

# Measuring Parameters of Black holes

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- X chromosome
- Future computing
- Stem cells
- Bird flu
- Mars
- GM crops

- [My news](#)
- [Biotechnology](#)
- [Careers](#)
- [Drug discovery](#)
- [Earth and environment](#)
- [Medical Research](#)
- [Physical Sciences](#)

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[04 April 2005](#)

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[04 April 2005](#)

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## NEWS

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### Black holes 'do not exist'

[Philip Ball](#)

#### These mysterious objects are dark-energy stars, physicist claims.

Black holes are staples of science fiction and many think astronomers have observed them indirectly. But according to a physicist at the Lawrence Livermore National Laboratory in California, these awesome breaches in space-time do not and indeed cannot exist.



Black holes, such as the one pictured in this artist's impression, may in fact be pockets of 'dark energy'.

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Over the past few years, observations of the motions of galaxies have shown that some 70% the Universe seems to be composed of a strange 'dark energy' that is driving the Universe's accelerating expansion.

George Chapline thinks that the collapse of the massive stars, which was long believed to generate black holes, actually leads to the formation of stars that contain dark energy. "It's a near certainty that black holes don't exist," he claims.

Black holes are one of the most celebrated predictions of Einstein's general theory of relativity, which explains gravity as the warping of space-time caused by massive objects. The theory suggests that

a sufficiently massive star, when it dies, will collapse under its own gravity to a single point.

But Einstein didn't believe in black holes, Chapline argues. "Unfortunately", he adds, "he couldn't articulate why." At the root of the problem is the other revolutionary theory of twentieth-century physics, which Einstein also helped to formulate: quantum mechanics.

**It's a near certainty that black holes don't exist.**

George Chapline  
Lawrence Livermore National  
Laboratory

In general relativity, there is no such thing as a 'universal time' that makes clocks tick at the same rate everywhere. Instead, gravity makes clocks run at different rates in different places. But quantum mechanics, which describes physical phenomena at infinitesimally small scales, is meaningful only if time is universal; if not, its equations make no sense.

This problem is particularly pressing at the boundary, or event horizon, of a black hole. To a far-off observer, time seems to stand still here. A spacecraft falling into a black hole would seem, to someone watching it from afar, to be stuck forever at the event horizon, although the astronauts in the spacecraft would feel as if they were continuing to fall. "General relativity predicts that nothing happens at the event horizon," says Chapline.

### Quantum transitions

However, as long ago as 1975 quantum physicists argued that strange things do happen at an event horizon: matter governed by quantum laws becomes hypersensitive to slight disturbances. "The result was quickly forgotten," says Chapline, "because it didn't agree with the prediction of general relativity. But actually, it was absolutely correct."

This strange behaviour, he says, is the signature of a 'quantum phase transition' of space-time. Chapline argues that a star doesn't simply collapse to form a black hole; instead, the space-time inside it becomes filled with dark energy and this has some intriguing gravitational effects.

Outside the  
'surface' of a

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dark-energy star, it behaves much like a black hole, producing a strong gravitational tug. But inside, the 'negative' gravity of dark energy may cause matter to bounce back out again.



If the dark-energy star is big enough, Chapline predicts, any electrons bounced out will have been converted to positrons, which then annihilate other electrons in a burst of high-energy radiation.

Chapline says that this could explain the radiation observed from the centre of our galaxy, previously interpreted as the signature of a huge black hole.

He also thinks that the Universe could be filled with 'primordial' dark-energy stars. These are formed not by stellar collapse but by fluctuations of space-time itself, like blobs of liquid condensing spontaneously out of a cooling gas. These, he suggests, could be stuff that has the same gravitational effect as normal matter, but cannot be seen: the elusive substance known as dark matter.

[◀ Top](#)

## References

1. Chapline G. *Arxiv*, <http://xxx.arxiv.org/abs/astro-ph/0503200> (2005).

[◀ Top](#)



# Outline of my talk

- History
- Black holes in astrophysics
- The iron  $K_{\alpha}$  -line as a tool for BH characteristics
- Movies

# Outline of my talk

- Wrong pictures of black holes
- Mirages around BHs and retro-lensing
- Black Hole Images
- Conclusions

# Black hole history (I)

- 1783 : The Reverend John Michell (invisible sphere)
- 1798,1799 : P.S. Laplace (Exposition du Systeme du Monde Part II, p. 305, Allgemeine Geographifche Ephemeriden, 4, S.1, 1799)
- 1915 : K. Schwarzschild
- 1928 : Ya.I Frenkel (EOS for degenerate electron Fermi-gas with arbitrary relativistic degree and typical WD masses)
- 1930 : E. Stoner (the upper limit for masses of white dwarfs for uniform mass distribution)
- 1931 : S. Chandrasekhar (the upper limit for masses of white dwarfs for polytrope mass distribution)
- 1932 : E. Stoner (EOS for degenerate electron Fermi-gas with arbitrary relativistic degree)
- 1934, 1935 : S. Chandrasekhar (the upper limit for masses of white dwarfs for arbitrary relativistic degree)
- 1935 : A.Eddington (rejections of the upper limit for WDs)
- 1939 : R.Oppenheimer & G.Volkoff (the upper limit for NSs and the GR approach)
- 1939 : R.Oppenheimer & R.Snyder (the collapse of pressureless stars and the GR approach) “Every statement of this paper is in accordance with ideas that remain valid today”(Novikov & Frolov, 2001)

## Black hole history (II)

- 1939: Einstein considered a possibility “to create a field having Schwarzschild singularity by gravitating masses”;
- Einstein (1939): “The main result of this investigation is a clear understanding that Schwarzschild singularities do not exist in real conditions”;
- 1942: Bergmann:” In reality, mass has no possibility to concentrate by the following way that the Schwarzschild singular surface would be in vacuum”
- 1958 : D. Finkelstein & 1960 M.Kruskal (causal structure of Schwarzschild metric)
- 1962 : R. Feynman “Lectures on gravitation” (“it would be interesting to investigate dust collapse” (23 years later OS paper!)
- 1967 : J.A. Wheeler: black holes predicted to result from “continued gravitational collapse of over-compact masses” (the birth of the BH concept)

Таблица 5. Параметры двойных систем с ЧД

Система	Спектр оптической звезды	$P_{orb}$ , сут	$f_1(m)$ , в $M_{\odot}$	$m_x$ , в $M_{\odot}$	$m_y$ , в $M_{\odot}$	$V_{pec}$ , км с $^{-1}$	Примечание
Cyg X-1 V 1357 Cyg	O 9,7 Iab	5,6	0,24 ± 0,01	16 ± 5	33 ± 9	2,4 ± 1,2	Стационарная
LMC X-3	B3 Ve	1,7	2,3 ± 0,3	9 ± 2	6 ± 2	—	Стационарная
LMC X-1	O (7-9) III	4,2	0,14 ± 0,05	7 ± 3	22 ± 4	—	Стационарная
A0 620-00 (V616 Mon)	K5 V	0,3	2,91 ± 0,08	10 ± 5	0,6 ± 0,1	-15 ± 5	Трагзвездная
GS 2023 + 338 (V404 Cyg)	K0 IV	6,5	6,08 ± 0,06	12 ± 2	0,7 ± 0,1	8,5 ± 2,2	Трагзвездная
GRS 1124-68 (GU Mus)	K2 V	0,4	3,01 ± 0,15	6(+5 - 2)	0,8 ± 0,1	25 ± 5	Трагзвездная
GS 2000+25 (QZ Vul)	K5 V	0,3	4,97 ± 0,10	10 ± 4	0,5 ± 0,1	—	Трагзвездная
GRO J0422+32 (V518 Per)	M2 V	0,2	1,13 ± 0,09	10 ± 5	0,4 ± 0,1	—	Трагзвездная
GRO J1655-40 (XN Sco 1994)	F5 IV	2,6	2,73 ± 0,09	6,3 ± 0,5	2,4 ± 0,4	-114 ± 19	Трагзвездная
H 1705-250 (V2107 Oph)	K5 V	0,5	4,86 ± 0,13	6 ± 1	0,4 ± 0,1	38 ± 20	Трагзвездная
4U 1543-47 (HL Lup)	A2 V	1,1	0,22 ± 0,02	4,0-6,7	~ 2,5	—	Трагзвездная
GRS 1009-45 (MM Vel)	(K6-M0) V	0,3	3,17 ± 0,12	3,6-4,7	0,5-0,7	—	Трагзвездная
SAX J1819,3-2525 (V4641 Sgr)	B9 III	2,8	2,74 ± 0,12	9,61(+2,08-0,88)	6,53(+1,6-1,03)	—	Трагзвездная
XTE J1118+480	(K7-M0) V	0,17	6,1 ± 0,3	6,0-7,7	0,09-0,5	145*	Трагзвездная
GRS 1915+105	(K-M) III	33,5	9,5 ± 3,0	14 ± 4	1,2 ± 0,2	—	Трагзвездная

**Таблица 6.** Микроквазары в нашей Галактике

Название источника	Компактный объект	$V$ джета
GRS 1915 + 105	ЧД	0,92c – 0,98c
GRO J1655 – 40	ЧД	0,92c
XTE J1748 – 288	ЧД	0,93c – 0,23c
SS 433	ЧД	0,26c
Cygn X-3	ЧД	$\sim 0,3c - \geq 0,8c$
CI Cam	НЗ?	$\sim 0,15c$
Sco X-1	НЗ	$\sim 0,5c$
Cir X-1	НЗ	$\geq 0,1c$
IE 1740.7 – 2942	ЧД	
GRS 1758 – 258	ЧД	
SAX J1819.3 – 2525	ЧД	$\geq 0,95c$
LS 5039	?	$\geq 0,15c$
Cygn X-1	ЧД	$> 0,6c$
XTE J1550 – 564	ЧД	

- Ho1
- Ho2

Black holes in centers of galaxies

(L.Ho, ApJ 564, 120 (2002))



TABLE 1: GALAXIES WITH BLACK HOLE MASSES

Galaxy Name (1)	Hubble Type (2)	$T$ (3)	Spectral Class (4)	$c_z$ (km s <sup>-1</sup> ) (5)	$D$ (Mpc) (6)	Ref. (7)	$M_{\text{BH}}$ ( $M_{\odot}$ ) (8)	Method (9)	Ref. (10)
3C 120 (Mrk 1506)	S0:	-1.0	S1	9896	137.8	1	$2.3 \times 10^7$	R	1
3C 390.3 (VII w 838)	E?	-5.0	S1	16818	241.2	1	$3.4 \times 10^8$	R	1
Ark 120 (Mrk 1095)	S0/a	0.0	S1	9682	134.6	1	$1.84 \times 10^8$	R	1
Arp 102B	E0	-5.0	L1.8	7245	99.7	1	$2.2 \times 10^8$	G	2
Circinus	Sb:	3.0	S2	449	4.0	2	$1.3 \times 10^6$	M	3
Fairall 9	S?	...	S1	14095	199.8	1	$8.0 \times 10^7$	R	1
IC 342	SABcd	6.0	H	31	1.8	3	$<5.0 \times 10^5$	S	4
IC 1459	E3	-5.0	L2	1691	29.2	4	$3.7 \times 10^8$	G	5
IC 4329A	S0+	-1.0	S1	4813	65.5	1	$5.0 \times 10^6$	R	1
Milky Way	Sbc	3.0	...	...	0.008	5	$2.95 \times 10^6$	S	6
Mrk 79 (UGC 3973)	SBb	3.0	S1.5	6652	91.3	1	$5.2 \times 10^7$	R	1
Mrk 110	Pair?	...	S1	10580	147.7	1	$5.6 \times 10^6$	R	1
Mrk 279 (UGC 8823)	S0	-1.0	S1.5	9129	126.6	1	$4.2 \times 10^7$	R	1
Mrk 335	S0/a	0.0	S1.0	7730	106.6	1	$6.3 \times 10^6$	R	7
Mrk 509	comp	...	S1	10312	143.8	1	$5.78 \times 10^7$	R	1
Mrk 590 (NGC 863)	Sa:	1.0	S1.2	7910	109.2	1	$1.78 \times 10^7$	R	1
Mrk 817 (UGC 9412)	S?	...	S1.5	9430	131.0	1	$4.4 \times 10^7$	R	1
NGC 205 (M110)	dE5	-5.0	A	-241	0.74	6	$<9.3 \times 10^4$	S	8
NGC 221 (M32)	E2	-6.0	A	-145	0.81	4	$3.9 \times 10^6$	S	9
NGC 224 (M31)	Sb	3.0	A	-300	0.76	4	$3.3 \times 10^7$	S	10

NGC 224 (M31)	Sb	3.0	A	-300	0.76	4	$3.3 \times 10^7$	S	10
NGC 598 (M33)	Scd	6.0	H	-179	0.87	6	$<1.5 \times 10^3$	S	11
NGC 821	E6?	-5.0	A	1735	24.1	4	$5.0 \times 10^7$	S	12
NGC 1023	SB0-	-3.0	A	637	11.4	4	$3.9 \times 10^7$	S	13
NGC 1068 (M77)	Sb	3.0	S1.9	1137	14.4	7	$1.6 \times 10^7$	M	14
NGC 2778	E	-5.0	...	2049	22.9	4	$2.0 \times 10^7$	S	12
NGC 2787	SB0+	-1.0	L1.9	696	7.5	4	$3.9 \times 10^7$	G	15
NGC 3031 (M81)	Sab	2.0	S1.5	-34	3.9	4	$6.3 \times 10^7$	S	16
NGC 3115	S0-	-3.0	A	720	9.7	4	$9.1 \times 10^8$	S	17
NGC 3227	SABa	1.0	S1.5	1157	20.6	7	$3.9 \times 10^7$	R	1
NGC 3245	S0?	-2.0	T2	1358	20.9	4	$2.1 \times 10^8$	G	18
NGC 3377	E5+	-5.0	A	665	11.2	4	$1.0 \times 10^8$	S	12
NGC 3379 (M105)	E1	-5.0	L2/T2:	911	10.6	4	$1.0 \times 10^8$	S	19
NGC 3384	SB0-:	-3.0	A	704	11.6	4	$1.8 \times 10^7$	S	12
NGC 3516	SB0:	-2.0	S1.2	2649	38.9	7	$2.3 \times 10^7$	R	7
NGC 3608	E2	-5.0	L2/S2:	1253	22.9	4	$1.1 \times 10^8$	S	12
NGC 3783	SBa	1.0	S1	2917	38.5	7	$9.4 \times 10^6$	R	1
NGC 3998	S0?	-2.0	L1.9	1040	14.1	4	$5.6 \times 10^8$	S	16
NGC 4051	SABbc	4.0	S1.2	725	17.0	7	$1.3 \times 10^6$	R	1
NGC 4151	SABab	2.0	S1.5	995	20.3	7	$1.53 \times 10^7$	R	1
NGC 4203	SAB0	-3.0	L1.9	1086	14.1	4	$<1.2 \times 10^7$	G	15
NGC 4258 (M106)	SABbc	4.0	S1.9	448	7.3	4	$4.1 \times 10^7$	M	20
NGC 4261 (3C 270)	E2+	-5.0	L2	2238	31.6	4	$5.2 \times 10^8$	G	21
NGC 4291	E	-5.0	A	1757	26.2	4	$1.5 \times 10^8$	S	12
NGC 4342	S0-	-3.0	...	751	16.8	7	$3.4 \times 10^8$	S	22
NGC 4374 (M84, 3C 272.1)	E1	-5.0	L2	1060	18.4	4	$1.6 \times 10^9$	G	23
NGC 4395	Sm:	9.0	S1.5	319	3.6	7	$<1.1 \times 10^5$	S	24
NGC 4459	S0+	-1.0	T2:	1210	16.1	4	$6.5 \times 10^7$	G	15
NGC 4473	E5	-5.0	A	2244	15.7	4	$1.0 \times 10^8$	S	12
NGC 4486 (M87, 3C 274)	E0+	-4.0	L2	1307	16.1	4	$3.4 \times 10^9$	G	25

Galaxy Name (1)	Hubble Type (2)	$T$ (3)	Spectral Class (4)	$c_z$ (km s $^{-1}$ ) (5)	$D$ (Mpc) (6)	Ref. (7)	$M_{\text{BH}}$ ( $M_{\odot}$ ) (8)	Method (9)	Ref. (10)
NGC 4486B	E0	-6.0	...	1555	16.1	8	$6.0 \times 10^8$	S	26
NGC 4564	E	-5.0	A	1142	15.0	4	$5.7 \times 10^7$	S	12
NGC 4593	SBb	3.0	S1	2698	39.5	7	$8.1 \times 10^6$	R	7
NGC 4594 (M104)	Sa	1.0	L2	1024	9.8	4	$1.1 \times 10^9$	S	27
NGC 4596	SB0	-1.0	L2::	1874	16.8	7	$5.8 \times 10^7$	G	15
NGC 4649 (M60)	E2	-5.0	A	1117	16.8	4	$2.0 \times 10^9$	S	12
NGC 4697	E6	-5.0	...	1241	11.7	4	$1.2 \times 10^8$	S	12
NGC 4945	SBcd	6.0	S2	560	4.2	9	$1.1 \times 10^6$	M	28
NGC 5548	S0/a	0.0	S1.5	5149	70.2	1	$1.23 \times 10^8$	R	1
NGC 5845	E	-5.0	...	1456	25.9	4	$3.2 \times 10^8$	S	12
NGC 6251	E0	-5.0	S2	6900	94.8	1	$5.4 \times 10^8$	G	29
NGC 7052	E4	-5.0	...	4672	63.6	1	$3.6 \times 10^8$	G	30
NGC 7457	S0-?	-3.0	A	812	13.2	4	$3.4 \times 10^6$	S	12
NGC 7469	SABa	1.0	S1.0	4892	66.6	1	$6.5 \times 10^6$	R	1
PG 0026+129	...	...	QSO	0.142	627.4	1	$5.4 \times 10^7$	R	1
PG 0052+251	S	...	QSO	0.155	690.4	1	$2.2 \times 10^8$	R	1
PG 0804+761	...	...	QSO	0.100	429.9	1	$1.89 \times 10^8$	R	1
PG 0844+349	...	...	QSO	0.064	268.4	1	$2.16 \times 10^7$	R	1
PG 0953+414	S	...	QSO	0.239	1118	1	$1.84 \times 10^8$	R	1
PG 1211+143	...	...	QSO	0.085	361.7	1	$4.05 \times 10^7$	R	1
PG 1226+023 (3C 273)	E	...	QSO	0.158	705.1	1	$5.5 \times 10^8$	R	1
PG 1229+204	S	...	QSO	0.064	268.4	1	$7.5 \times 10^7$	R	1
PG 1307+085	E	...	QSO	0.155	690.4	1	$2.8 \times 10^8$	R	1
PG 1351+640	...	...	QSO	0.087	370.7	1	$4.6 \times 10^7$	R	1
PG 1411+442	...	...	QSO	0.089	379.8	1	$8.0 \times 10^7$	R	1
PG 1426+015 (Mrk 1383)	...	...	QSO	0.086	366.2	1	$4.7 \times 10^8$	R	1
PG 1613+658 (Mrk 876)	...	...	QSO	0.129	565.3	1	$2.41 \times 10^8$	R	1
PG 1617+175 (Mrk 877)	...	...	QSO	0.114	494.7	1	$2.73 \times 10^8$	R	1
PG 1700+518	...	...	QSO	0.292	1406	1	$6 \times 10^7$	R	1
PG 1704+608 (3C 351)	E	...	QSO	0.371	1857	1	$3.7 \times 10^7$	R	1
PG 2130+099	...	...	QSO	0.061	255.3	1	$1.44 \times 10^8$	R	1



NOTE.— Col. (1) Galaxy name. Col. (2) Revised Hubble type from de Vaucouleurs et al. 1991 (RC3), except for QSOs, which is estimated by Hamilton, Casertano, & Turnshek 2001. Col. (3) Morphological type index from the RC3. Col. (4) Spectral class of the nucleus from Ho et al. 1997, and otherwise from Whittle 1992a and NED, where A = absorption-line nucleus, H = H II nucleus, L = LINER, S = Seyfert, T = “transition object” (LINER/H II), 1 = type 1, 2 = type 2, and a fractional number between 1 and 2 denotes various intermediate types; uncertain and highly uncertain classifications are followed by a single and double colon, respectively. Col. (5) Heliocentric radial velocity (redshift for QSOs) from NED. Col. (6) Adopted distance. Col. (7) Reference for  $D$ . Col. (8) Black hole mass, scaled to our adopted distances. Col. (9) Method for determining  $M_{\text{BH}}$ : G, gas kinematics; M, maser kinematics; R, reverberation mapping; S, stellar kinematics. Col. (10) Reference for  $M_{\text{BH}}$ .

REFERENCES.— *Distance*: (1) Luminosity distance derived from heliocentric redshift,  $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $\Omega_M = 0.3$ , and  $\Omega_\Lambda = 0.7$ ; (2) Freeman et al. 1977; (3) McCall 1989; (4) Tonry et al. 2001; (5) Reid 1993; (6) Ferrarese et al. 2000; (7) Tully 1988, who also uses our value of  $H_0$ ; (8) Assumed to be at the distance of NGC 4486; (9) Assumed to be at the distance of NGC 5128, which is known from Tonry et al. 2001.

REFERENCES.— *Black hole mass*: (1) Kaspi et al. 2000; (2) Newman et al. 1997; (3) Greenhill et al. 2000; (4) Böker, van der Marel, & Vacca 1999; (5) Verdoes Kleijn et al. 2000; (6) Genzel et al. 2000; (7) Ho 1999a; (8) Jones et al. 1996; (9) van der Marel et al. 1998; (10) Kormendy & Bender 1999; (11) Gebhardt et al. 2001; (12) Gebhardt et al. 2000a; (13) Bower et al. 2001a; (14) Greenhill et al. 1996; (15) Sarzi et al. 2001; (16) Bower et al. 2001b; (17) Emselfem, Dejonghe, & Bacon 1999; (18) Barth et al. 2001; (19) Gebhardt et al. 2000b; (20) Miyoshi et al. 1995; (21) Ferrarese, Ford, & Jaffe 1996; (22) Cretton & van den Bosch 1999; (23) Bower et al. 1998; (24) Filippenko & Ho 2001; (25) Macchetto et al. 1997; (26) Kormendy et al. 1997a; (27) Kormendy et al. 1997b; (28) Greenhill, Moran, & Herrnstein 1997; (29) Ferrarese & Ford 1999; (30) van der Marel & van den Bosch 1998.

- Macho 96 5 light curve
- Macho 96 6 light curve
- Likelihood functions for BH microlenses
- Probable masses and distances for BH microlenses

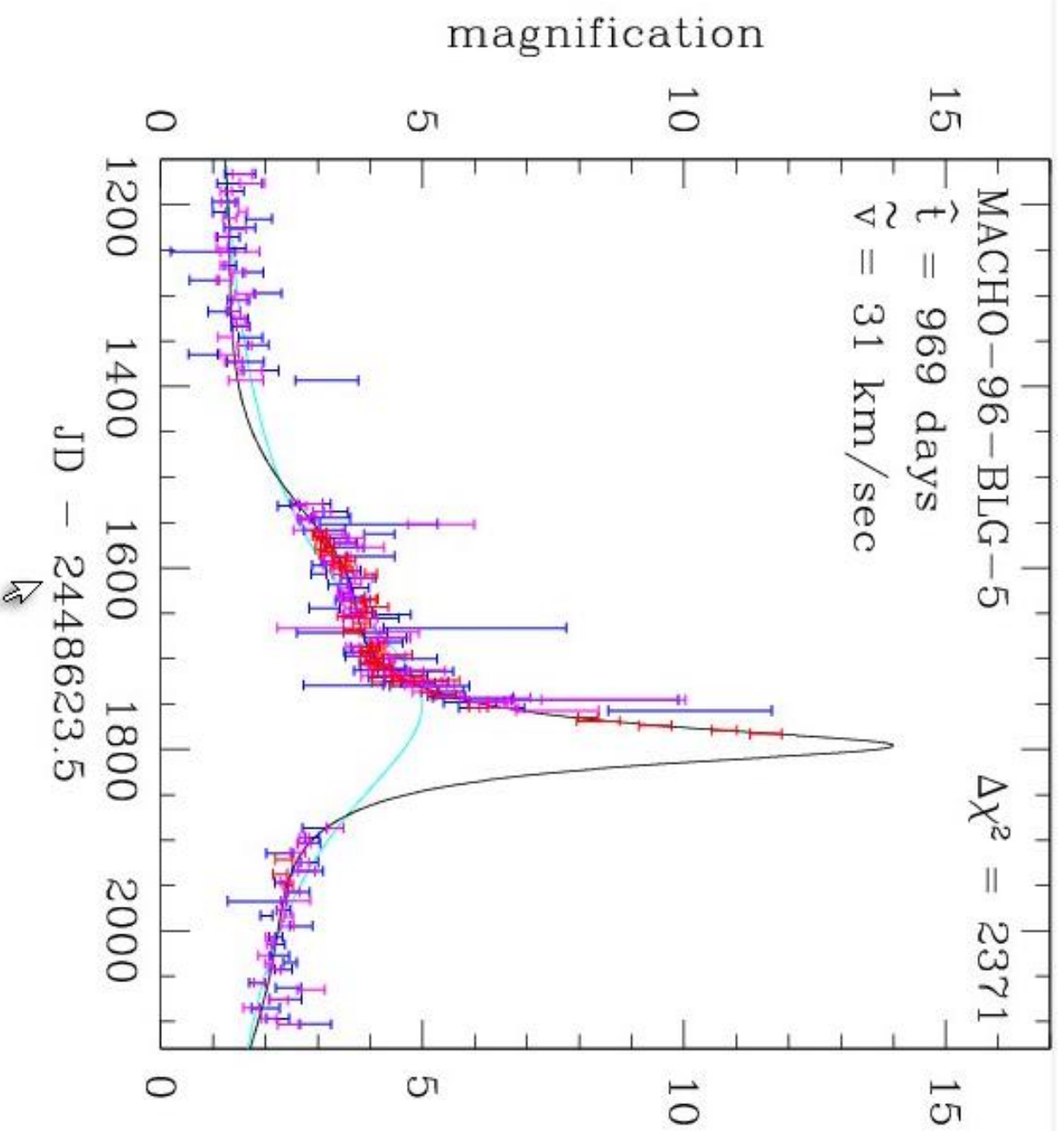


Fig. 7.— MACHO-96-BLG-5 lightcurves normalized to the unlensed flux of the lensed star. The MACHO red and blue data are plotted in magenta and blue, respectively, and the CTIO data are shown in red. The black curve is the parallax fit while the cyan curve is the best fit standard microlensing lightcurve. An additional 4 years of data showing very little photometric variation are not shown.

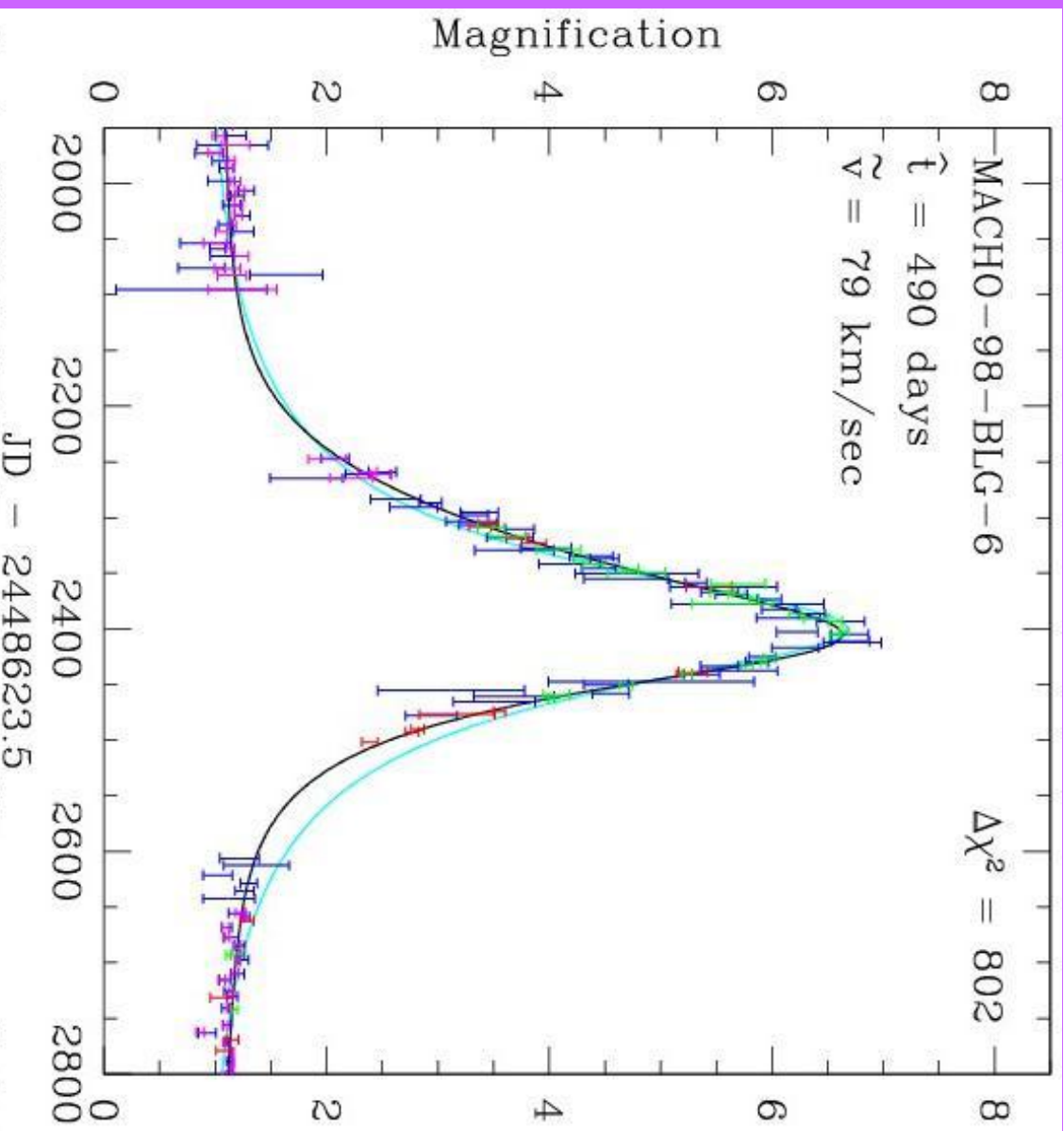


Fig. 4.— MACHO-98-BLG-6 lightcurve closeup with lightcurves normalized to the unlensed flux of the lensed star. The MACHO red and blue data are plotted in magenta and blue, respectively, the CTIO data are shown in red, and the MPS data are shown in green. The black curve is the parallax fit while the cyan curve is the best fit standard microlensing lightcurve. The gap in the MACHO red data during the day 2280-2650 interval is due to a CCD failure. An additional year of data showing no photometric variation is not shown.



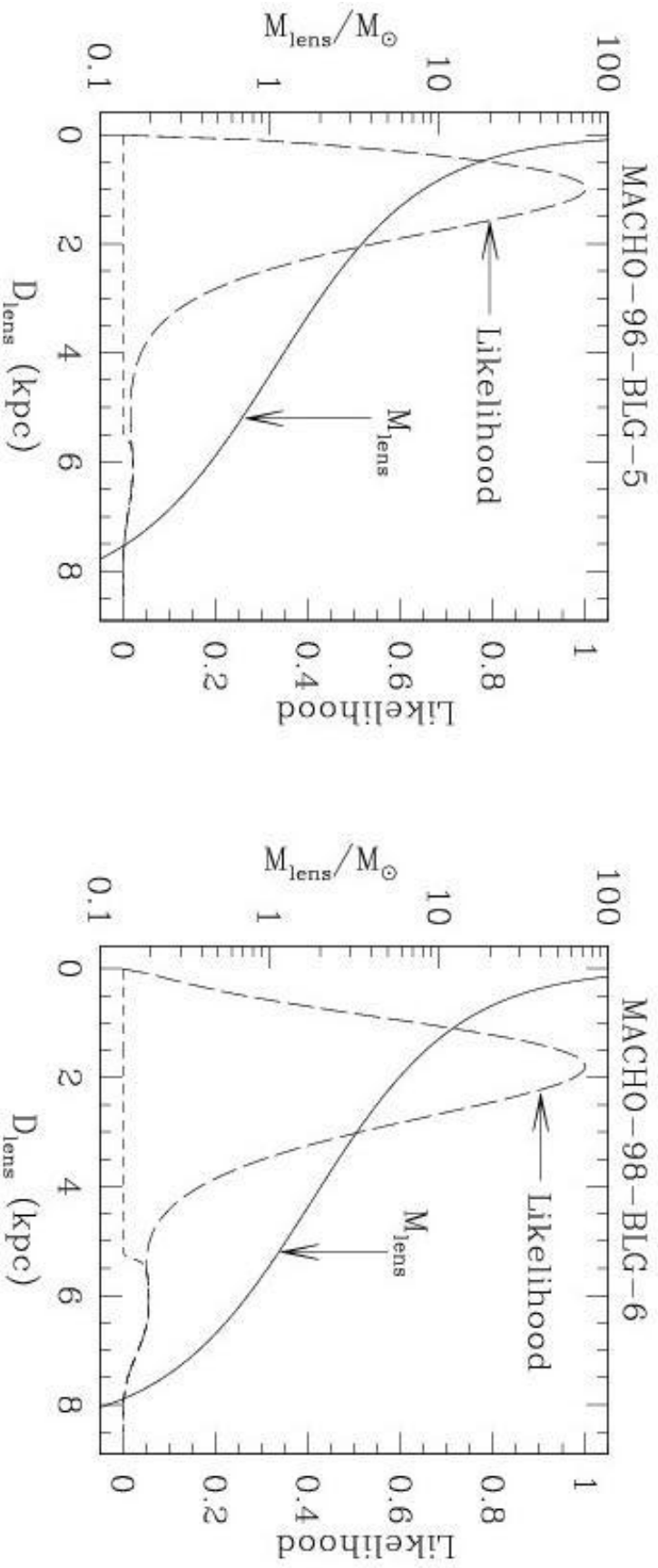


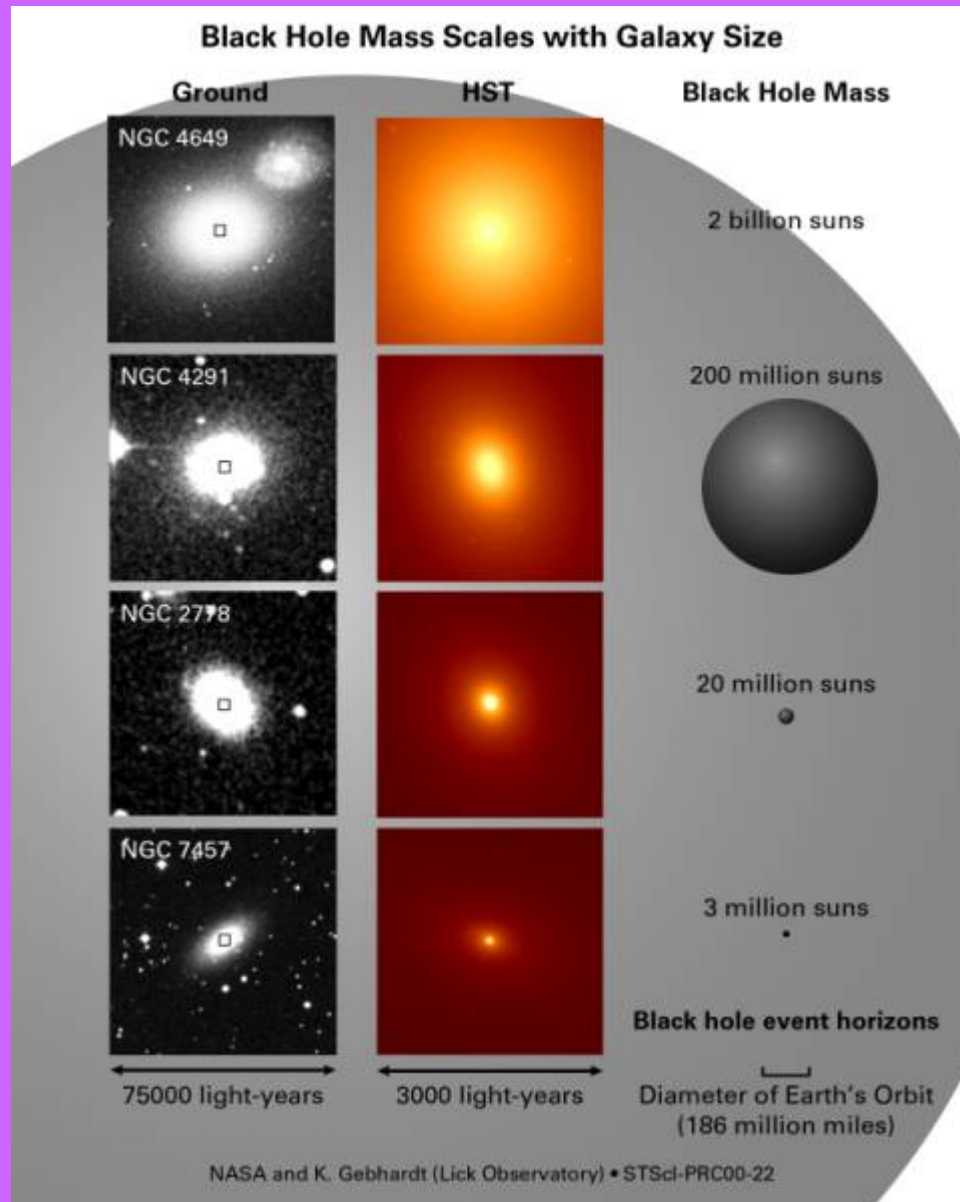
Fig. 11.— The mass vs. distance relations (solid curves) for our candidate black hole lenses are shown along with the likelihood functions (long dashed curves) computed assuming a standard model for the Galactic phase space distribution. The source star is assumed to reside in the bulge for both events. The implied best fit masses are  $M = 6_{-3}^{+10} M_{\odot}$  for the MACHO-96-BLG-5 lens and  $M = 6_{-3}^{+7} M_{\odot}$  for the MACHO-98-BLG-6. The 95% confidence level lower limits on the masses are  $1.6 M_{\odot}$  and  $0.94 M_{\odot}$  respectively. The short dashed curves delineate the portion of the likelihood functions that is allowed when the lens is assumed to be a main sequence star. The ratio of the area below this portion to the entire area below the likelihood curve gives a probability that a lens is a main sequence star. For MACHO-96-BLG-5, the upper limit on the lens brightness is very stringent because of the HST images, and a main sequence lens is ruled out.

Table 7. Mass & Magnitude Estimates for the MACHO Microlensing Parallax Events

Event	$M/M_{\odot}$	$M_{MS}/M_{\odot}$	$D_{\ell-MS}$	sep-MS	$V_s$	$\Delta I_{\ell s}$	$\Delta V_{\ell s}$	$\Delta B_{\ell s}$	$\Delta U_{\ell s}$
104-C	$1.1^{+1.1}_{-0.5}$	0.74	2.7 kpc	40 mas	17.3	3.5	3.5	3.5	3.2
96-BLG-5	$6^{+10}_{-8}$	-	-	-	-	-	-	-	-
96-BLG-12	$1.3^{+1.8}_{-0.7}$	0.75	2.0 kpc	28 mas	18.0	2.1	2.2	2.2	2.3
98-BLG-6	$2.5^{+1.7}_{-0.9}$	0.88	5.7 kpc	5 mas	20.1	2.2	1.9	1.6	1.1
99-BLG-1	$0.7^{+1.2}_{-0.4}$	0.40	1.7 kpc	17 mas	18.9	1.8	3.2	3.6	3.9
99-BLG-8	$1.2^{+1.6}_{-0.6}$	1.2	1.6 kpc	25 mas	16.3	1.3	0.7	-0.3	-1.1

Note. — These are the parameters of the “most likely” main sequence star lenses for our best microlensing parallax events. For MACHO-96-BLG-5, a main sequence lens is ruled out.

# Black holes in galaxy centers

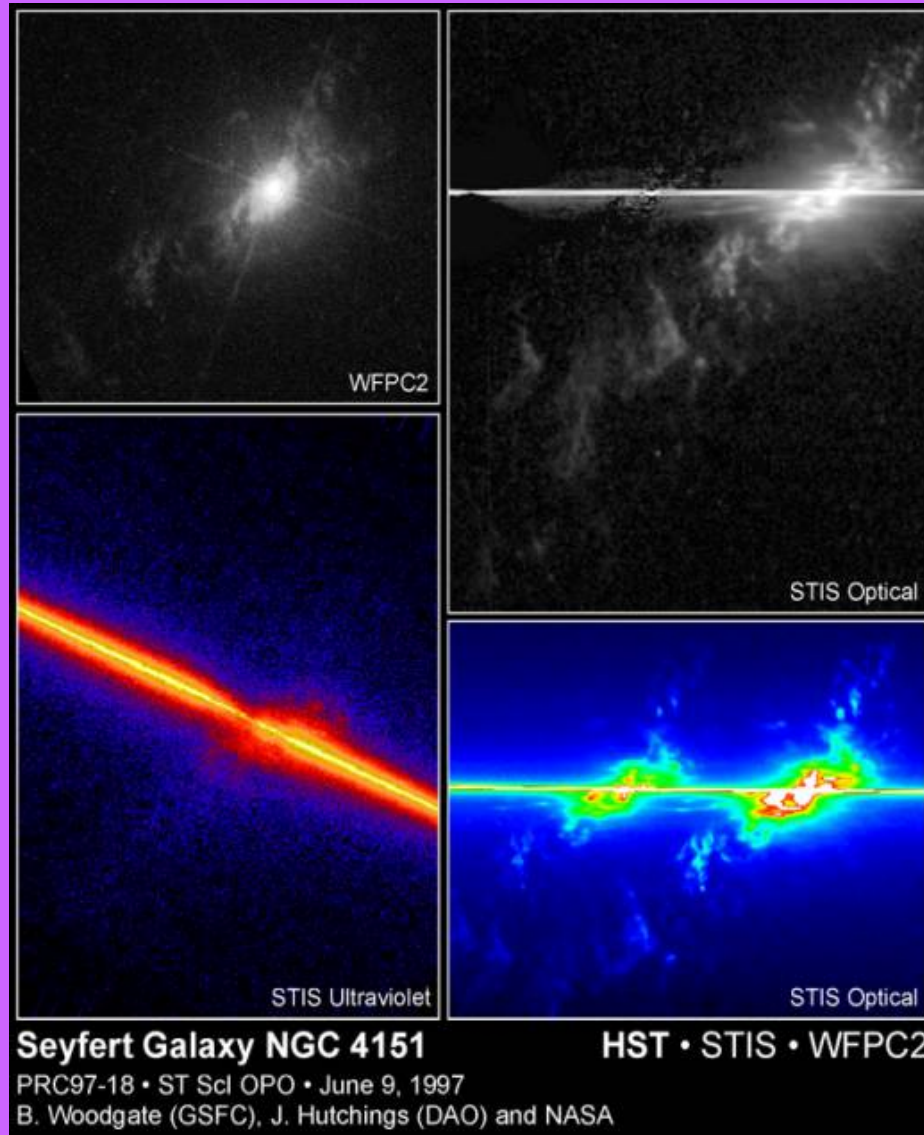


Many galaxies are assumed to have the black holes in their centers.

The black hole masses vary from million to dozens of billion Solar mass.

Because of the small size we cannot observe the black hole itself, but can register the emission of the accretion disk, rotating around the black hole.

## Seyfert galaxies and $K\alpha$ line

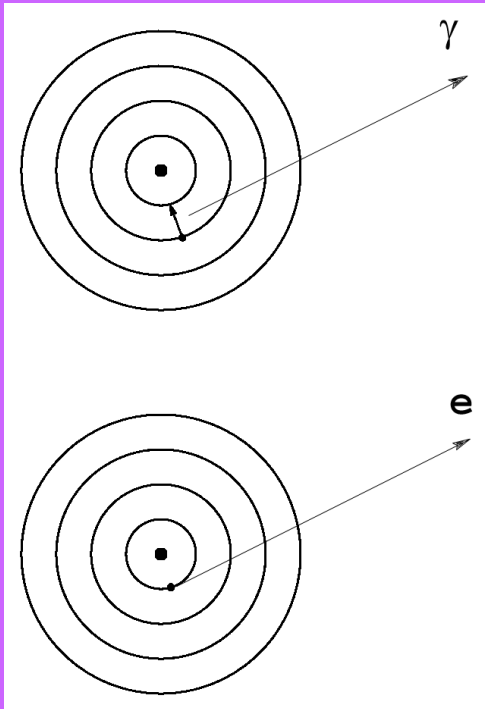


Seyfert galaxies give us a wonderful possibility of direct observations of black holes in their centers.

They often have a wide iron  $K\alpha$  line in their spectra, which seems to arise in the innermost part of the accretion disk close to the event horizon.

Hubble image of Seyfert galaxy NGC 4151 shown at the left.

## Fe K $\alpha$ line origin



$K\alpha$  (6.4 keV) analogous to  $L\alpha$  in hydrogen,  
electron transition to the lowest level

excitation by electronic shock

$h\nu > 7.1$  keV neutral iron  
photoionization and recombination

Fe XXV, XXVI – 6.9 keV hydrogen-like Fe



## Emission lines in Seyfert galaxies

O VIII	0.653 keV	Fe L	0.7– 0.8 keV
Ne IX	0.915 keV	Ne X	1.02 keV
Fe L	1.03 – 1.25 keV	Mg XI	1.34 keV
Mg XII	1.47 keV	Si XIII	1.85 keV
Si XIV	2.0 keV	S XIV	2.35 keV
S XV	2.45 keV	S XVI	2.62 keV
Ar XVII	3.10 keV	Ar XVIII	3.30 keV

Fe I – Fe XVI	6.4 keV
Fe XVII – Fe XXIII	6.5 keV
Fe XXV	6.68 keV
Fe XXVI	6.96 keV

**K  $\alpha$**

Turner, George, Nandra, Mushotzky

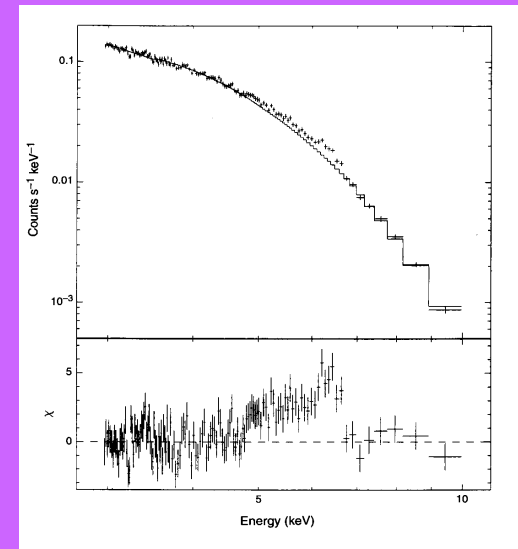
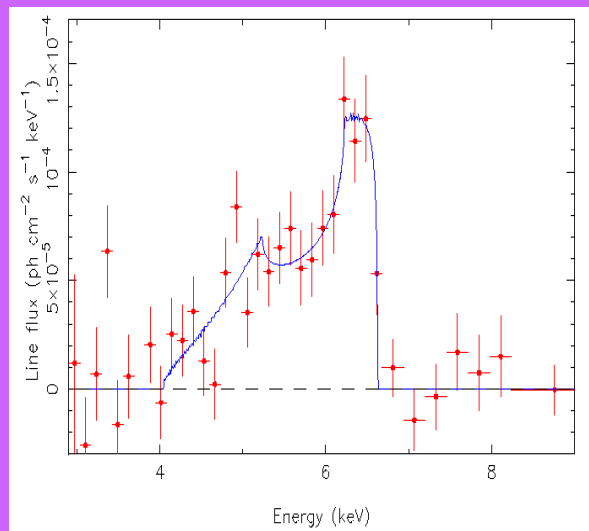
ApJSS, 113, 23, 1997, November

We find a 6.4 keV emission line in 72% of the sample (18 of 25 sources) at the 99% confidence level. The 5 – 7 keV regime is dominated by emission from neutral iron (< Fe XVI).

# Observations

Tanaka, Nandra, Fabian. Nature, 1995, **375**, 659.  
Galaxy MCG-6-30-15, ASCA satellite, SIS detectors

## Sy 1 type



The line profile of iron K $\alpha$  line in  
X-ray emission from MCG-6-30-15.

Width corresponds to 80000 – 100000 km/s.

- **Variability**

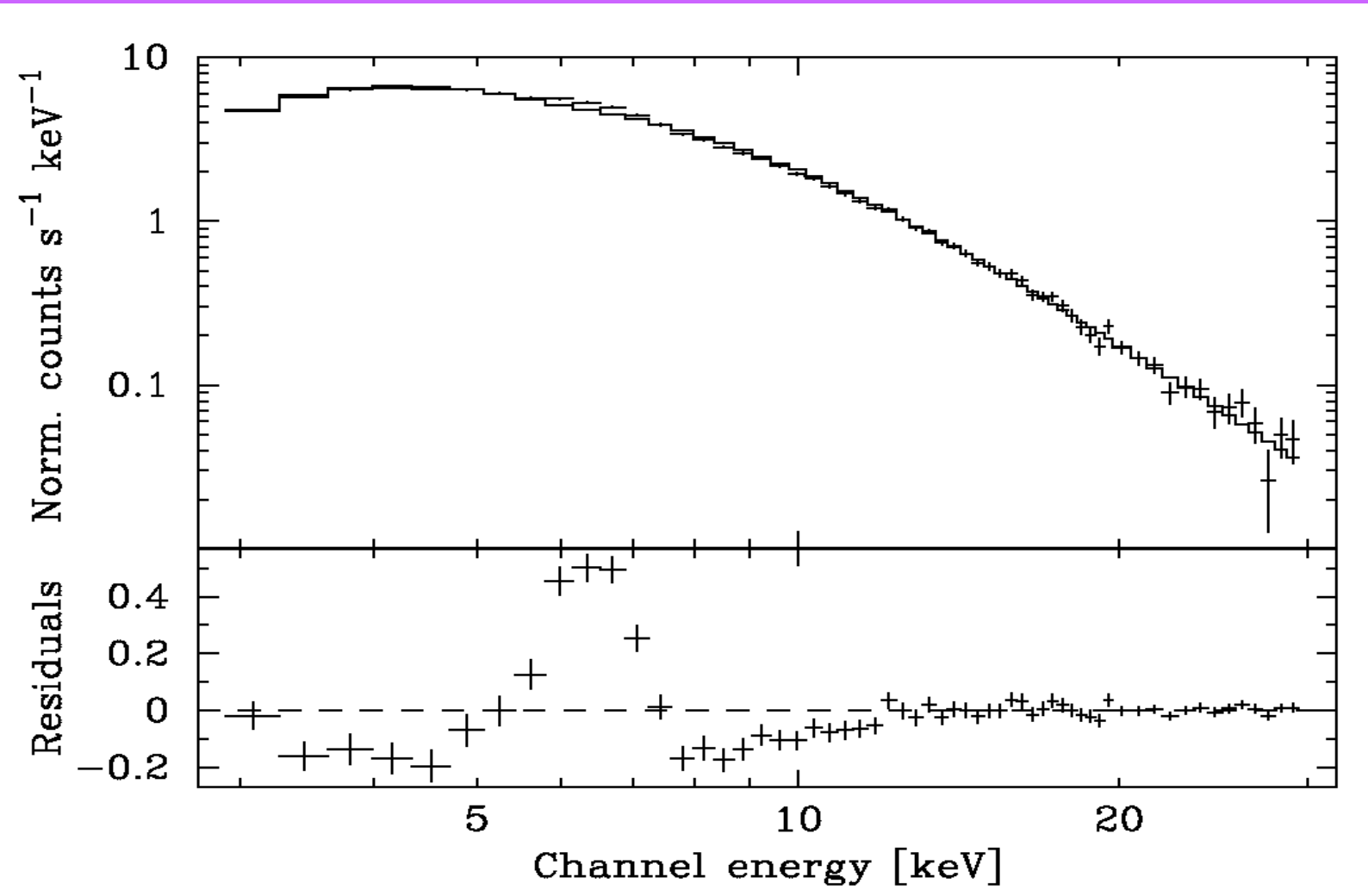
Sulentic, Marziani, Calvani. ApJL, 1998, **497**, L65.



