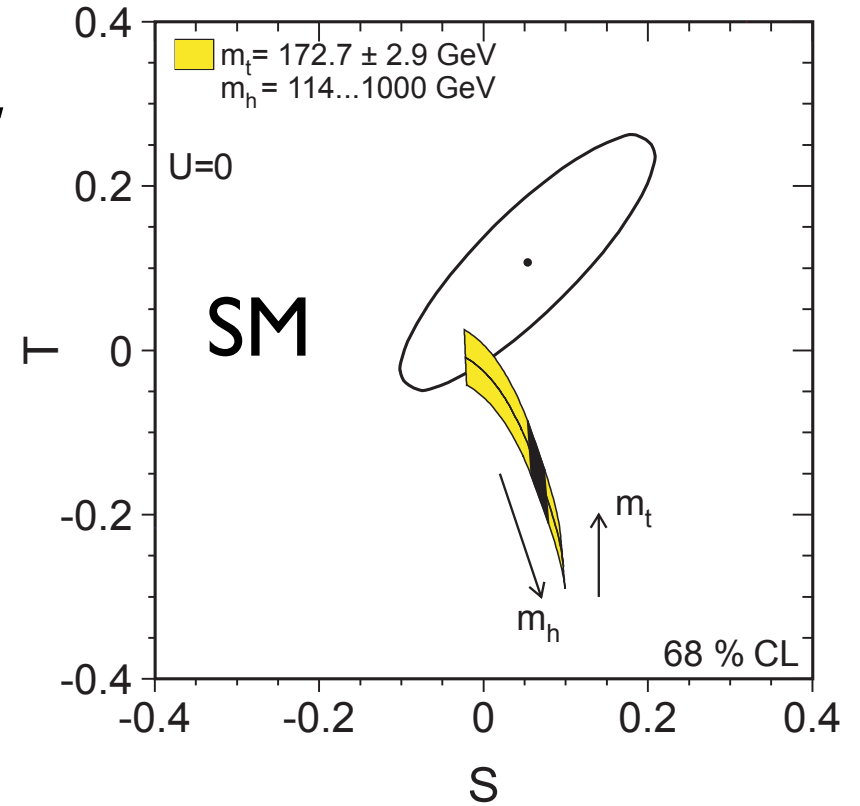
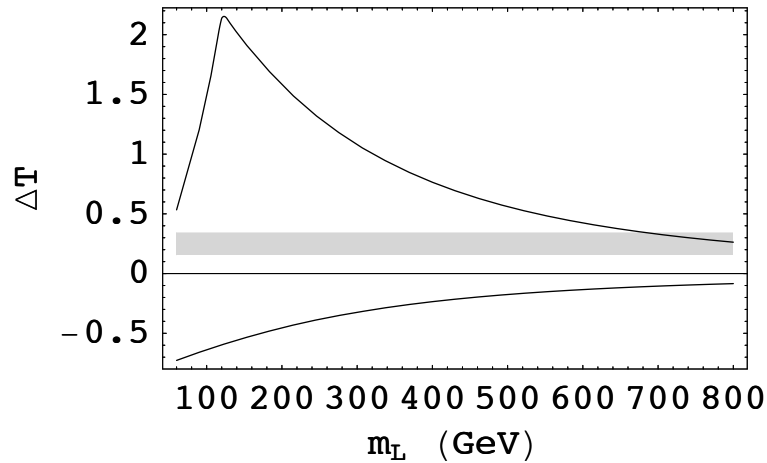
### 3. EWPT

$$T_{IDM} = T_{SM} + \Delta T$$

$$S_{IDM} = S_{SM} + \Delta S$$

$\Delta S$  negligible

$$\Delta T \approx \frac{1}{24\pi^2\alpha v^2} (m_H - m_A)(m_H - m_S)$$



easily constrained by custodial and PQ symmetries

In the Standard Model:

$$m_h = 91_{-32}^{+45} \text{ GeV}$$

In the IDM:

$$m_h = 400 \div 600 \text{ GeV}$$

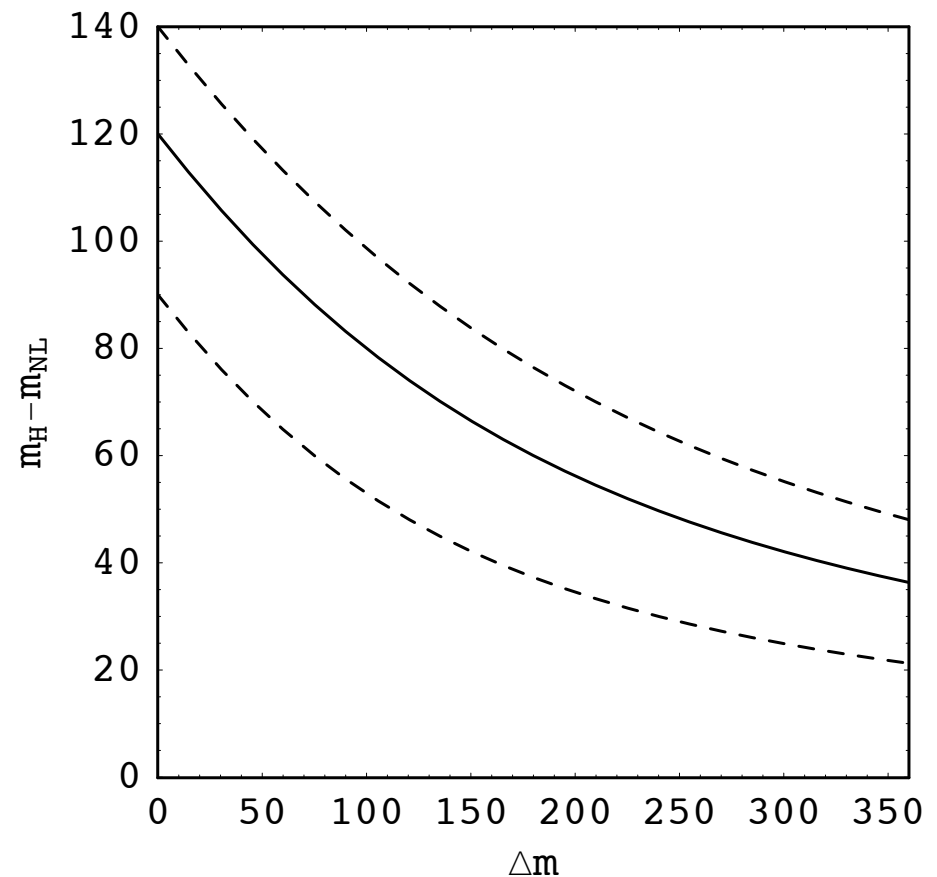
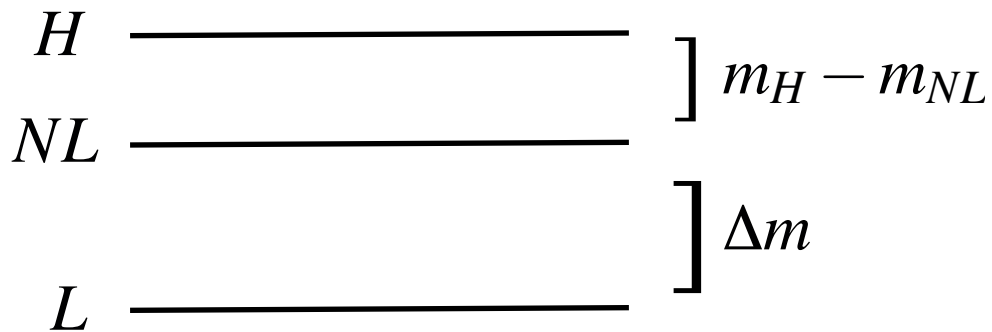
$$(m_H - m_S)(m_H - m_A) = M^2, \quad M = 120_{-30}^{+20} \text{ GeV}$$

The IDM is natural and perturbative up to  $\sim 1.5$  TeV  
 (instead of the SM only up to  $\sim 400$  GeV)

with

$$m_h = 400 \div 600 \text{ GeV}$$

and

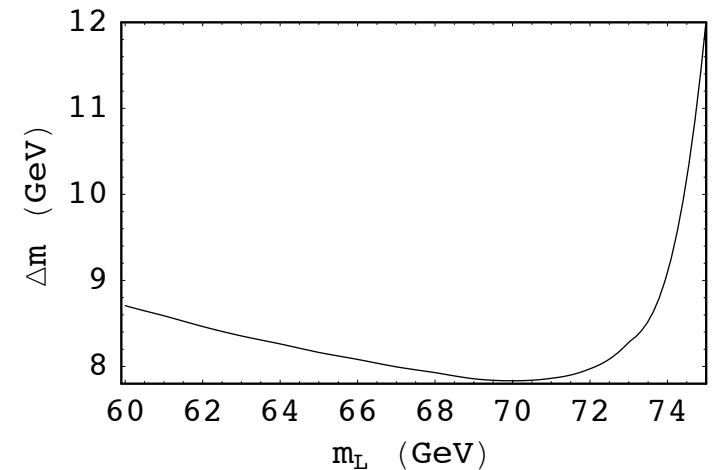


# A Dark Matter candidate

Unbroken  $H_2 \Rightarrow -H_2$   
 (for natural flavour conservation)  $\Rightarrow$