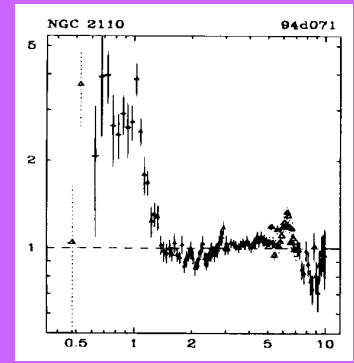
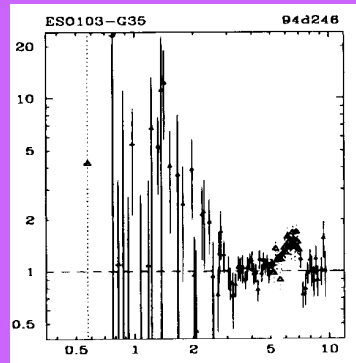
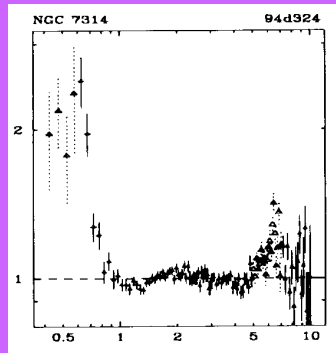
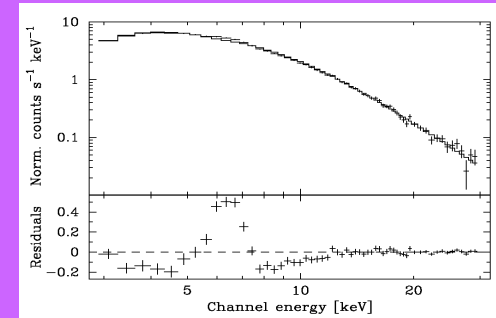
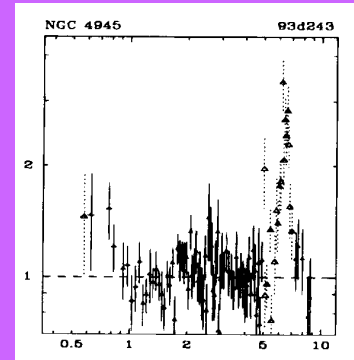
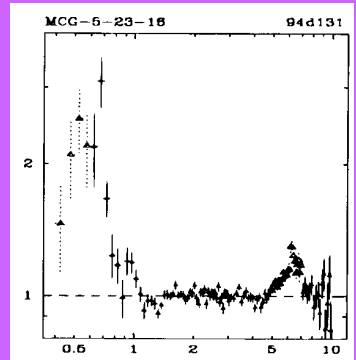
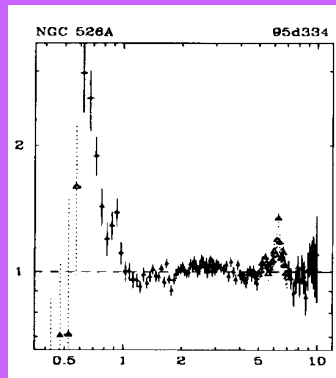
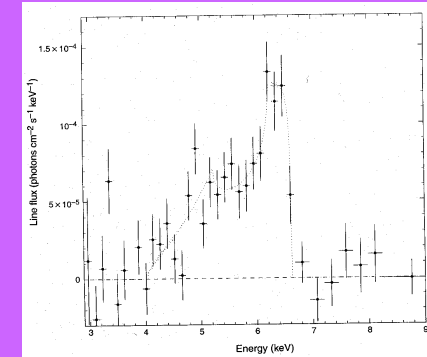
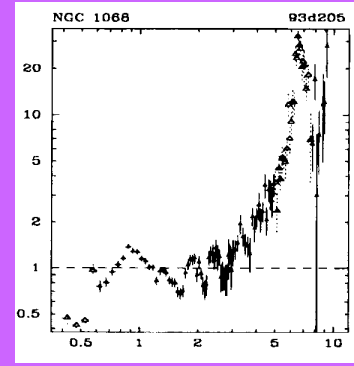
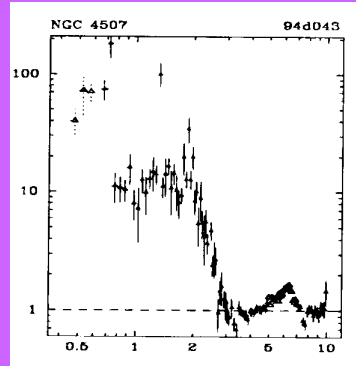
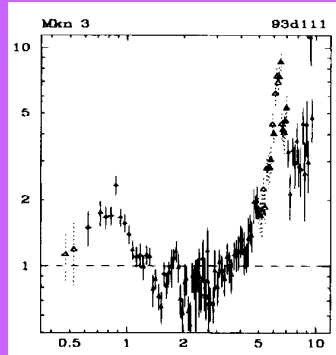
# Observations

Weaver, Krolik, Pier. ApJ, 1998, **498**, 213. (astro-ph / 9712035).

MCG-5-23-16  $K\alpha$  FWHM = 48000 km/s RXTE observations (launched Dec.95)



# ASCA observations. Seyfert 2 galaxies.



Turner, George,  
Nandra, Mushotzky,  
ApJSS, **113**, 23, 1997.

## Properties of wide lines at 6.4 keV

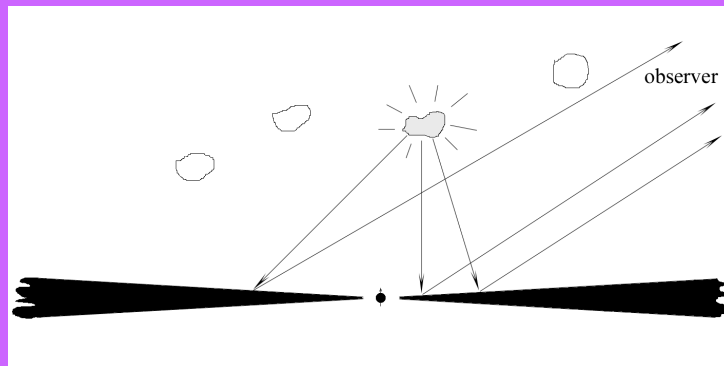
- Line width corresponds to velocity
  - $v \sim 80000 - 100000$  km/s MCG-6-30-15
  - $v \sim 48000$  km/s MCG-5-23-16
  - $v \sim 20000 - 30000$  km/s many other galaxies
- Asymmetric structure (profile)
  - two-peak shape
  - narrow bright **blue** wing
  - wide faint **red** wing
- Variability of both
  - line shape
  - intensity

## Possible interpretation

- iron  $K\alpha$  emission line
  - 6.4 – 6.9 – 7.1 keV
- radiation of inner part of accretion disk around a supermassive **black hole** in the center of the galaxy

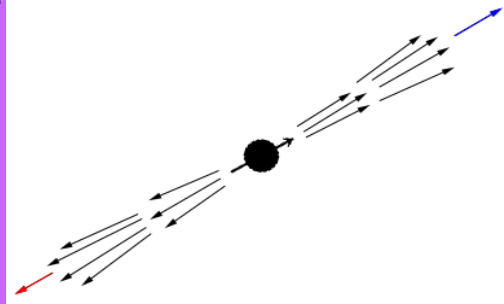
r emission  $\sim 1 - 4 r_g$

$$r_g = \frac{2km}{c^2}$$



# Interpretation

## 1. Jets



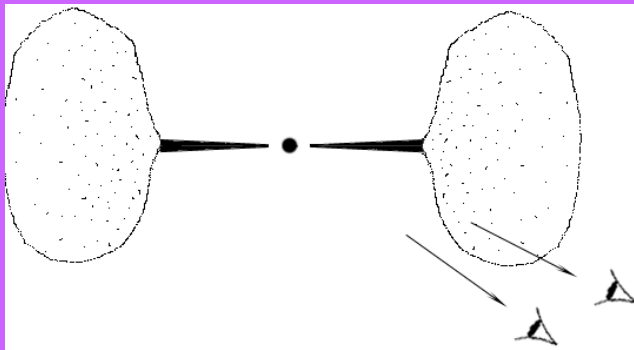
observer



? Blue shift has never been seen

? Broad red wing

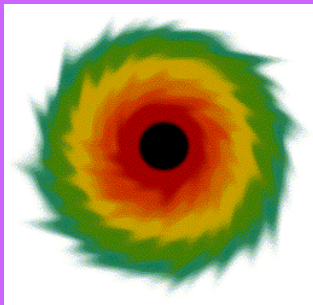
## 2. Multiple Compton scattering



? Line profile

? High frequency variability

## 3. Accretion disk



!!! Line profile !!!

Variability !

## Equations of motion

Kerr metric

$$ds^2 = -\frac{\Delta}{\rho^2} (dt - a \sin^2 \theta d\phi)^2 + \frac{\rho^2}{\Delta} dr^2 + \rho^2 d\theta^2 +$$
$$+ \frac{\sin^2 \theta}{\rho^2} [(r^2 + a^2) d\phi - a dt]^2$$

or

$$ds^2 = -\left(1 - \frac{2Mr}{\rho^2}\right) dt^2 + \frac{\rho^2}{\Delta} dr^2 + \rho^2 d\theta^2 +$$
$$+ \left(r^2 + a^2 + \frac{2Mra^2}{\rho^2} \sin^2 \theta\right) \sin^2 \theta d\phi^2 - \frac{4Mra}{\rho^2} \sin^2 \theta d\phi dt,$$

## Equations of motion

Equations of photon motion:

$$\begin{aligned}\frac{dt}{d\lambda} &= -\frac{r_g r a}{\rho^2 \Delta} L + \frac{\omega_0}{\Delta} \left( r^2 + a^2 + \frac{r_r r a^2}{\rho^2} \sin^2 \theta \right) \\ \frac{d\phi}{d\lambda} &= \frac{L}{\Delta \sin^2 \theta} \left( 1 - \frac{r_g r}{\rho^2} \right) + \frac{r_g r a}{\rho^2 \Delta} \omega_0 \\ \left( \frac{dr}{d\lambda} \right)^2 &= \frac{1}{\rho^4} \left[ (r^2 + a^2) \omega_0 - aL \right] - \frac{K\Delta}{\rho^4} \\ \left( \frac{d\theta}{d\lambda} \right)^2 &= \frac{K}{\rho^4} - \frac{1}{\rho^4} \left[ a \omega_0 \sin \theta - \frac{L}{\sin \theta} \right]^2\end{aligned}$$

where

$$\begin{aligned}\Delta &= r^2 - r_g r + a^2, & \rho^2 &= r^2 + a^2 \cos^2 \theta, \\ r_g &= 2km, & a &= M/m\end{aligned}$$



## Equations of motion

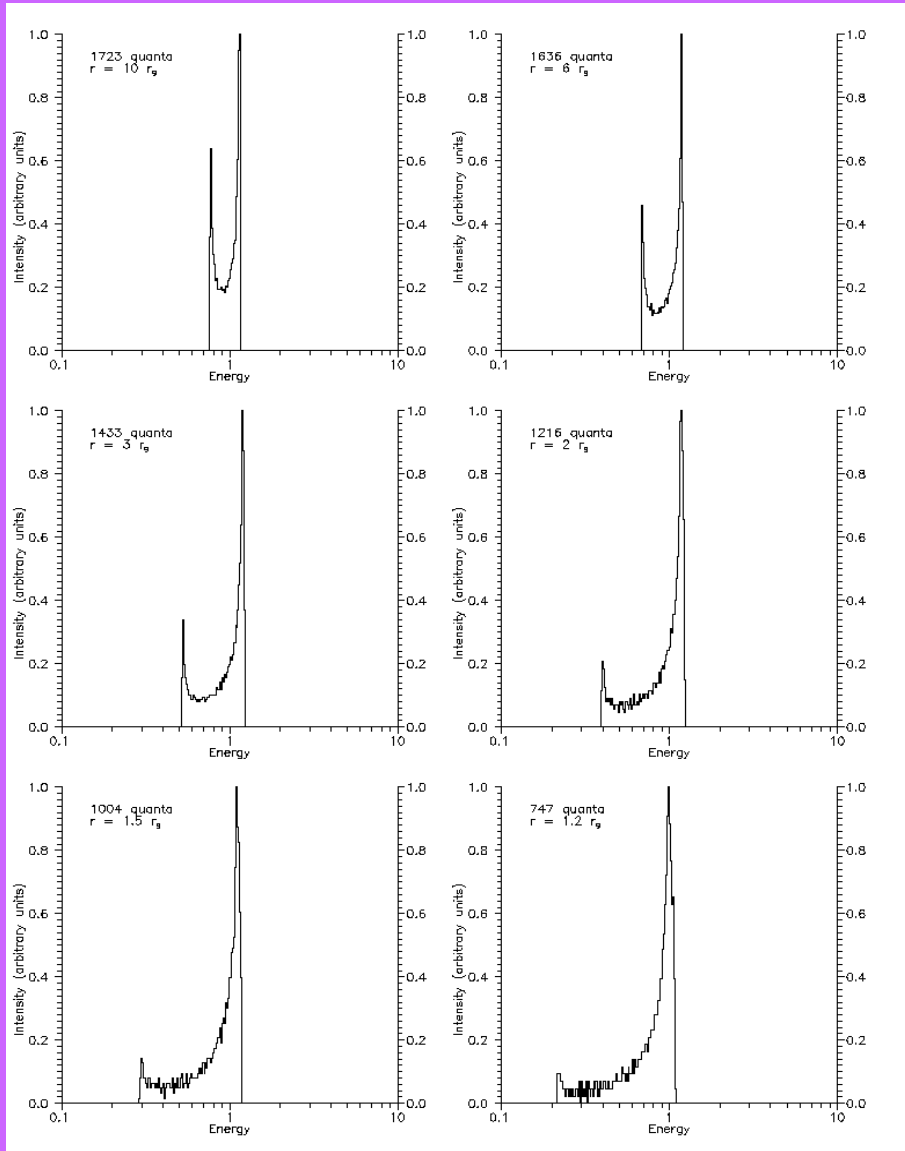
For numerical solution the system should be replaced with

$$\begin{aligned}\frac{dt'}{d\sigma} &= -\hat{a} (\hat{a} \sin^2 \theta - \xi) + \frac{\hat{r}^2 + \hat{a}^2}{\hat{\Delta}} (\hat{r}^2 + \hat{a}^2 - \xi \hat{a}), \\ \frac{d\hat{r}}{d\sigma} &= r_1, \\ \frac{dr_1}{d\sigma} &= 2\hat{r}^3 + (\hat{a}^2 - \xi^2 - \eta) \hat{r} + (\hat{a} - \xi) + \eta, \\ \frac{d\theta}{d\sigma} &= \theta_1, \\ \frac{d\theta_1}{d\sigma} &= \cos \theta \left( \frac{\xi^2}{\sin^3 \theta} - \hat{a}^2 \sin \theta \right), \\ \frac{d\phi}{d\sigma} &= -\left( \hat{a} - \frac{\xi}{\sin^2 \theta} \right) + \frac{\hat{a}}{\hat{\Delta}} (\hat{r}^2 + \hat{a}^2 - \xi \hat{a}).\end{aligned}$$

The system has two integrals:

$$\begin{aligned}\epsilon_1 &\equiv r_1^2 - \hat{r}^4 - (\hat{a}^2 - \xi^2 - \eta) \hat{r}^2 - 2 [(\hat{a} - \xi)^2 + \eta] \hat{r} + \hat{a}^2 \eta = 0, \\ \epsilon_2 &\equiv \theta_1^2 - \eta - \cos^2 \theta \left( \hat{a}^2 - \frac{\xi^2}{\sin^2 \theta} \right) = 0,\end{aligned}$$

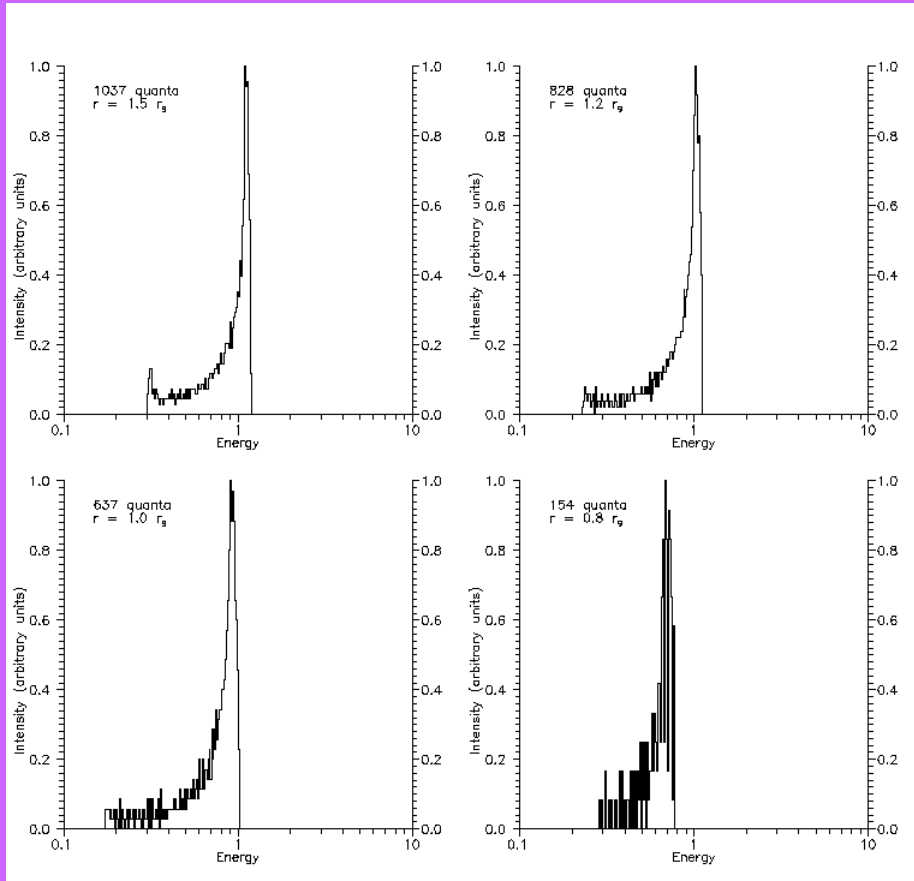
# Simulation result



Spectrum of a hot spot for  $a=0.9$ ,  $\theta=60$  deg. and different values of radial coordinate.

Marginally stable orbit lays at  $r = 1.16 r_g$ .

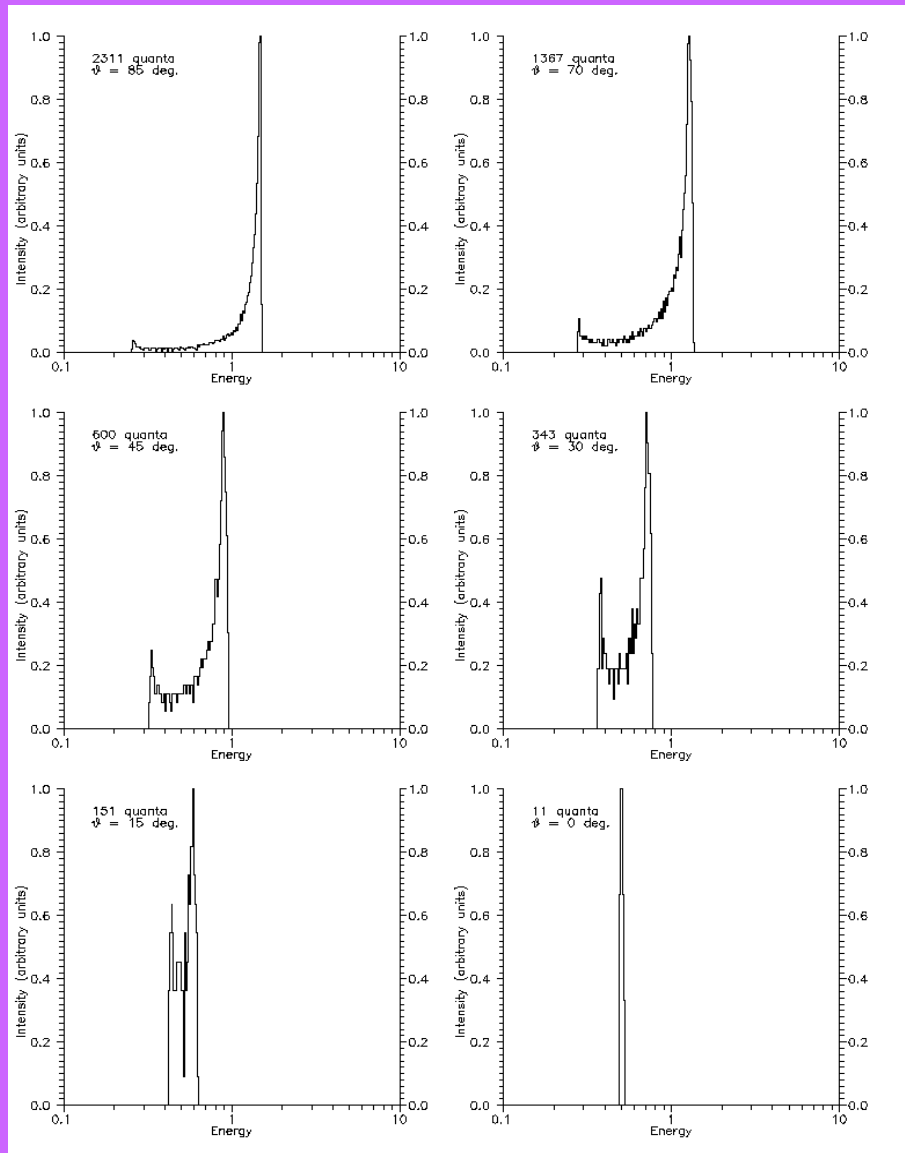
# Simulation result



Spectrum of a hot spot for  $a=0.99$ ,  $\theta=60$  deg. and different values of radial coordinate.

Marginally stable orbit lays at  $r = 0.727 r_g$ .

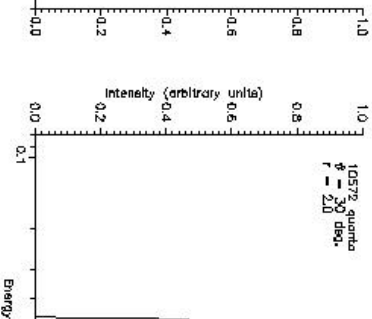
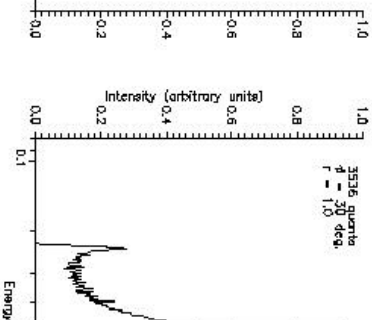
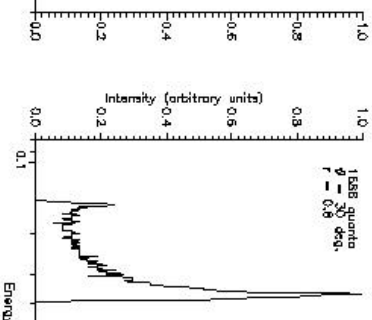
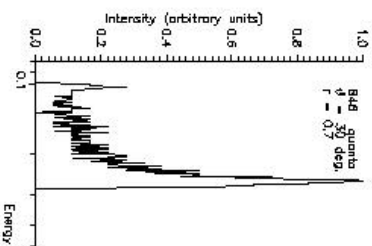
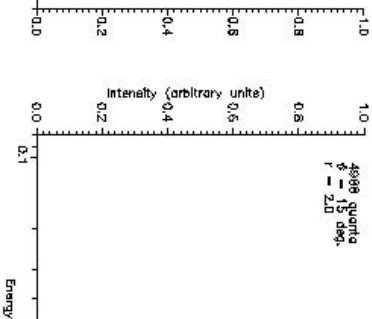
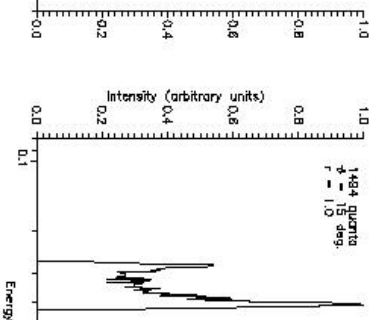
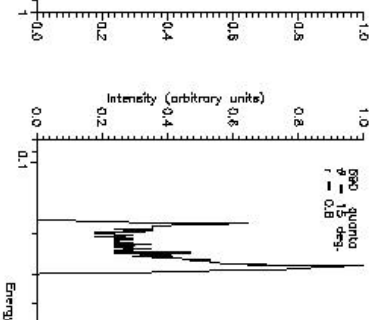
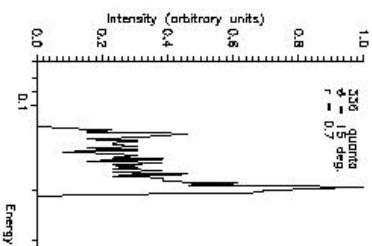
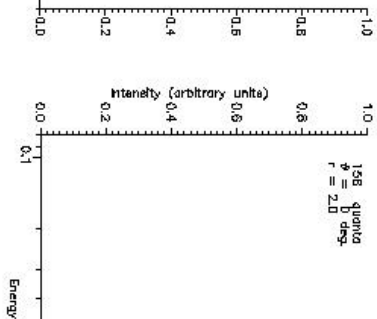
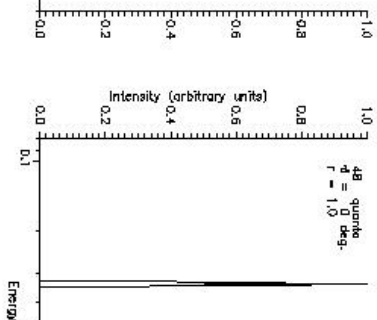
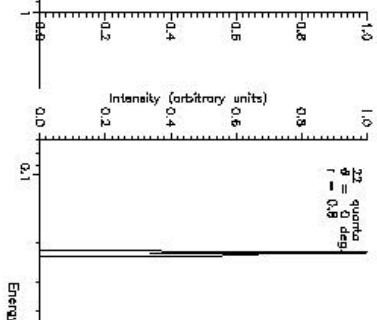
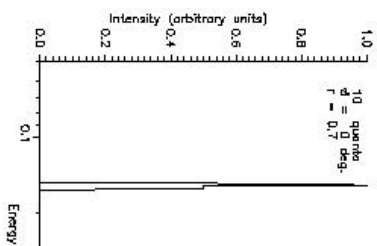
# Simulation result

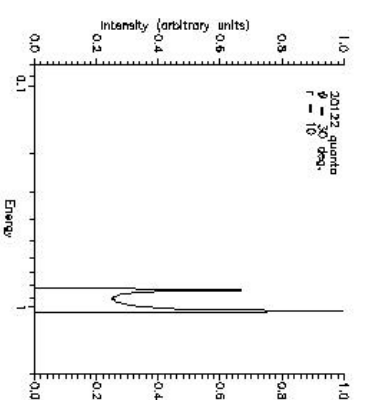
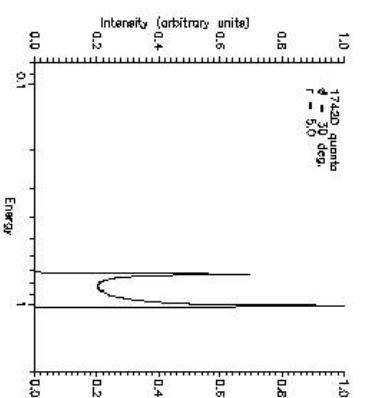
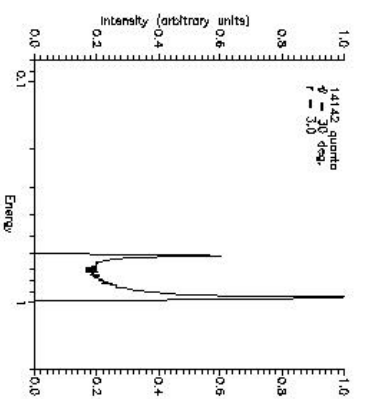
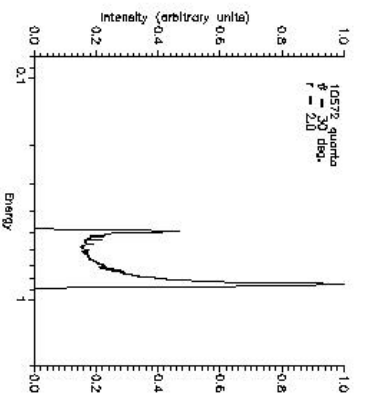
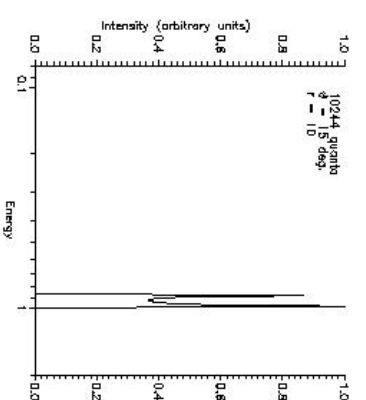
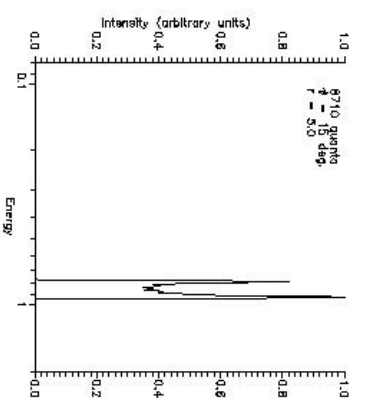
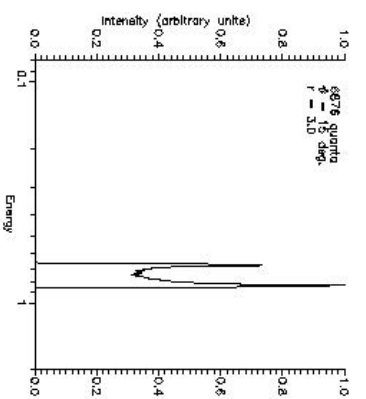
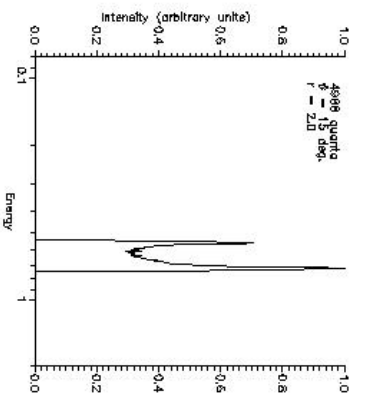
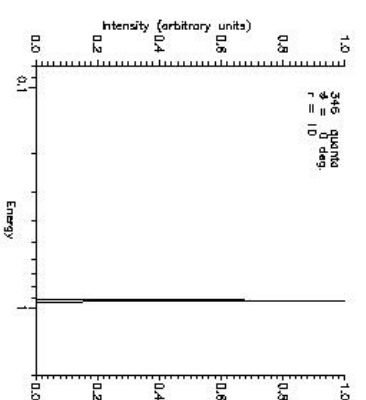
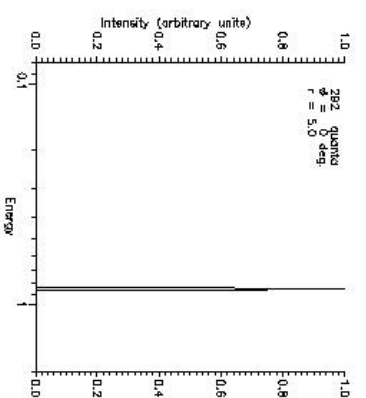
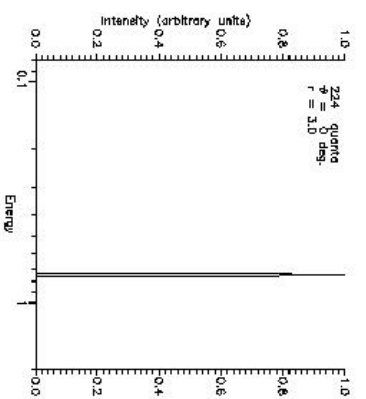
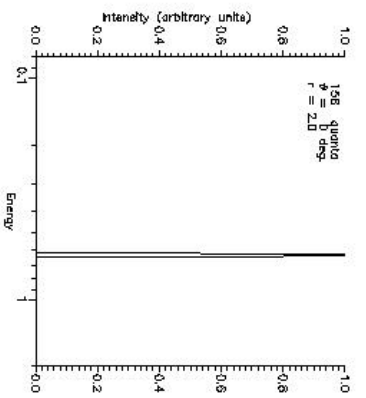


Spectrum of a hot spot for  $a=0.99$ ,  $r = 1.5 r_g$  and different values of  $\theta$  angle.

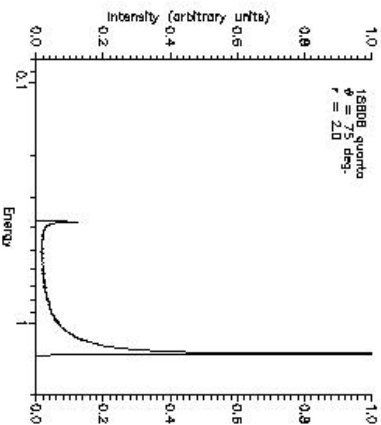
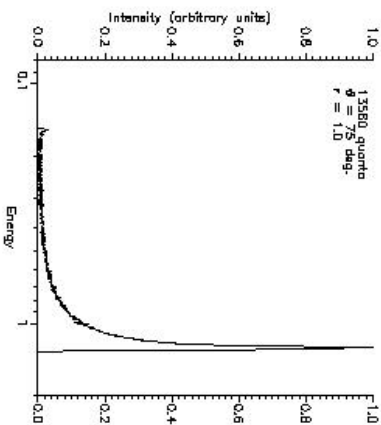
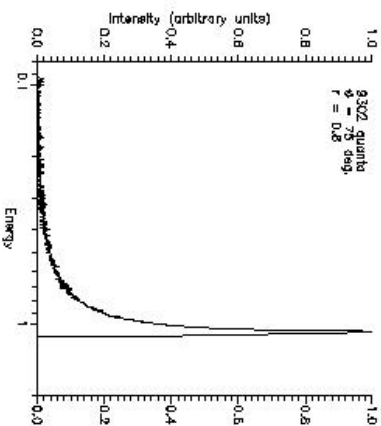
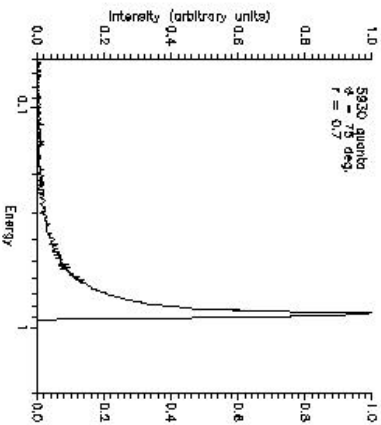
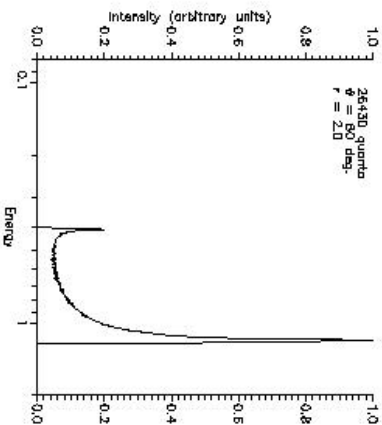
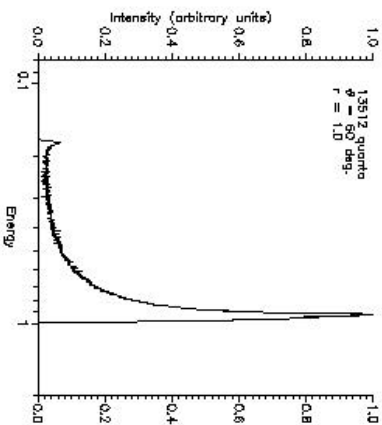
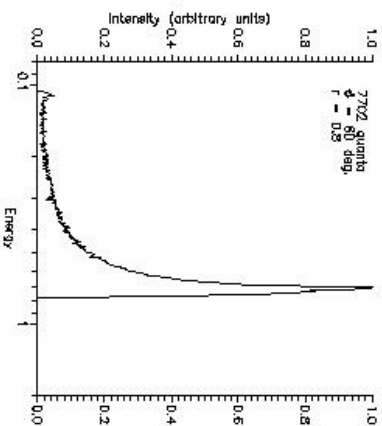
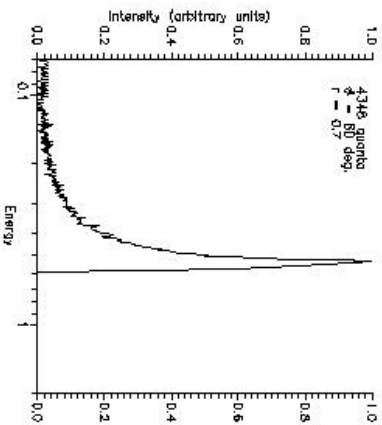
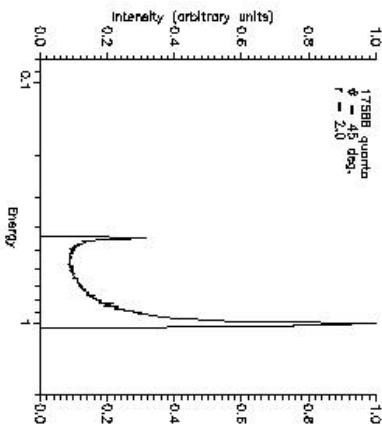
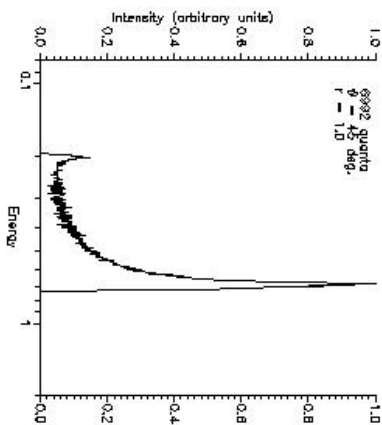
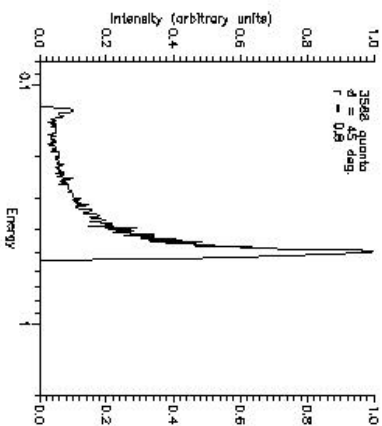
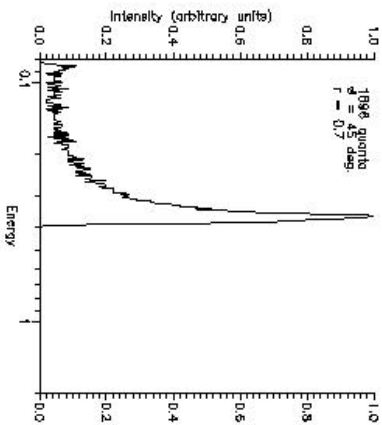
# Gallery of profiles

with S.V. Repin (in preparation)





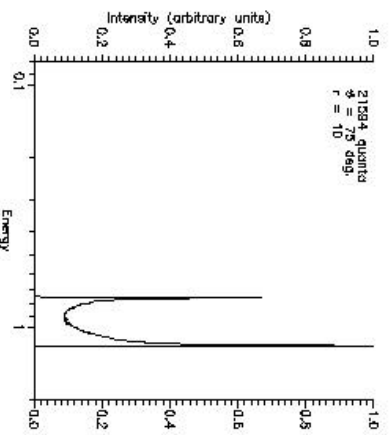
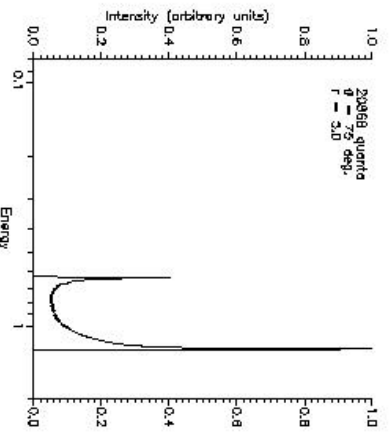
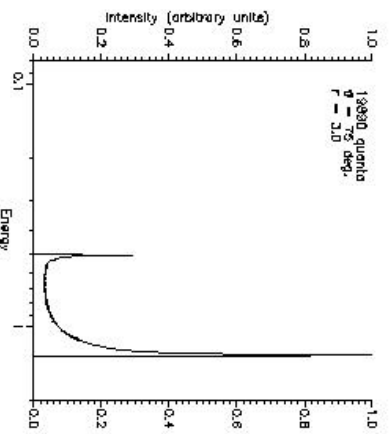
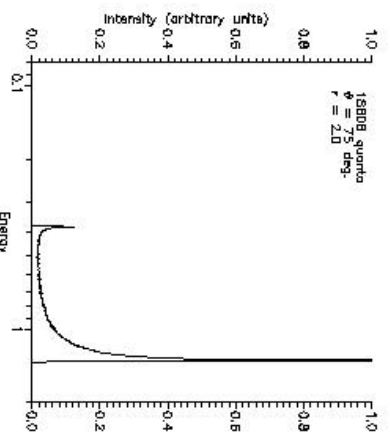
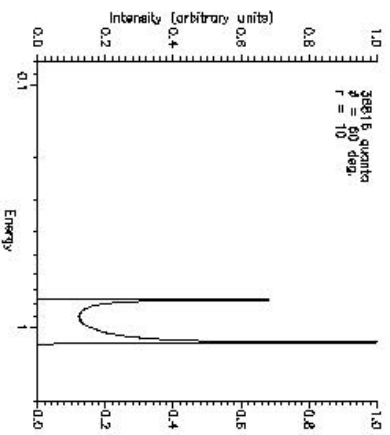
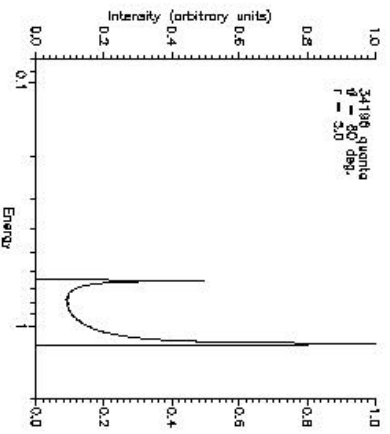
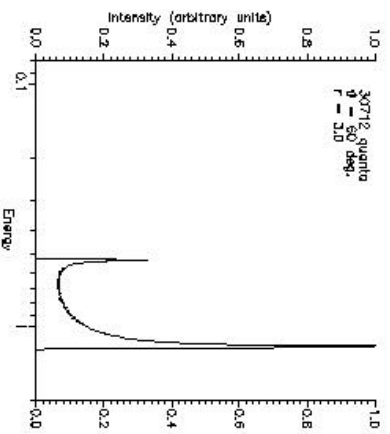
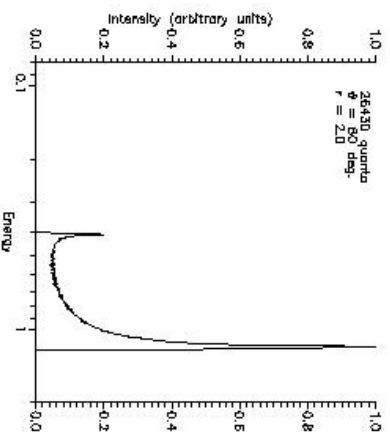
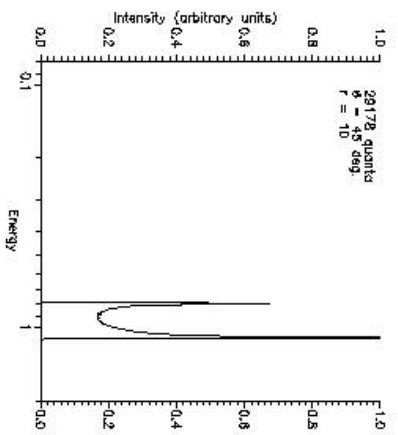
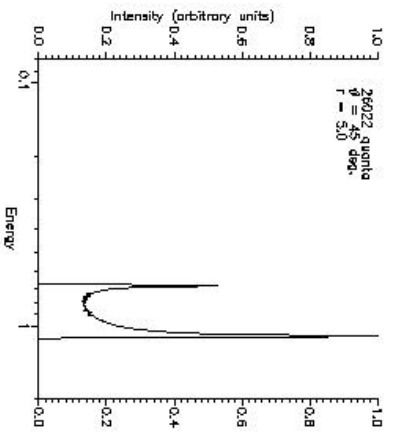
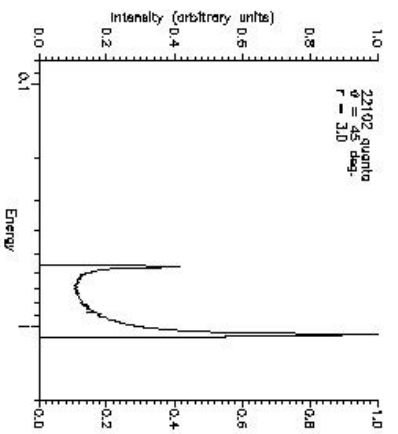
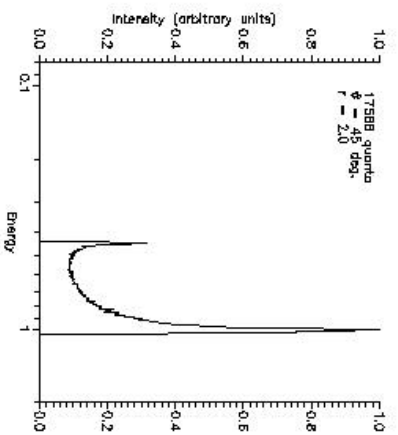


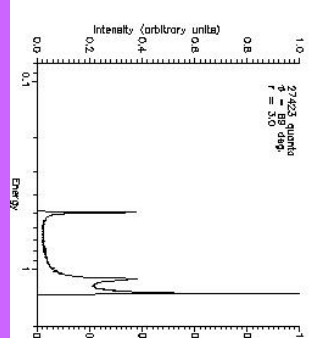
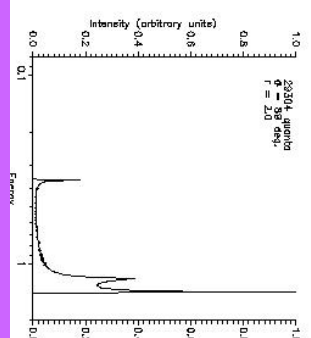
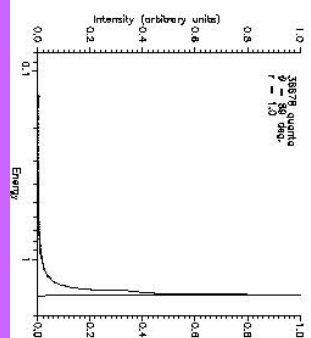
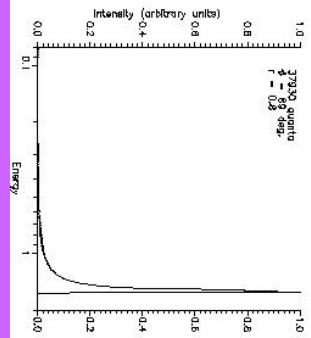
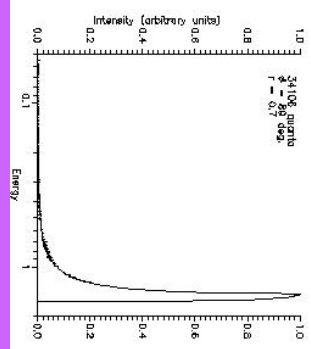
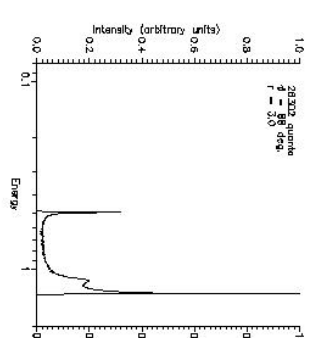
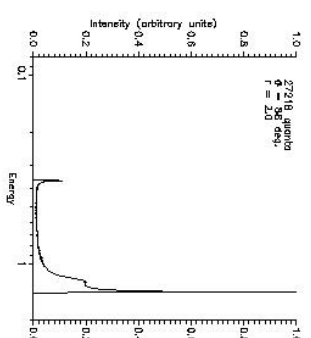
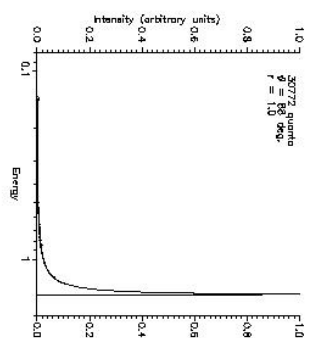
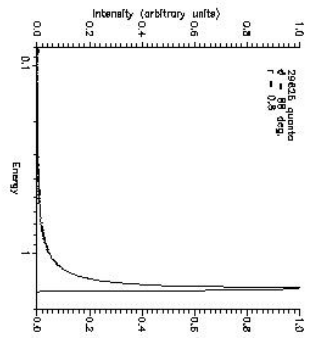
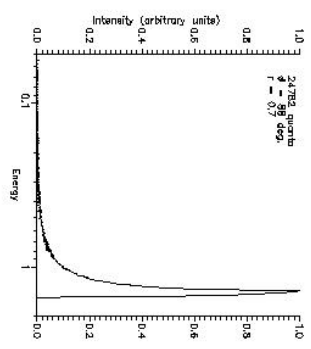
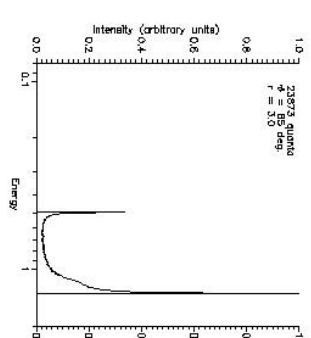
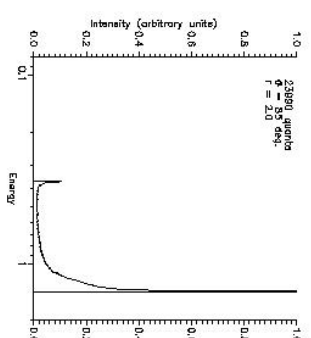
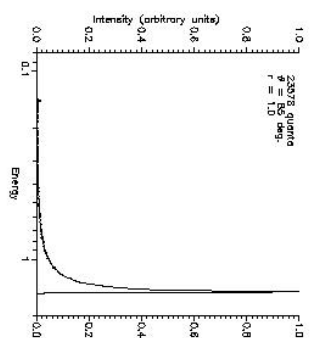
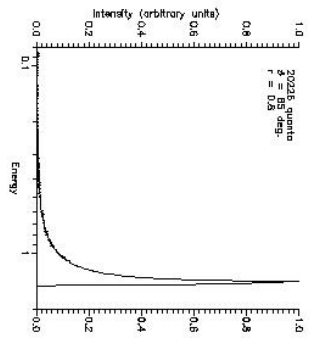
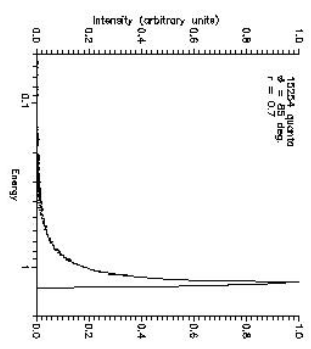
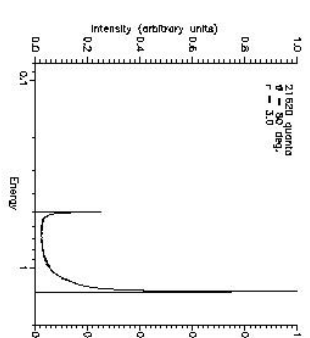
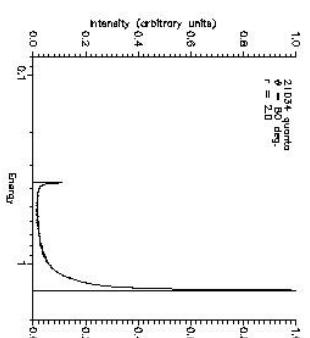
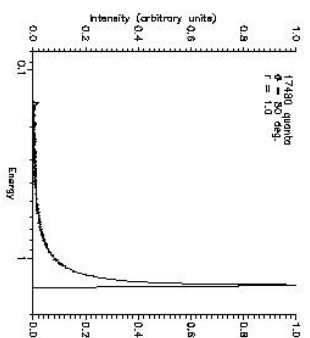
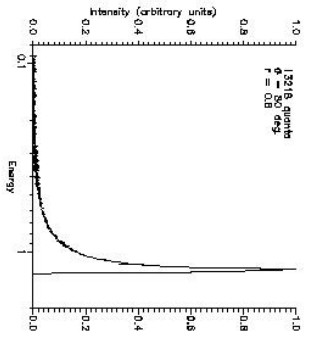
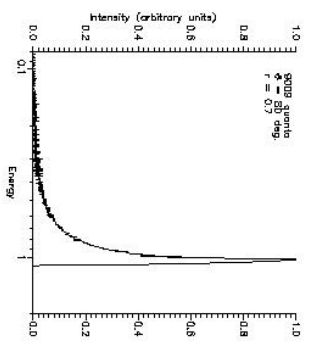


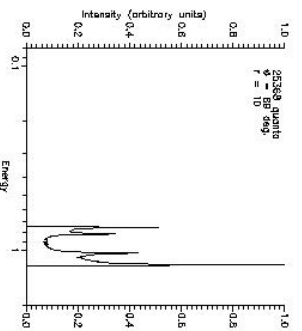
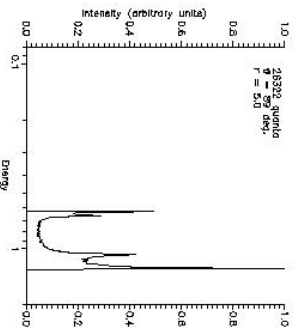
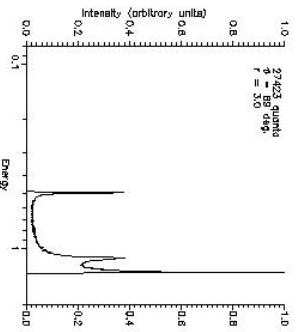
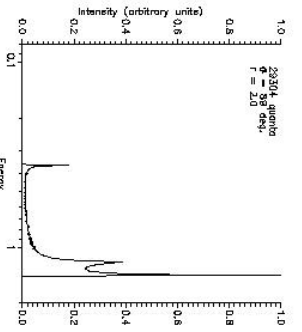
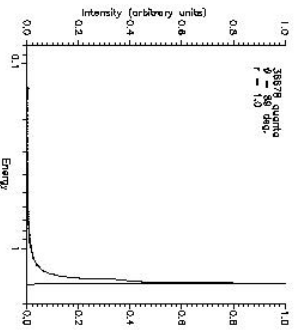
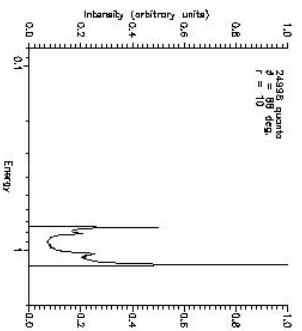
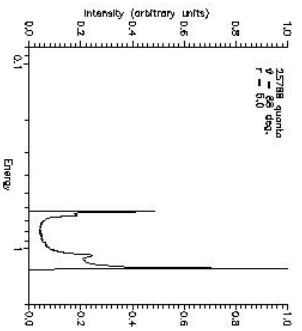
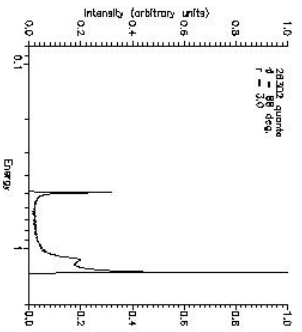
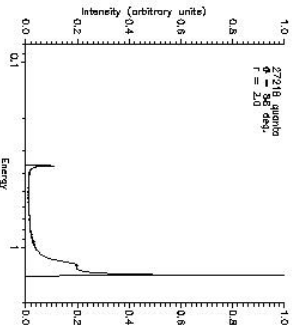
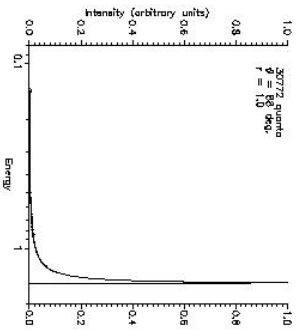
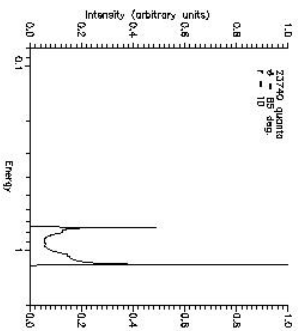
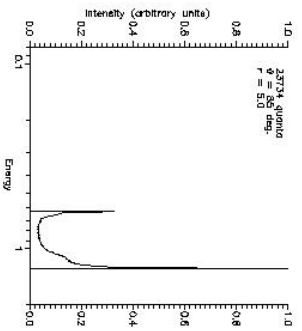
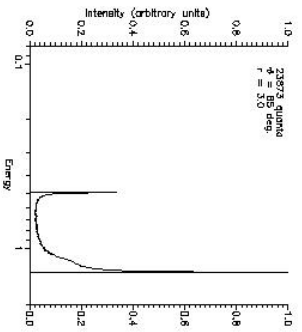
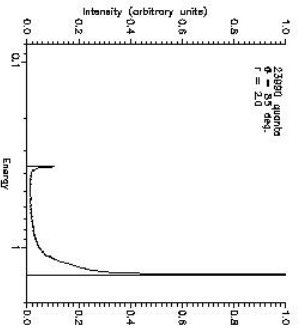
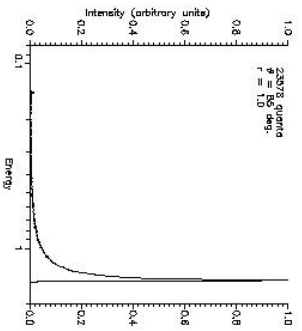
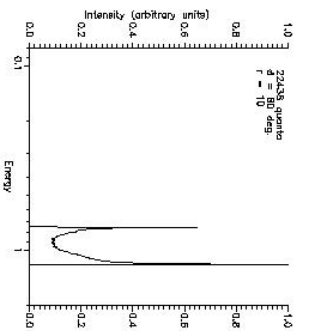
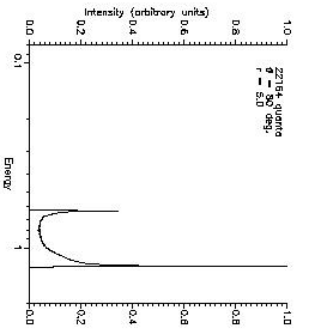
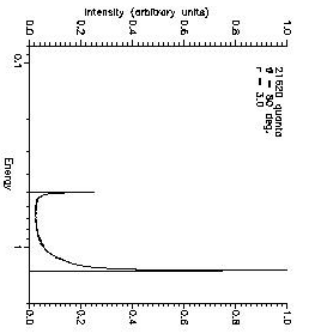
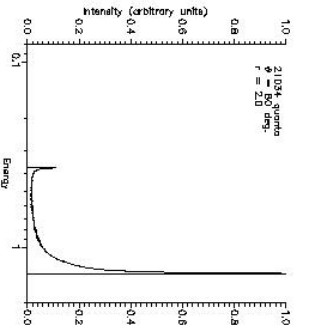
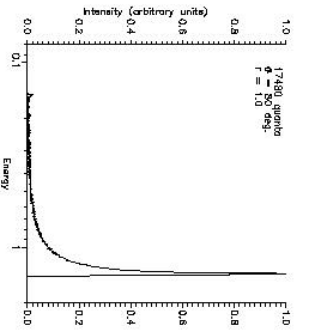
Intensity (arbitrary units)

Intensity (arbitrary units)

Intensity (arbitrary units)







## Rings summation

Classical expression for the ring area

$$dS = 2\pi r dr$$

should be replaced in General Relativity with

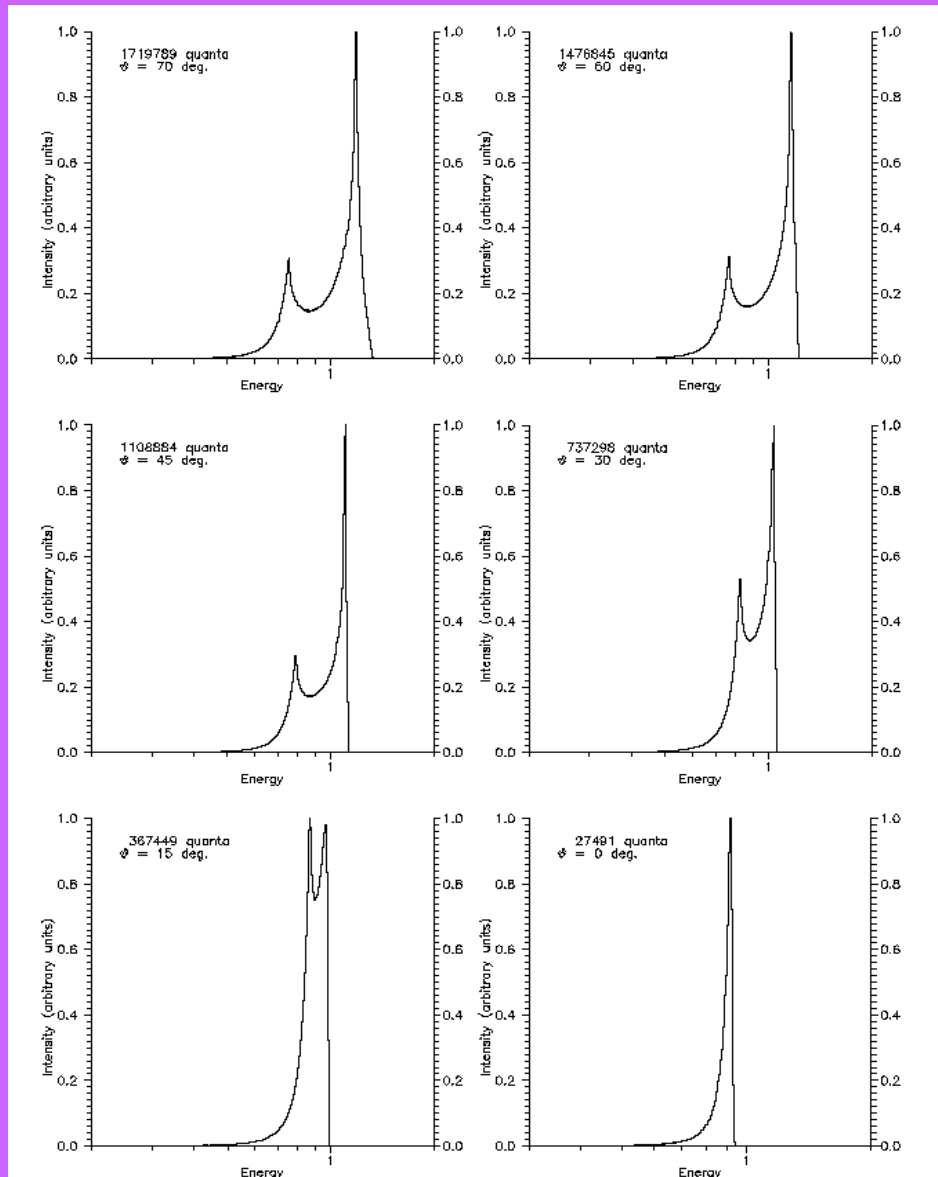
$$dS = \frac{2\pi (r^2 + a^2)}{\sqrt{r^2 - rr_g + a^2}} dr$$

where

$$f_{GR} = \frac{r^2 + a^2}{r \sqrt{r^2 - rr_g + a^2}}$$

is the additional relativistic factor, appearing due to the frame dragging.

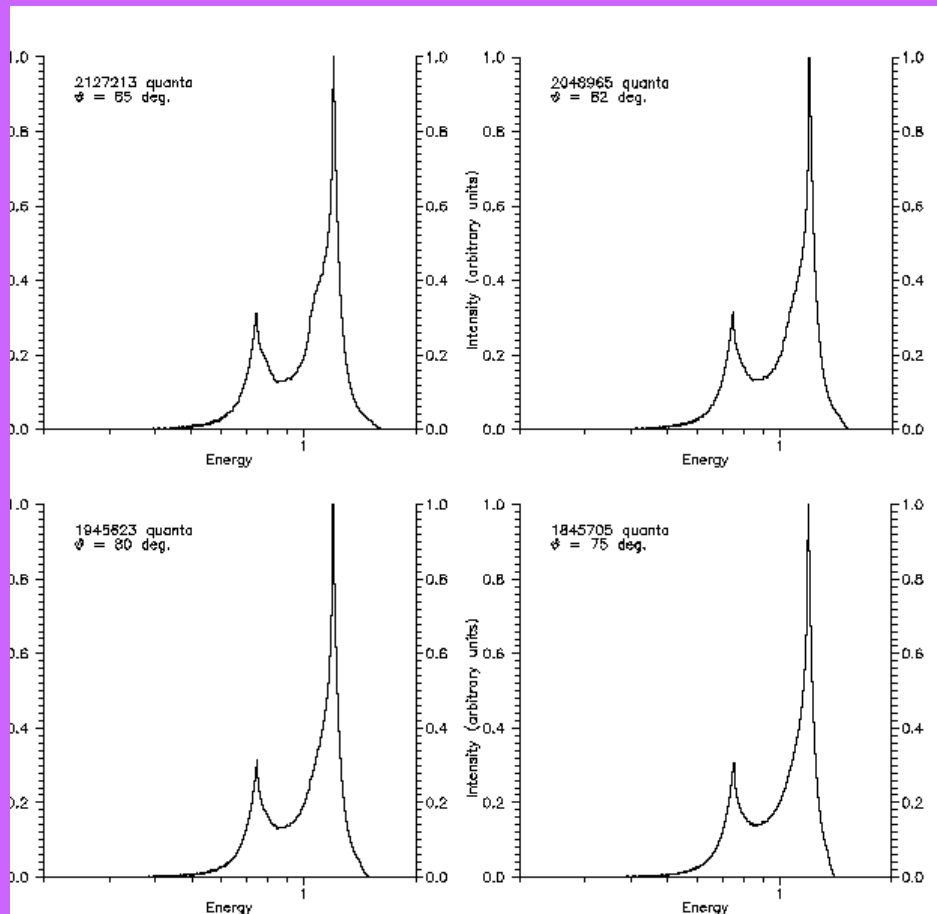
# Simulation result



Spectrum of Fe K $\alpha$  line in isothermal disk with  $a = 0.9$  and emission region between  $10 r_g$  and marginally stable orbit at  $1.16 r_g$ .

The figure presents the dependence on  $\theta$  angle.

# Simulation result

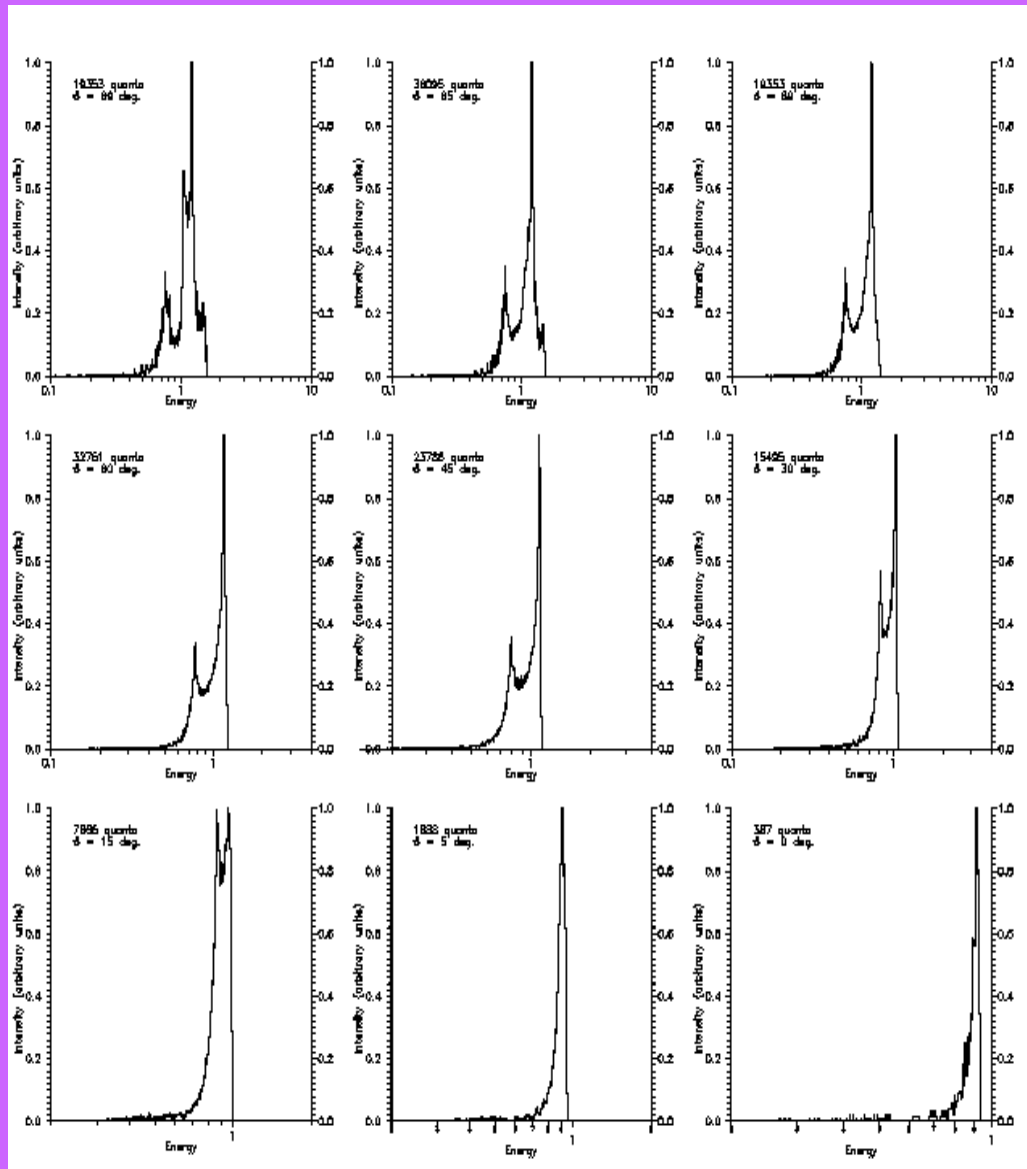


Spectrum of Fe K $\alpha$  line in isothermal disk with  $a = 0.9$  and emission region between  $10 r_g$  and marginally stable orbit at  $1.16 r_g$ .

The figure presents the dependence on  $\theta$  angle (large  $\theta$  values).



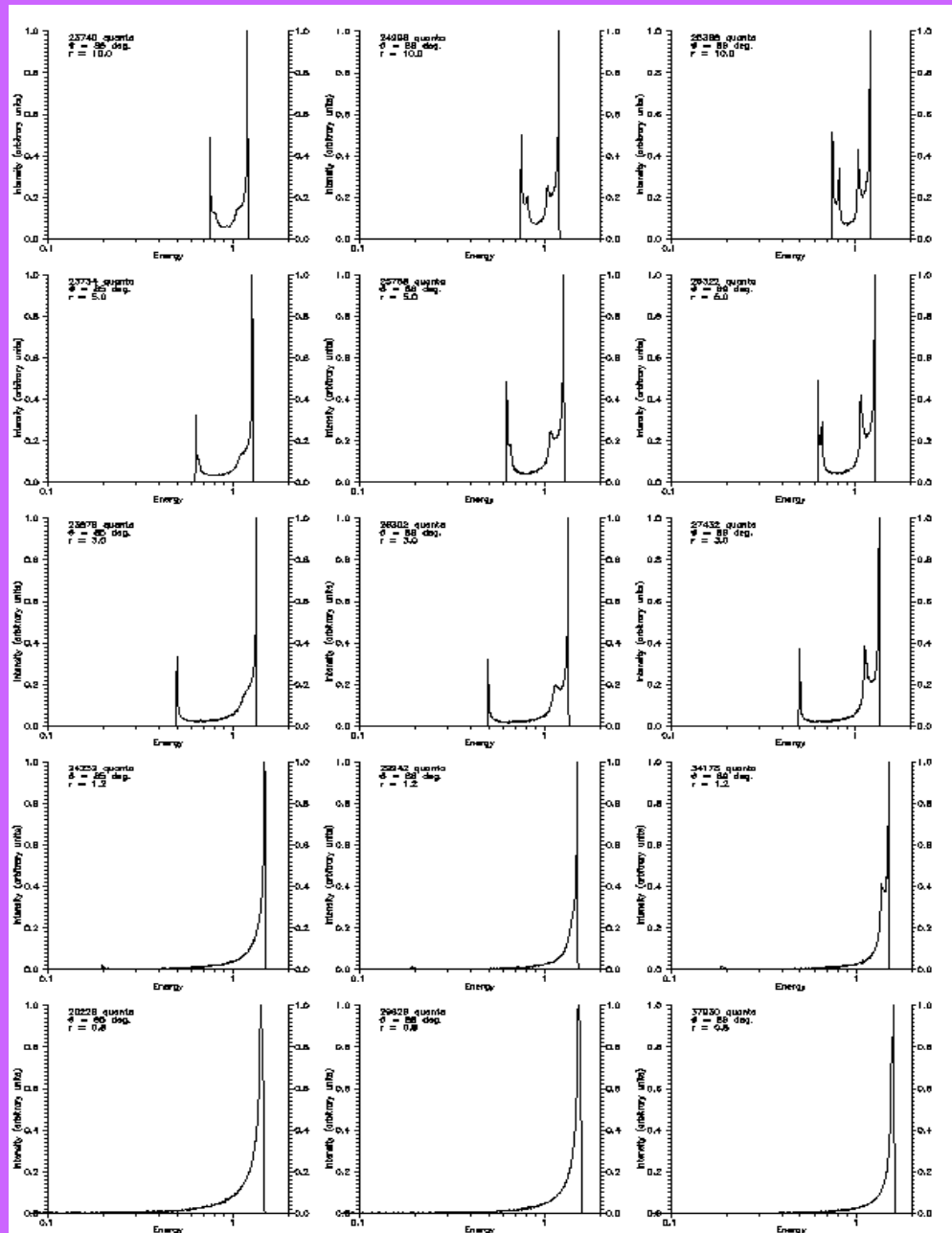
# Simulation result



Spectrum of Fe K $\alpha$  line in isothermal disk with  $a = 0.99$  and emission region between  $10 r_g$  and marginally stable orbit at  $0.727 r_g$ .

At large  $\theta$  one can see the lensing effect.

# Simulation result

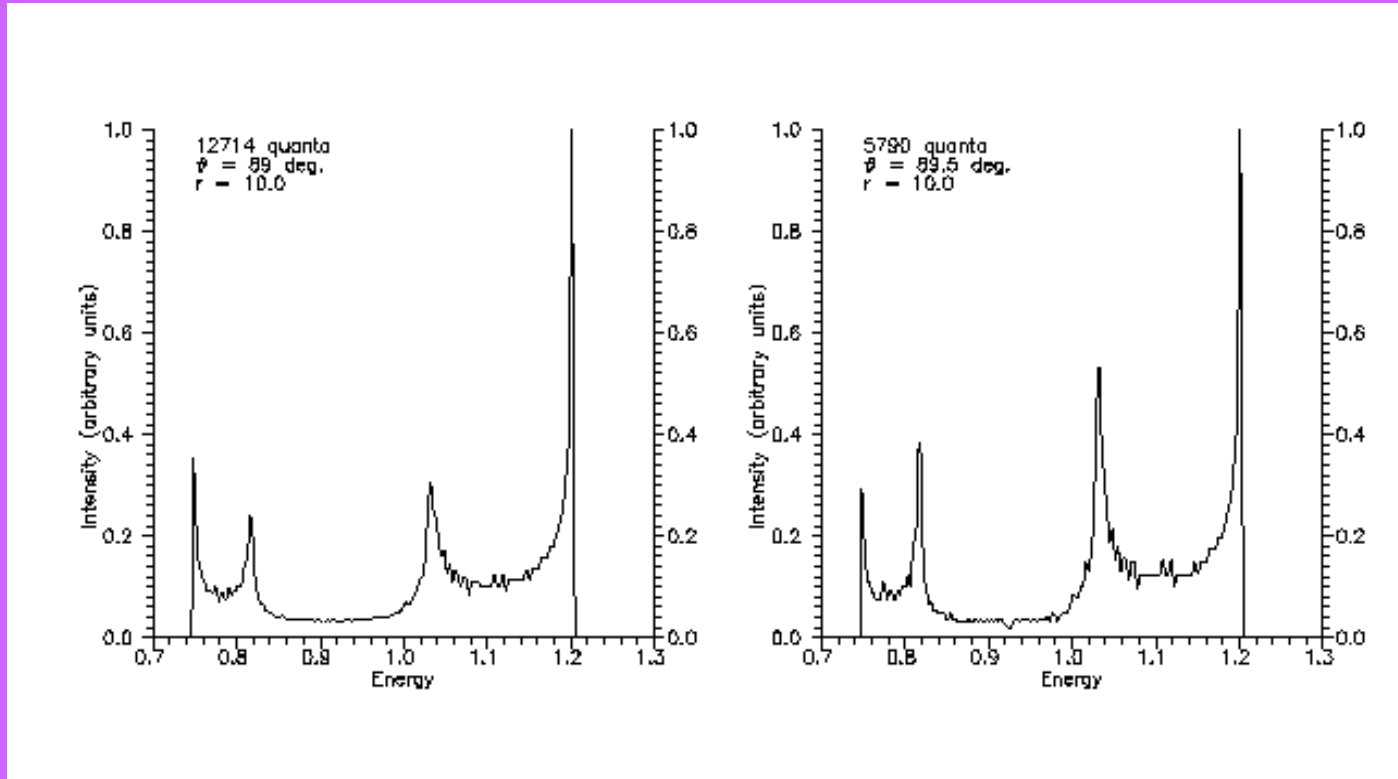


Overview of possible line profiles of a hot spot for different values of radial coordinate and inclination angle.

The radial coordinate decreases from  $10 r_g$  on the top to  $0.8 r_g$  on the bottom. The inclination angle increases from 85 degrees in the left column to 89 degrees in the right.

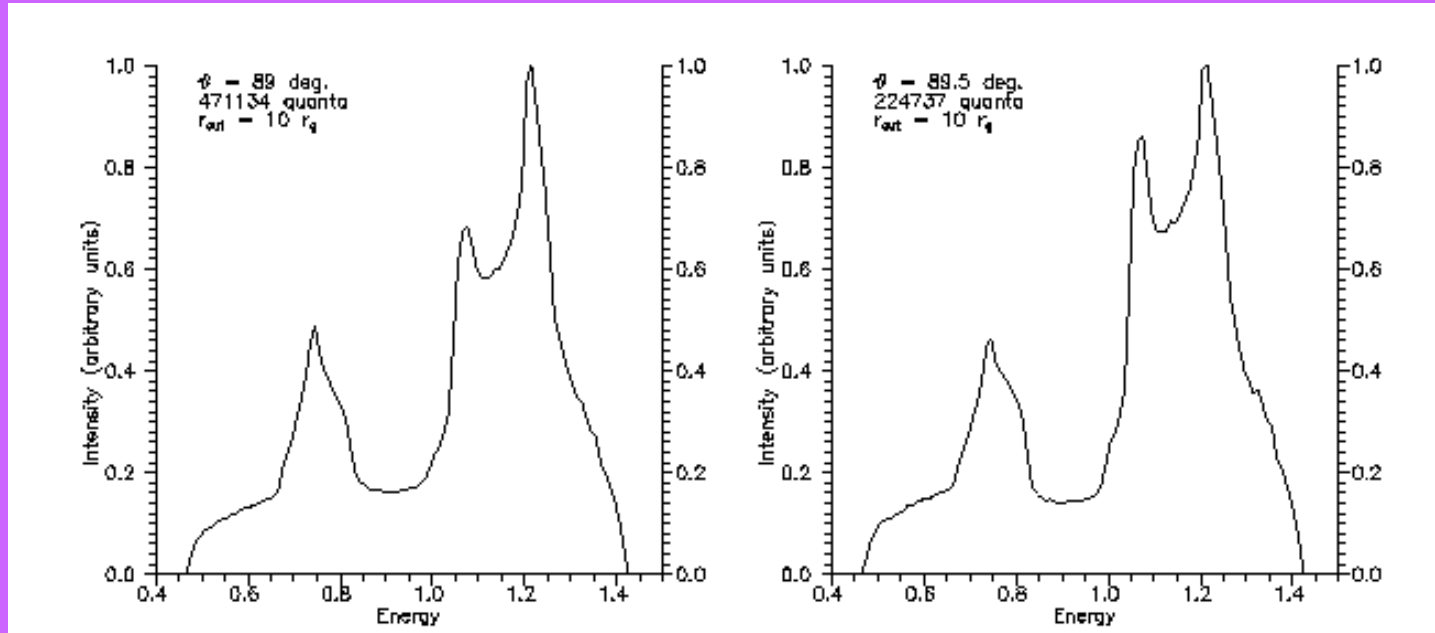
Zakharov A.F, Repin S.V. A&A, 2003, 406, 7.

## Simulation result



Spectrum of a hot spot rotating at the distance  $10 r_g$  and observed at large inclination angles. Left panel includes all the quanta with  $\theta > 89$  degrees. The right one includes the quanta with  $\theta > 89.5$  degrees.

## Simulation result

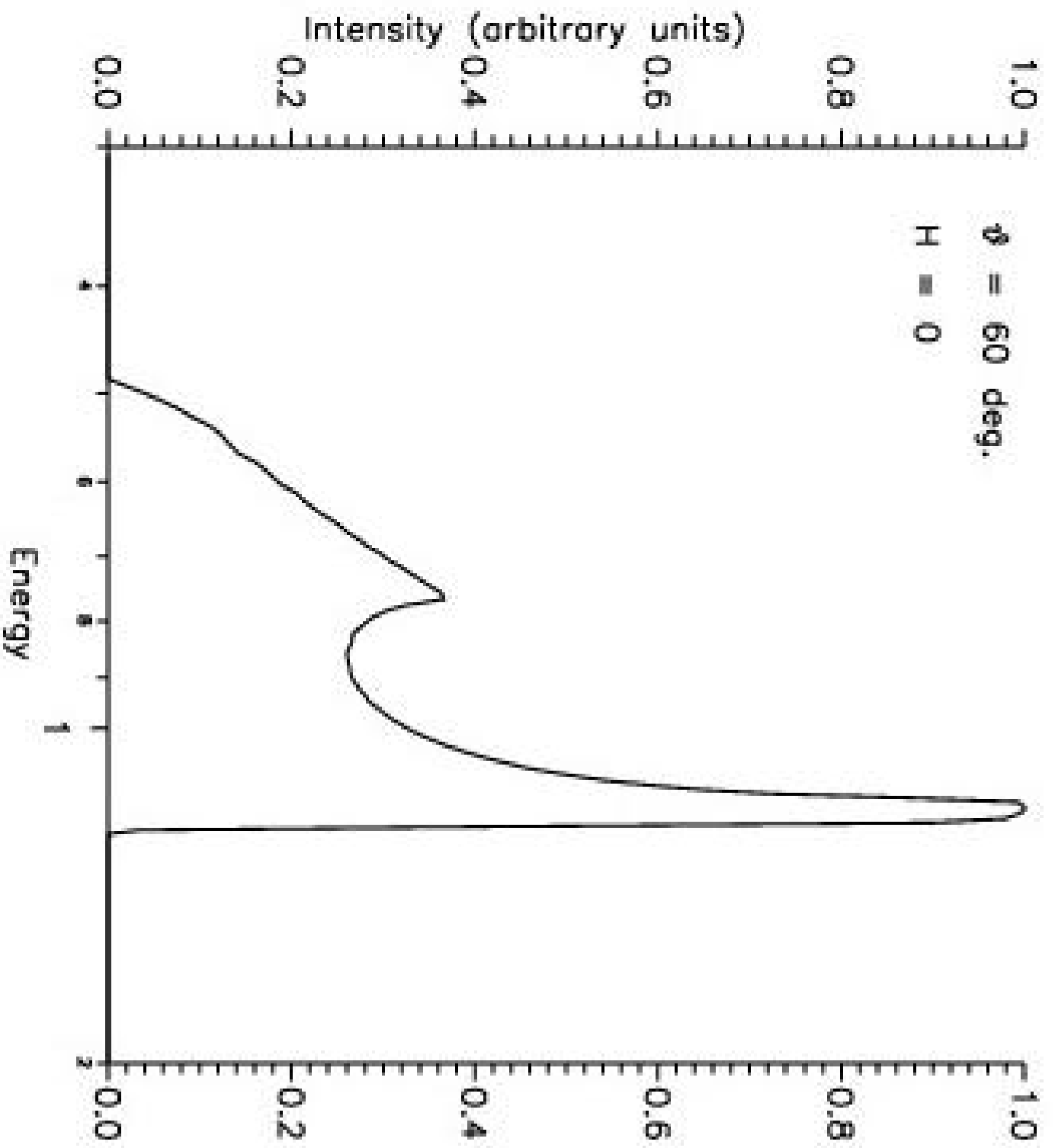


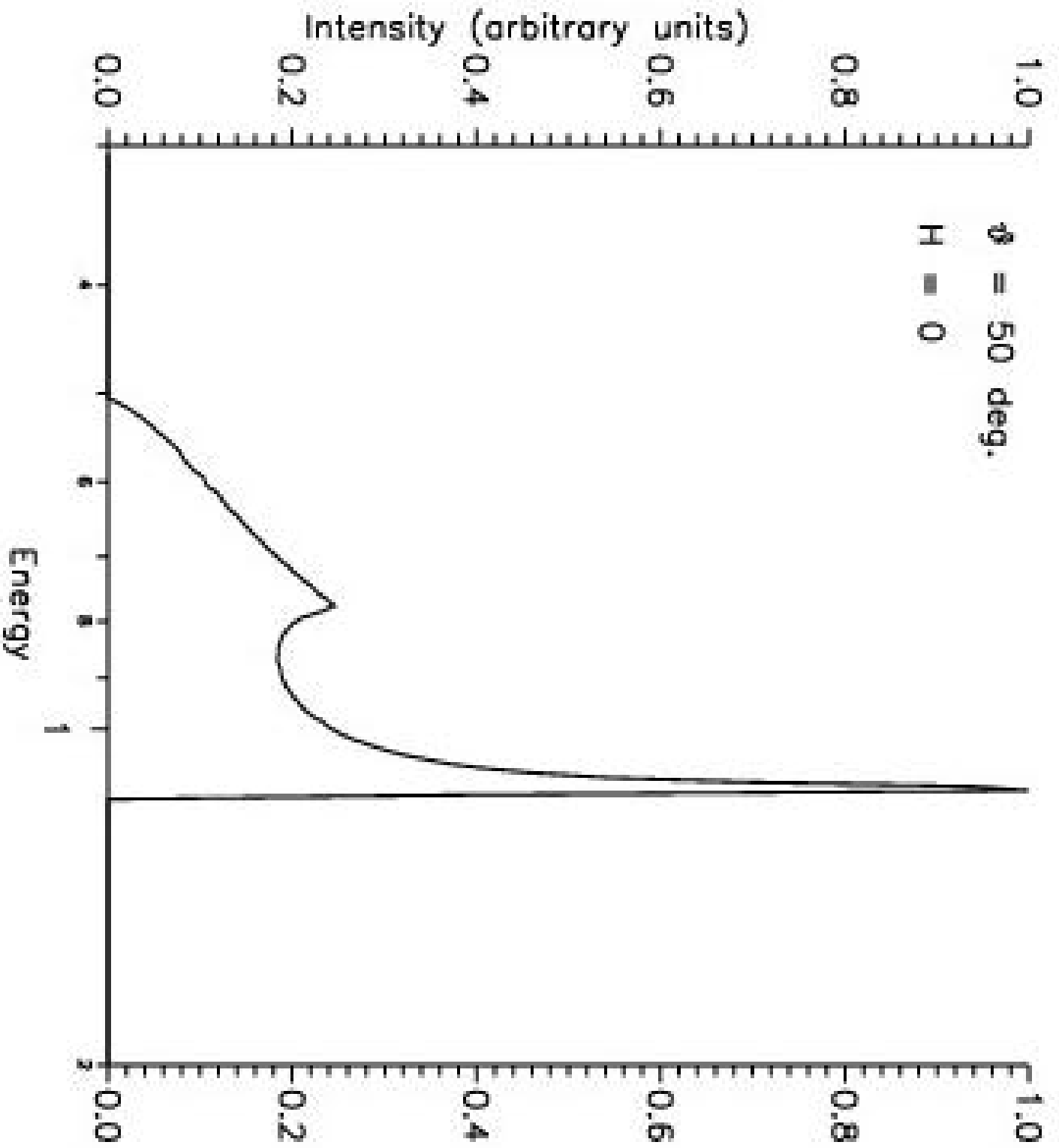
Spectrum of an entire  $\alpha$ -disk observed at large inclination angles. Emitting region lies between  $3 r_g$  and  $10 r_g$ . Left panel includes all the quanta with  $\theta > 89$  degrees. The right one includes the quanta with  $\theta > 89.5$  degrees.

## Magnetic field estimations near BH horizon in AGNs and GBHCs

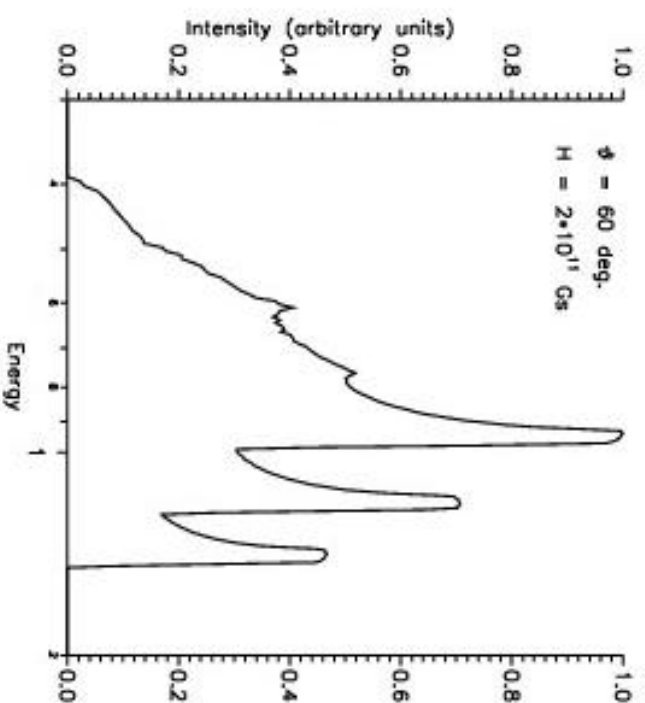
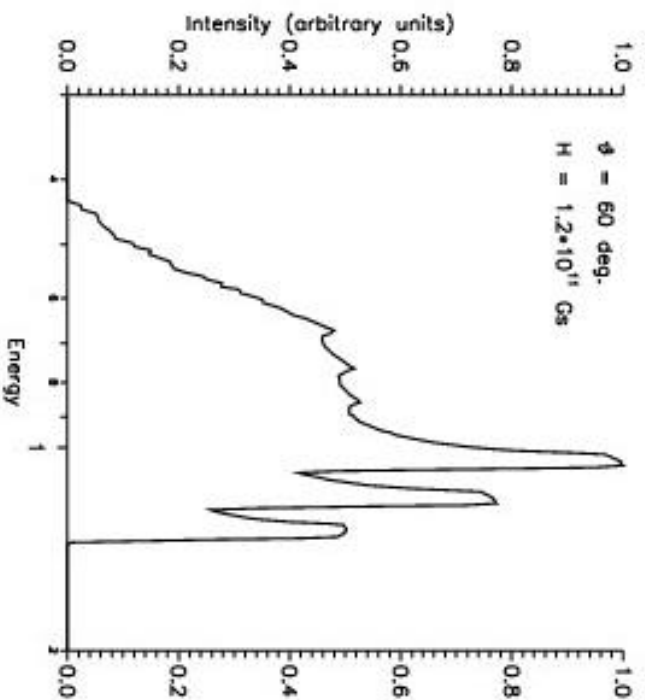
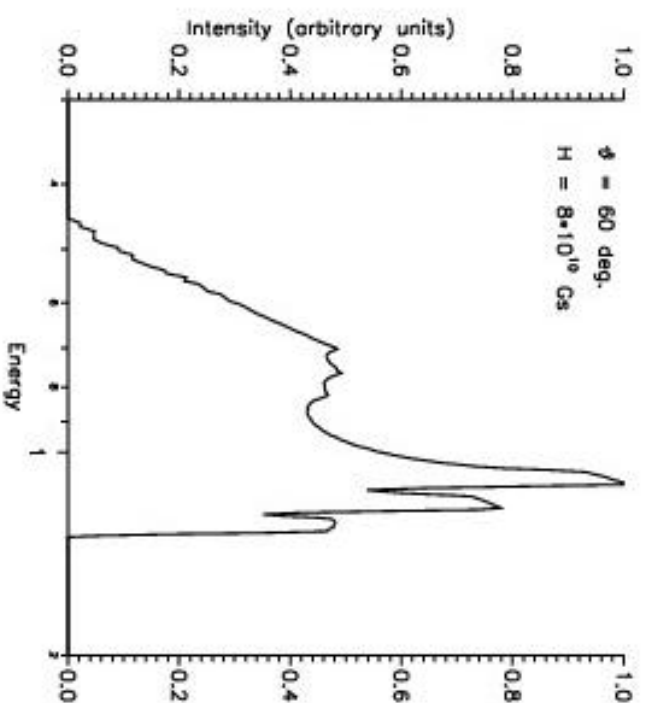
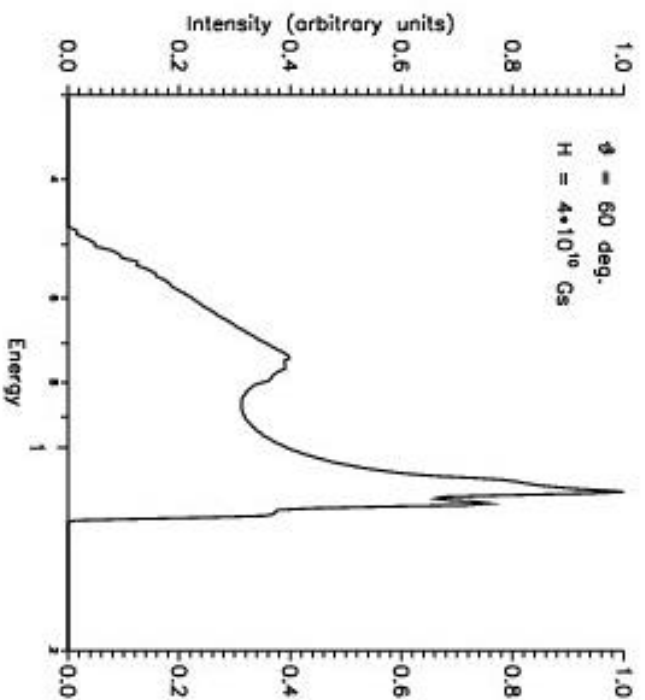
(Zakharov, Kardashev, Lukash, Repin, MNRAS, 342,1325, (2003))

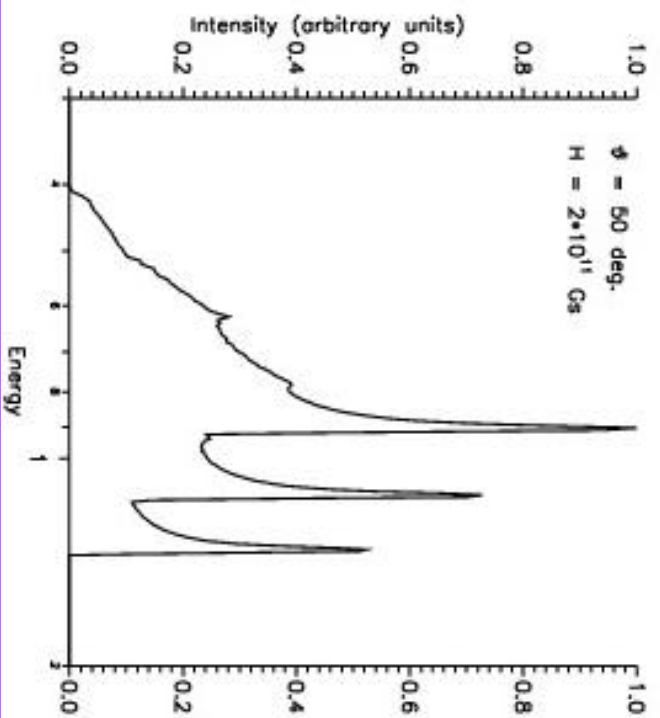
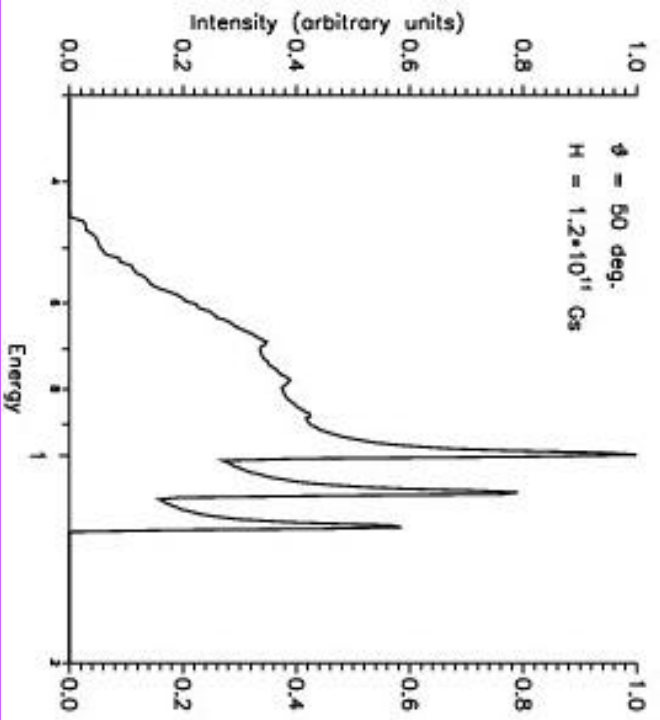
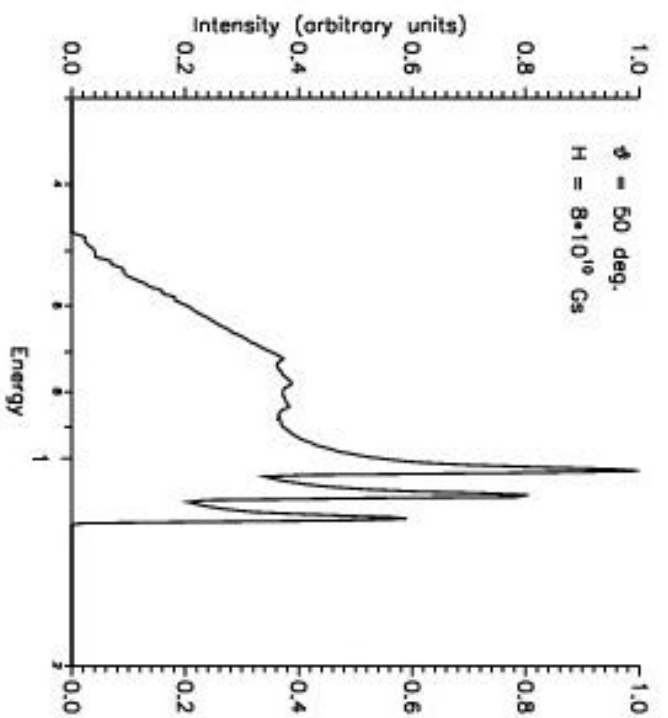
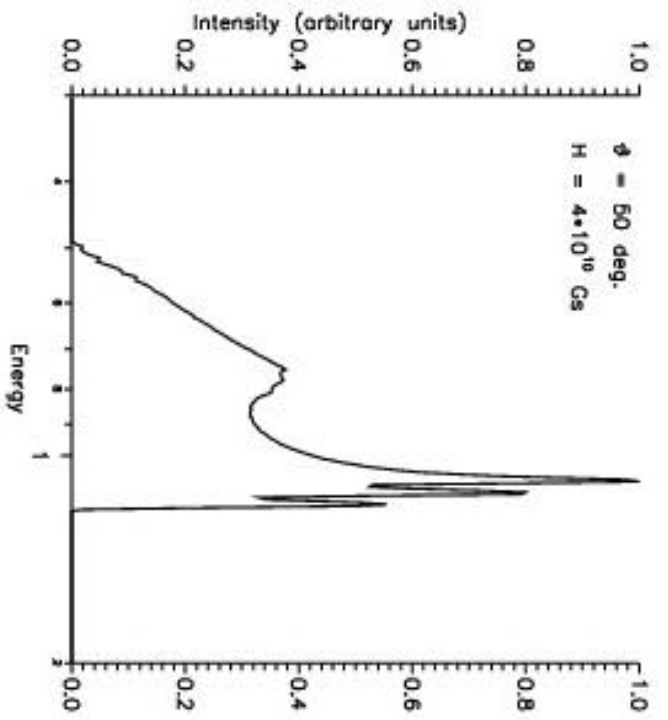
- Zeeman splitting  $E_1 = E_0 - \mu_B H$ ,  $E_2 = E_0 + \mu_B H$ ,  
 $\mu_B = e\hbar/(2m_e c)$ ,  $\mu_B = 9.3 * 10^{-21}$  erg/G
- Figure1
- Figure2
- Figure3
- Figure4
- Figure5
- Figure6
- ASCAdata