Inert scalars always in pair  
 Stable lightest inert scalar

To get the observed  $\Omega_m$   
 need co-annihilation of S, A into  
 light fermions as dominant process  $\Rightarrow$



$\Rightarrow$  Shouldn't one have seen S and A at LEP2 via

$$e^+e^- \rightarrow A + S \rightarrow (Z^* + S) + S$$

$\Rightarrow$  What about direct DM detection

$$\sigma_h(Lp \rightarrow Lp) \approx 2 \times 10^{-9} \text{ pb} \left( \frac{\lambda_L}{0.5} \right)^2 \left( \frac{70 \text{ GeV}}{m_L} \right)^2 \left( \frac{500 \text{ GeV}}{m_h} \right)^4$$

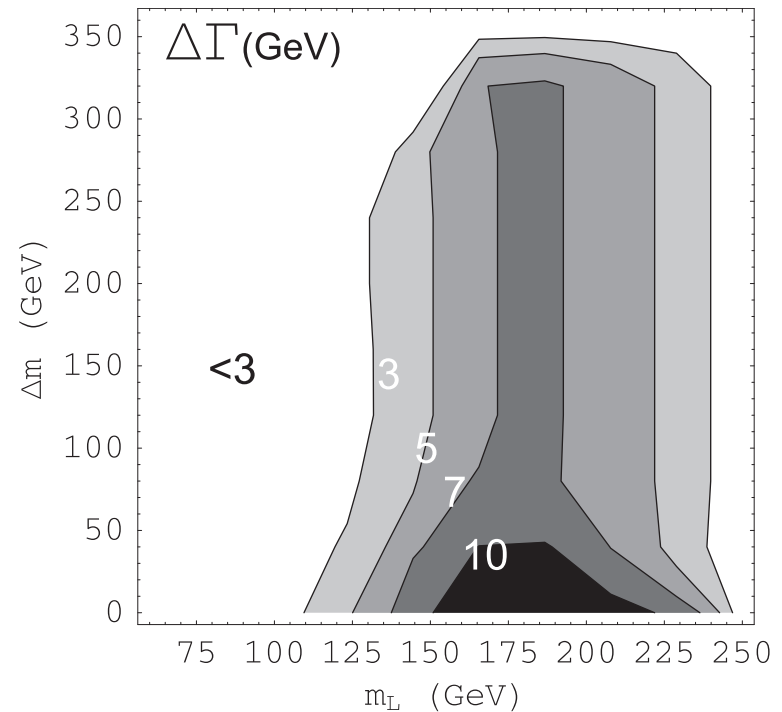
# Collider Signals

1.  $m_h = 400 \div 600 \text{ GeV}$

A standard Higgs boson?

$$h \rightarrow SS, AA, H^+H^-$$

$$\Gamma_h = 68 \text{ GeV} \text{ at} \\ m_h = 500 \text{ GeV}$$



2.  $pp \rightarrow W^* \rightarrow HA \text{ or } HS$

$$H \rightarrow AW \text{ or } SW$$

$$A \rightarrow SZ^{(*)}$$

for the DM parameters, looking for 3 charged leptons

$$\sigma_{\text{signal}} \approx 3.5 \text{ fb} \quad \sigma_{\text{bg}} \approx 20 \text{ fb}$$

# Conclusions

The SM as an effective low energy theory

⇒ Why the perturbative Higgs among its degrees of freedom?

⇒ Where is the cut-off?  $\Lambda_{SM} \approx 400 \text{ GeV} \left( \frac{m_h}{115 \text{ GeV}} \right)$

**Qualitatively:** supersymmetry, ...

**Quantitatively:** can we be fooled by the EWPT?

(more modest in scope but physically motivated)

E.g.: The IDM as a simple way to a perturbative and fully natural description of EW physics up to 1.5 TeV

Alternatives? UV completion?

# “Beyond the SM” Physics defined

(in absence of a better name)

(NOT a naively reductionistic view,  
a definition of hierarchies in physics,  
a research program)

Everything that fits in Page 1  
by coherent addition or emendation,  
meeting the same or better standards of **synthesis**  
and **empirical adequacy**

The central question:  
What will replace current Page 1?