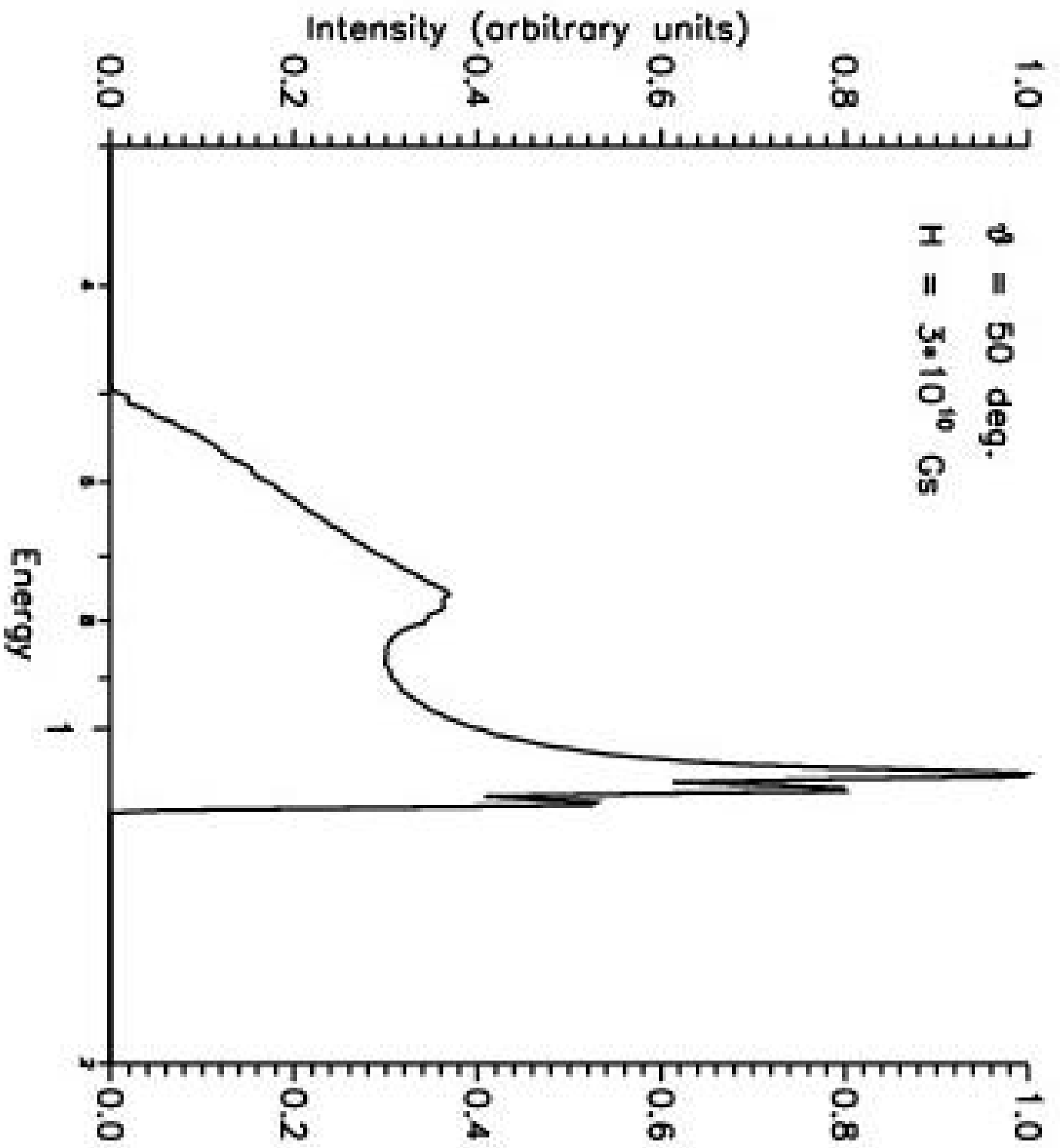


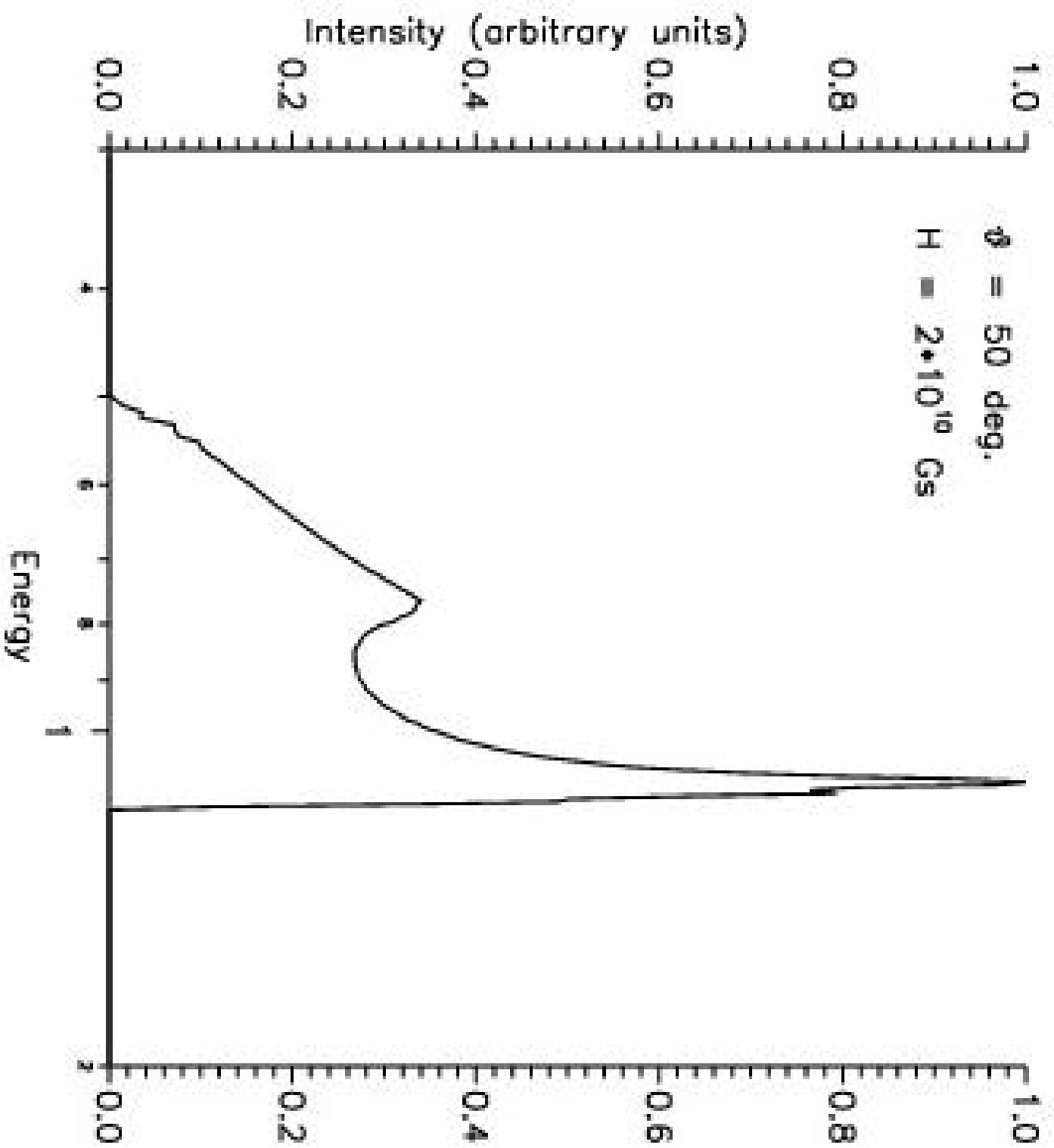


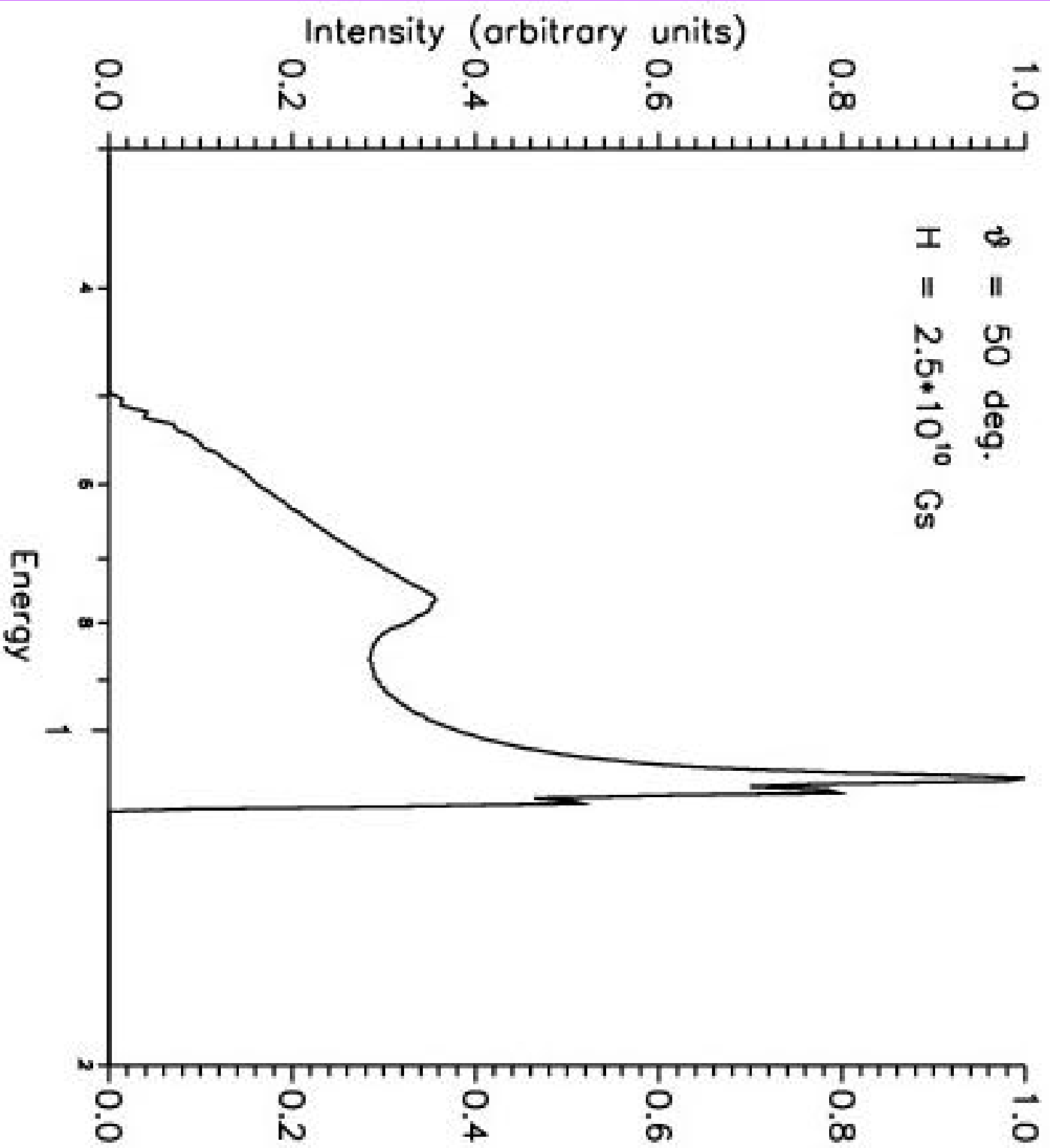


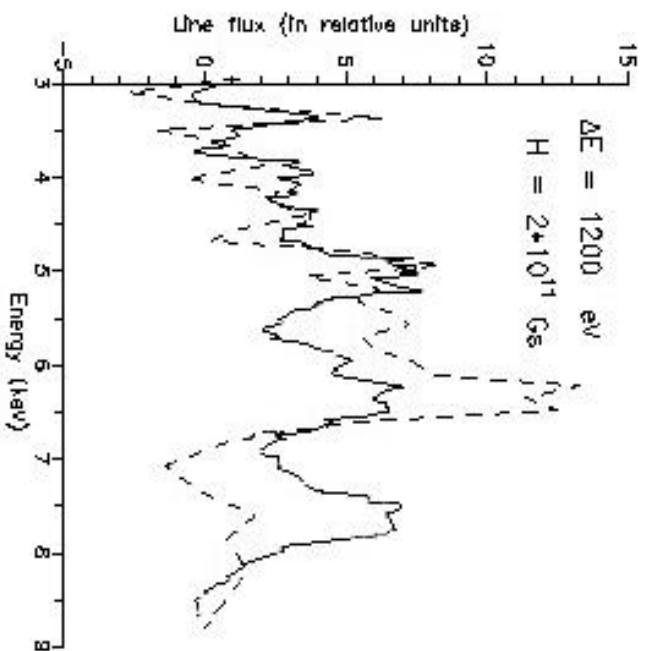
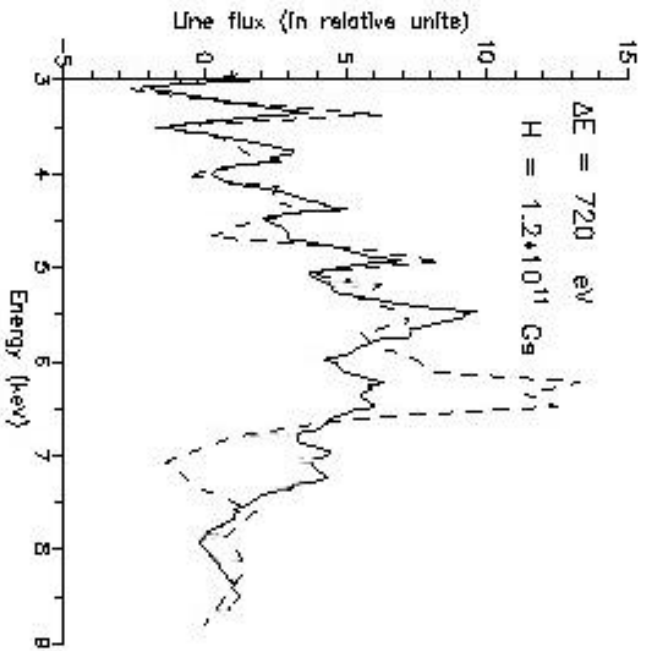
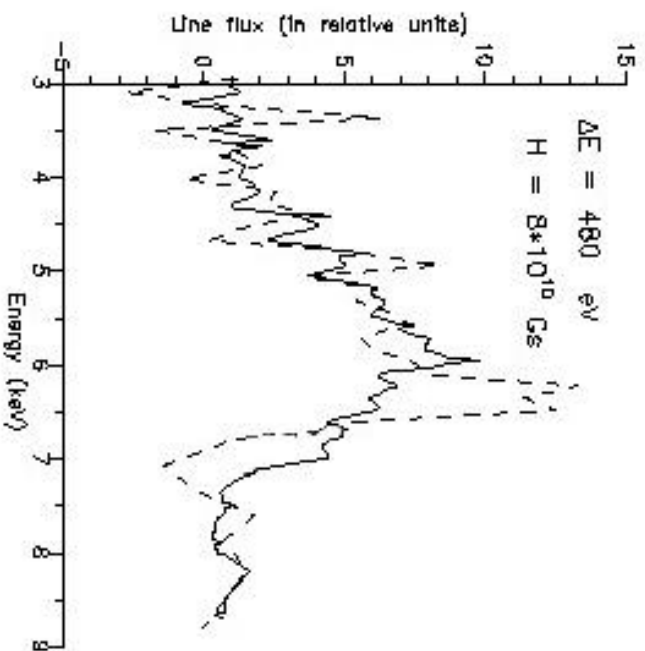
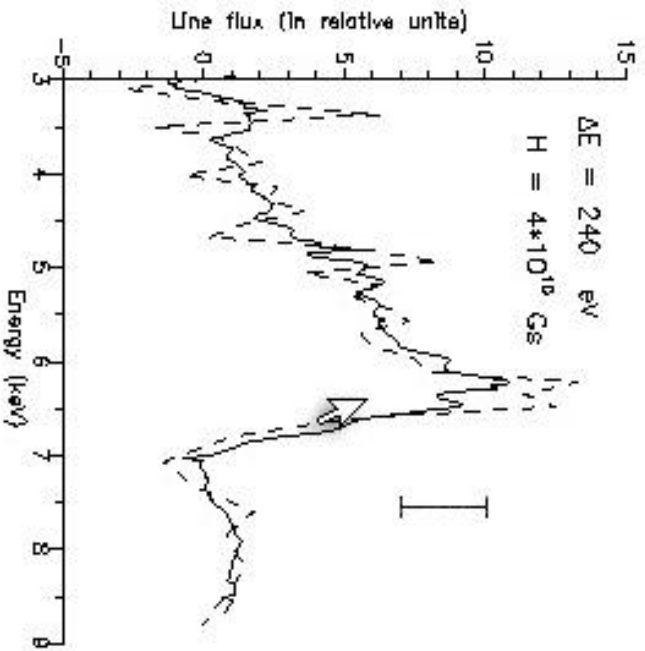








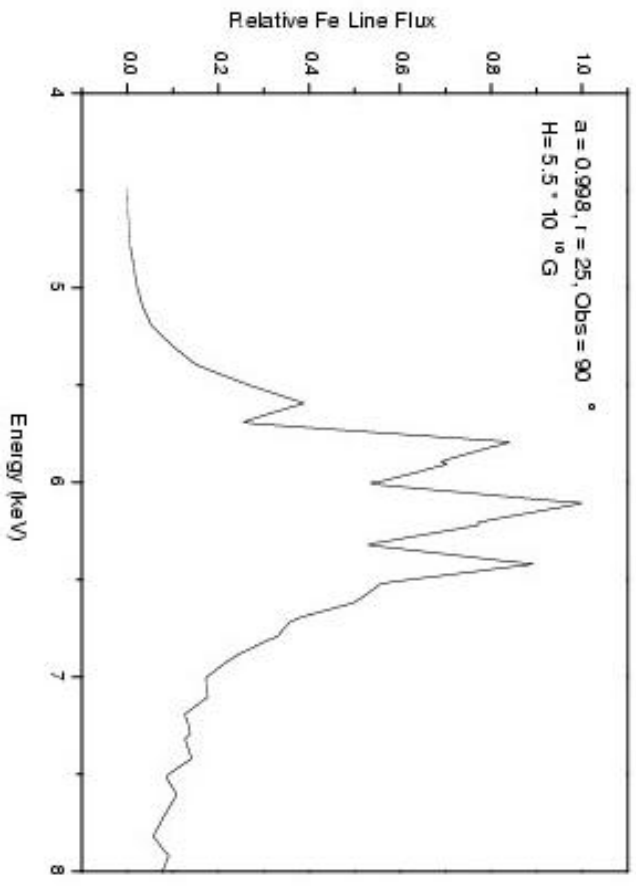
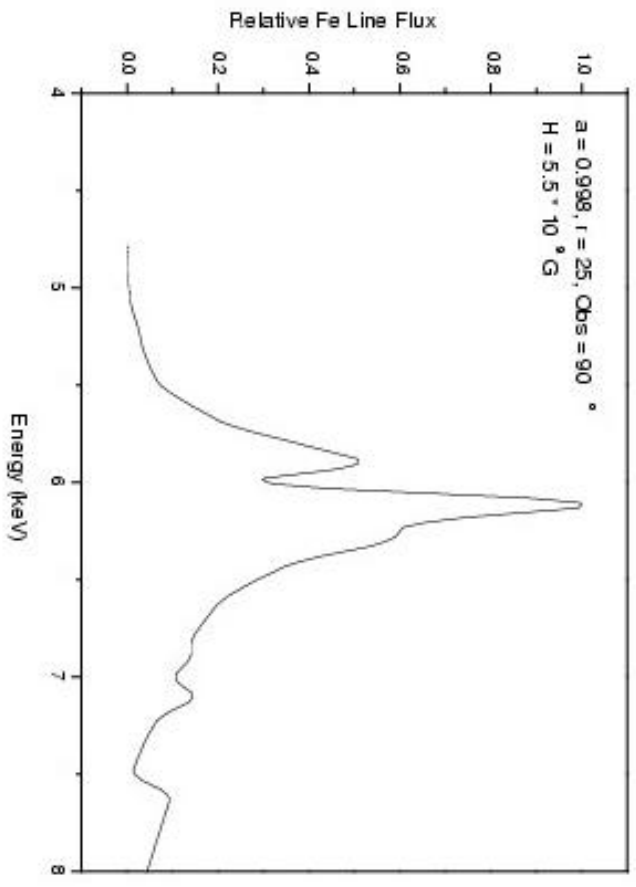
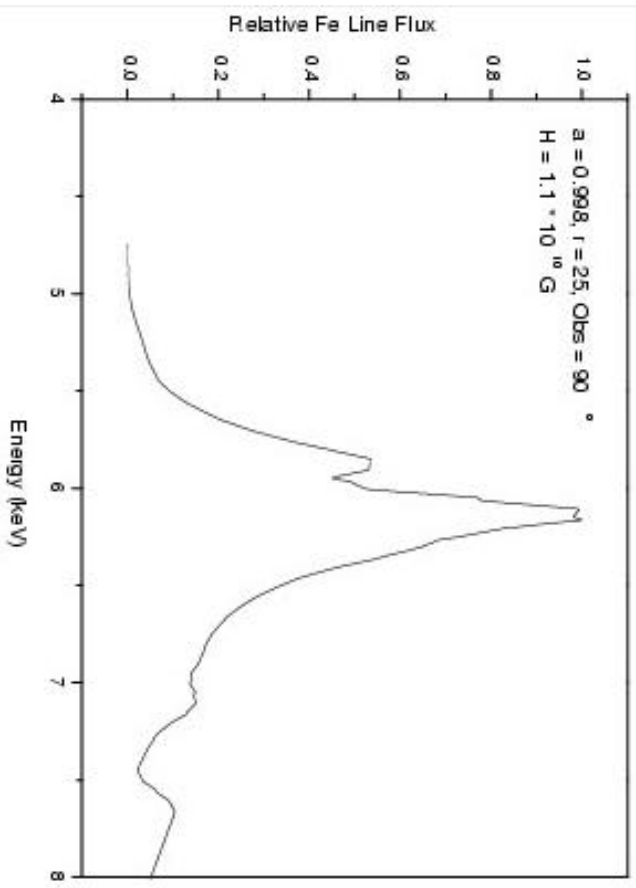
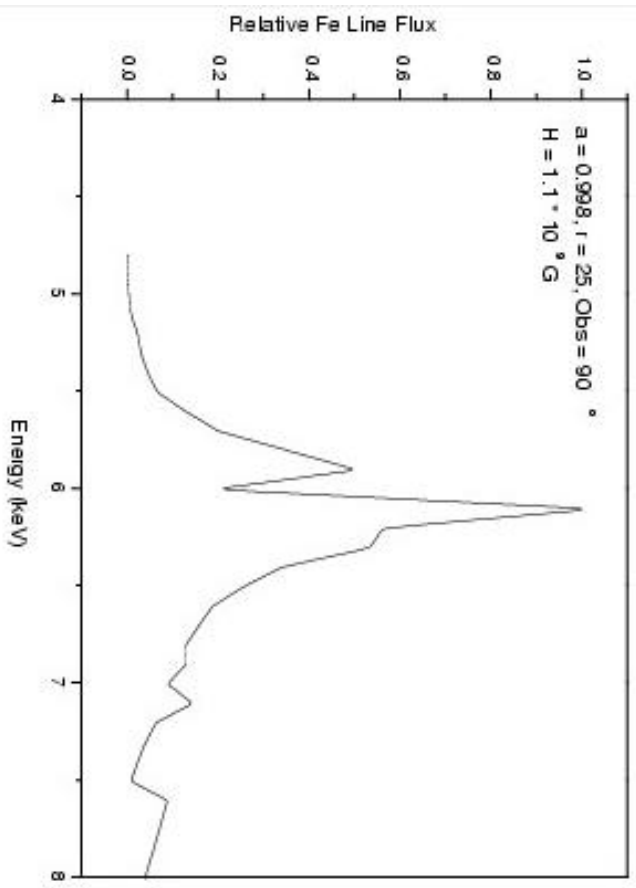


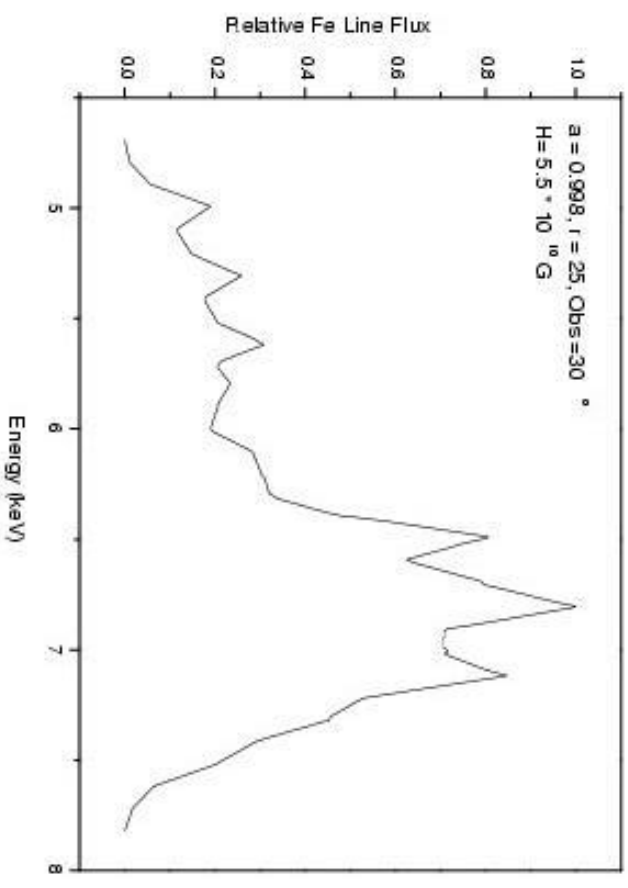
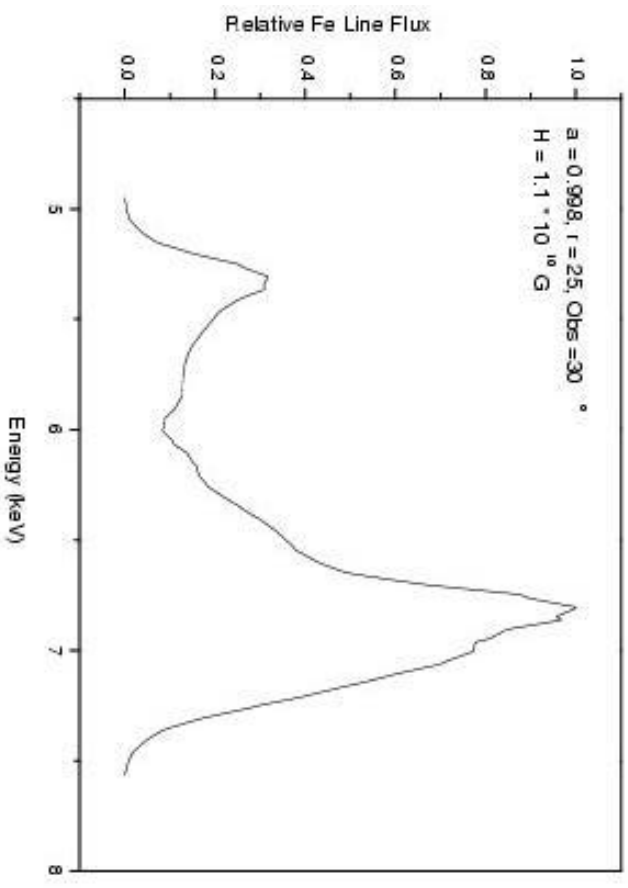
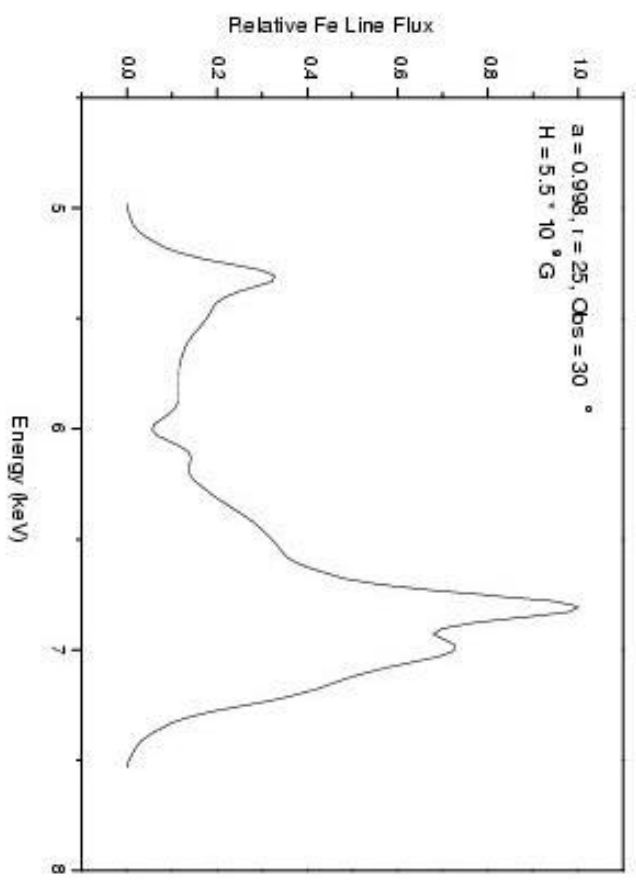
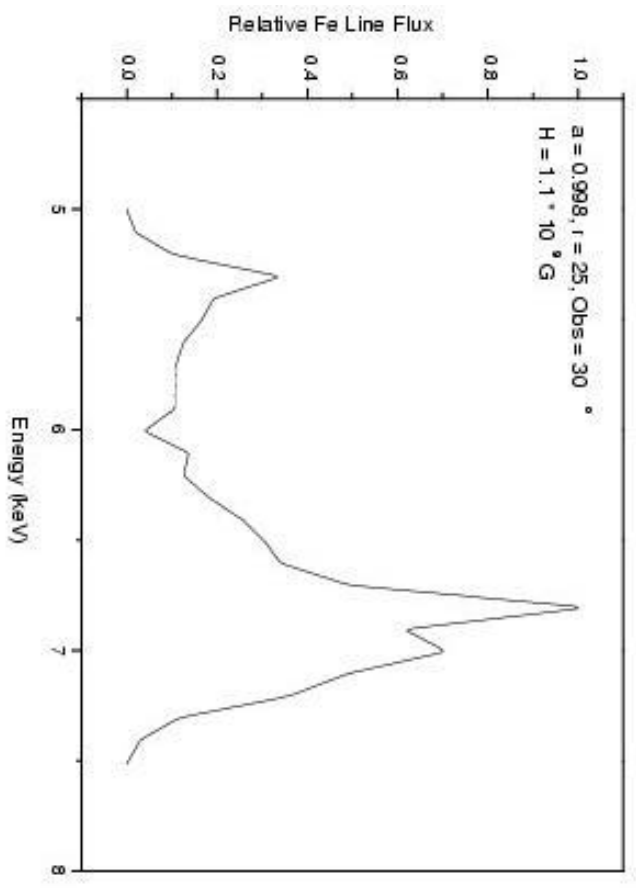


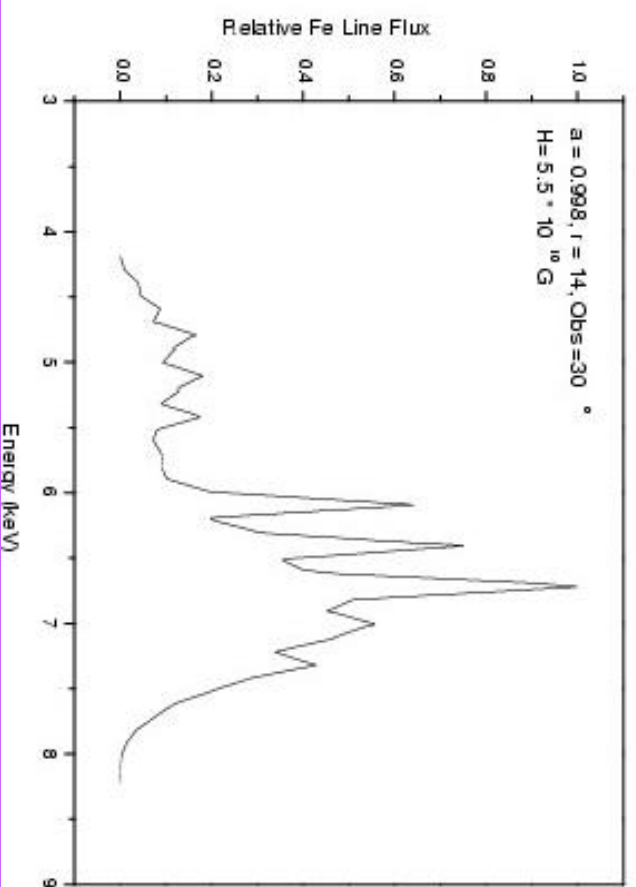
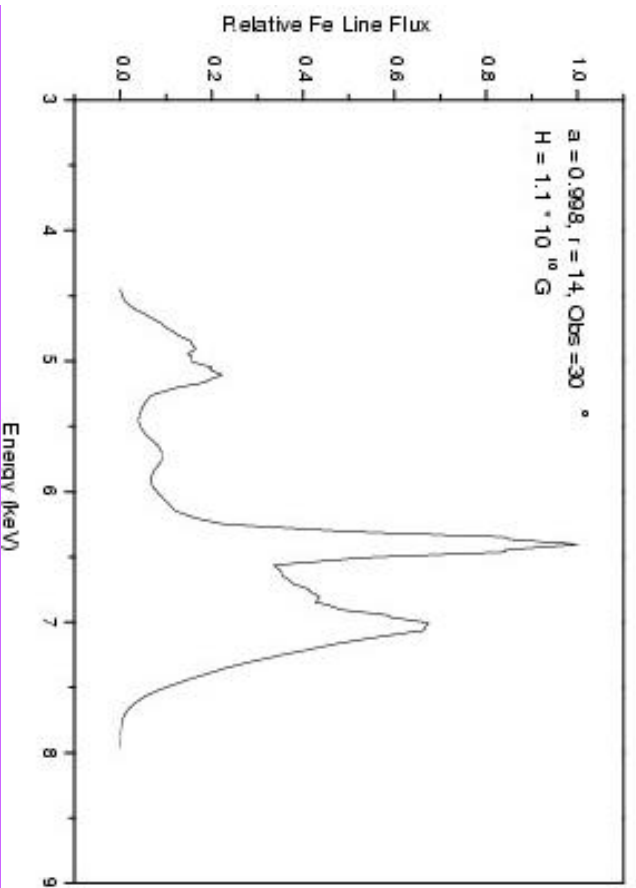
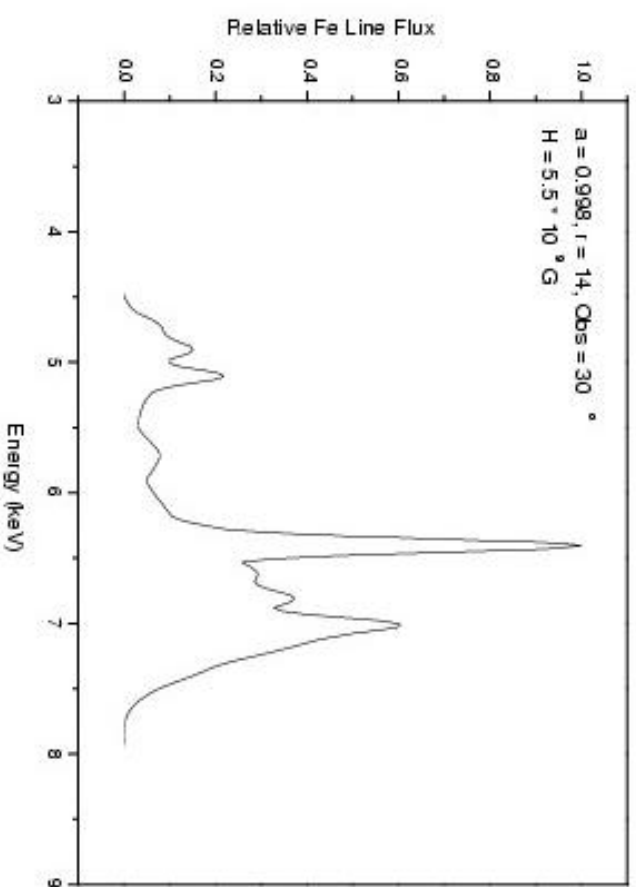
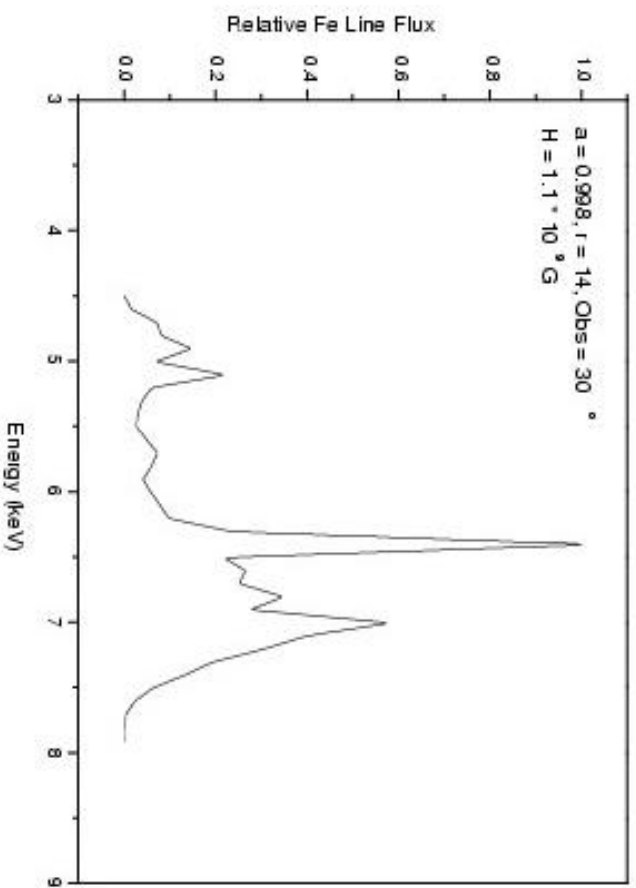
Magnetic field estimations near BH horizon in AGNs and  
GBHCs for non-flat accretion flows  
(Zakharov, Ma, Bao, New Astronomy, **9**, 663 (2004))

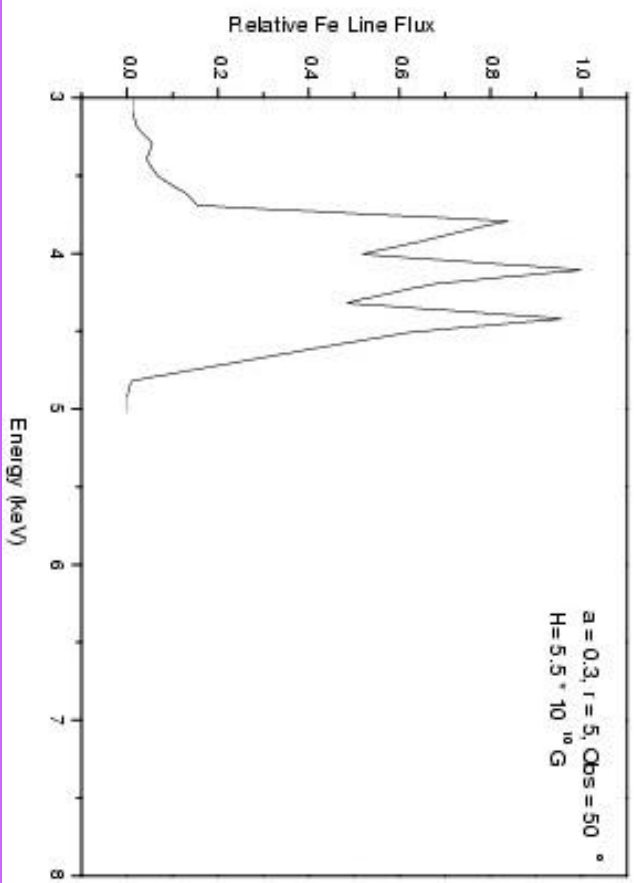
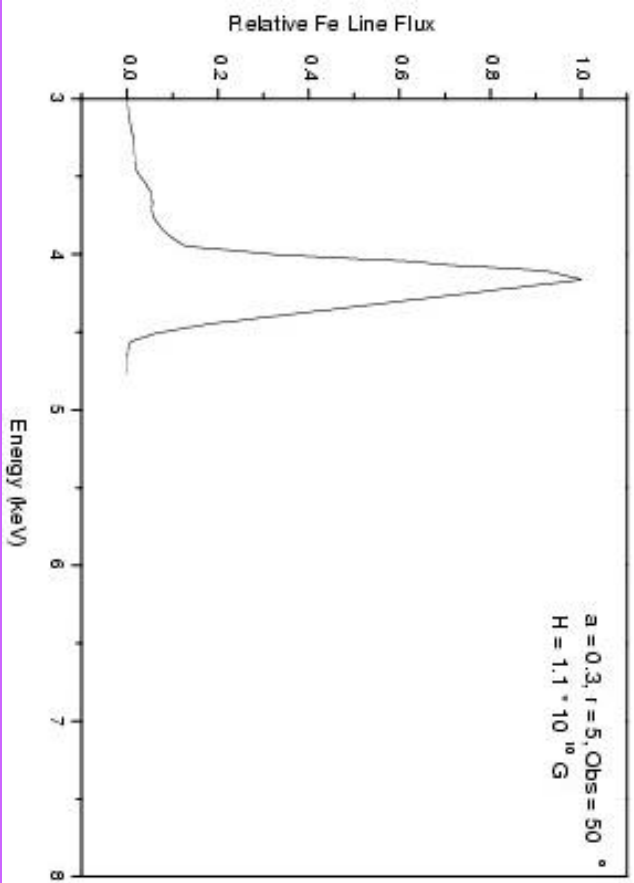
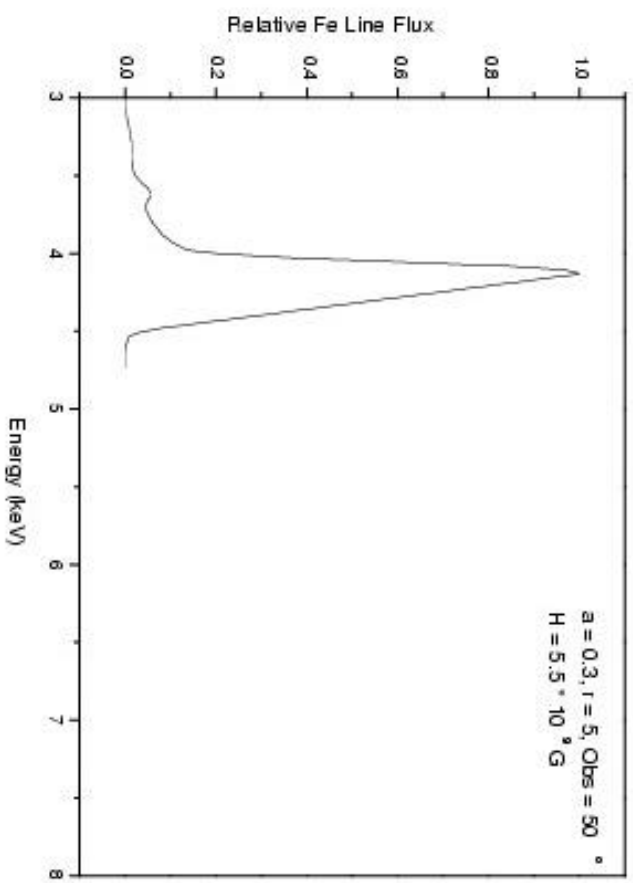
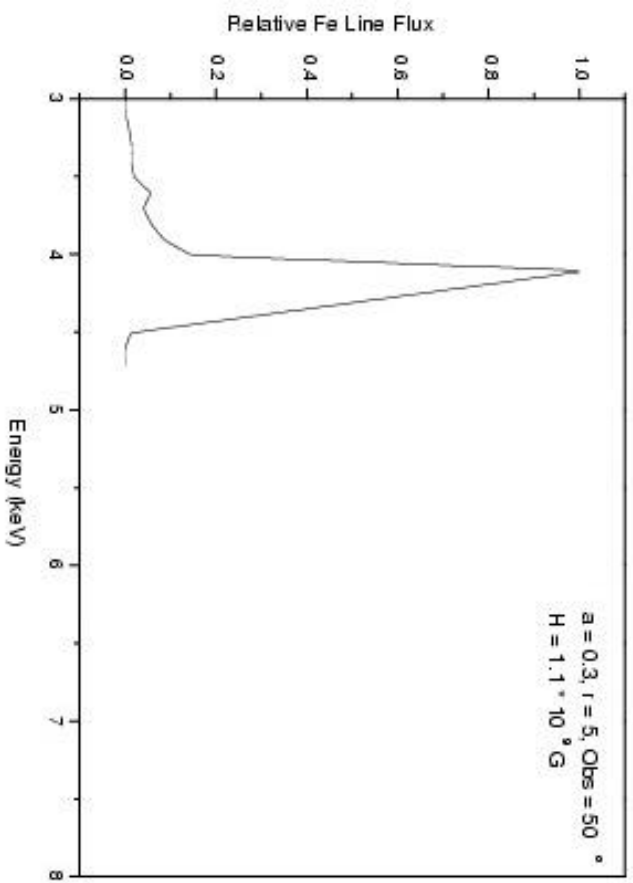
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- Figure6

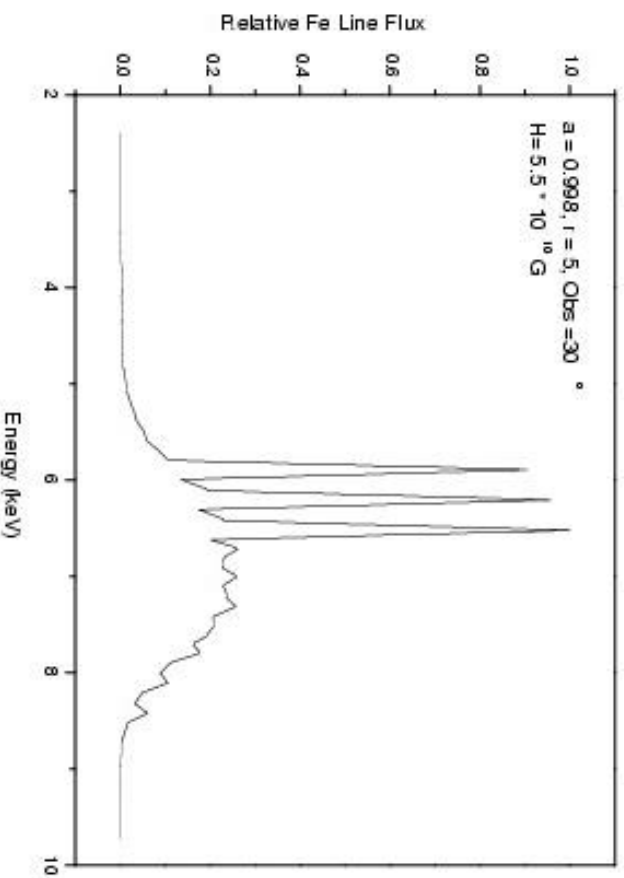
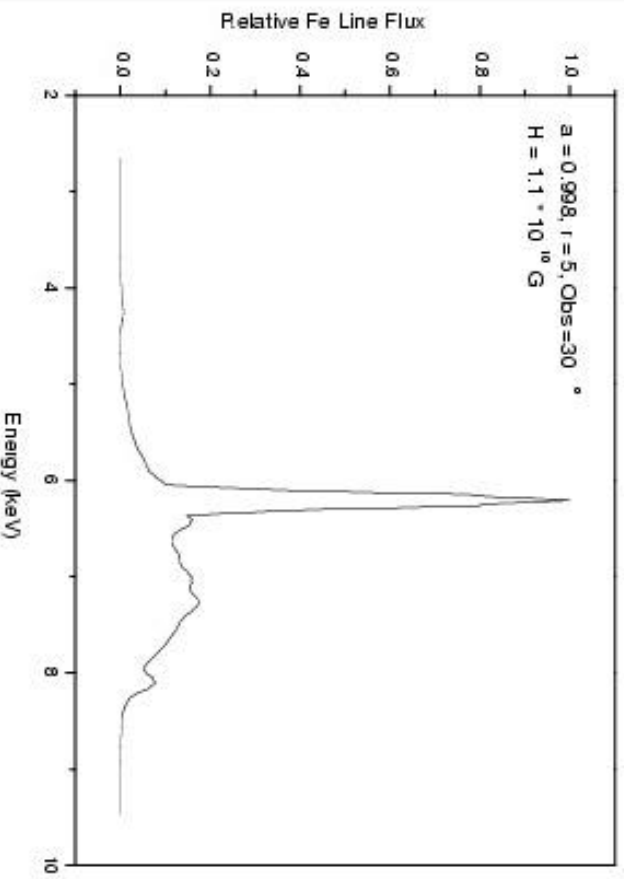
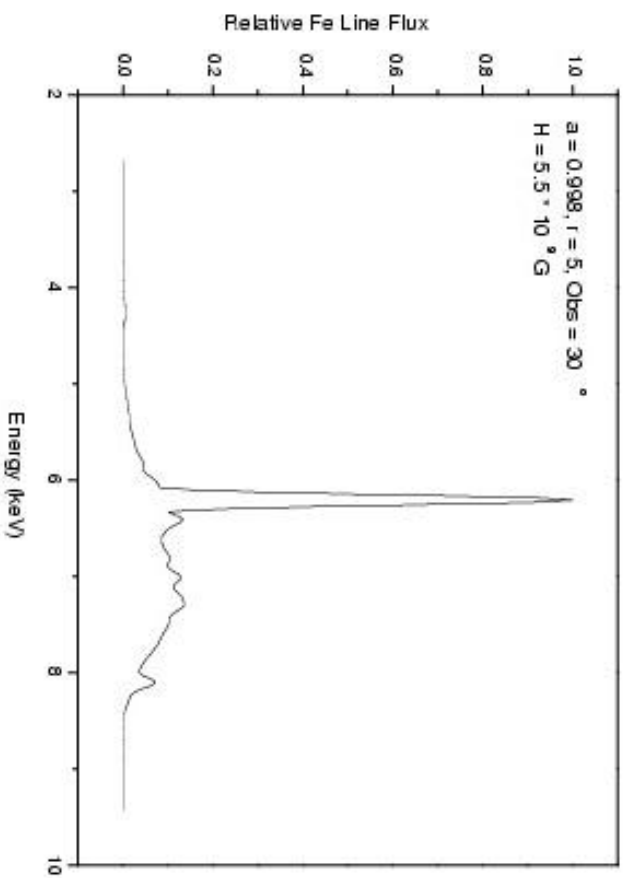
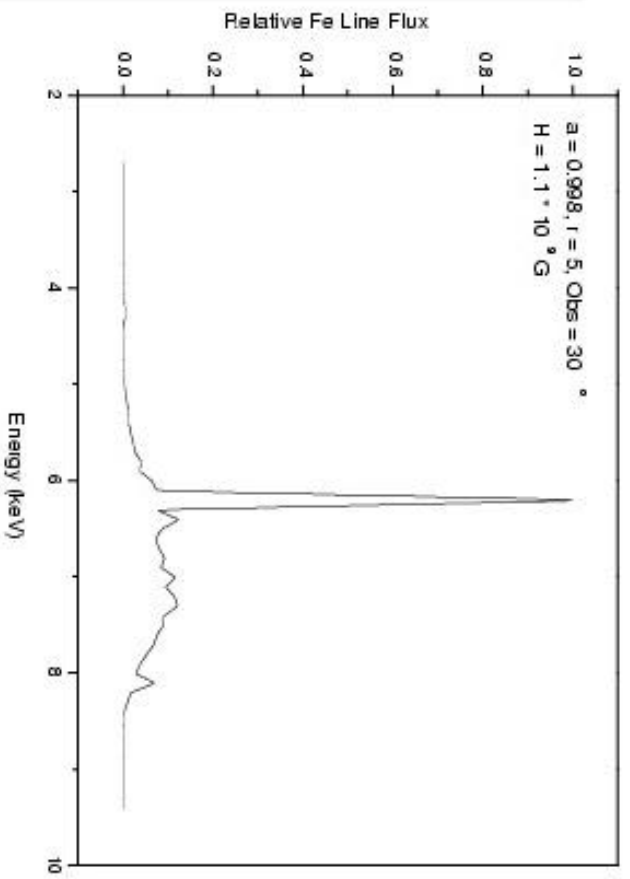


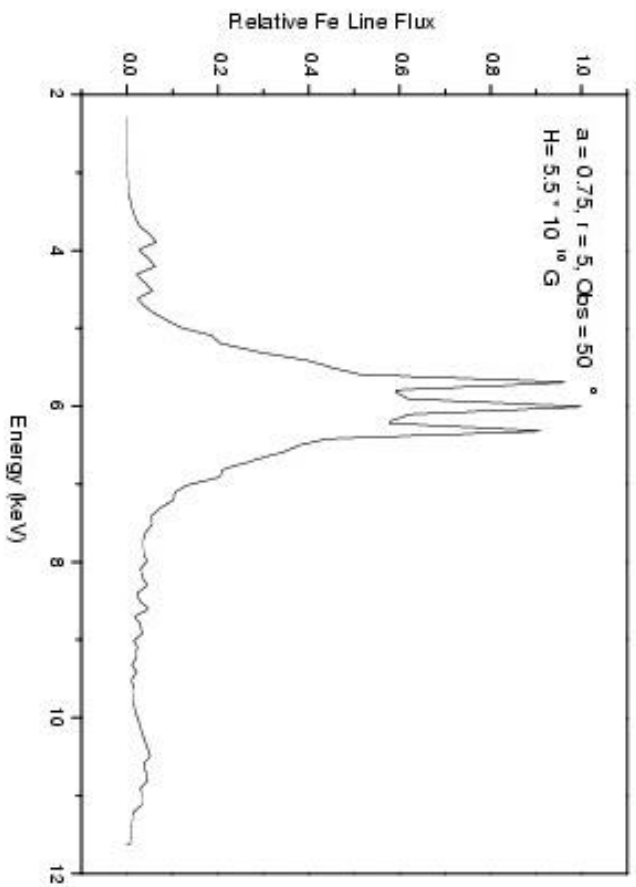
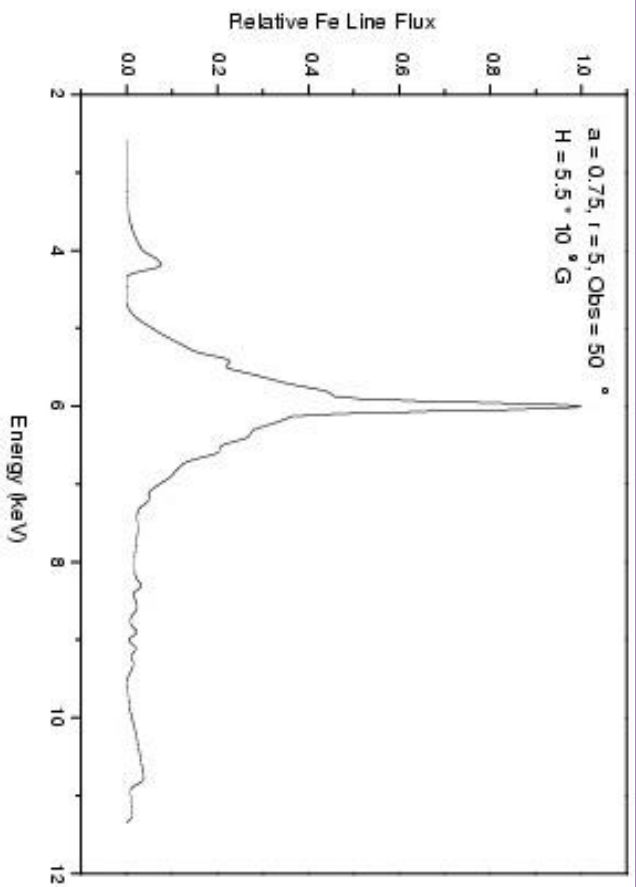
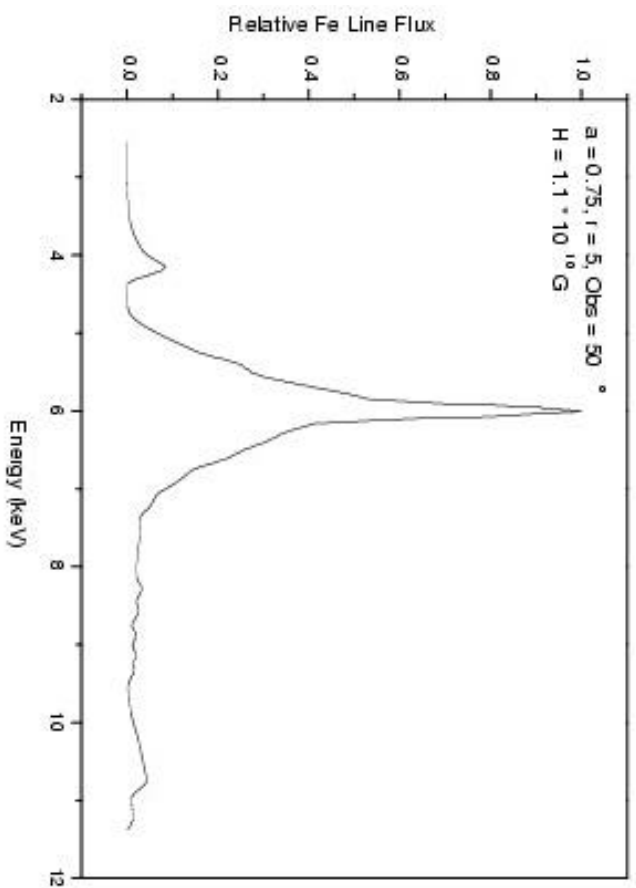
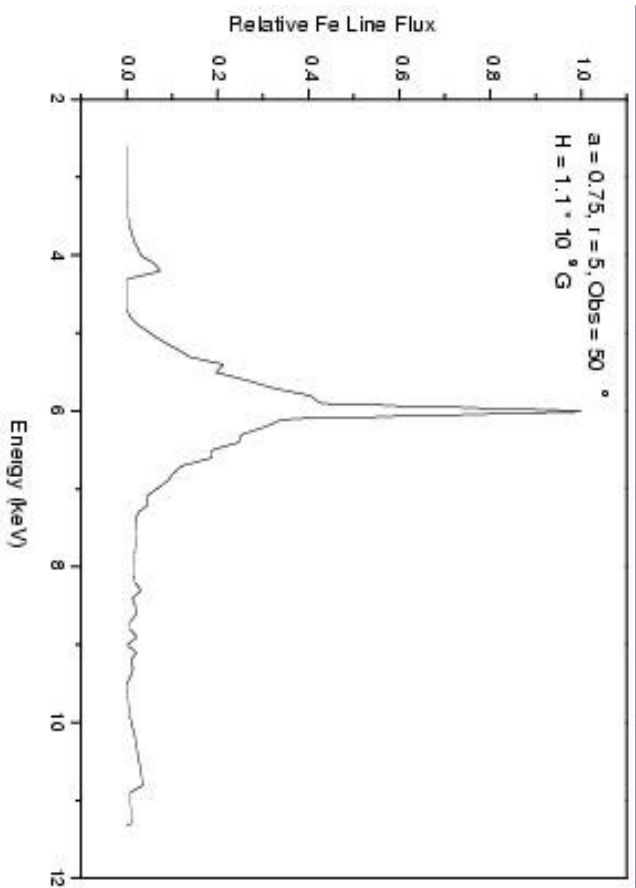












# **XMM-EPIC observation of MCG–6-30-15: direct evidence for the extraction of energy from a spinning black hole?**

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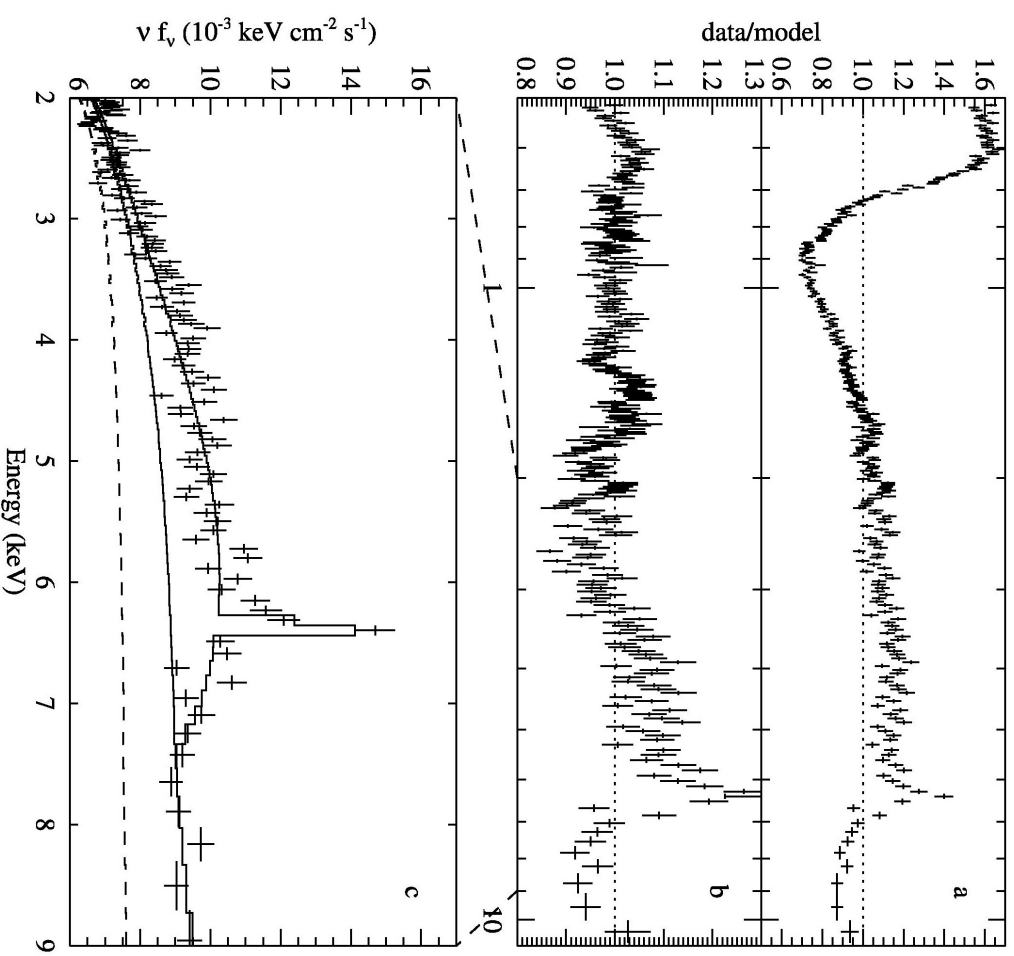
Accepted 2001 October 22. Received 2001 October 22; in original form 2001 August 24

## **ABSTRACT**

We present XMM-Newton European Photon Imaging Camera (EPIC) observations of the bright Seyfert 1 galaxy MCG–6-30-15, focusing on the broad Fe K $\alpha$  line at  $\sim 6$  keV and the associated reflection continuum, which is believed to originate from the inner accretion disc. We find these reflection features to be *extremely* broad and redshifted, indicating an origin in the very central regions of the accretion disc. It seems likely that we have caught this source in the ‘deep minimum’ state first observed by Iwasawa et al. The implied central concentration of X-ray illumination is difficult to understand in any pure accretion disc model. We suggest that we are witnessing the extraction and dissipation of rotational energy from a spinning black hole by magnetic fields connecting the black hole or plunging region to the disc.

**Key words:** accretion, accretion discs – black hole physics – galaxies: individual: MCG–6-30-15 – galaxies: Seyfert – X-rays: galaxies.





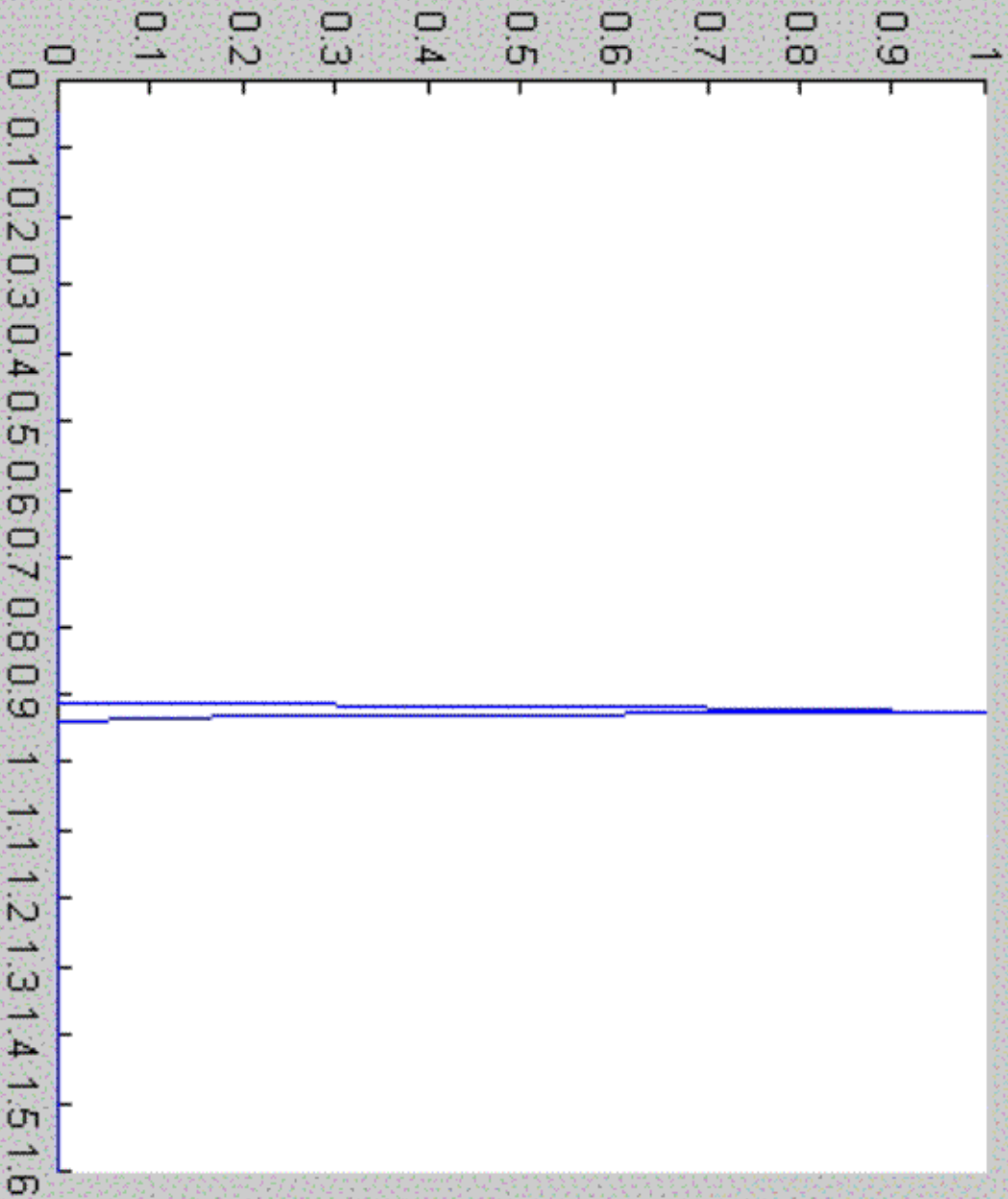
**Figure 1.** (a) Ratio between data and model from fitting a power law to the 0.5–11 keV data. (b) Ratio from fitting a power law and the empirical warm absorber model (see text). (c) Deconvolved spectrum of the Fe  $K\alpha$  band, showing the total  $\text{LAOR}$  model and the continuum with and without (dashed) the reflection component for a model with reflection from an ionized disc. For clarity, the data have been rebinned and only the single-event data points are shown.





Figure No. 1

File Edit Window Help



Observer position:

theta = **0** deg.

r = **10.0** rg

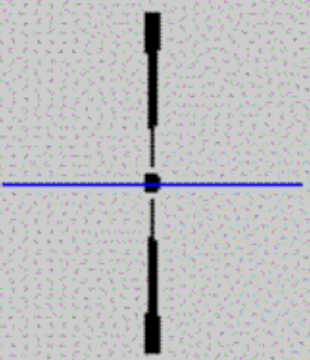
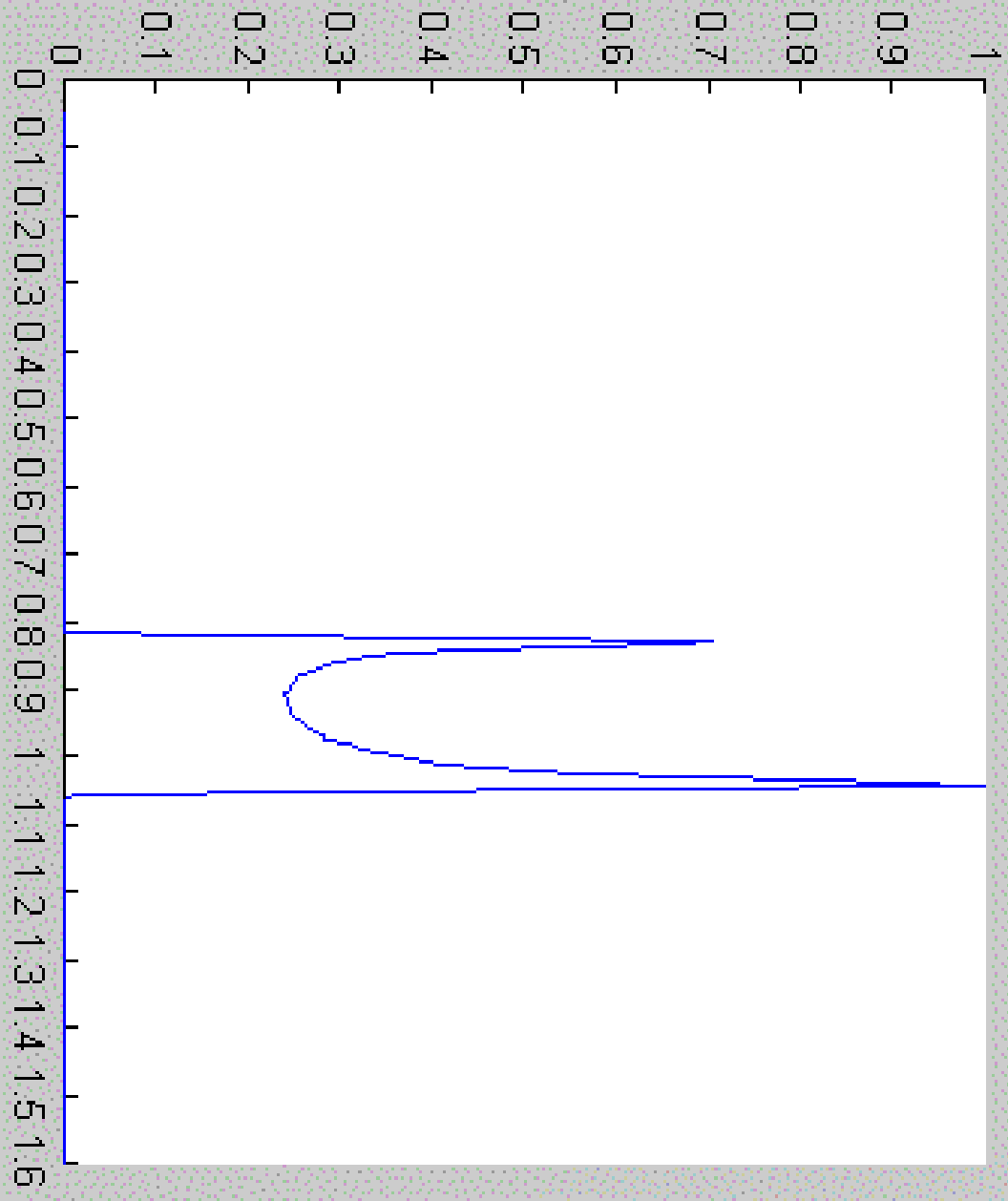




Figure No. 1

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Observer position:  
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r = 10.0 rg

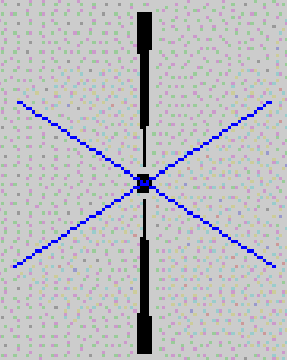
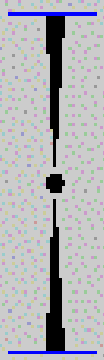
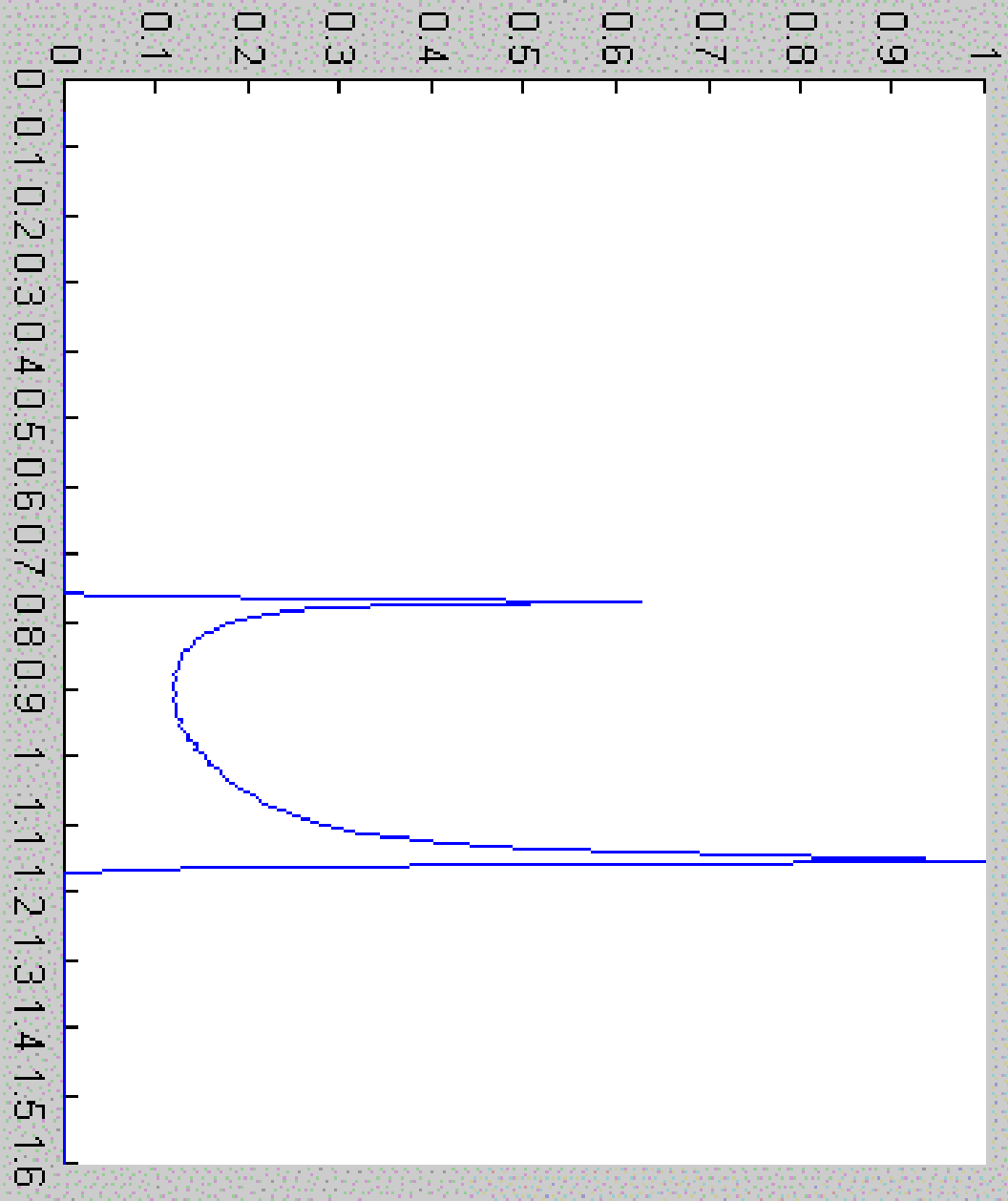




Figure No. 1

File Edit Window Help



Observer position:  
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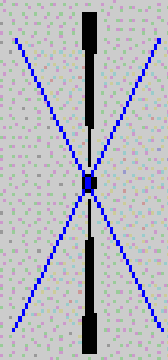
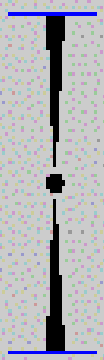
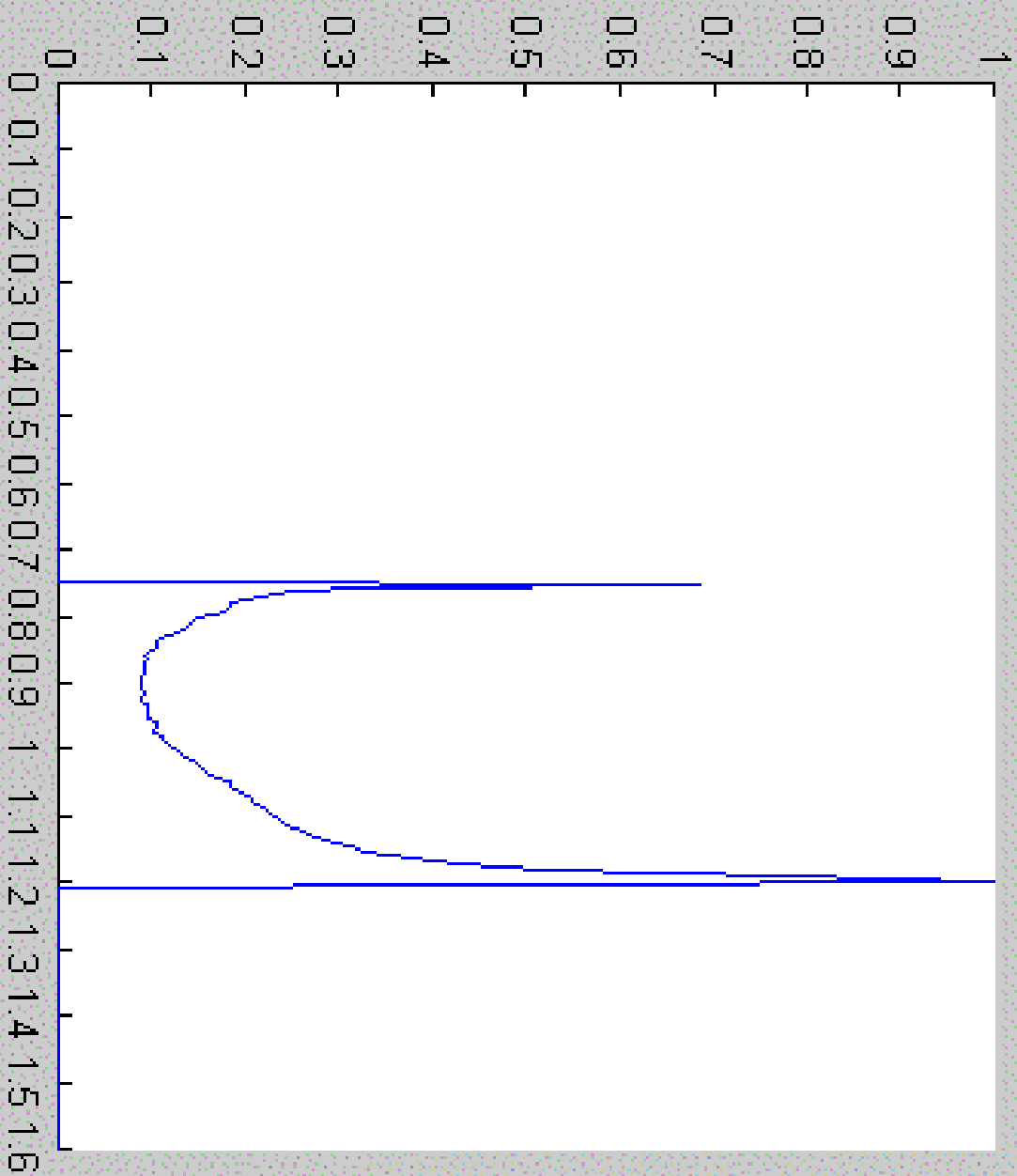




Figure No. 1



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Observer position:

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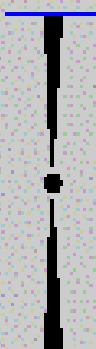
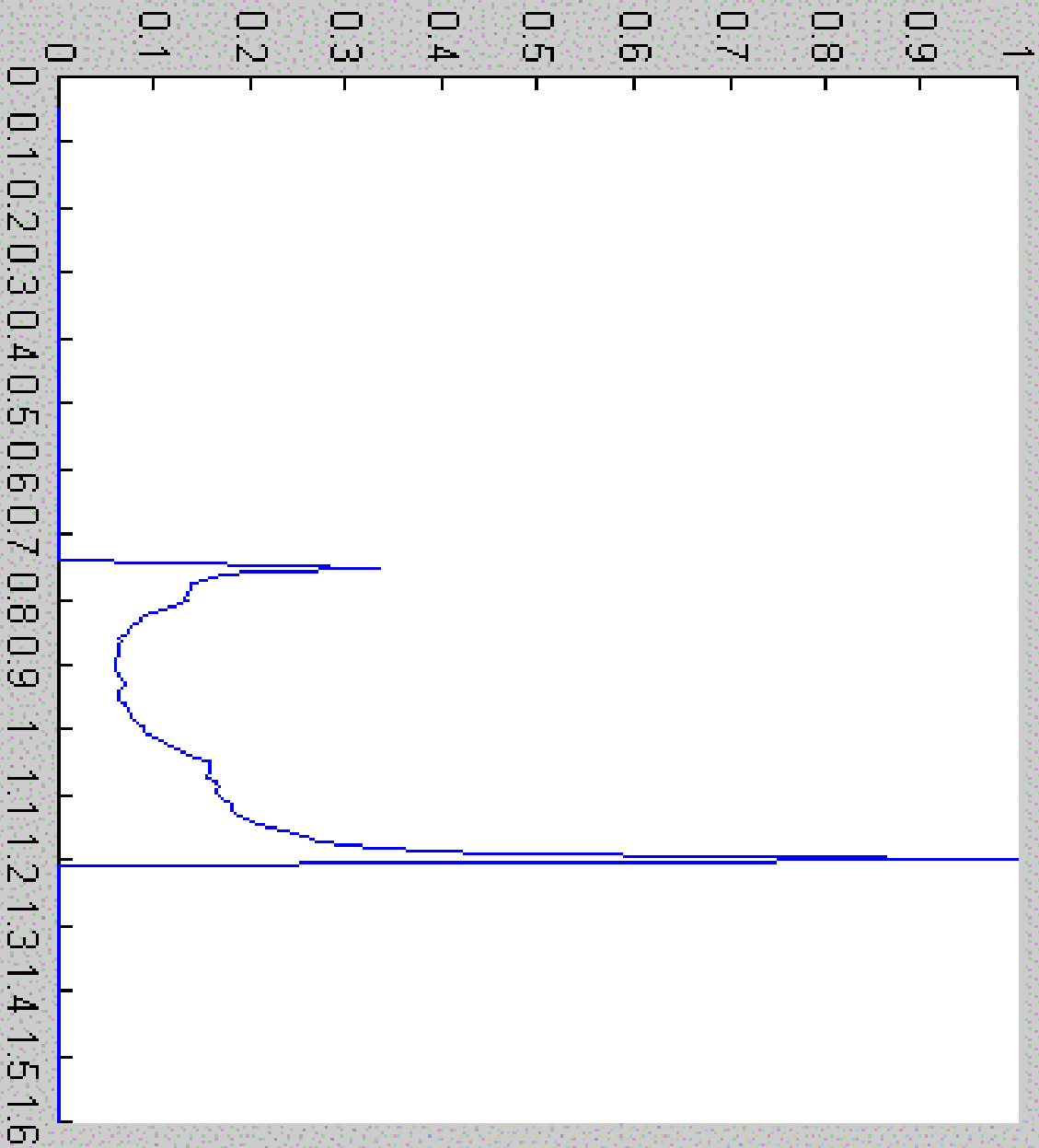




Figure No. 1

File Edit Window Help



Observer position:

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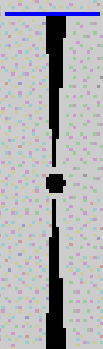
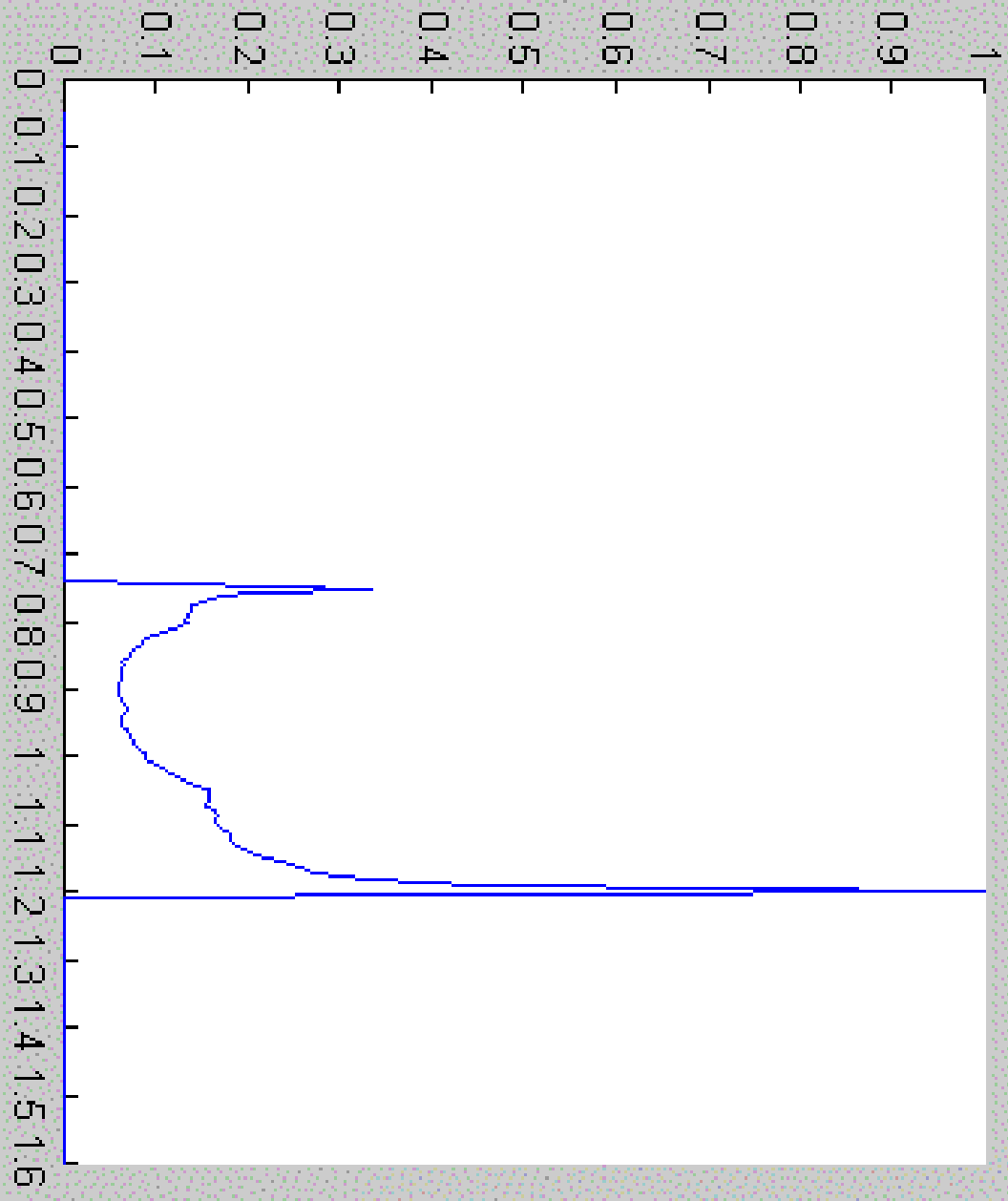




Figure No. 1

File Edit Window Help



Observer position:  
theta = **85** deg.  
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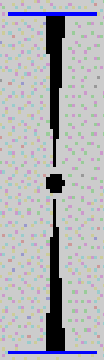
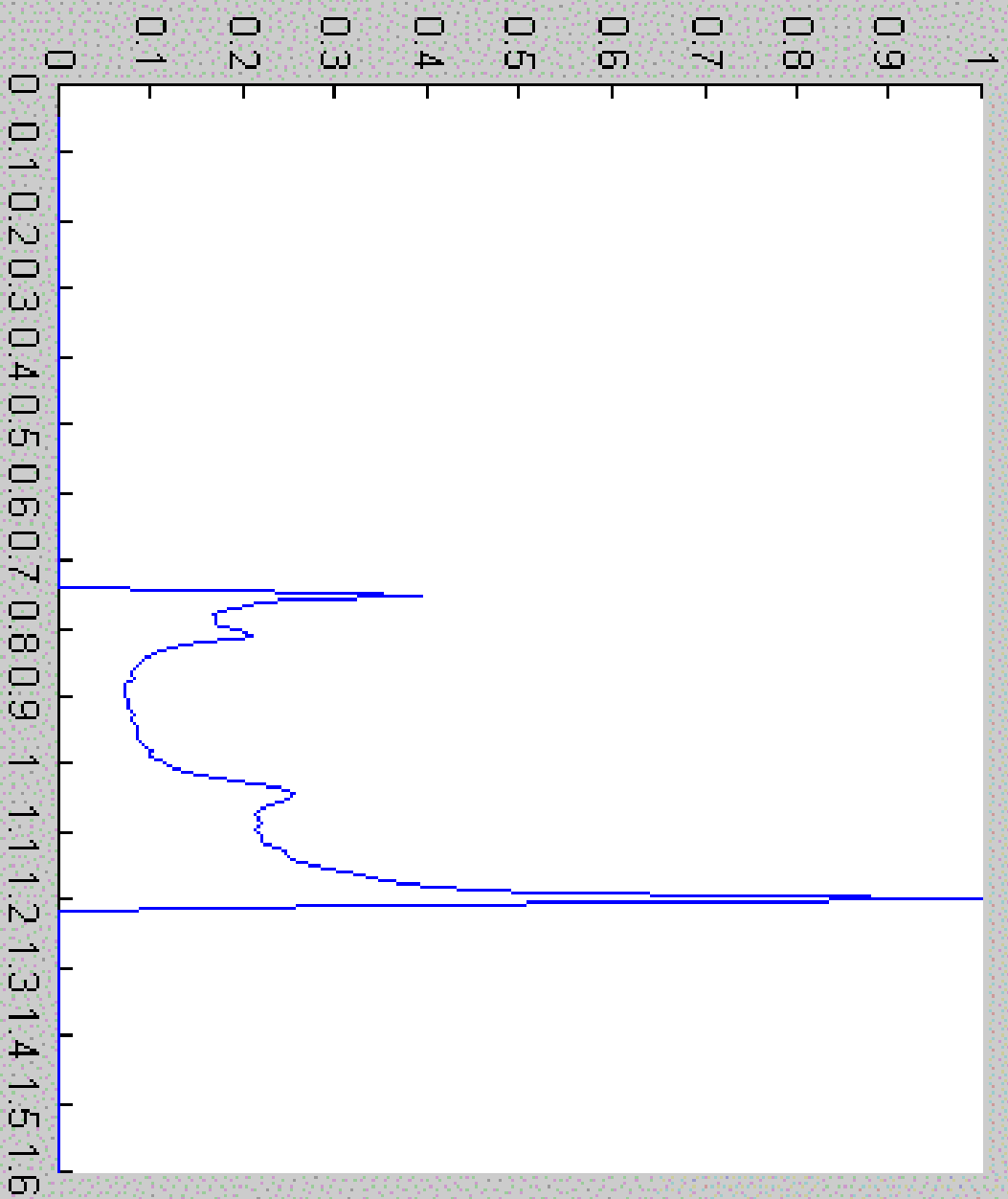




Figure No. 1

File Edit Window Help



Observer position:

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r = **10.0** rg

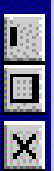
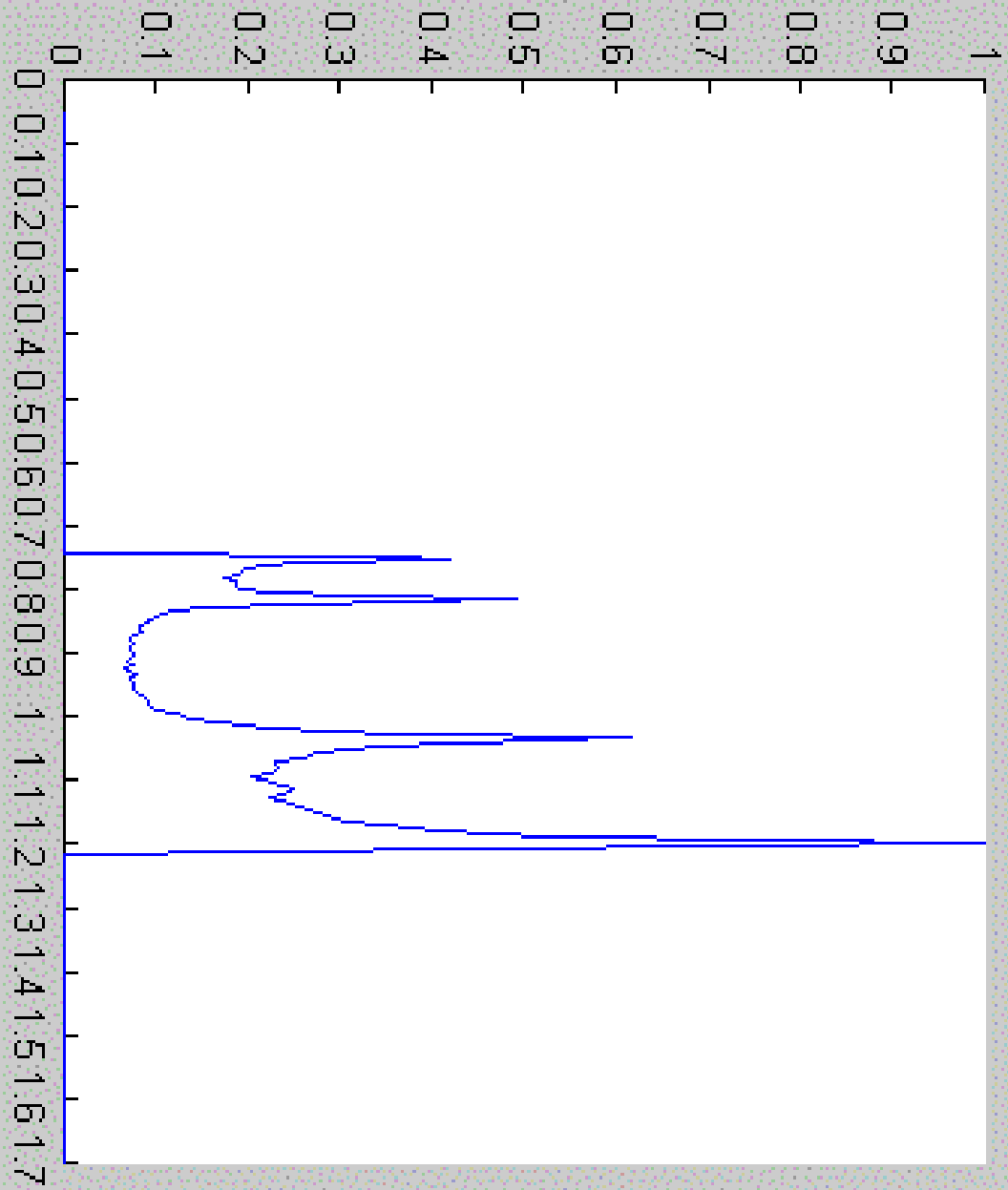




Figure No. 1

File Edit Window Help



Observer position:  
theta = **90** deg.  
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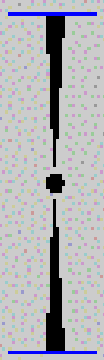
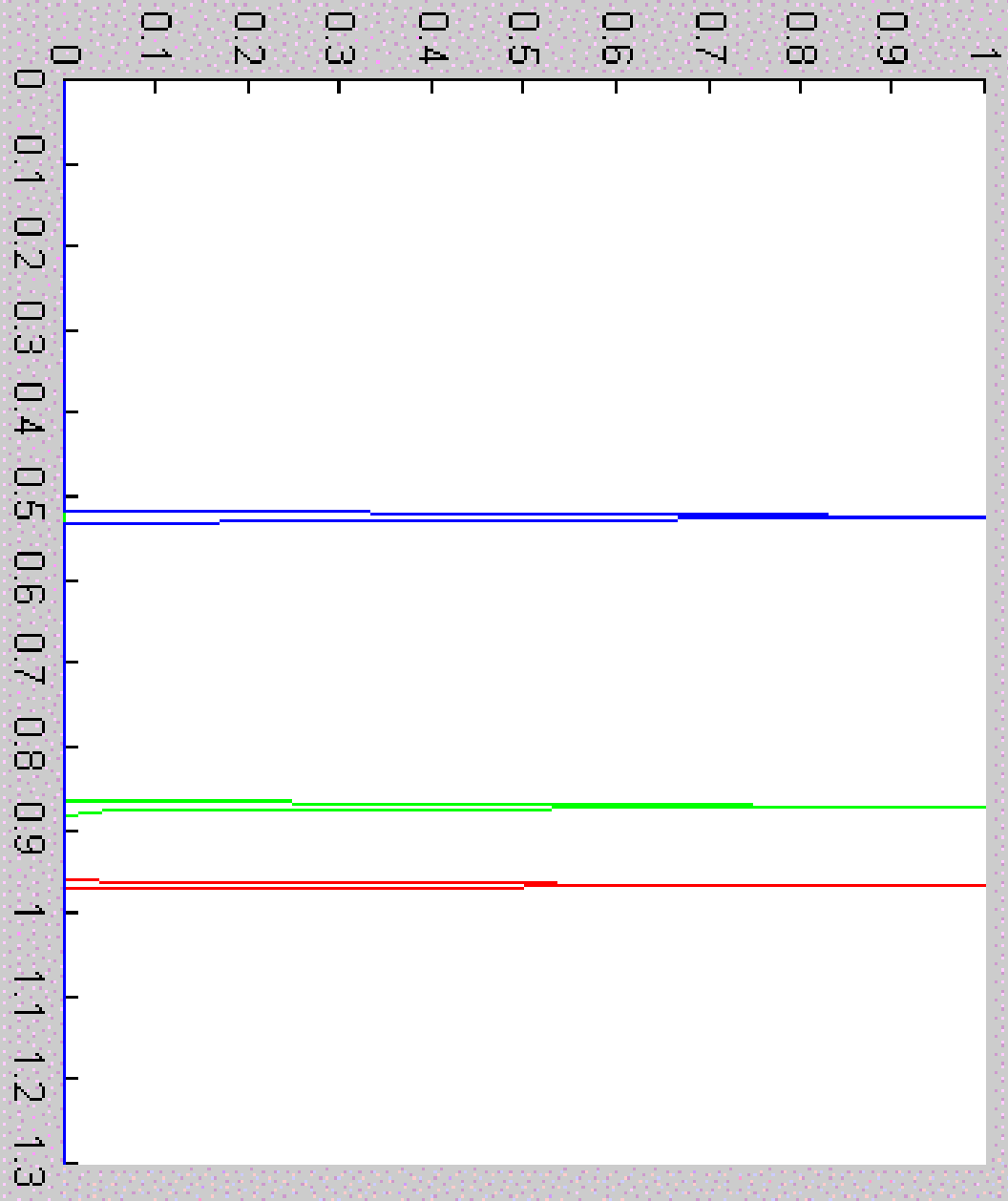




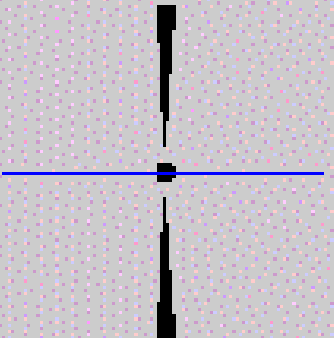


Figure No. 1

File Edit Window Help



Observer position:  
theta = 0 deg.



- <http://www.gsfc.nasa.gov/gsfc/spacesci/pictures/blackhole/BH1m.jpg>



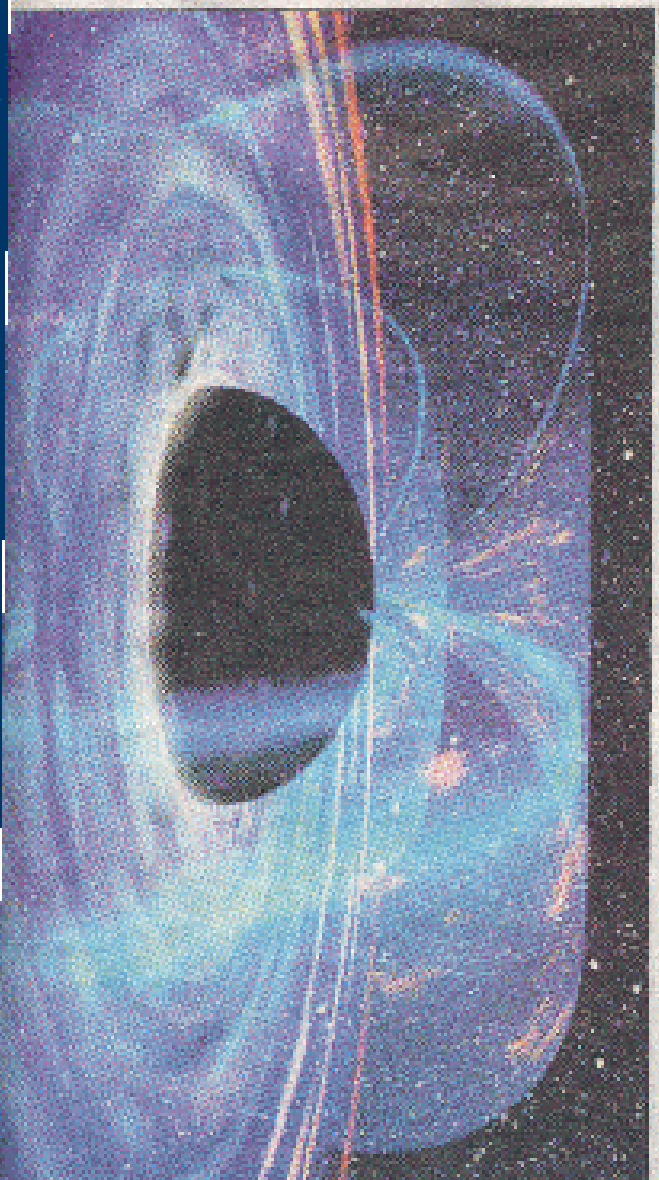
# What is a black hole?

Everyone already seems to know!

## NATIONAL POST

VOL. 3 NO. 304 THURSDAY, OCTOBER 28, 2001 WWW.NATIONALPOST.COM

*Energy-sipping black hole puts on cosmic show for astronomers*



**Will it rip in two?**  
Asteroid has mathematician to beg in 'deep freeze'

**By Robert F. Brunner**  
The asteroid that is expected to pass within 100,000 kilometers of Earth in early 2002 has a mathematician to beg in "deep freeze" to help solve a puzzle that has baffled astronomers for decades. The asteroid, named 1999 KW4, is the only one of its kind to be found in the "frozen" region of the solar system, where temperatures are so low that the rocks and metals that make up the asteroid are frozen solid. The asteroid is thought to have originated in the inner solar system, but its presence in the "frozen" region is a mystery. Mathematician John J. O'Keefe, who has spent the last 10 years studying the asteroid, says that the only way to explain its presence is if it was once part of a larger body that was broken apart by a collision. O'Keefe says that the asteroid is made of a material that is very different from anything else found in the solar system. He says that the material is a mixture of rock and metal, but it is also very porous. This makes the asteroid very fragile, and it is likely that it was broken apart by a collision. O'Keefe says that the only way to explain the asteroid's presence is if it was once part of a larger body that was broken apart by a collision. He says that the asteroid is made of a material that is very different from anything else found in the solar system. He says that the material is a mixture of rock and metal, but it is also very porous. This makes the asteroid very fragile, and it is likely that it was broken apart by a collision.



# Mirages around Kerr black holes and retro-gravitational lenses

- Let us consider an illumination of black holes. Then retro-photons form caustics around black holes or mirages around black holes or boundaries around shadows.
- (Zakharov, Nucita, DePaolis, Ingrosso,
- *New Astronomy* (accepted); astro-ph/0411511)

# RETRO-MACHOS: $\pi$ IN THE SKY?

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*Draft version September 20, 2004*

## ABSTRACT

Shine a flashlight on a black hole, and one is greeted with the return of a series of concentric rings of light. For a point source of light, and for perfect alignment of the lens, source, and observer, the rings are of infinite brightness (in the limit of geometric optics). In this manner, distant black holes can be revealed through their reflection of light from the Sun. Such retro-MACHO events involve photons leaving the Sun, making a  $\pi$  rotation about the black hole, and then returning to be detected at the Earth. Our calculations show that, although the light return is quite small, it may nonetheless be detectable for stellar-mass black holes at the edge of our solar system. For example, all (unobscured) black holes of mass  $M$  or greater will be observable to a limiting magnitude  $\bar{m}$ , at a distance given by:  $0.02 \text{ pc} \times \sqrt[3]{10^{(\bar{m}-30)/2.5}} (M/10 M_{\odot})^2$ . Discovery of a Retro-MACHO offers a way to *directly* image the presence of a black hole, and would be a stunning confirmation of strong-field general relativity.

*Subject headings:* gravitational lensing—black hole physics—relativity

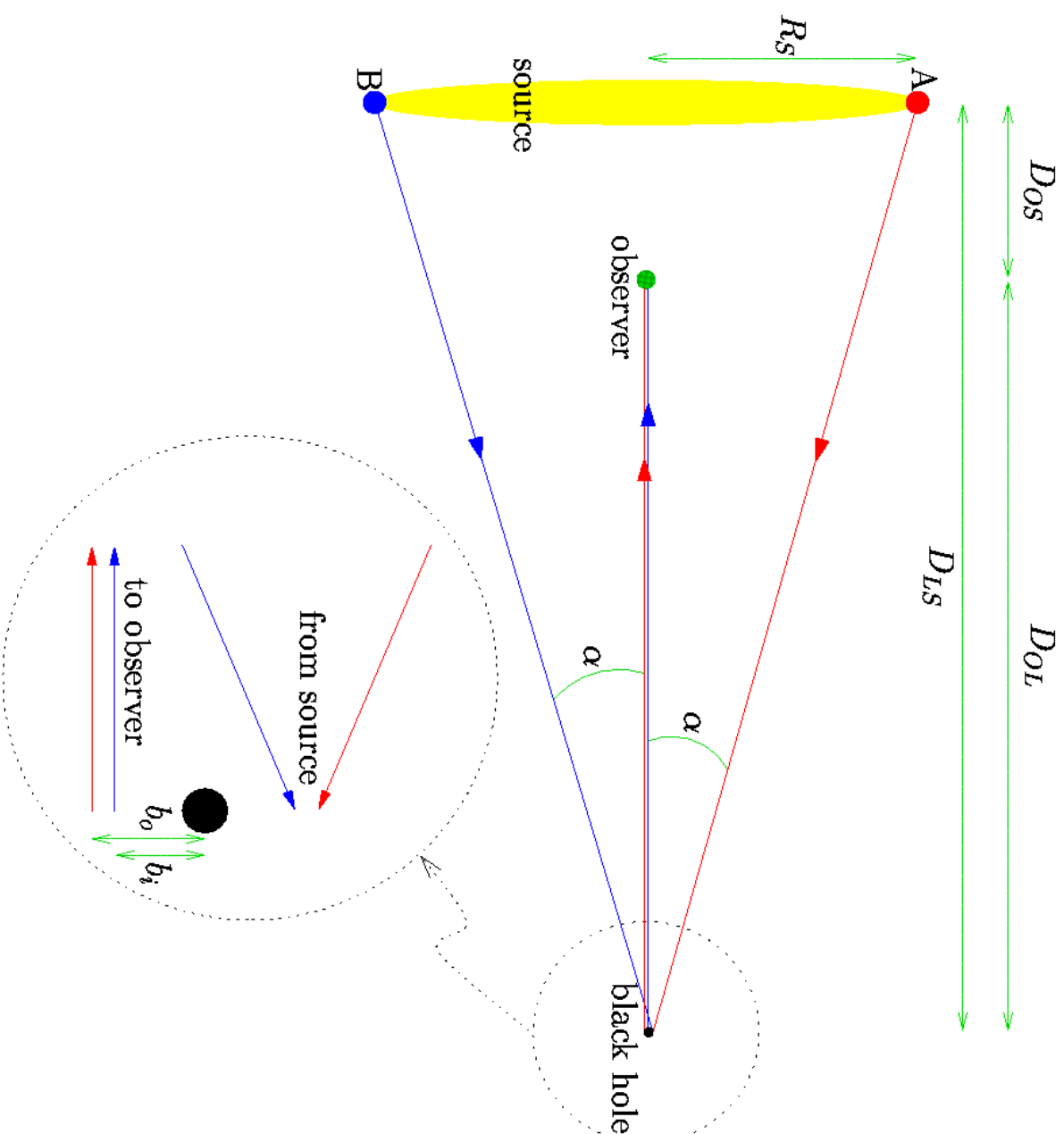


FIG. 1.— Perfect alignment: the (extended) source, observer, and lens are colinear. The resulting image of the source, as lensed by the black hole, is a ring. (The angles in this figure are greatly exaggerated.)



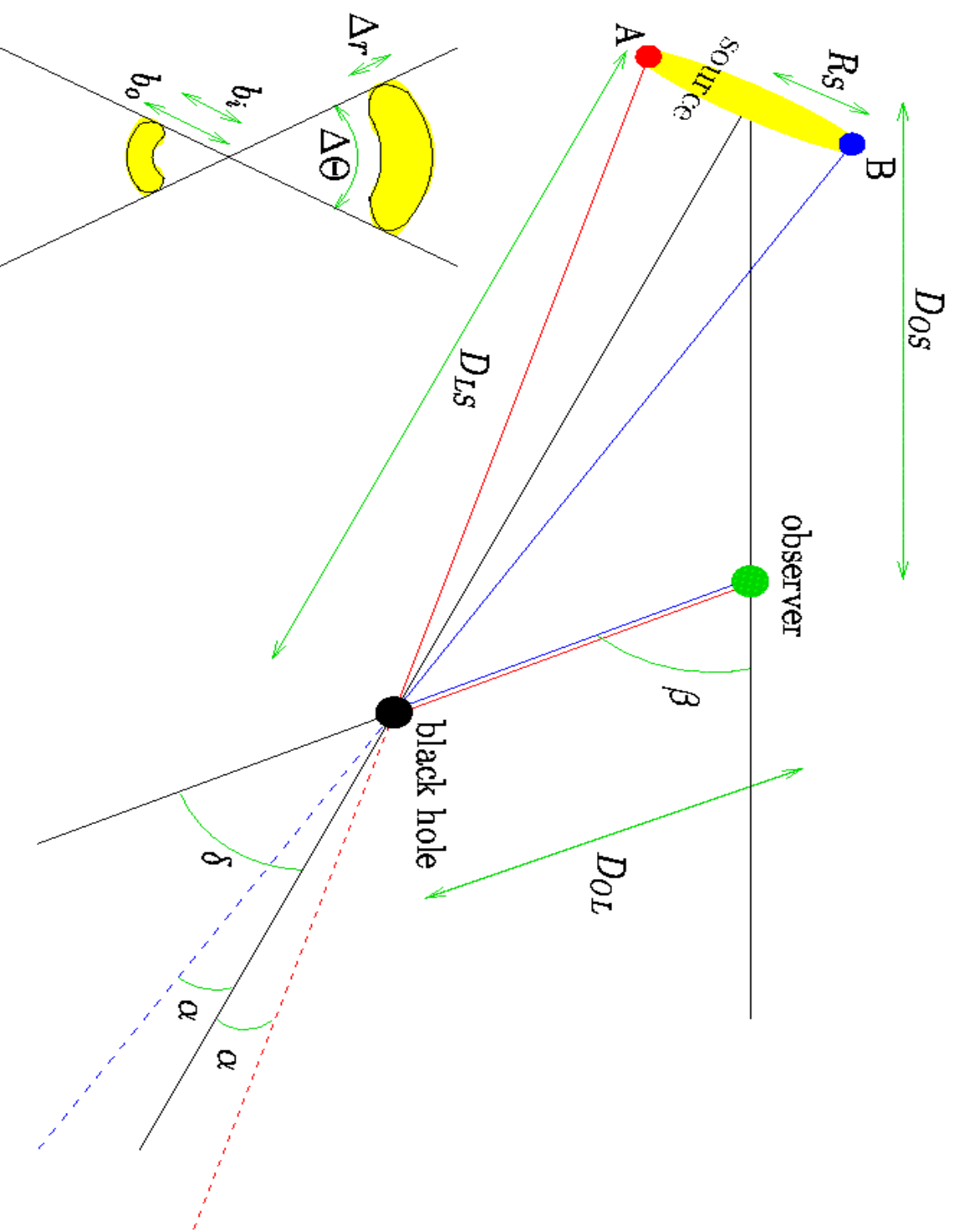


FIG. 2.— Imperfect alignment: the source, observer, and lens are not colinear. Pairs of images are produced, centered on the source–observer–lens plane, on opposite sides of the lens (see inset).

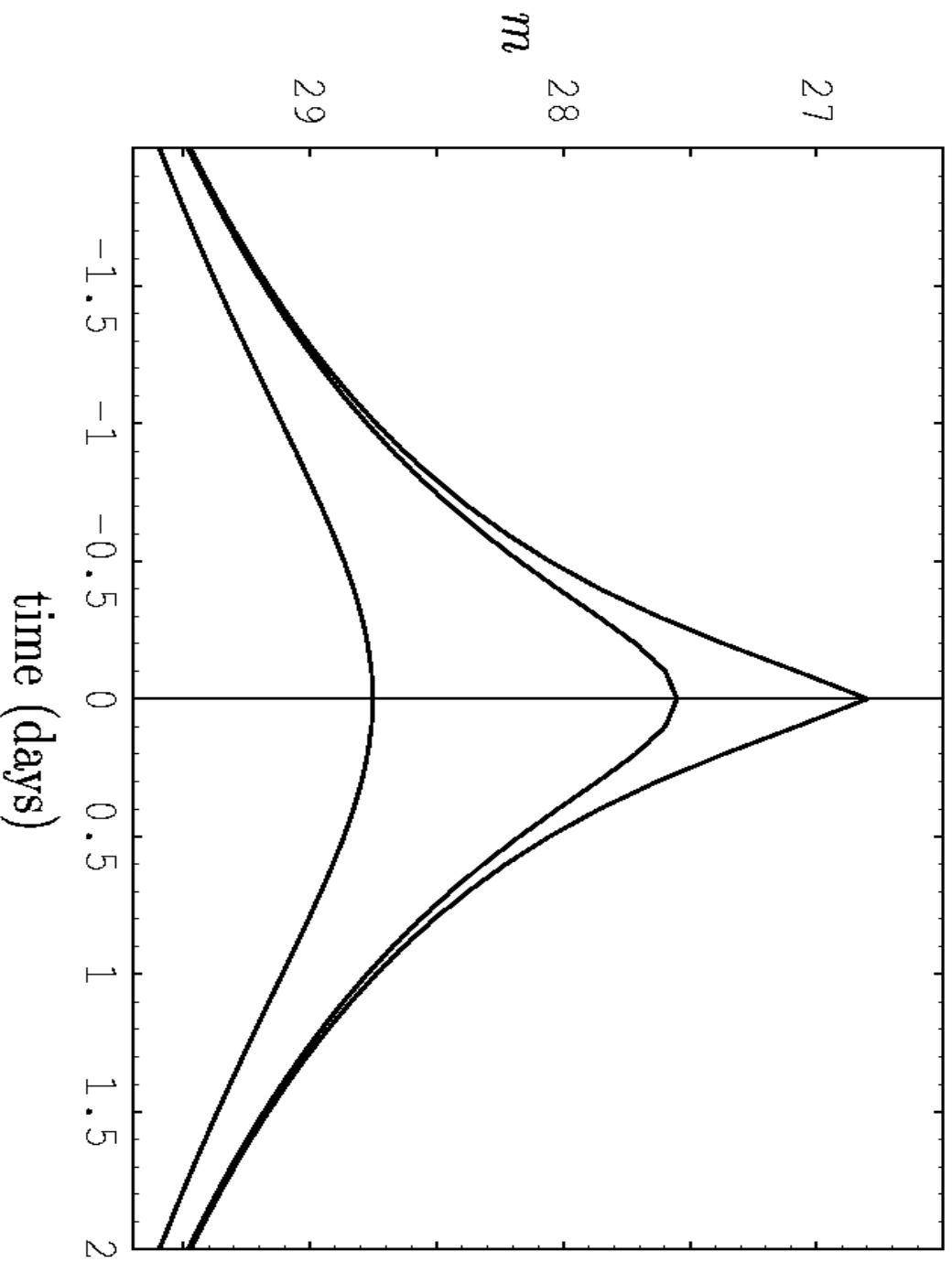


FIG. 3.— Solar retro-MACHO lightcurves: The apparent visual magnitude,  $m$ , of the Sun, imaged in a  $10 M_{\odot}$  black hole at a distance of 0.01 pc. The different curves are for the black hole at angular displacements from the ecliptic plane of 0,  $R_{\odot}/1 \text{ AU}$ , and  $1^\circ$  respectively (top to bottom).

TABLE 1  
RETRO-MACHO BRIGHTNESSES OF THE SUN

BH mass ( $M_{\odot}$ )	BH distance (pc)	$\beta = 0$ (perfect alignment)	$\beta = R_{\odot}/1 \text{ AU}$ (edge alignment)	$\beta = 1^{\circ}$	$\beta = \pi/4$	$\beta = \pi/2$ (max misalignment)
1	$10^{-2}$	31.0	32.6	34	38	38
1	$10^{-1}$	38.6	40.1	41	45	46
10	$10^{-2}$	26.1	27.6	29	33	33
10	$10^{-1}$	33.6	35.1	36	40	41
10	1	41.1	42.6	44	48	48

The full classification of geodesic types for Kerr metric is given by Zakharov (1986). As it was shown in this paper, there are three photon geodesic types: capture, scattering and critical curve which separates the first two sets. This classification fully depends only on two parameters  $\xi = L_z/E$  and  $\eta = Q/E^2$ , which are known as Chandrasekhar's constants (Chandrasekhar 1983). Here the Carter constant  $Q$  is given by Carter (1968)

$$Q = p_\theta^2 + \cos^2 \theta [a^2 (m^2 - E^2) + L_z^2 / \sin^2 \theta], \quad (1)$$

where  $E = p_t$  is the particle energy at infinity,  $L_z = p_\phi$  is  $z$ -component of its angular momentum,  $m = p_i p^i$  is the particle mass. Therefore, since photons have  $m = 0$

$$\eta = p_\theta^2 / E^2 + \cos^2 \theta [-a^2 + \xi^2 / \sin^2 \theta]. \quad (2)$$

The first integral for the equation of photon motion (isotropic geodesics) for a radial coordinate in the Kerr metric is described by the following equation (Carter 1968; Chandrasekhar 1983; Zakharov 1986, 1991a)

$$\rho^4 (dr/d\lambda)^2 = R(r),$$

where

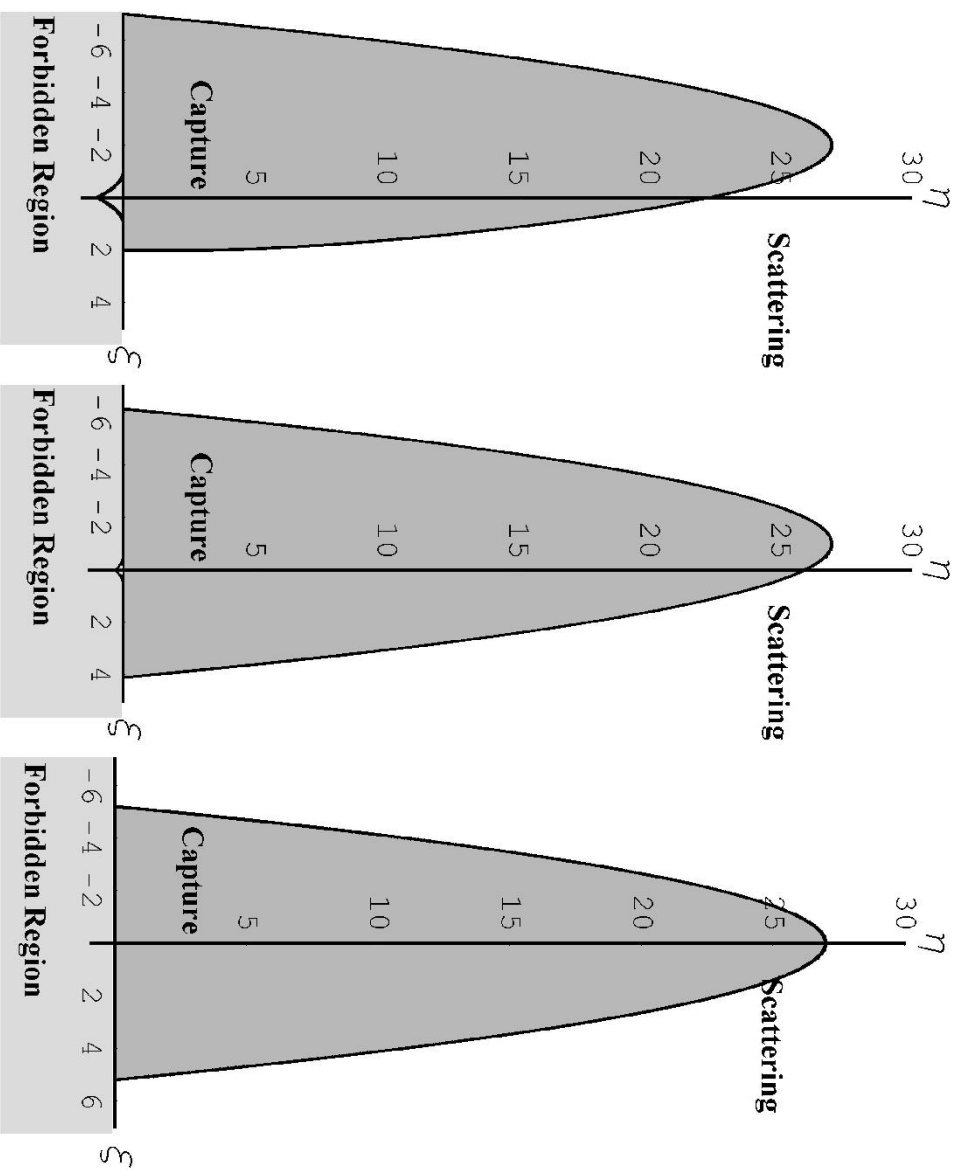
$$R(r) = r^4 + (a^2 - \xi^2 - \eta)r^2 + 2[\eta + (\xi - a)^2]r - a^2\eta, \quad (3)$$

and  $\rho^2 = r^2 + a^2 \cos^2 \theta$ ,  $\Delta = r^2 - 2r + a^2$ ,  $a = S/M^2$ . The constants  $M$  and  $S$  are the black hole mass and angular momentum, respectively. Eq. (3) is written in dimensionless variables (all lengths are expressed in black hole mass units  $M$ ).

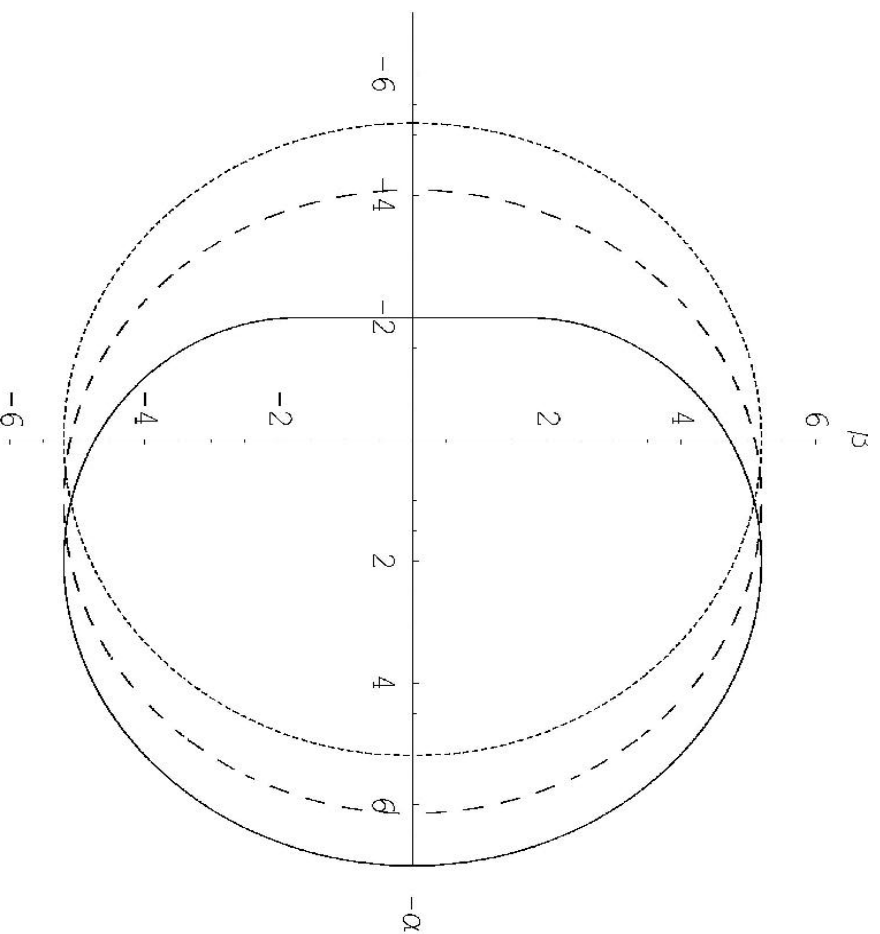
If we fix a black hole spin parameter  $a$  and consider a plane  $(\xi, \eta)$  and different types of photon trajectories corresponding to  $(\xi, \eta)$ , namely, a capture region, a scatter region and the critical curve  $\eta_{\text{crit}}(\xi)$  separating the scatter and capture regions. The critical curve is a set of  $(\xi, \eta)$  where the polynomial  $R(r)$  has a multiple root (a double root for this case). Thus, the critical curve  $\eta_{\text{crit}}(\xi)$  could be determined from the system (Zakharov 1986, 1991a)

$$\begin{aligned} R(r) &= 0, \\ \frac{\partial R}{\partial r}(r) &= 0, \end{aligned} \tag{4}$$

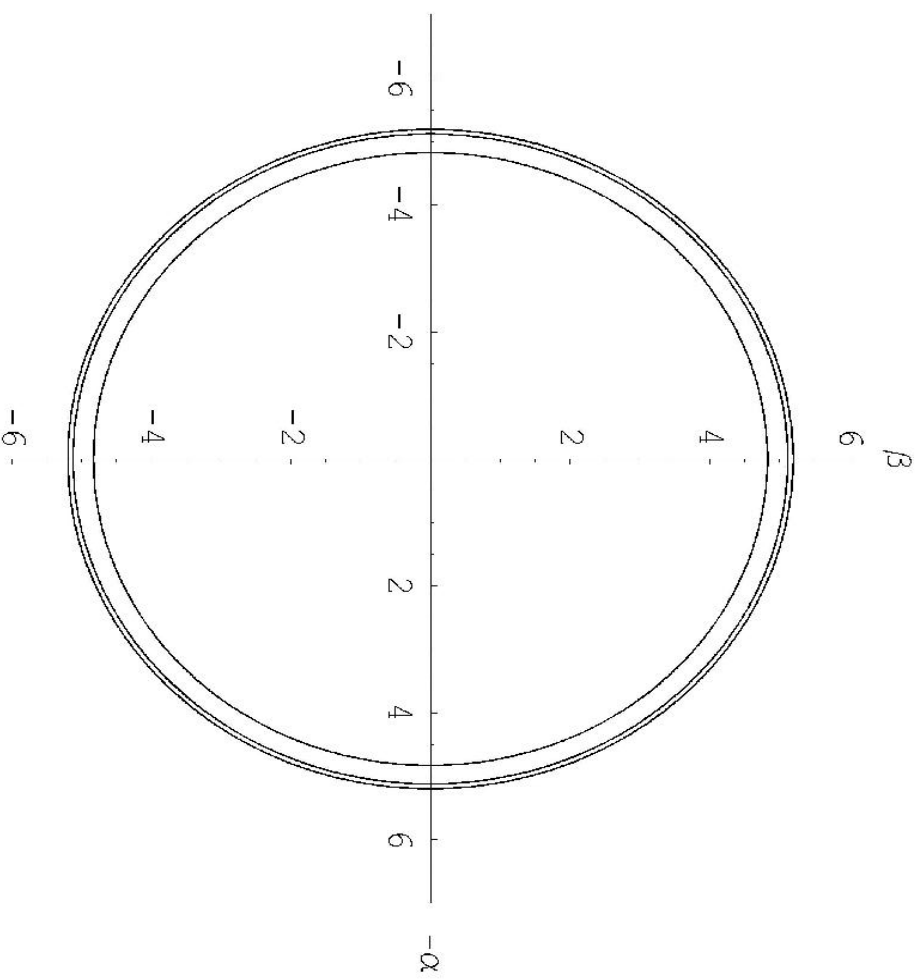
for  $\eta \geq 0, r \geq r_+ = 1 + \sqrt{1 - a^2}$ , because by analysing of trajectories along the  $\theta$  coordinate we know that for  $\eta < 0$  we have  $M = \{(\xi, \eta) | \eta \geq -a^2 + 2a|\xi| - \xi^2, -a \leq \xi \leq a\}$  and for each point  $(\xi, \eta) \in M$  photons will be captured. If instead  $\eta < 0$  and  $(\xi, \eta) \notin M$ , photons cannot have such constants of motion, corresponding to the forbidden region (see, (Chandrasekhar 1983; Zakharov 1986) for details).



**Fig. 1.** Different types for photon trajectories and spin parameters ( $a = 1, a = 0.5, a = 0$ .) Critical curves separate capture and scatter regions. Here we show also the forbidden region corresponding to constants of motion  $\eta < 0$  and  $(\xi, \eta) \in M$  as it was discussed in the text.



**Fig. 2.** Mirages around black hole for equatorial position of distant observer and different spin parameters. The solid line, the dashed line and the dotted line correspond to  $a = 1$ ,  $a = 0.5$ ,  $a = 0$  correspondingly



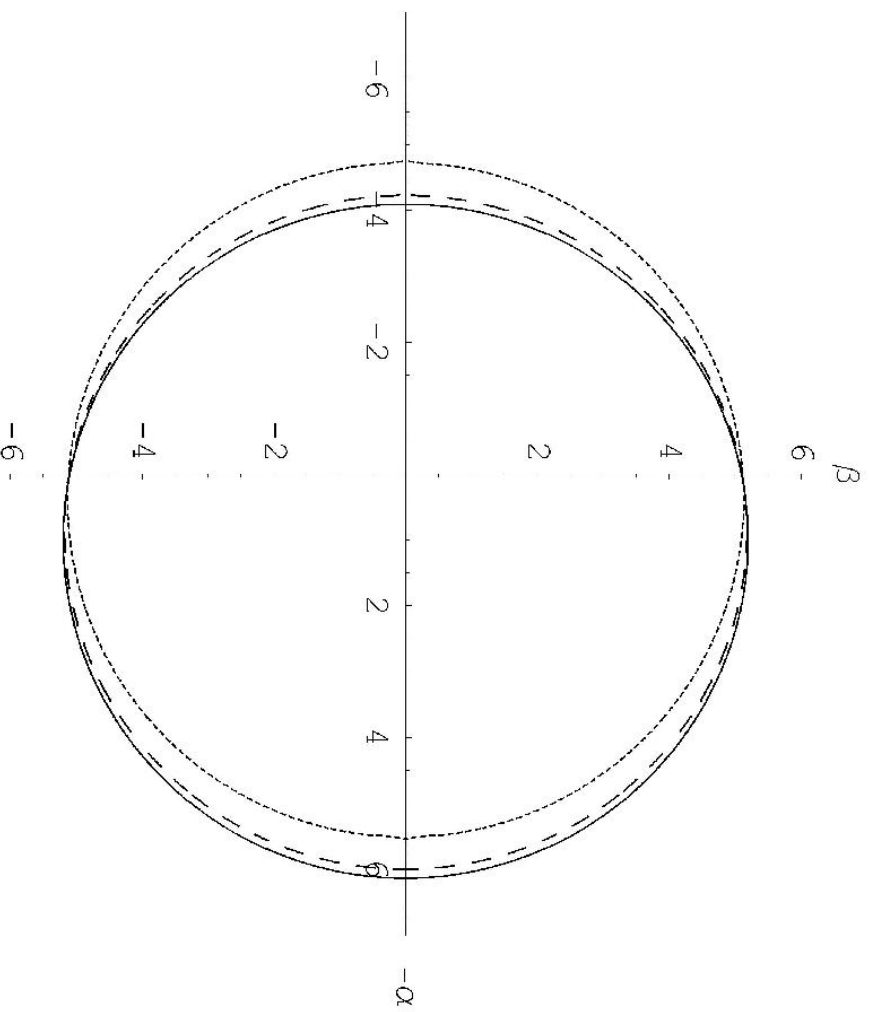
**Fig. 3.** Mirages around a black hole for the polar axis position of distant observer and different spin parameters ( $a = 0, a = 0.5, a = 1$ ). Smaller radii correspond to greater spin parameters.



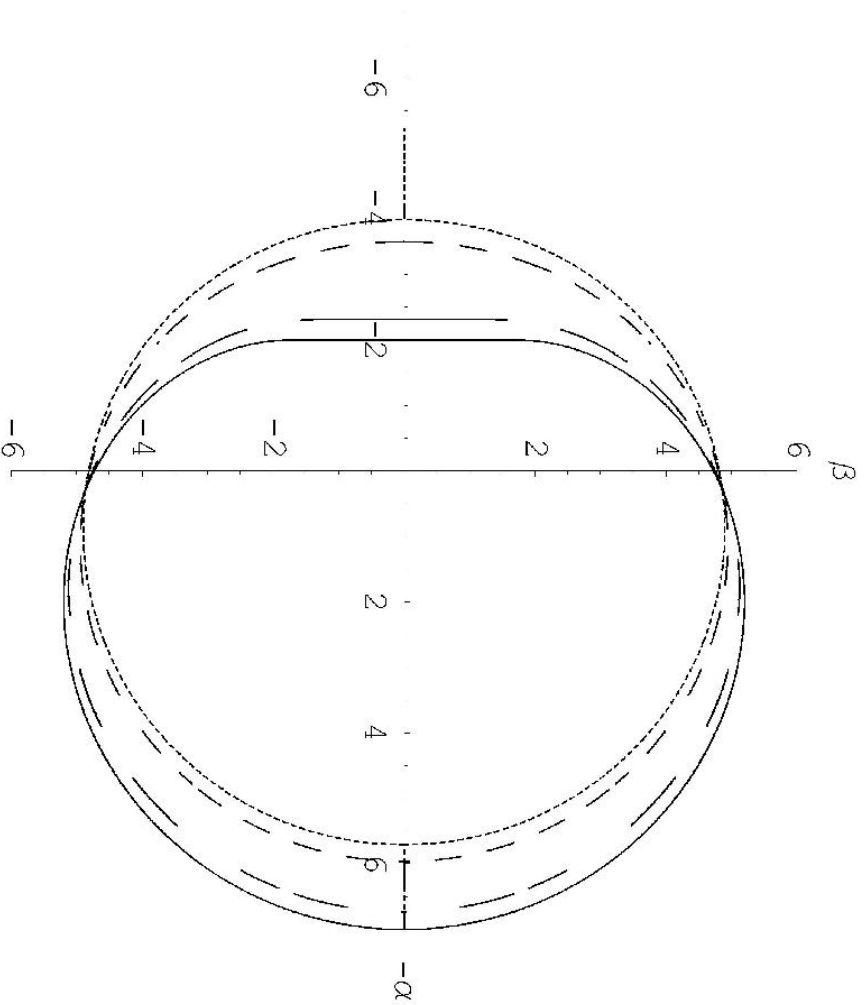


**Table 1.** Dependence of  $\eta(0)$  and mirage radii  $R_{\text{circ}} = (\eta(0) + a^2)^{1/2}$  on spins.

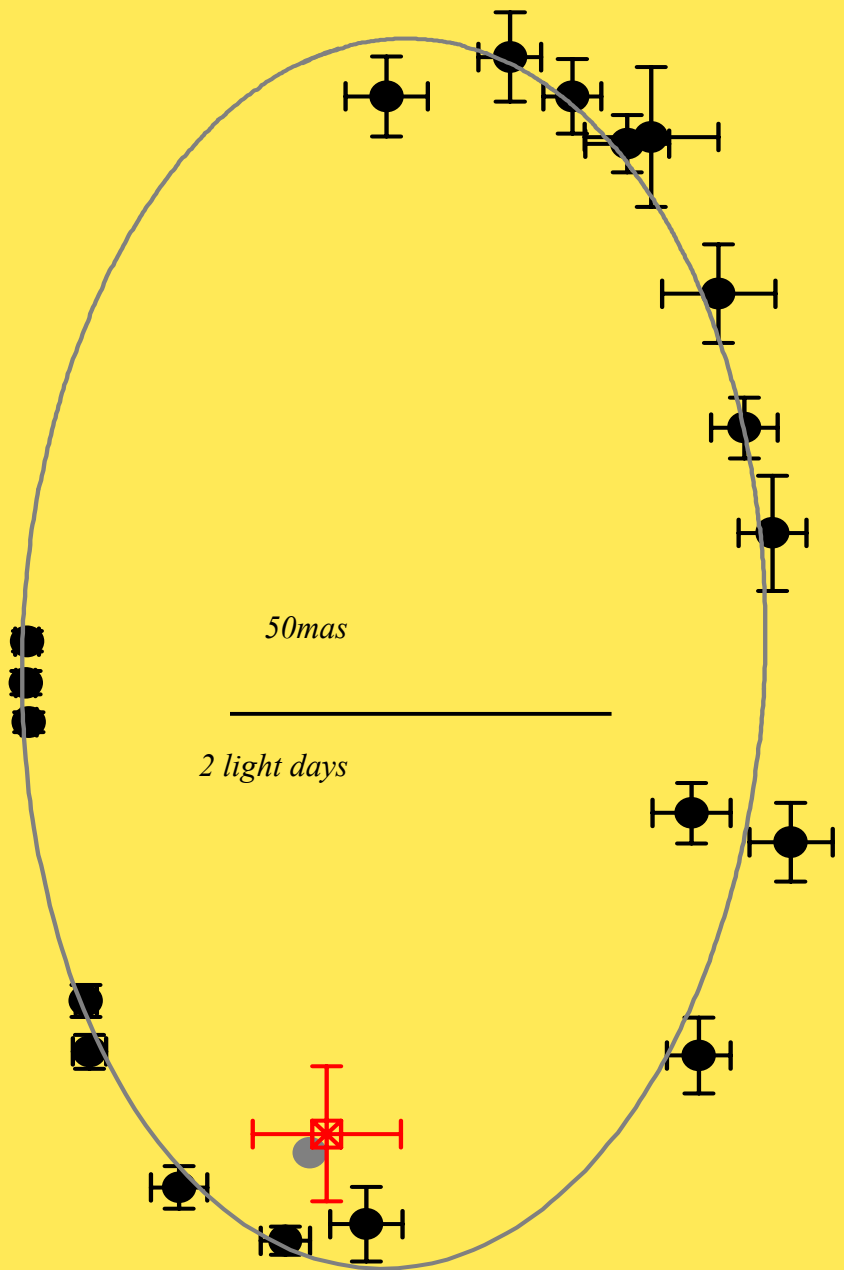
$a$	0	0.2	0.4	0.5	0.6	0.8	1.
$\eta(0)$	27	26.839	26.348	25.970	25.495	24.210	22.314
$R_{\text{circ}}$	5.196	5.185	5.149	5.121	5.085	4.985	4.828



**Fig. 4.** Mirages around black hole for different angular positions of a distant observer and the spin  $a = 0.5$ . Solid, dashed and dotted lines correspond to  $\theta_0 = \pi/2, \pi/3$  and  $\pi/8$ , respectively.



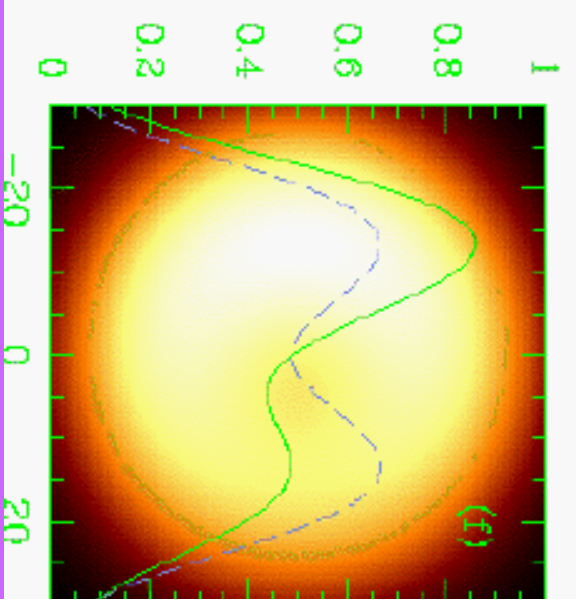
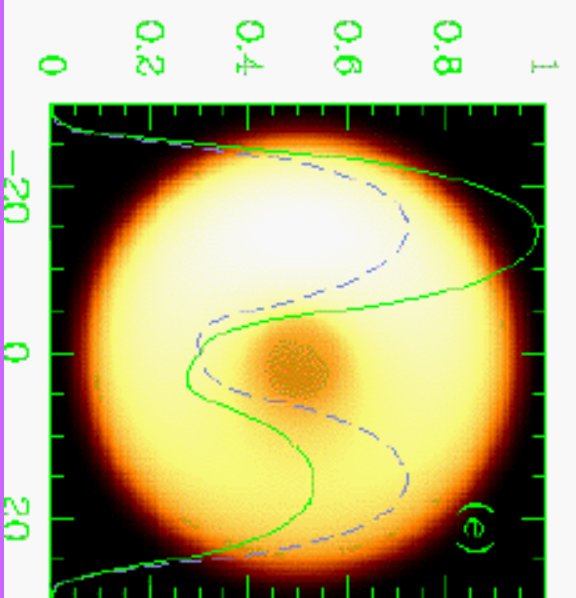
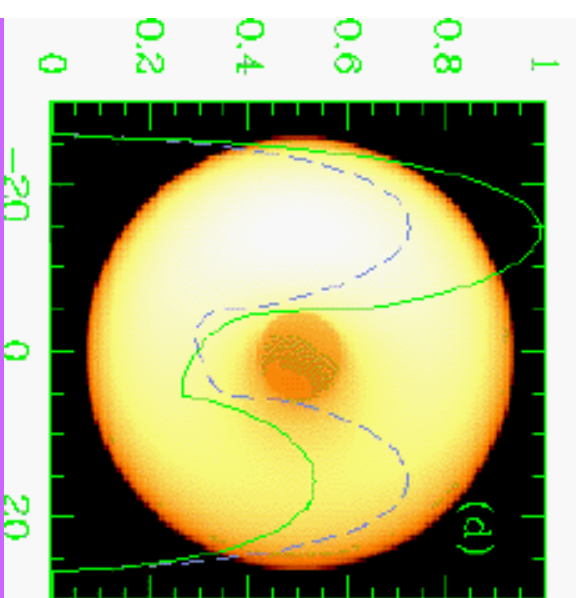
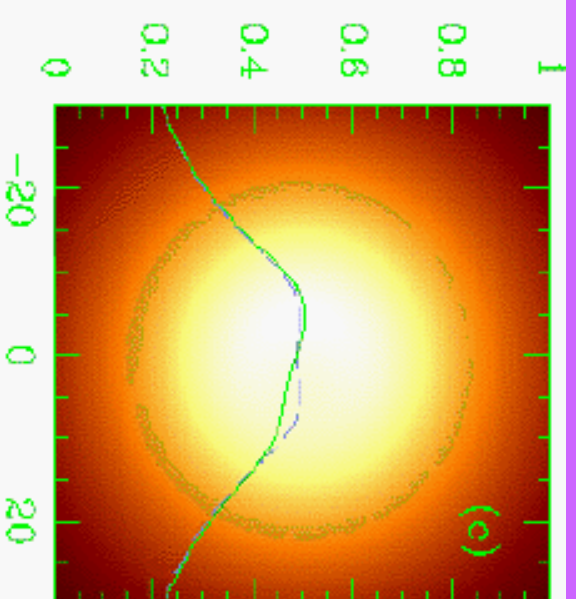
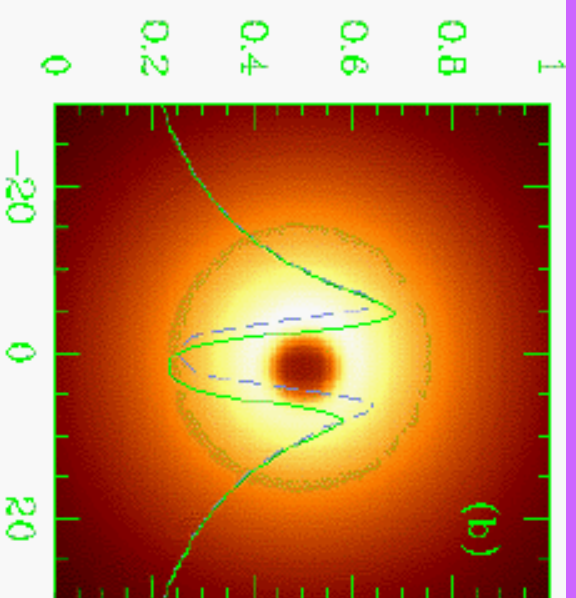
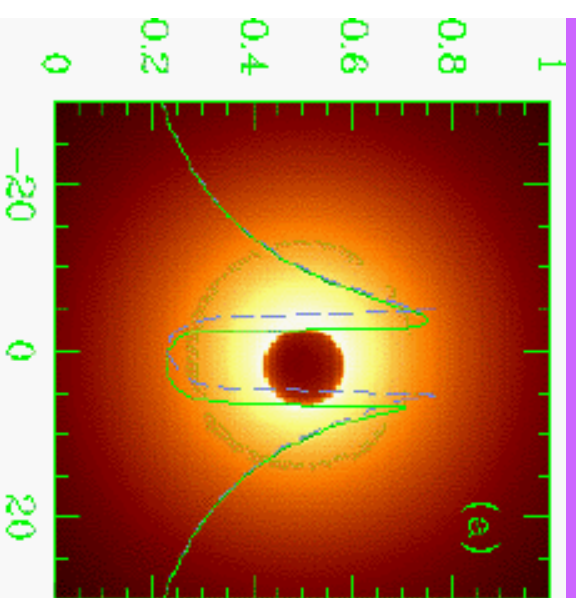
**Fig. 5.** Mirages around black hole for different angular positions of a distant observer and the spin  $a = 1$ . Solid, long dashed, short dashed and dotted lines correspond to  $\theta_0 = \pi/2, \pi/3, \pi/6$  and  $\pi/8$ , respectively.

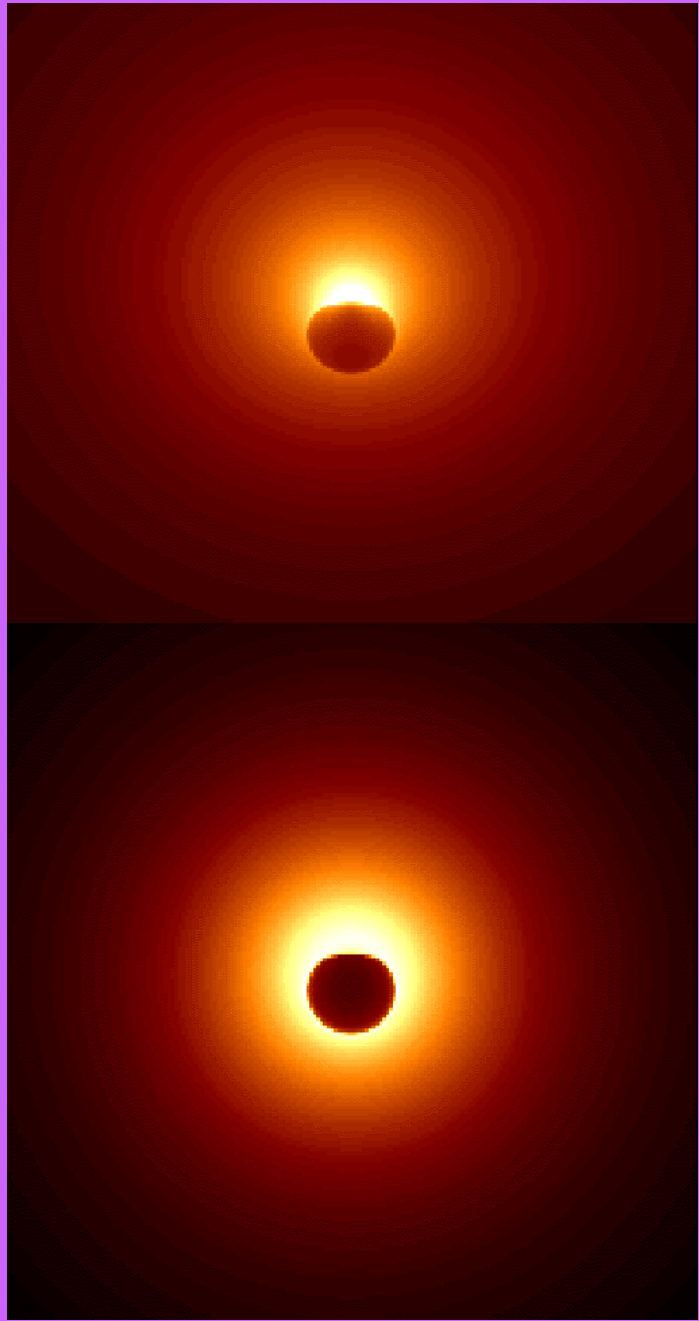


50mas

2 light days

Similarly to Falcke, Melia & Agol (2000) we propose to use VLBI technique to observe the discussed mirages around black holes. They used ray-tracing calculations to evaluate the shapes of shadows. The boundaries of the shadows are black hole mirages (glories or "faces") analyzed earlier. We use the length parameter  $r_g = \frac{GM}{c^2} = 6 \times 10^{11}$  cm to calculate all values in these units as it was explained in the text. If we take into account the distance towards the Galactic Center  $D_{GC} = 8$  kpc then the length  $r_g$  corresponds to angular sizes  $\sim 5 \mu\text{as}$ . Since the minimum arc size for the considered mirages are about  $2r_g$ , the standard RADIOASTRON resolution of about  $8 \mu\text{as}$  is comparable with the required precision. The resolution in the case of the higher orbit and shortest wavelength is  $\sim 1 \mu\text{as}$  (Table 2) good enough to reconstruct the shapes. Therefore, in principle it will be possible to evaluate  $a$  and  $\theta$  parameters after mirage shape reconstructions from observational data even if we will observe only the bright part of the image (the bright arc) corresponding to positive parameters  $\alpha$ . However, Gammie, Shapiro & McKinney (2004)



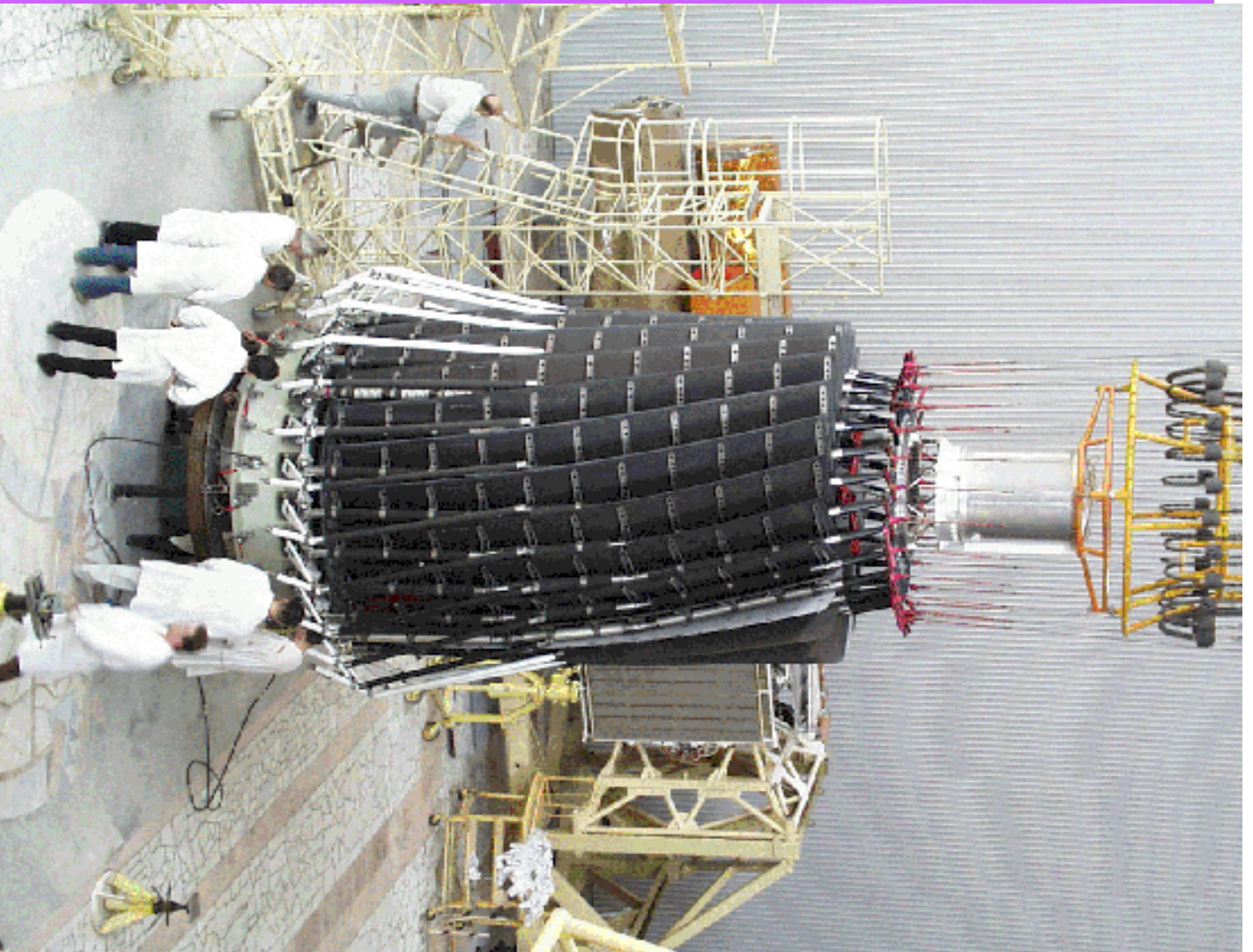


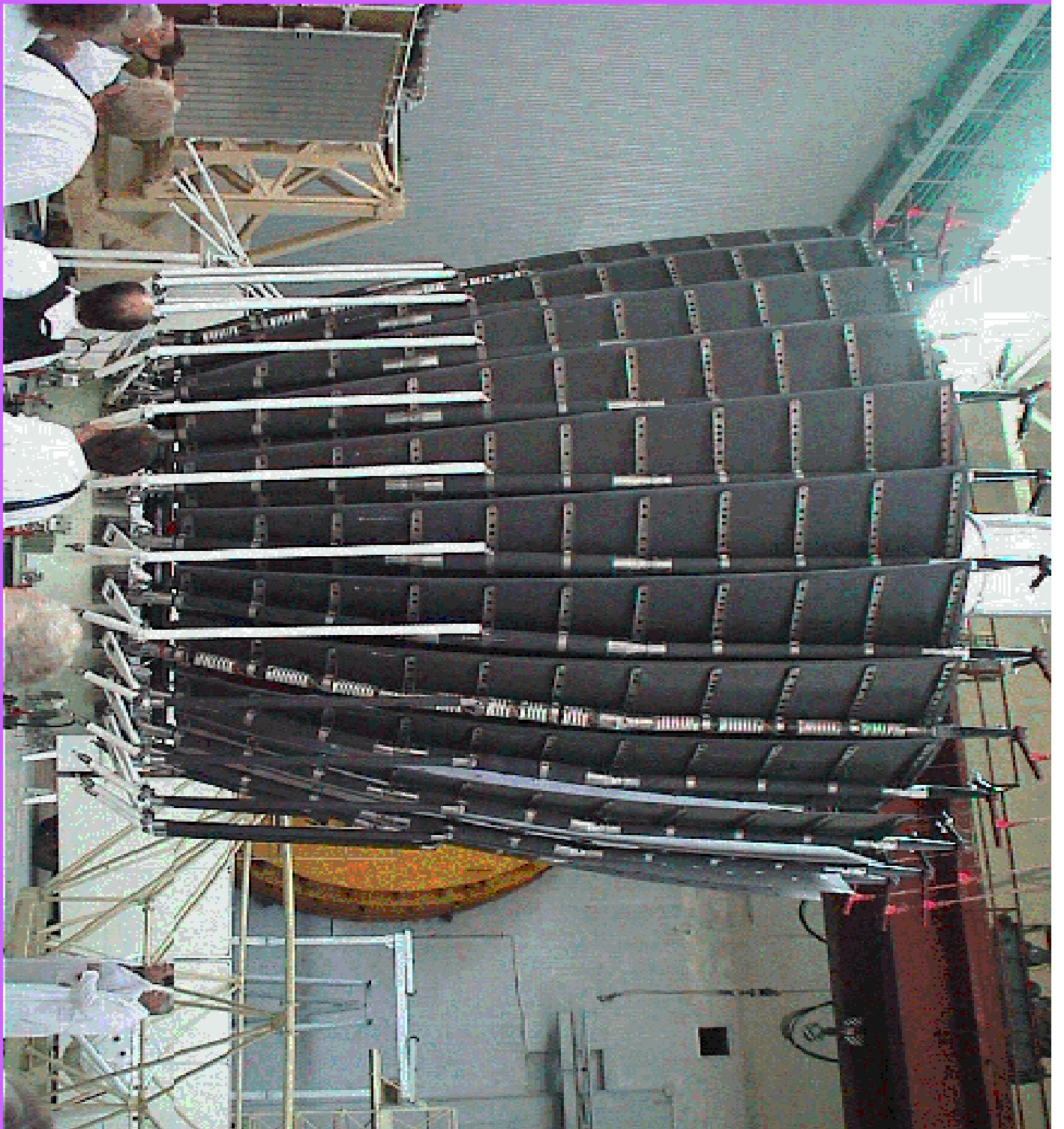


**Table 2.** The fringe sizes (in micro arc seconds) for the standard and advanced apogees  $B_{max}$  (350 000 and 3 200 000 km correspondingly).

$B_{max}$ (km) \ $\lambda$ (cm)	92	18	6.2	1.35
$3.5 \times 10^5$	540	106	37	8
$3.2 \times 10^6$	59	12	4	0.9





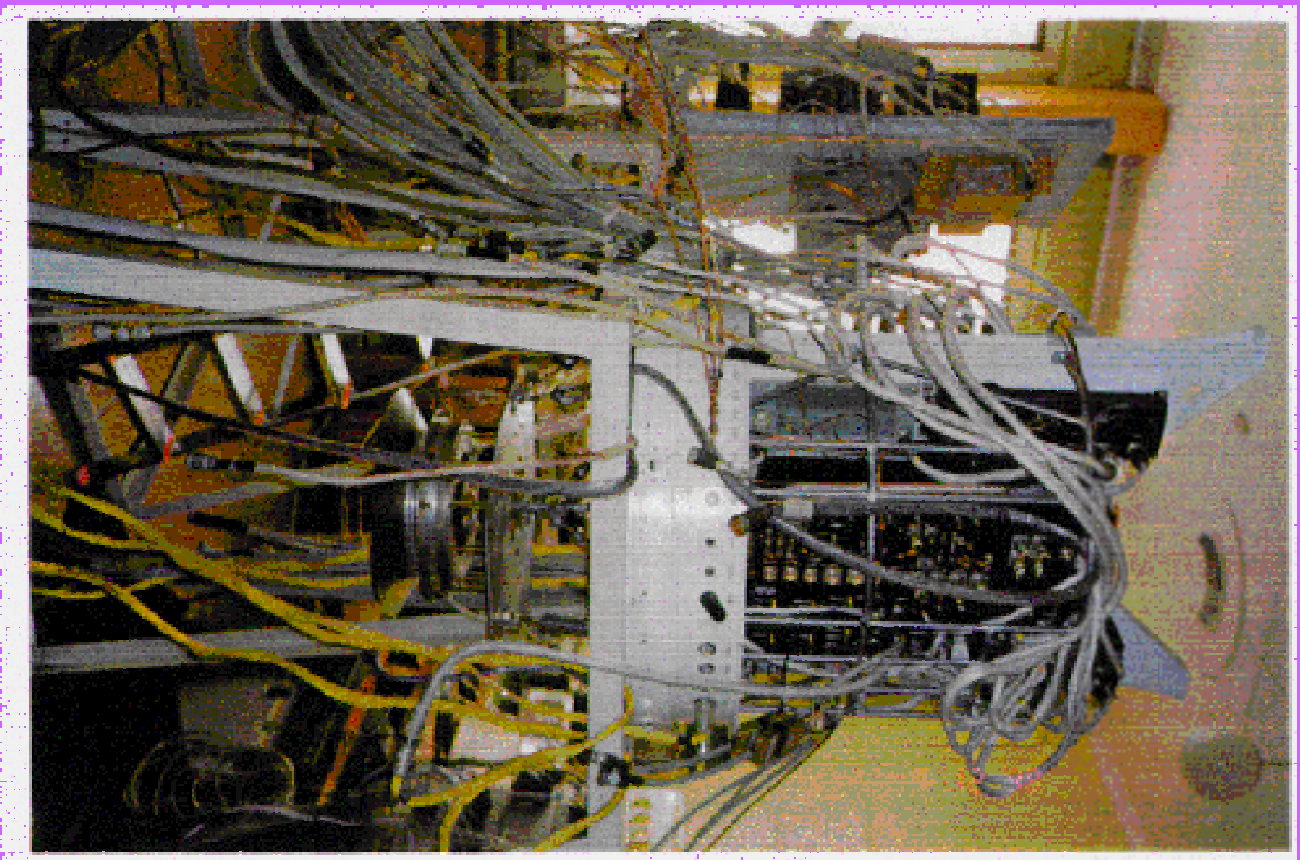












**SRT electronics - under testing in ASC**



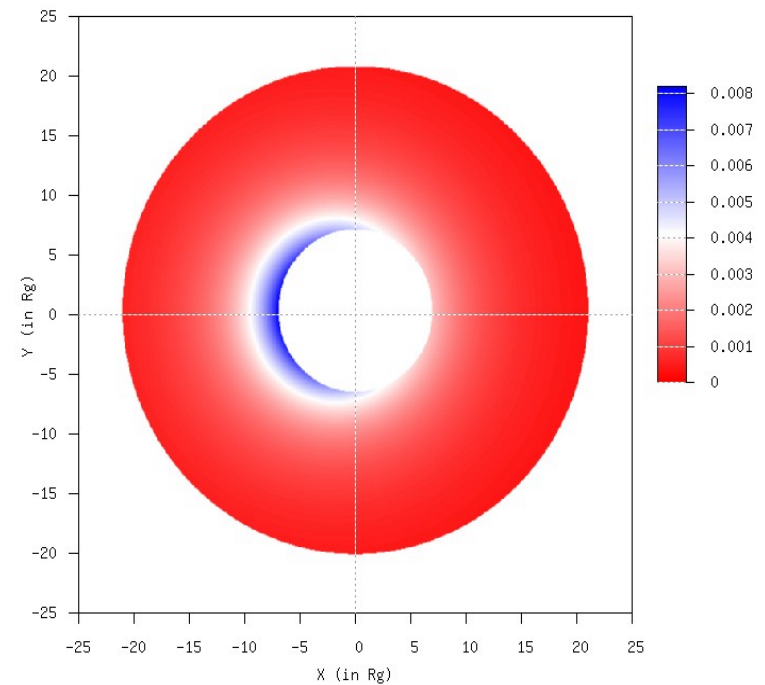
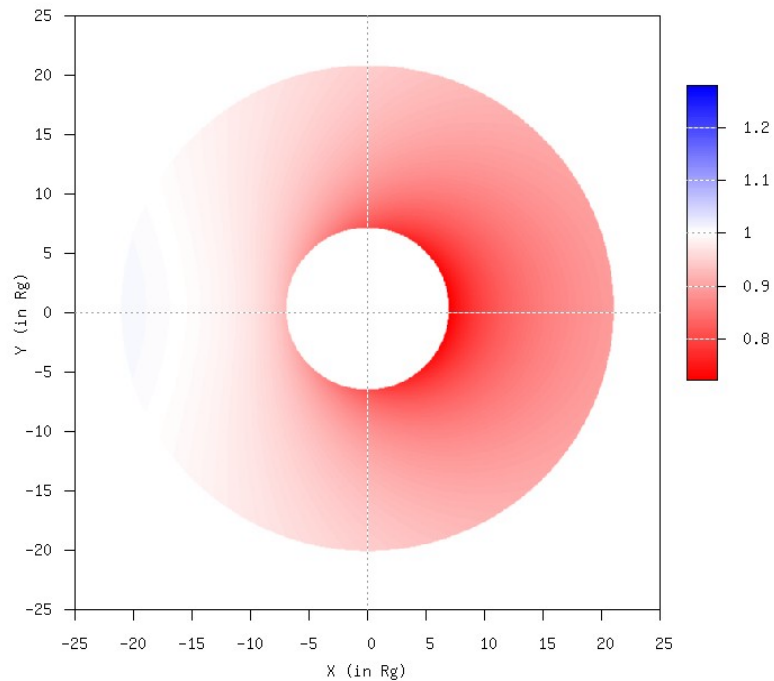


# Schwarzschild black hole images (with P. Jovanovic, L. Popovic in preparation)

$\theta=15$  deg

- Redshift map

Intensity map



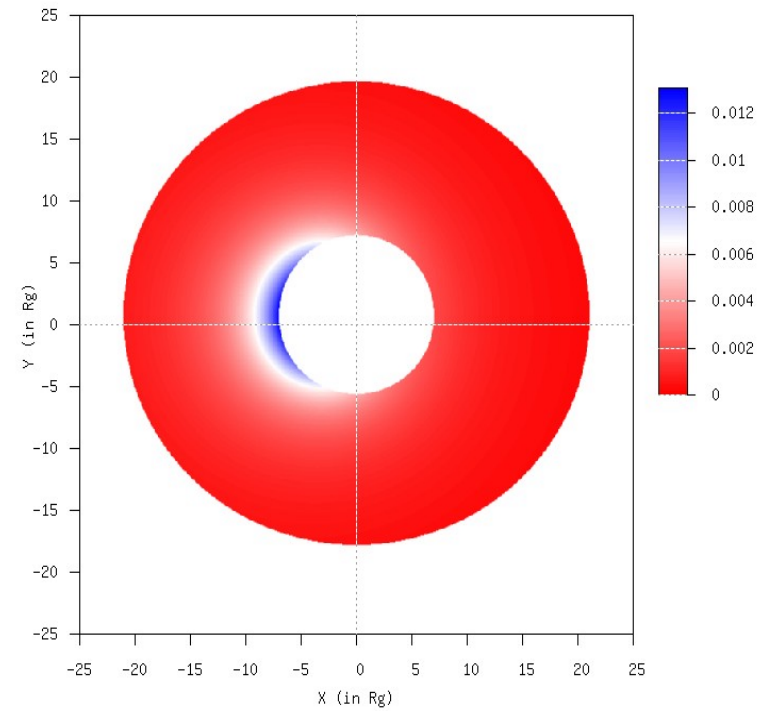
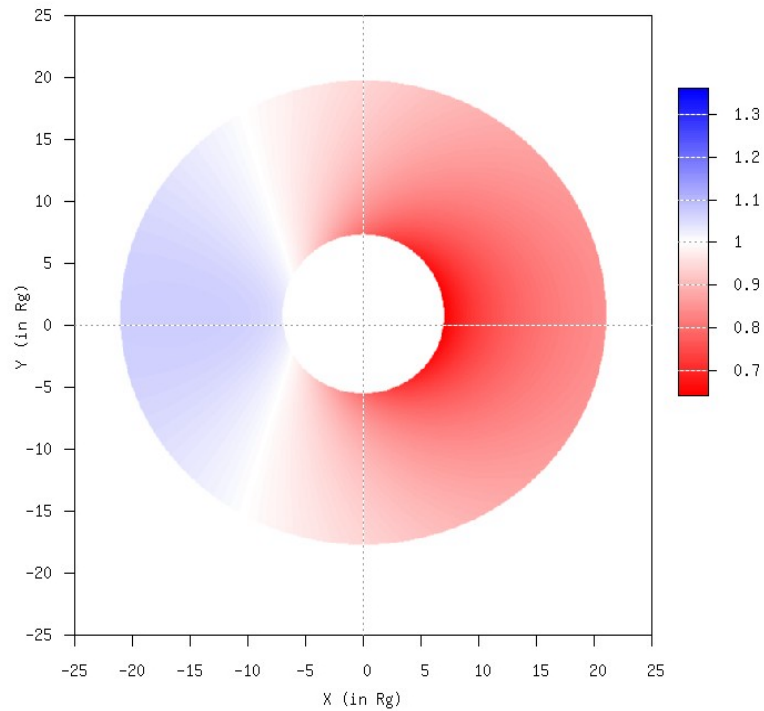


# Schwarzschild black hole images

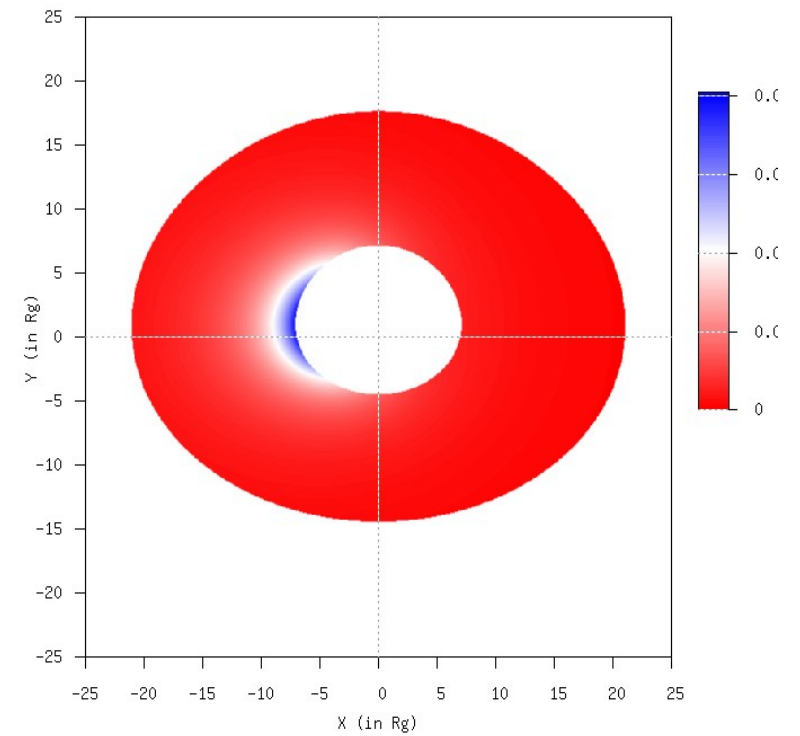
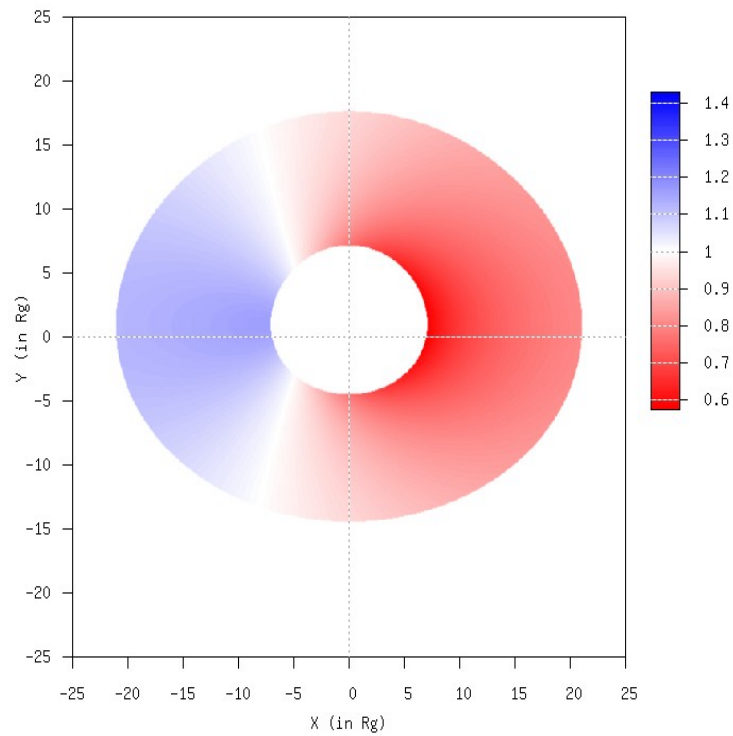
$\theta=30$  deg

- Redshift map

Intensity map



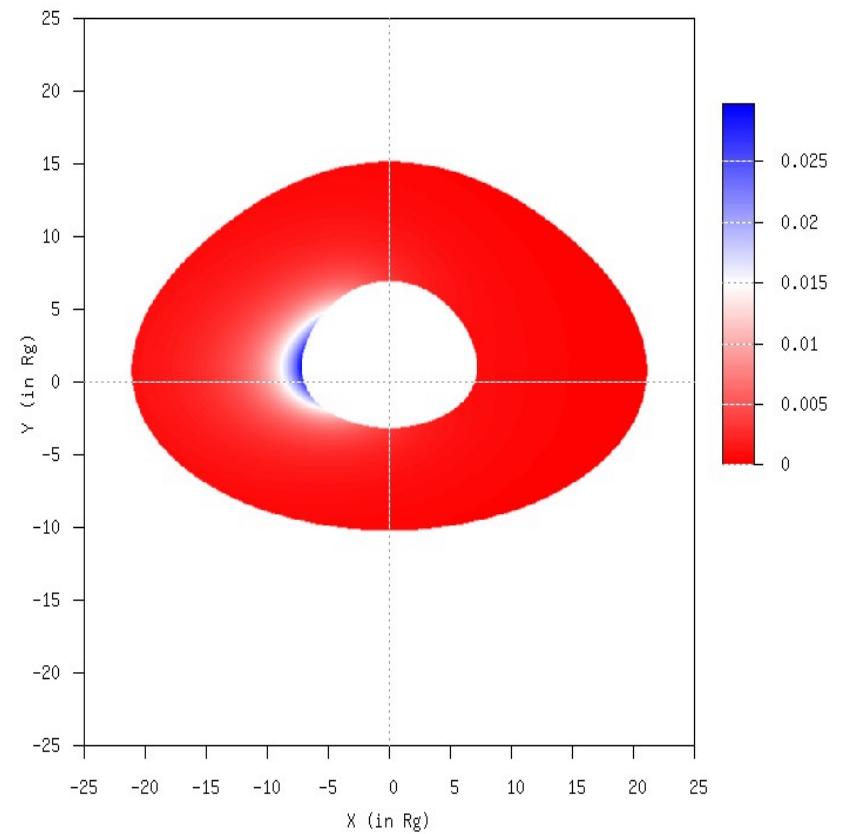
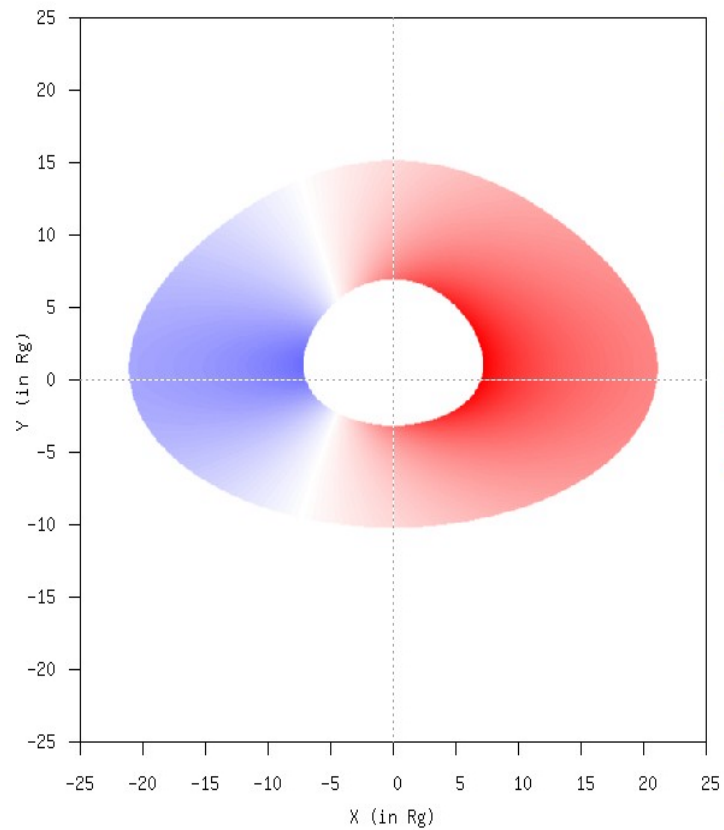
# Schwarzschild black hole images: $\theta=45$ deg



# Schwarzschild black hole images: $\theta=60$ deg

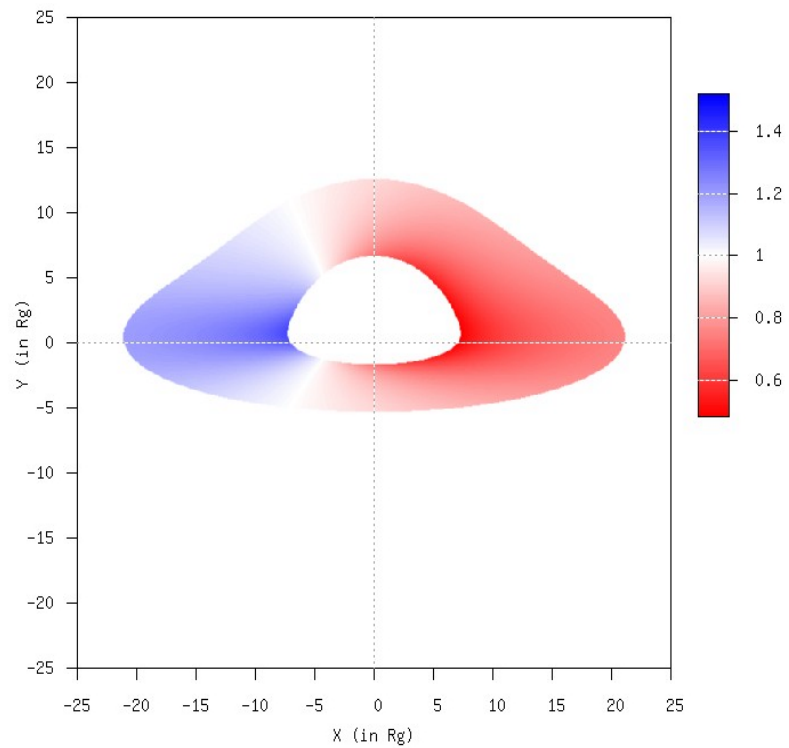
- Redshift map

- Intensity map



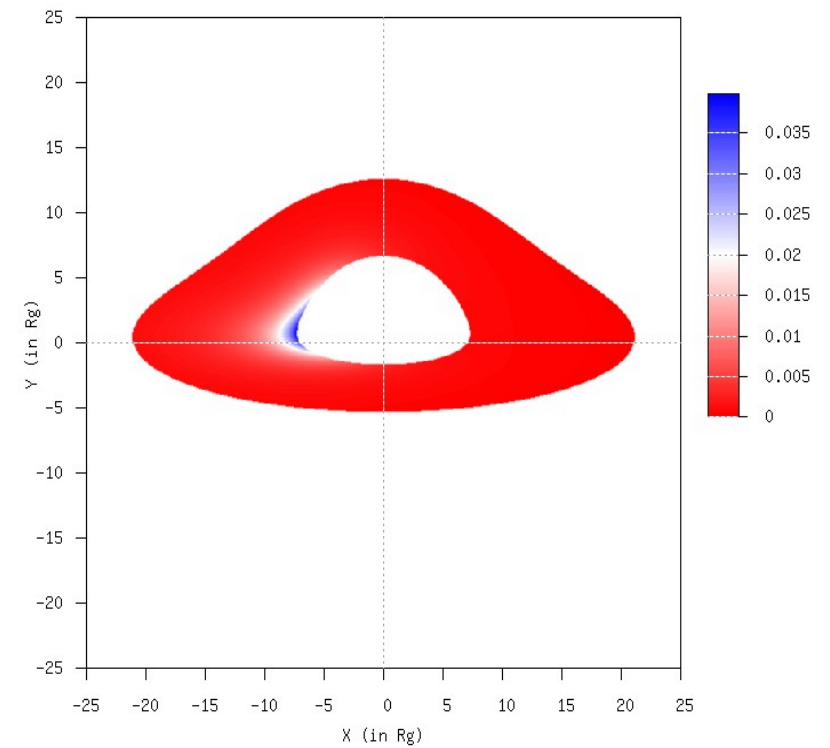
# Schwarzschild black hole images: $\theta=75$ deg

- Redshift map



- 

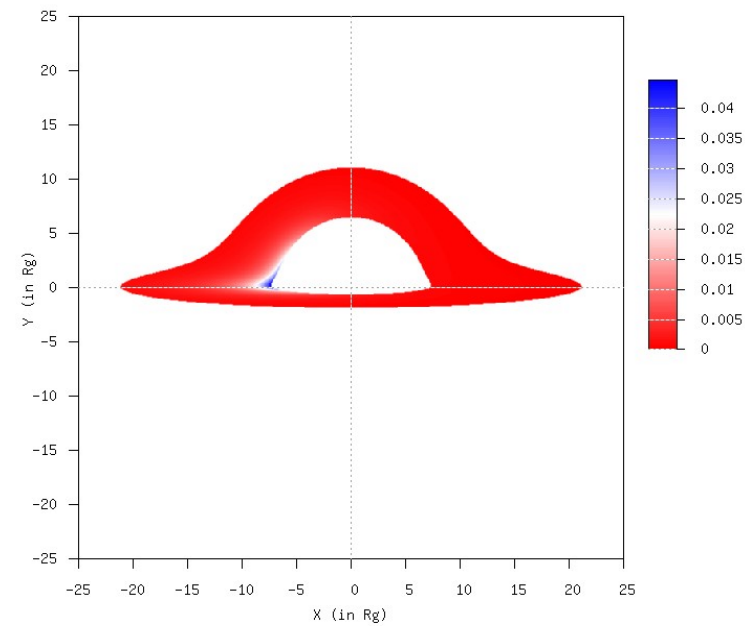
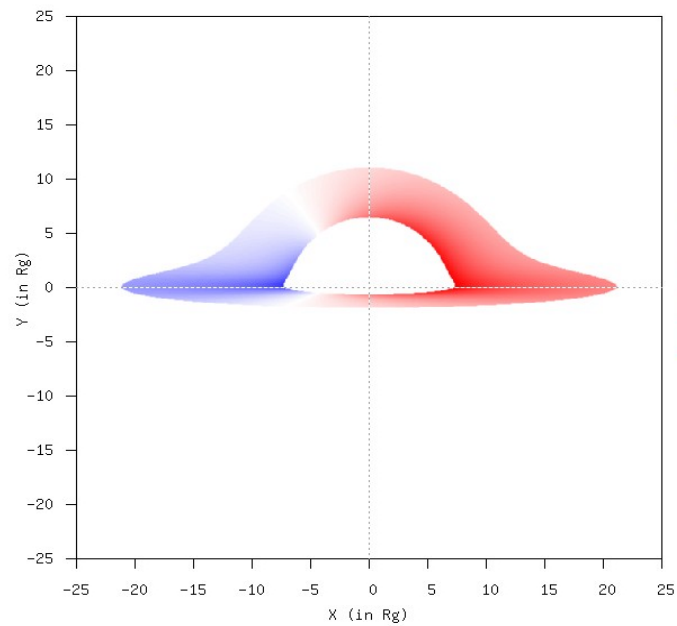
Intensity map



# Schwarzschild black hole images: $\theta=85$ deg

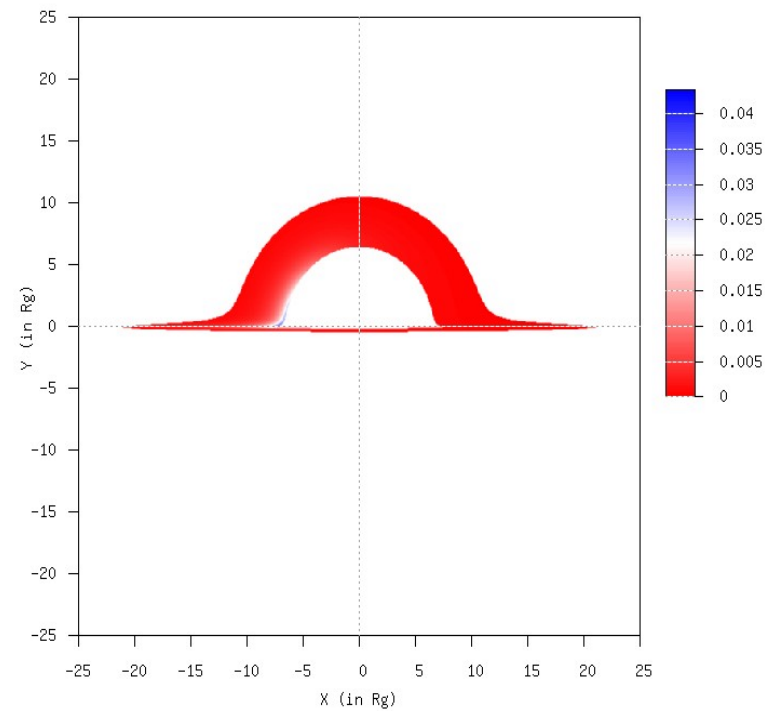
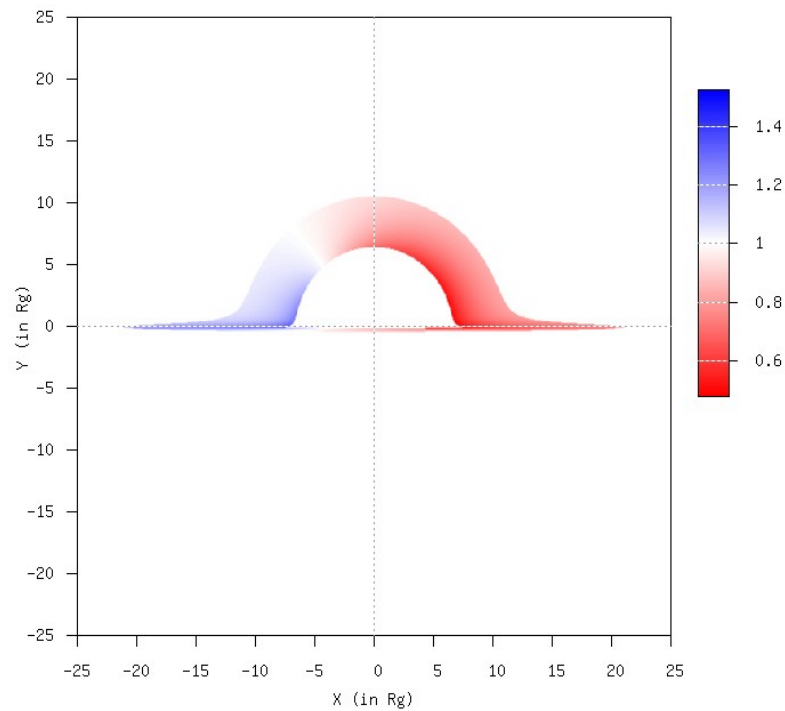
- Redshift map

Intensity map



# Schwarzschild black hole images: $\theta=89$ deg

- Redshift map

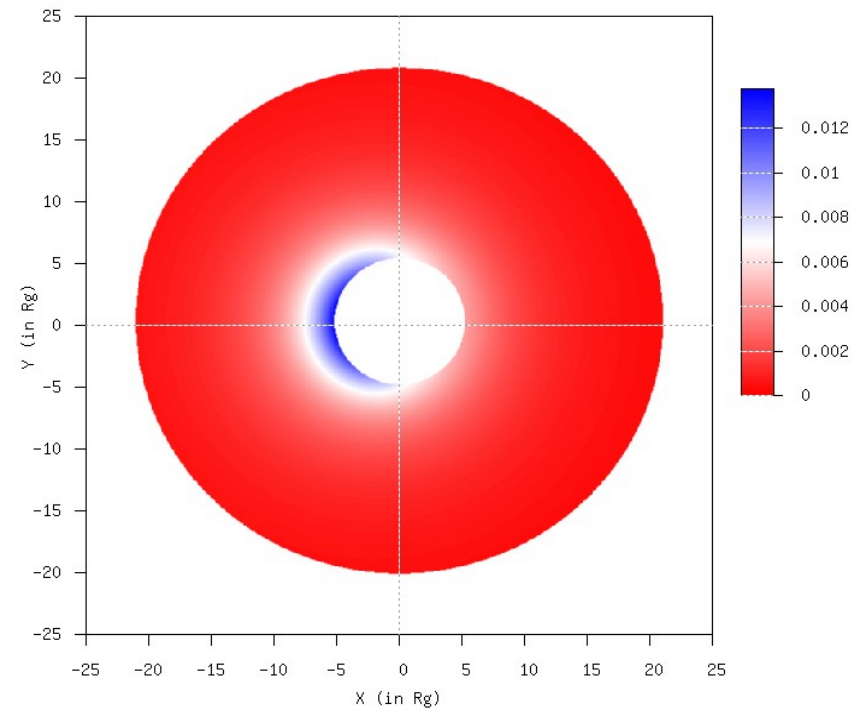
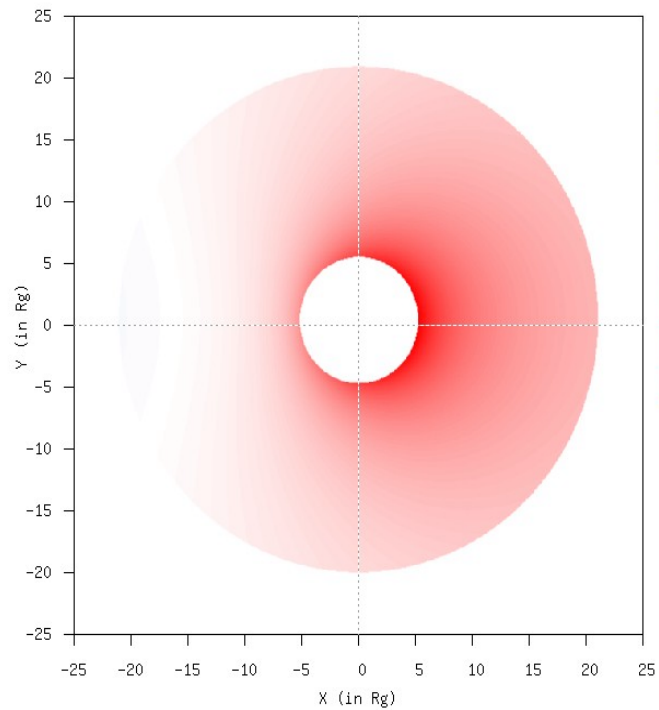


# Kerr black hole images ( $a=0.5$ ): $\theta=15$ deg

- Redshift map

•

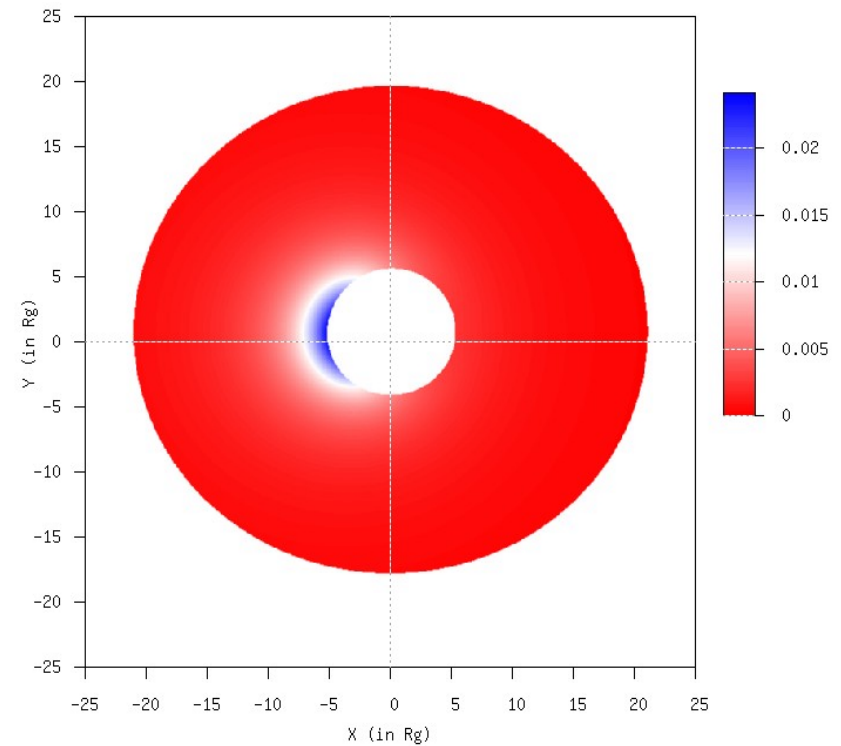
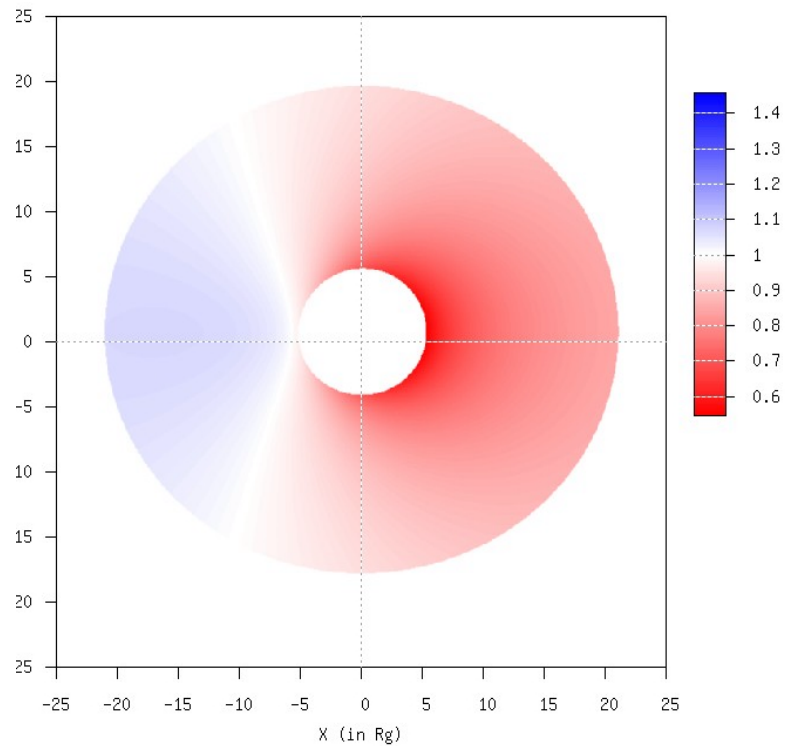
Intensity map



# Kerr black hole images ( $a=0.5$ ): $\theta=30$ deg

- Redshift map

• Intensity map

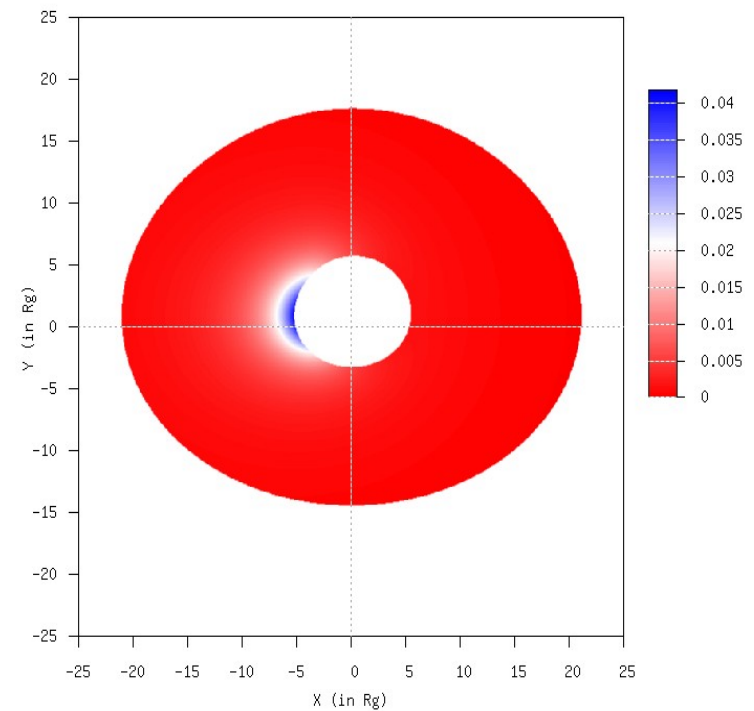
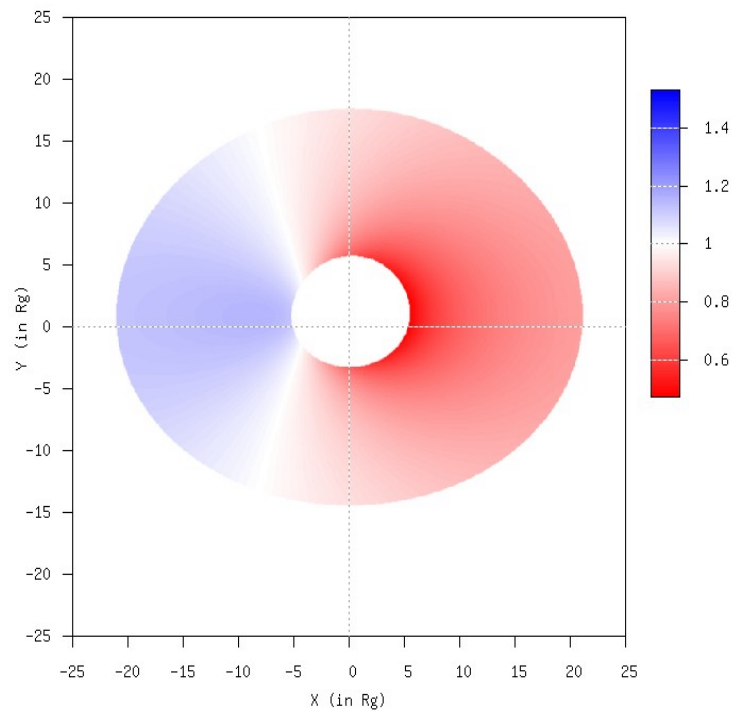




# Kerr black hole images ( $a=0.5$ ): $\theta=45$ deg

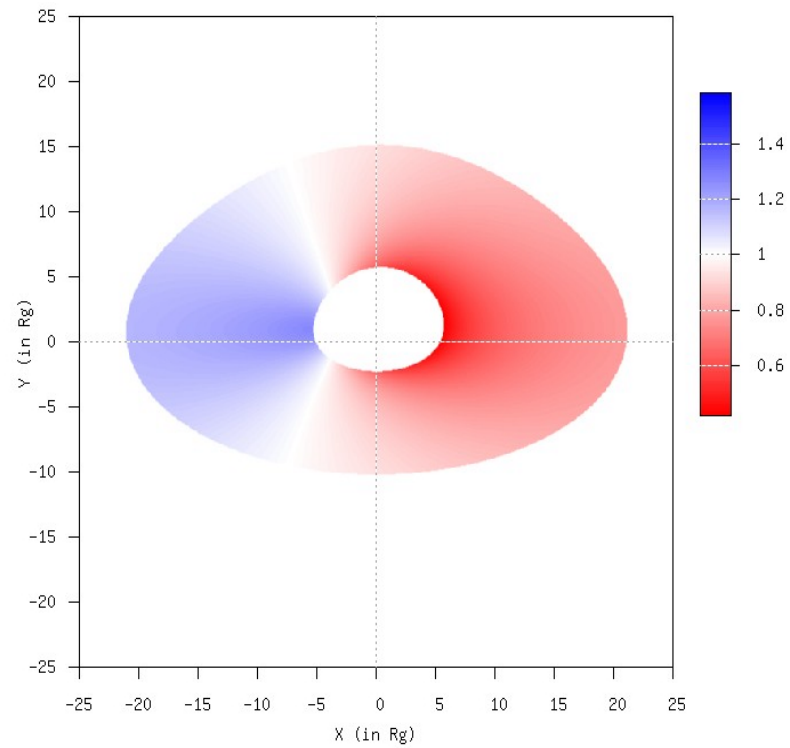
- Redshift map

• Intensity map



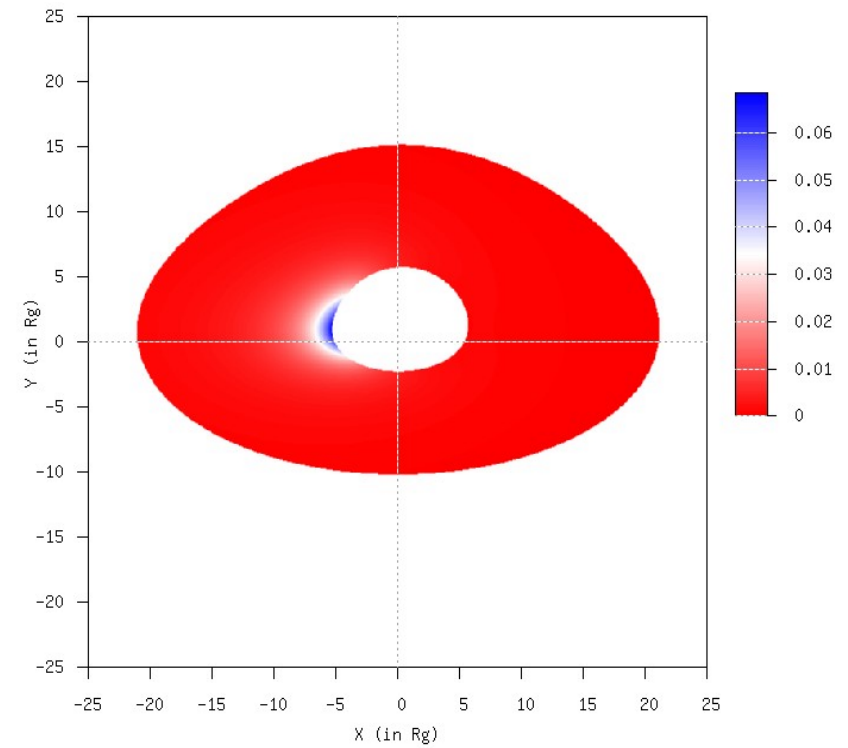
# Kerr black hole images ( $a=0.5$ ): $\theta=60$ deg

- Redshift map



- 

Intensity map

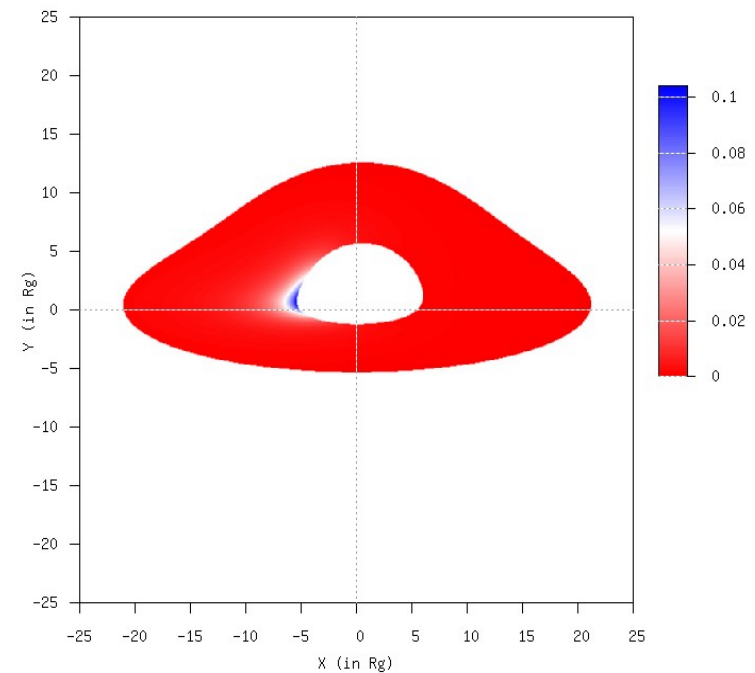
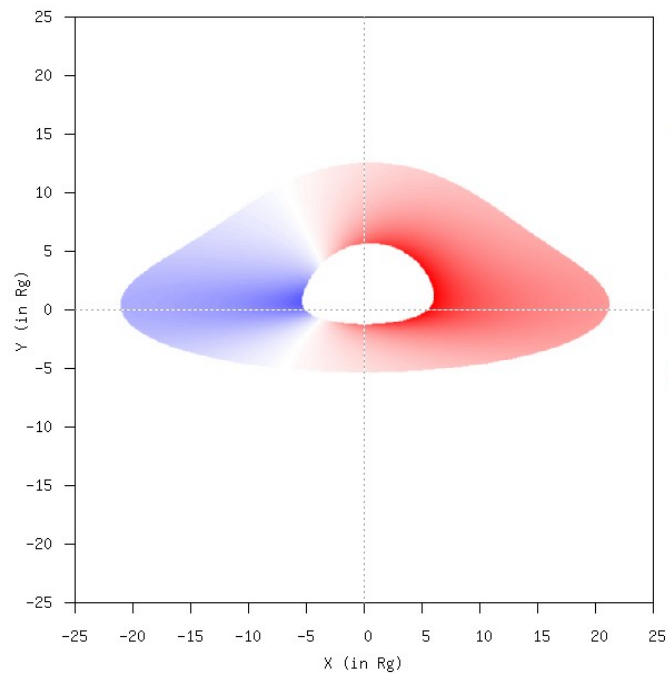


# Kerr black hole images ( $a=0.5$ ): $\theta=75$ deg

- Redshift map

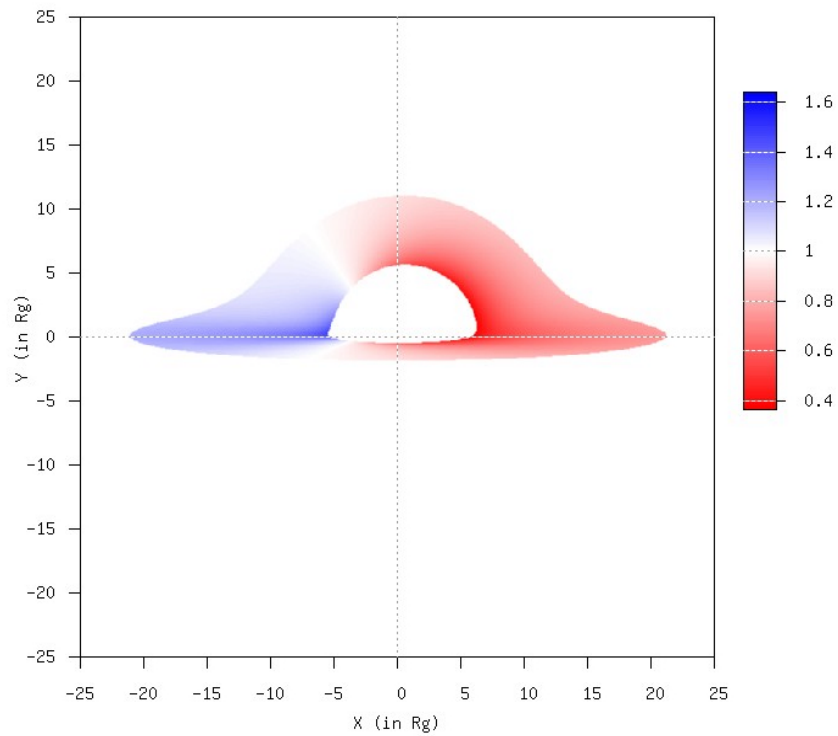
•

Intensity map



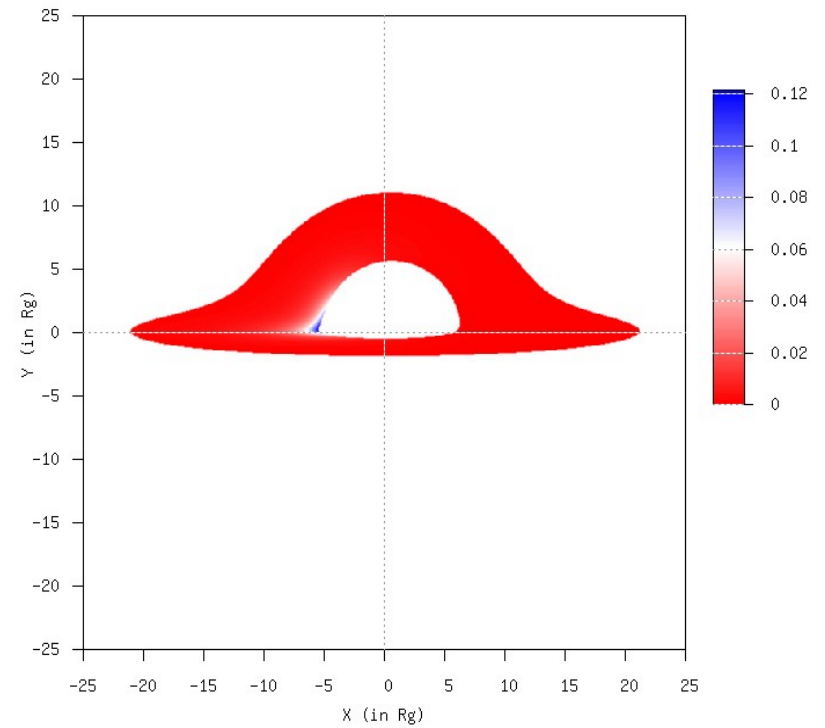
# Kerr black hole images ( $a=0.5$ ): $\theta=85$ deg

- Redshift map



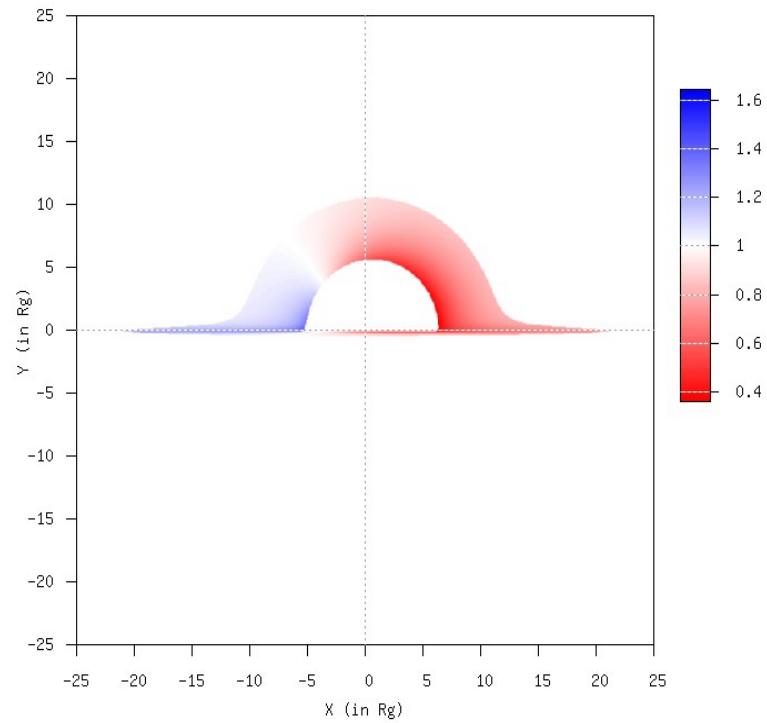
- 

Intensity map



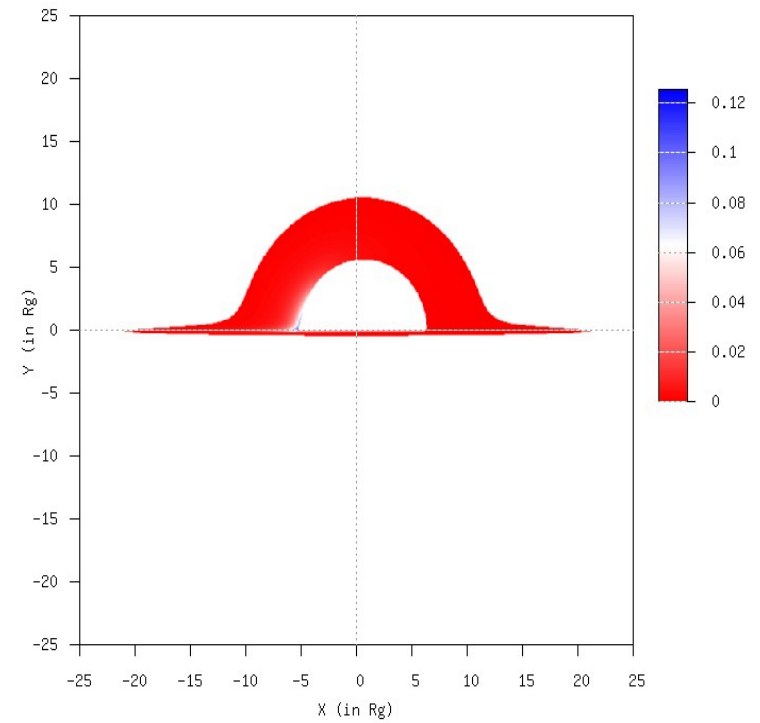
# Kerr black hole images ( $a=0.5$ ): $\theta=89$ deg

- Redshift map



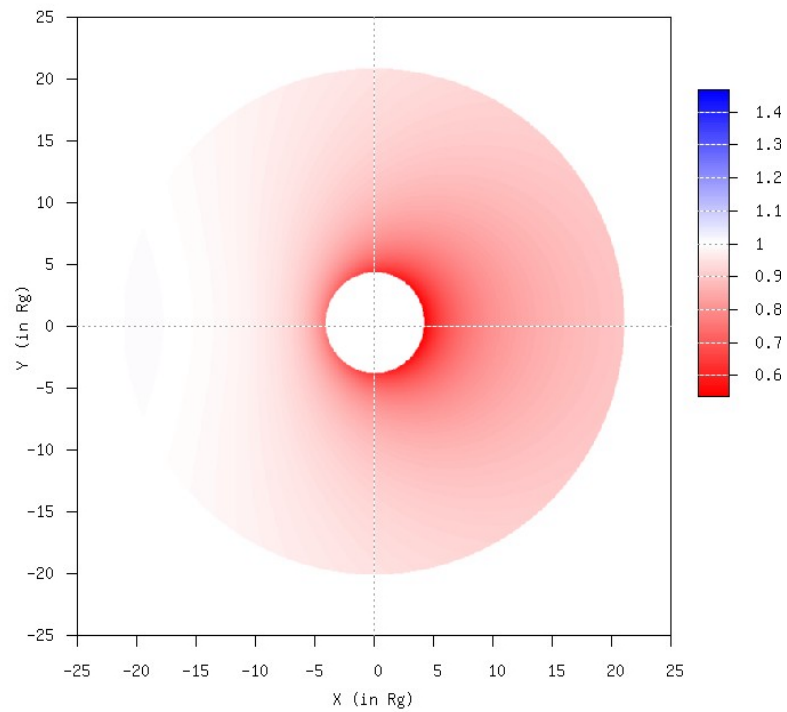
- 

Intensity map



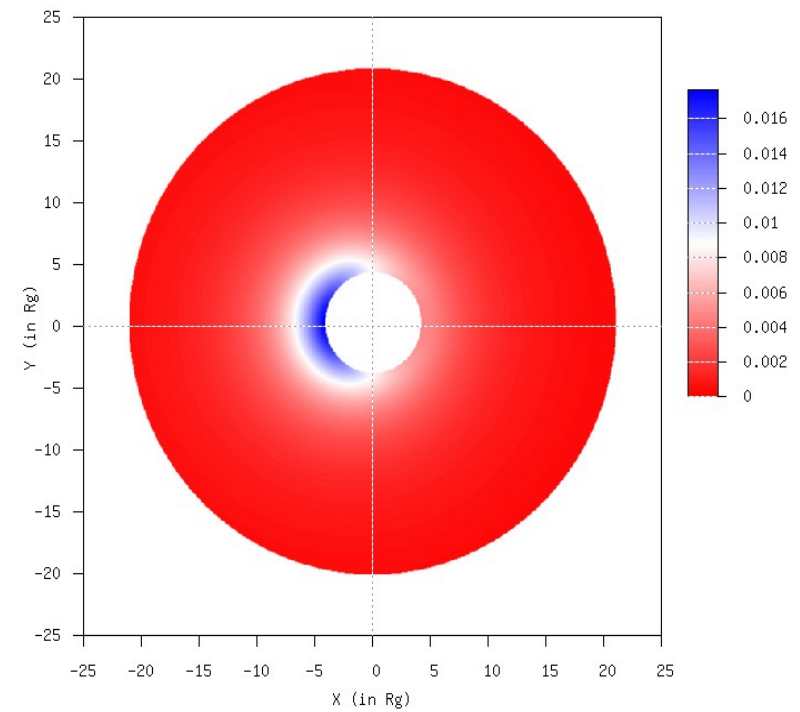
# Kerr black hole images ( $a=0.75$ ): $\theta=15$ deg

- Redshift map



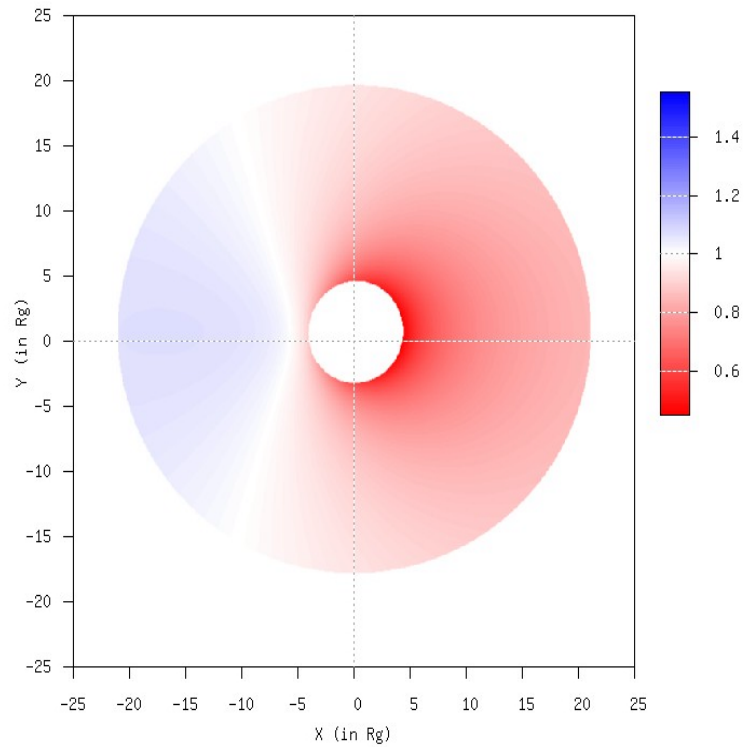
- 

Intensity map



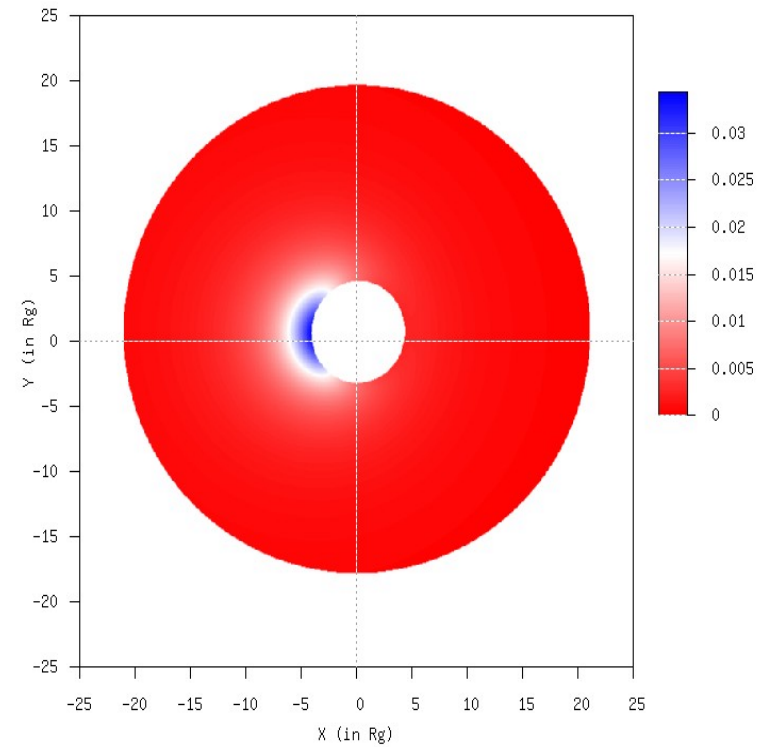
# Kerr black hole images ( $a=0.75$ ): $\theta=30$ deg

- Redshift map



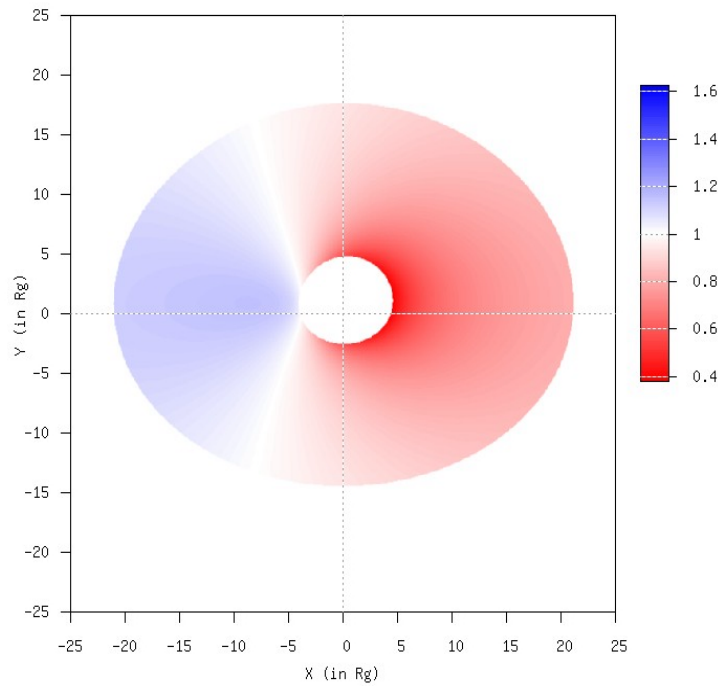
- 

Intensity map



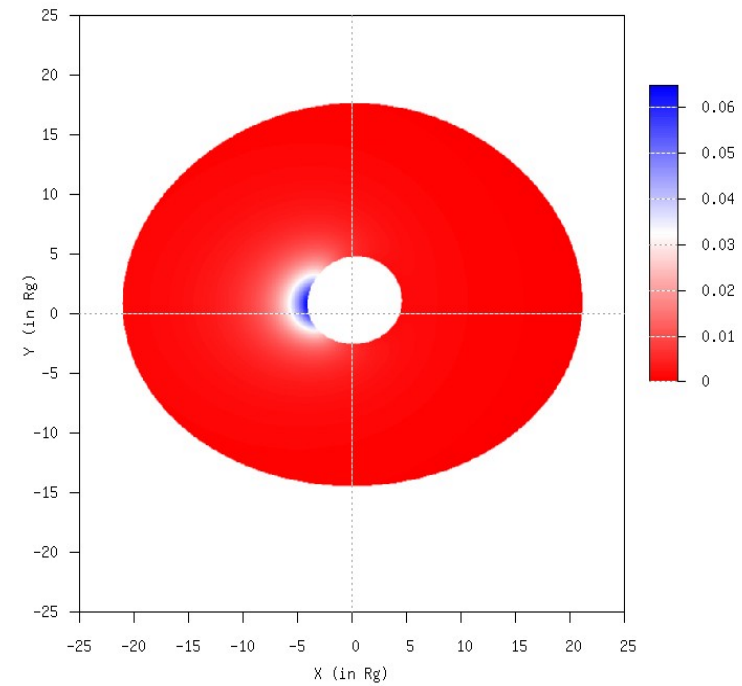
# Kerr black hole images ( $a=0.75$ ): $\theta=45$ deg

- Redshift map



- 

Intensity map



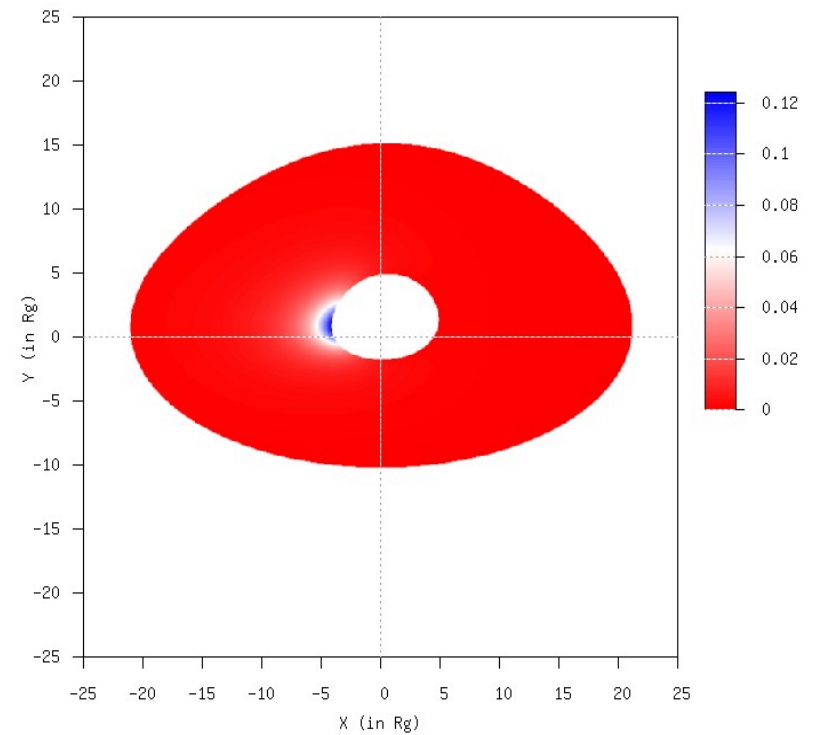
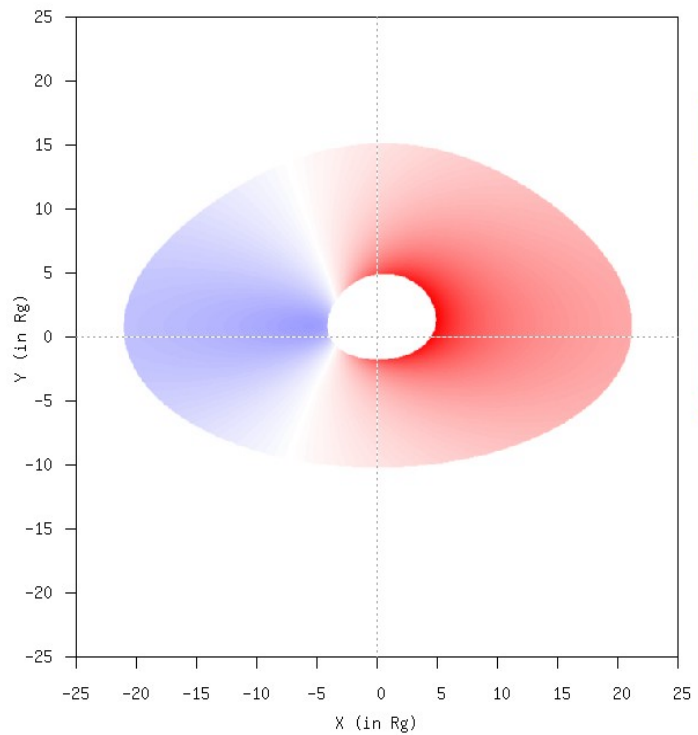


# Kerr black hole images ( $a=0.75$ ): $\theta=60$ deg

- Redshift map

•

- Intensity map

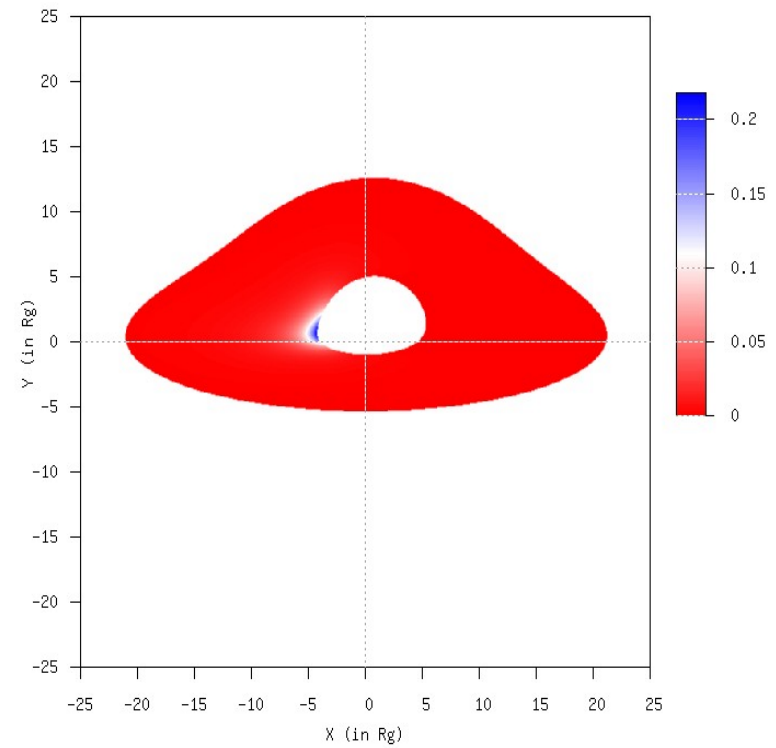
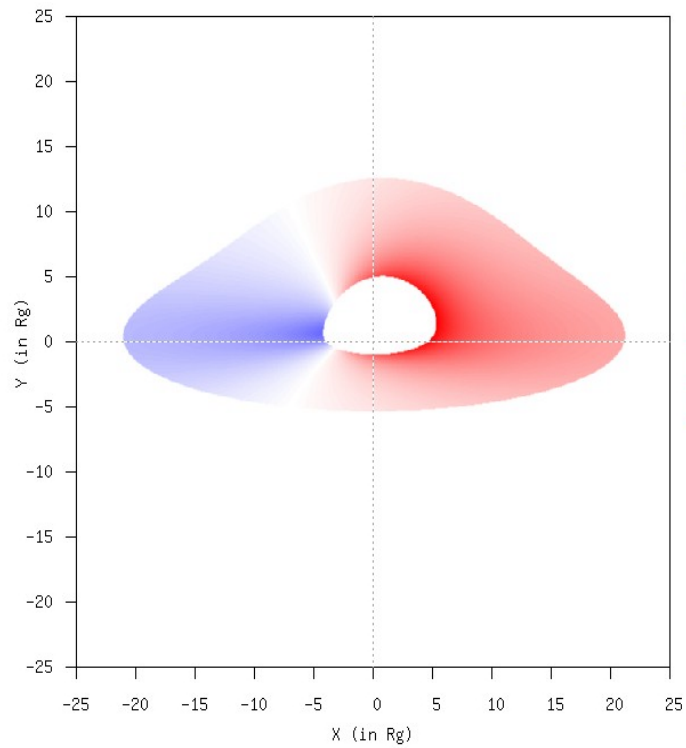


# Kerr black hole images ( $a=0.75$ ): $\theta=75$ deg

- Redshift map

•

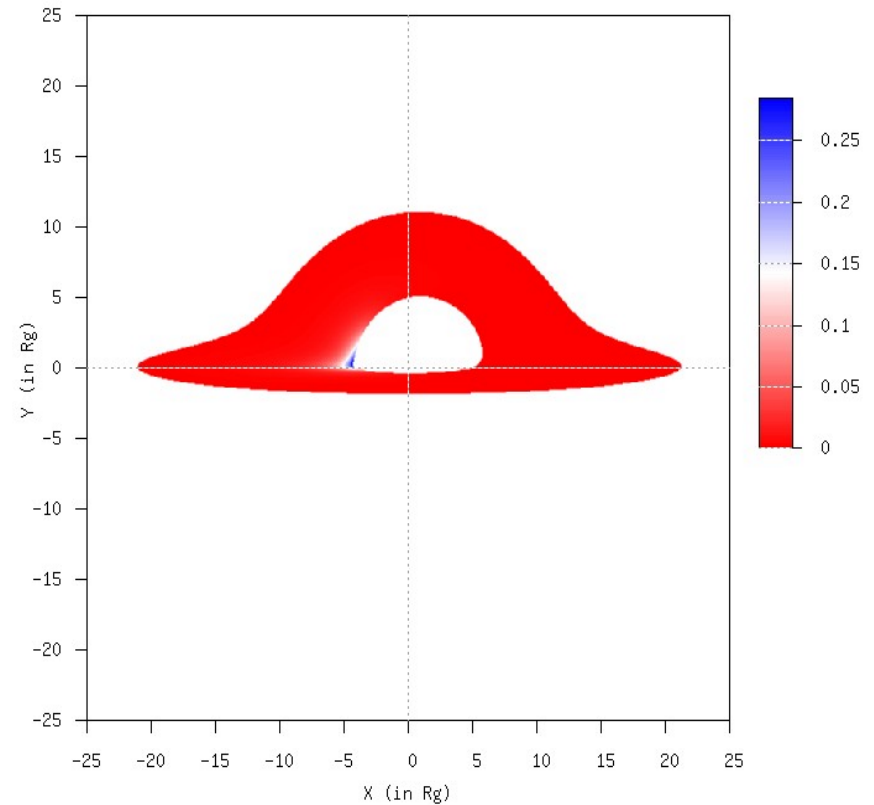
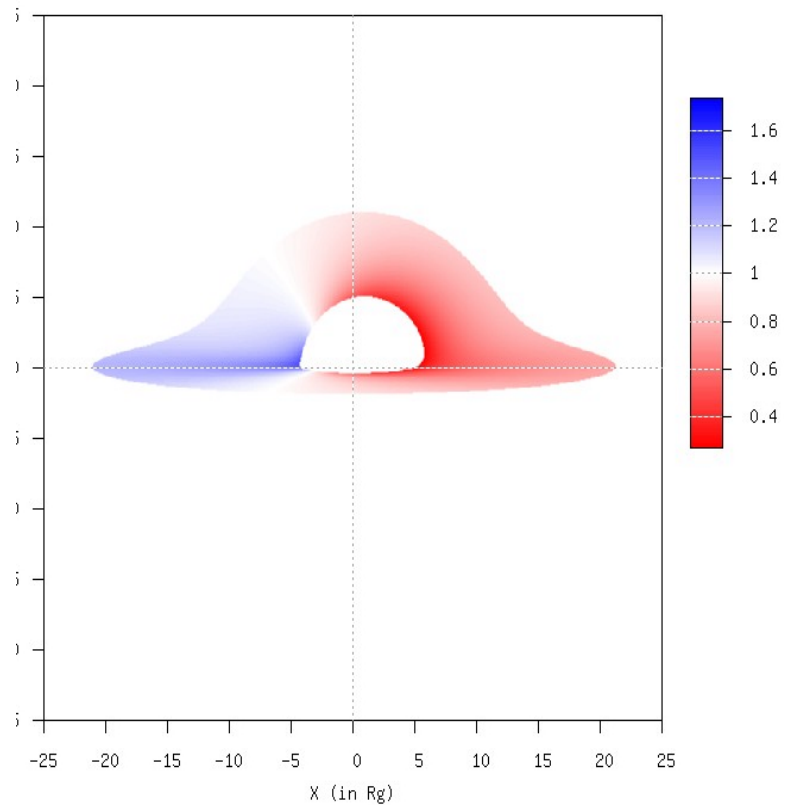
- Intensity map



# Kerr black hole images ( $a=0.75$ ): $\theta=85$ deg

- Redshift map

- Intensity map

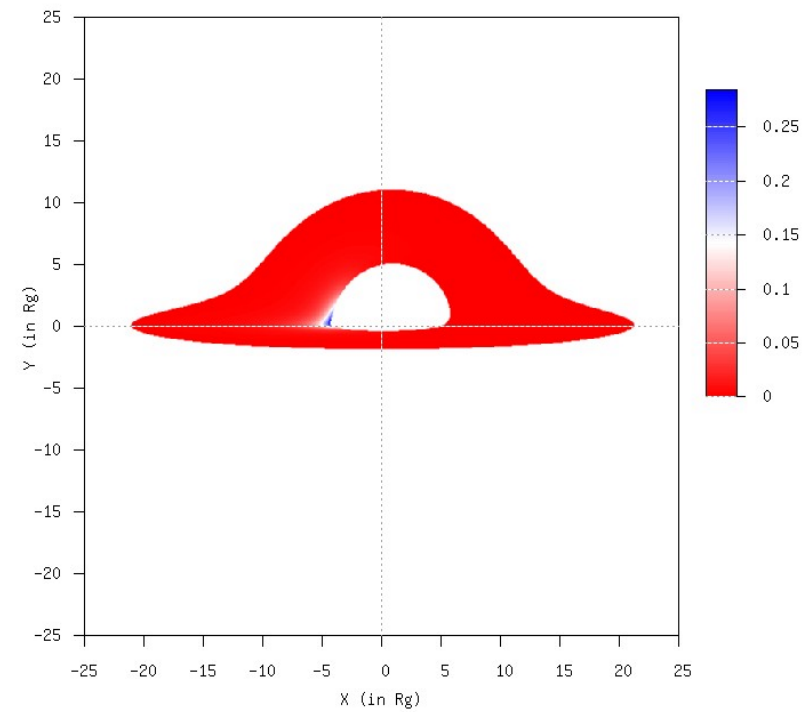
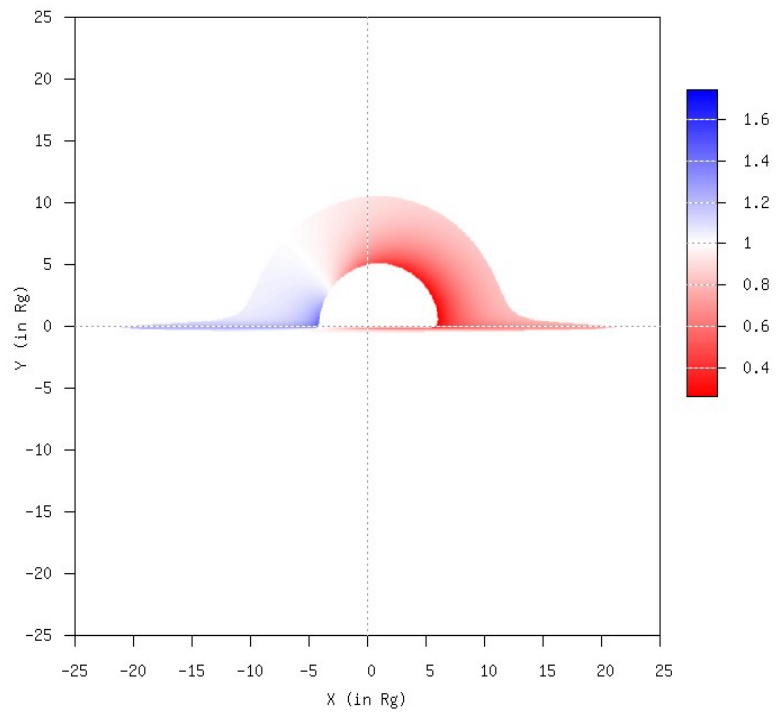


# Kerr black hole images ( $a=0.75$ ): $\theta=89$ deg

- Redshift map

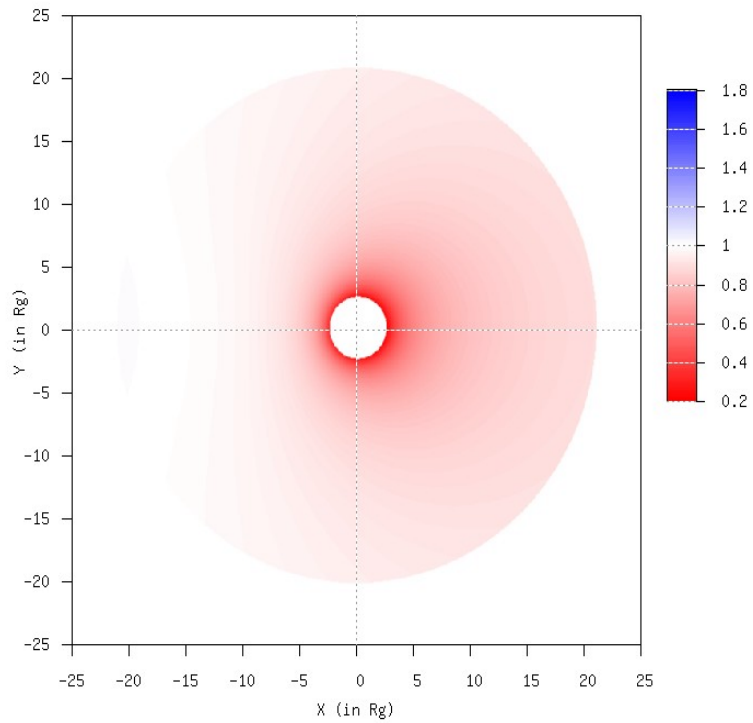
•

- Intensity map



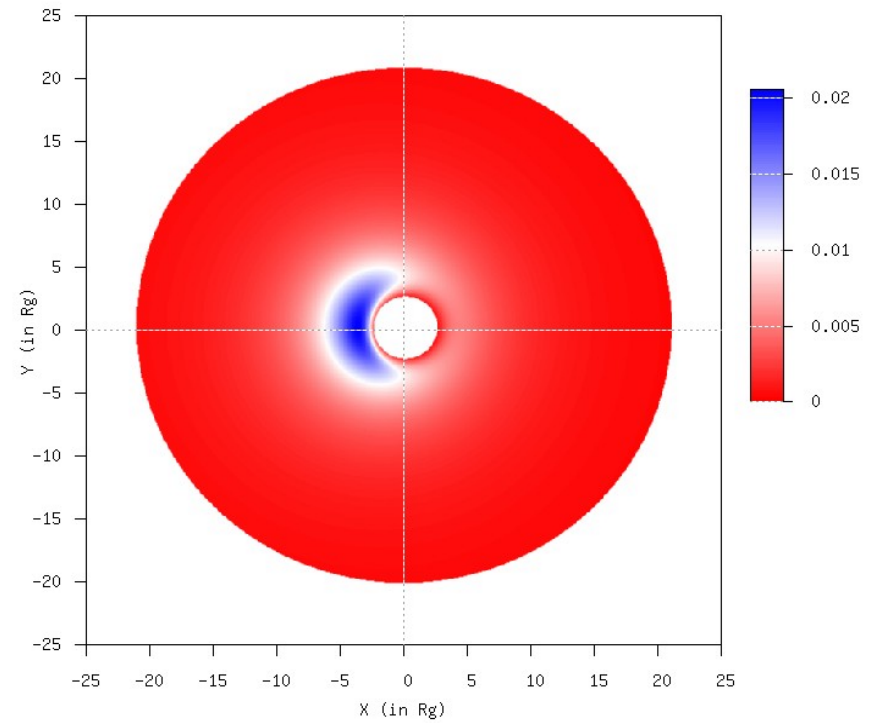
# Kerr black hole images ( $a=0.99$ ): $\theta=15$ deg

- Redshift map



- 

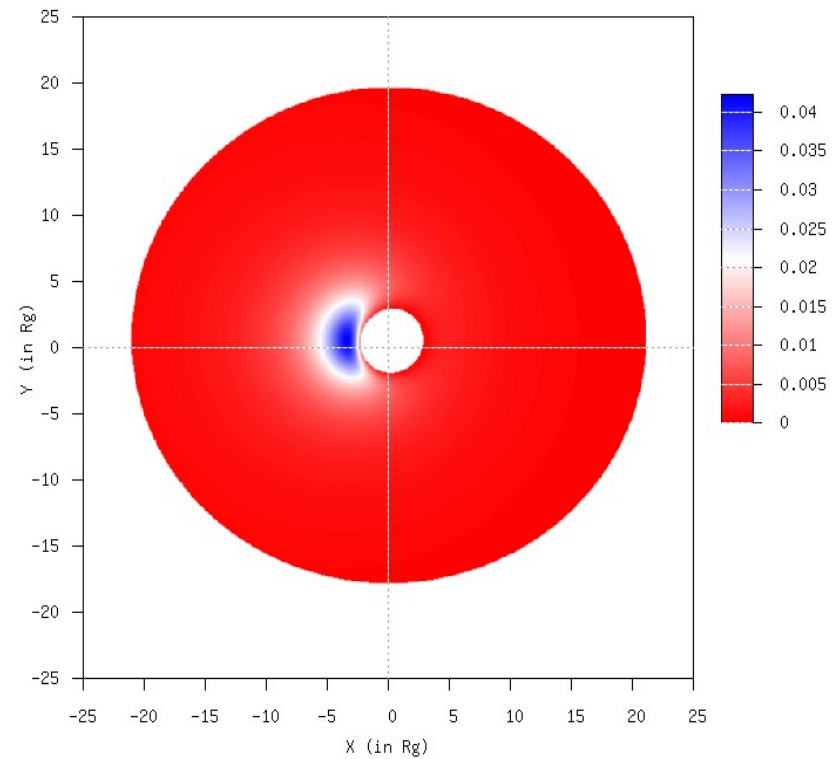
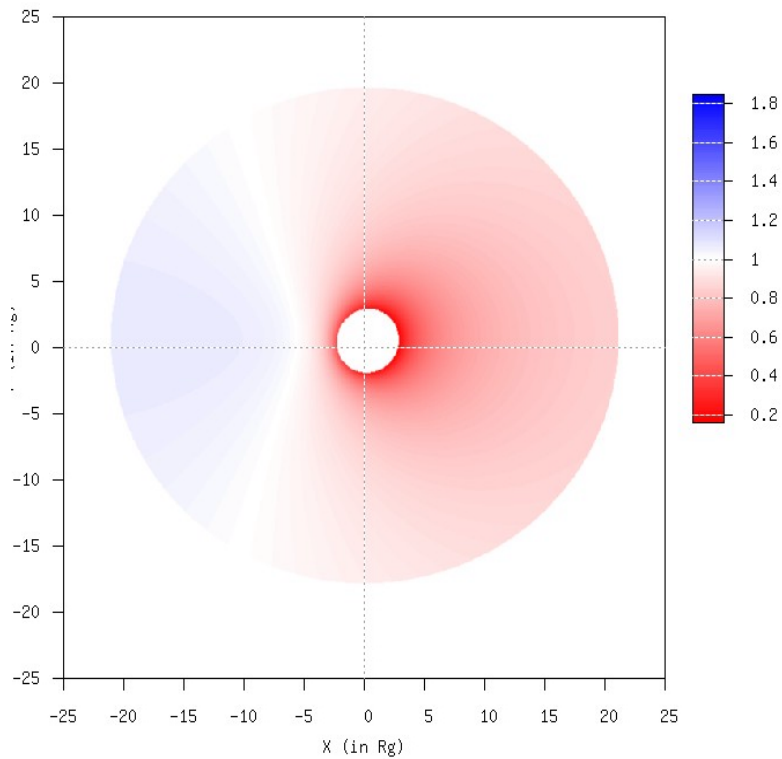
- Intensity map



# Kerr black hole images ( $a=0.99$ ): $\theta=30$ deg

- Redshift map

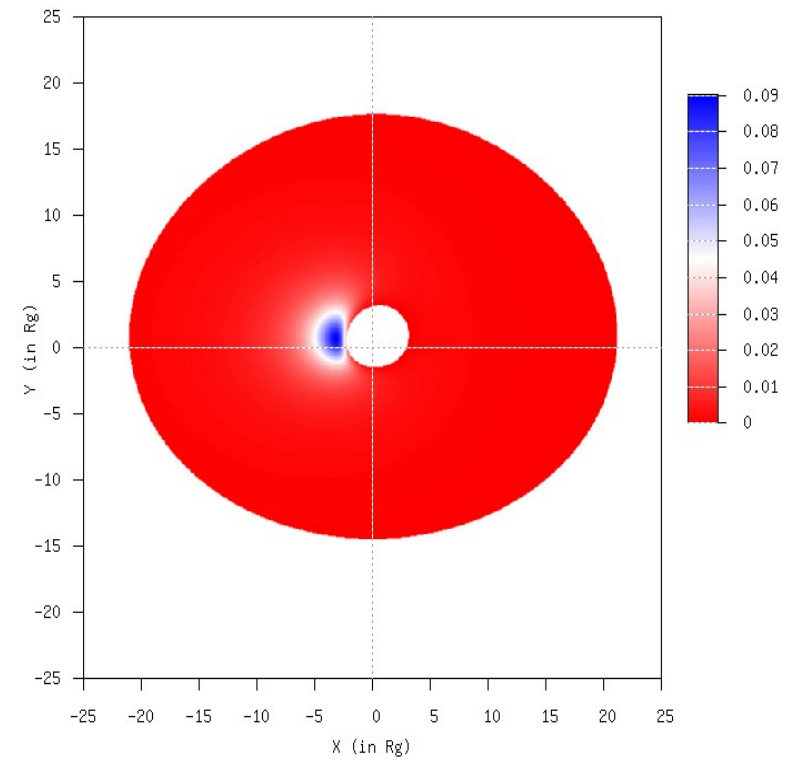
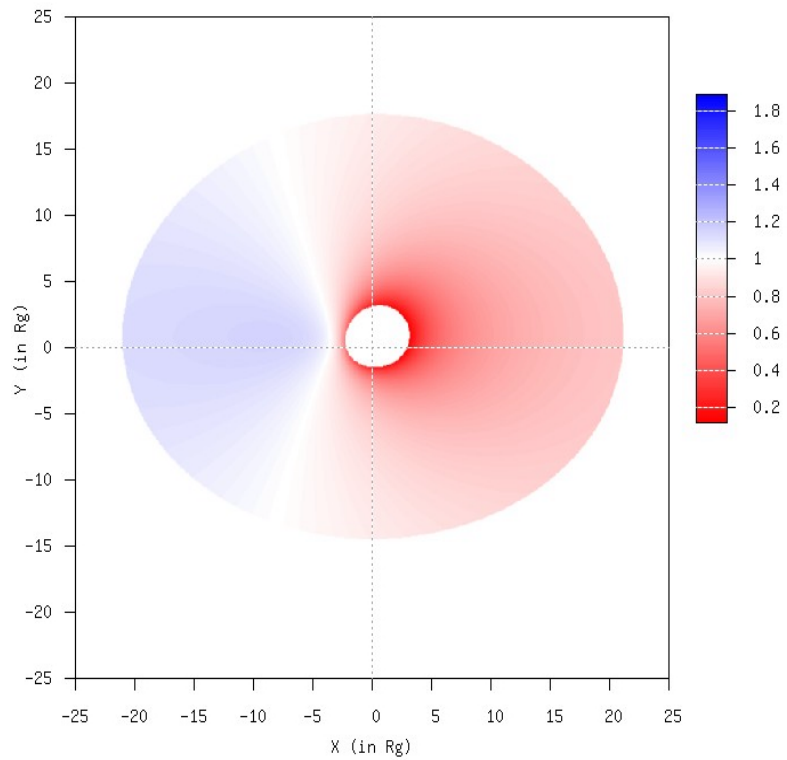
Intensity map



# Kerr black hole images ( $a=0.99$ ): $\theta=45$ deg

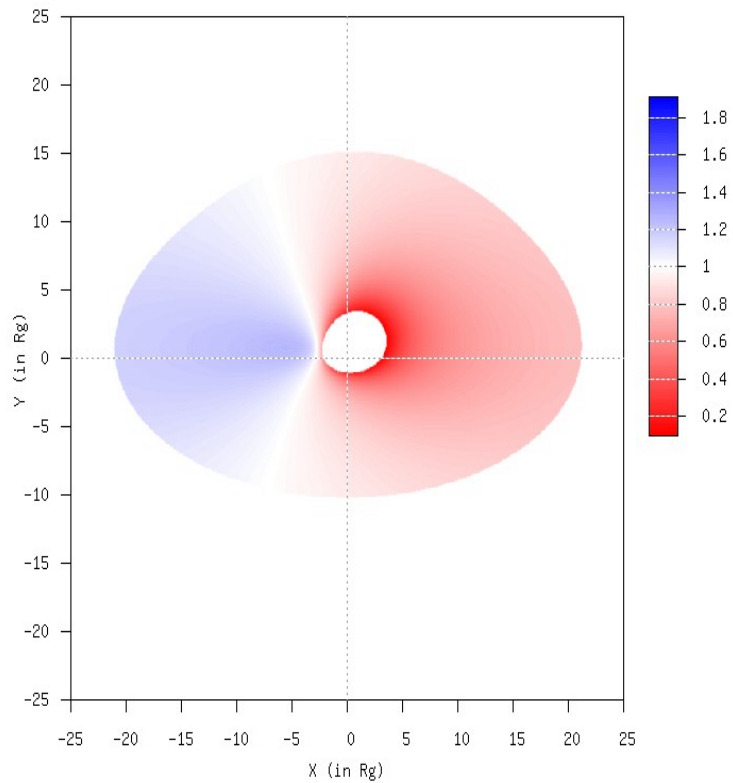
- Redshift map

- Intensity map

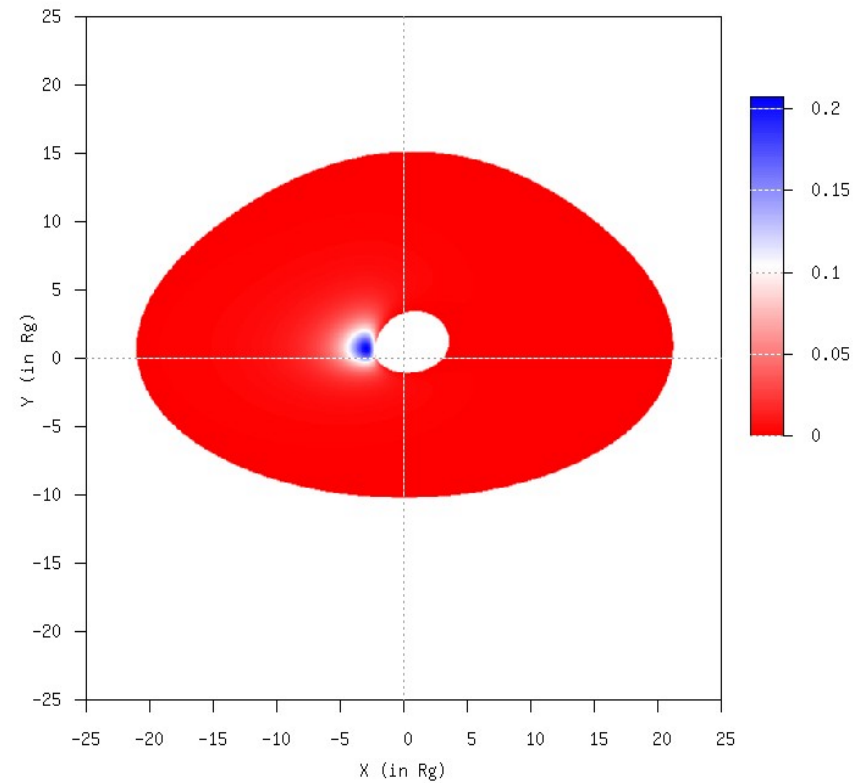


# Kerr black hole images ( $a=0.99$ ): $\theta=60$ deg

- Redshift map



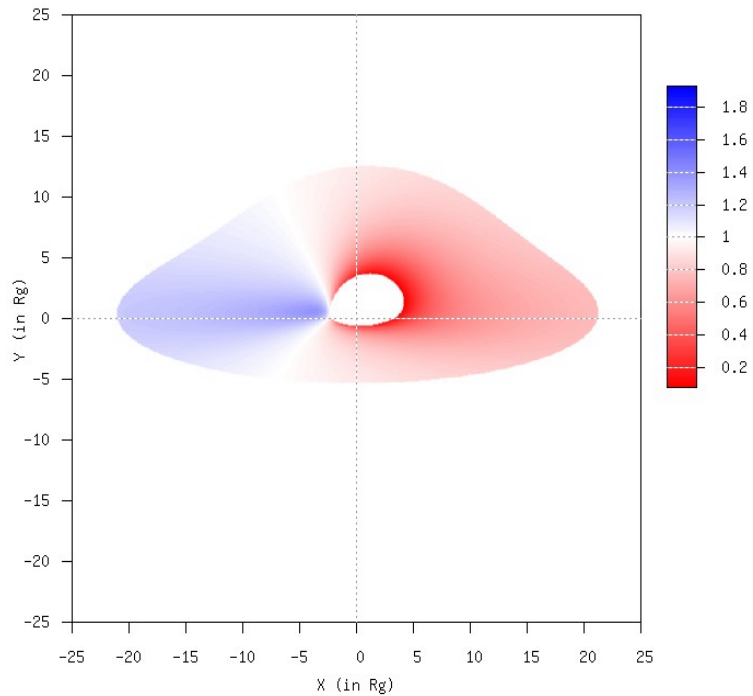
- Intensity map



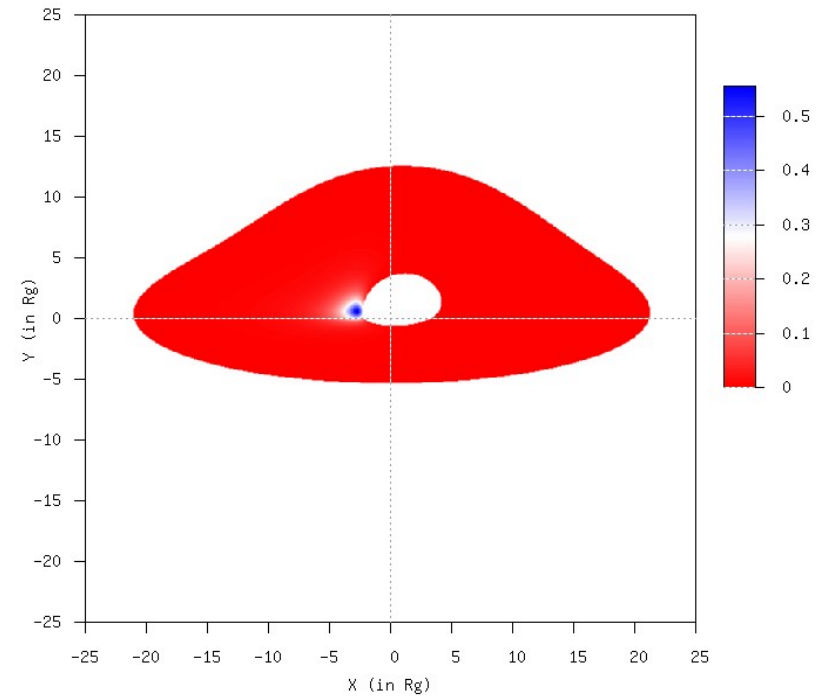


# Kerr black hole images ( $a=0.99$ ): $\theta=75$ deg

- Redshift map

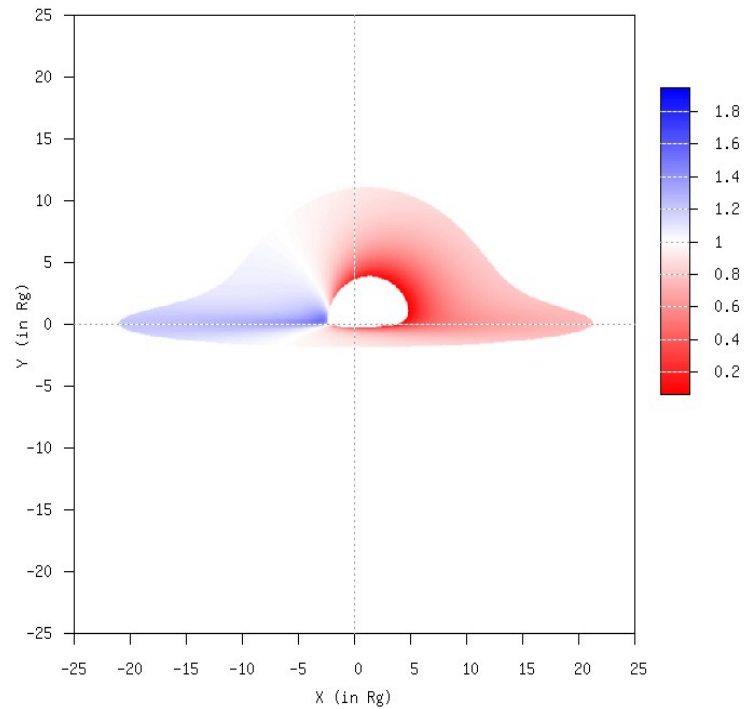


- Intensity map

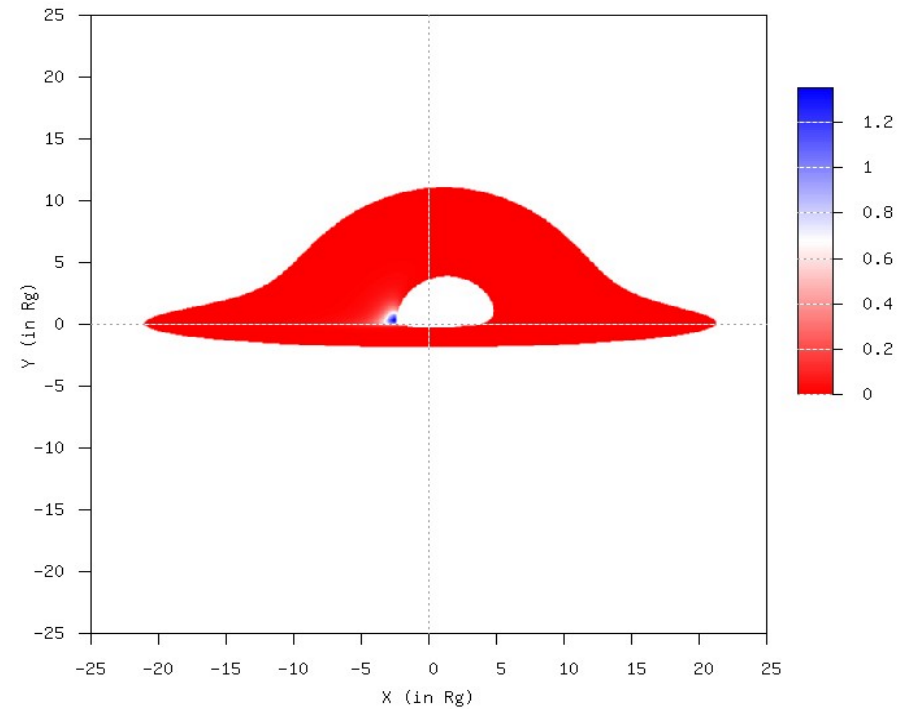


# Kerr black hole images ( $a=0.99$ ): $\theta=85$ deg

- Redshift map

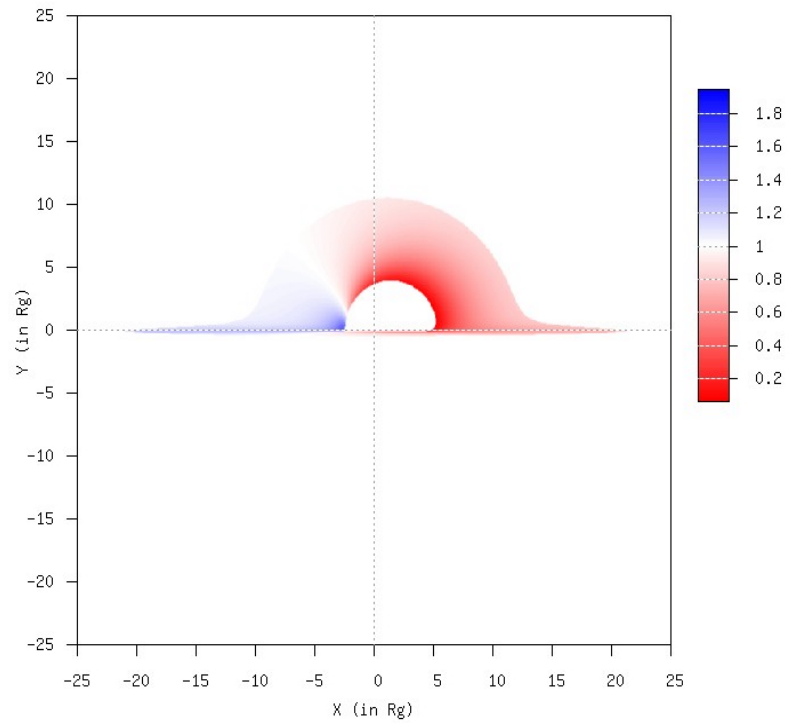


- Intensity map



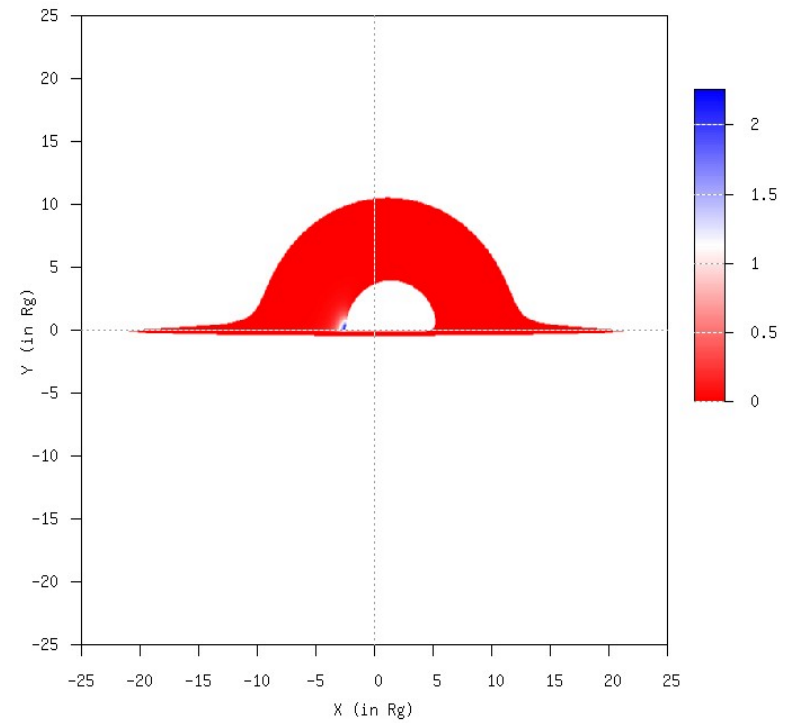
# Kerr black hole images ( $a=0.99$ ): $\theta=89$ deg

- Redshift map



- 

- Intensity map



## Conclusions

- Now the detailed structure of accretion disks is still unknown (in particular we do not know a thickness of accretion disks).
- Therefore, there is a possibility to observe highly inclined accretion disks (about 1% of all AGNs should have such high inclination. The situation is much better for microquasars; because of possible precession of accretion disks (for example, SS433).

In this case this analysis could give us a useful tool for a determination of such high inclination angles, however another factors (which are behind of this simple model) could cause such line profiles.

- Distortion of iron line profiles could give essential information about magnetic fields near BH horizons in AGNs and GBHCs.

**Searches for such features of spectral lines could useful to realize using present and future spacecrafts such as**

**Chandra, XMM, Integral, Constellation.**

- Radioastron could detect mirages (“faces”) around black holes.
- Shapes of images give an important information about BH parameters