

# New results from a search for $\nu_\mu \rightarrow \nu_\tau$ and $\nu_e \rightarrow \nu_\tau$ oscillation

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## Abstract

A first analysis of the complete set of data collected by CHORUS in the years 1994–1997 is presented. The search for  $\nu_\tau$  charged current events has been performed for both leptonic and hadronic decays of the  $\tau$  lepton. No  $\tau$  candidate has been found. A  $\nu_\mu \rightarrow \nu_\tau$  mixing is excluded down to  $\sin^2 2\theta_{\mu\tau} = 6.8 \times 10^{-4}$  for large  $\Delta m^2$  (90% C.L.). © 2001 Elsevier Science B.V. All rights reserved.

## 1. Introduction

CHORUS is an experiment designed to search for  $\nu_\mu \rightarrow \nu_\tau$  oscillation through the observation of charged current interactions  $\nu_\tau N \rightarrow \tau^- X$ , followed by the decay of the  $\tau$  lepton. The search is sensitive to very small mixings if the mass difference is of the order of a few eV or larger. In a scheme where the mass difference is essentially coinciding with the  $\nu_\tau$  mass, the latter becomes a good candidate for the hot component of the Dark Matter of the Universe. This consideration constitutes the main motivation of the experiment.

The experiment was performed in the CERN Wide Band Neutrino Beam, which contains mainly  $\nu_\mu$  with a contamination of  $\nu_\tau$  well below the level of sensitivity that can be reached by this experiment. Neutrino interactions occur in a target of nuclear emulsions, whose spatial resolution (below one micrometer) allows a three-dimensional *visual* reconstruction of the  $\tau$  lepton and its decay products. The experiment is sensitive to most of the decay channels of the  $\tau$ .

The collaboration has already reported [1,2] limits on  $\nu_\mu \rightarrow \nu_\tau$  oscillation obtained from an analysis of a subsample of neutrino interactions. In this Letter we describe in more detail the results of an analysis extended to the data sample collected in the four years of data taking (1994–1997). The present analysis is not the final one. In a second phase the sensitivity will be further improved.

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## 2. The experimental setup

### 2.1. The neutrino beam

The West Area Neutrino Facility (WANF) of the CERN SPS provides an intense beam of  $\nu_\mu$  with an average energy of 27 GeV, well above the  $\tau$  production threshold ( $E_\nu = 3.5$  GeV). The neutrino beam, besides the  $\nu_\mu$  component, also contains small fractions of  $\bar{\nu}_\mu$ ,  $\nu_e$ ,  $\bar{\nu}_e$ . Fig. 1 shows the spectrum of the various beam components, as resulting from a complete simulation of the beam, starting from the interaction of the primary protons. The  $\bar{\nu}_\mu$ ,  $\nu_e$  and  $\bar{\nu}_e$  contents are 5.6%, 0.9% and 0.2%, respectively. The figure also shows the tiny contamination of prompt  $\nu_\tau$ . Its contribution to the background to the oscillation search is discussed in Section 8.

It is worth mentioning that the CHORUS detector is capable of a direct measurement of the spectral shapes and of the relative abundances of the two main components of the beam. In fact, the apparatus includes a large mass calorimeter followed by a muon spectrometer (described in detail in the next section). Besides neutrino interactions in the emulsion target, data were also collected using the calorimeter as a neutrino target. The calorimeter allows a high resolution measurement of hadronic showers. The spectrometer following the calorimeter provides the reconstruction of

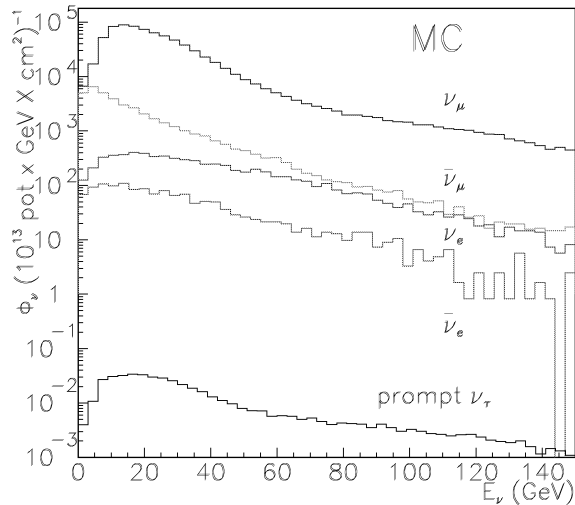


Fig. 1. Energy spectra of the various components of the neutrino beam (Monte Carlo simulation).

the muon and a precise measurement of its momentum. The analysis of the neutrino interactions in the calorimeter has allowed the cross-checking of various features of the MC simulation. In particular, agreement at the 10% level is found on the relative  $\bar{\nu}_\mu/\nu_\mu$  fluxes [3].

### 2.2. The apparatus

A schematic picture of the CHORUS apparatus is shown in Fig. 2.

The *hybrid* setup, described in detail in Ref. [4], is composed of an emulsion target, a scintillating fiber tracker system, trigger hodoscopes, a magnetic spectrometer, a lead-scintillator calorimeter and a muon spectrometer.

The nuclear emulsions act as the target and, simultaneously, as detector of the interaction vertex and the decay point of the  $\tau$  lepton [5]. The total mass of the target is 770 kg. The emulsions are subdivided in 4 stacks of 36 plates, oriented perpendicularly to the beam and with a surface of  $1.44 \times 1.44$  m<sup>2</sup>. Each plate is made of a 90  $\mu$ m transparent plastic film with 350  $\mu$ m emulsion sheets on both sides. The nuclear emulsion target is equipped with a high resolution tracker made out of planes of emulsions and of planes of scintillating fibers. Each stack is followed by three special interface emulsion sheets: two Changeable Sheets (CS), close to the fiber trackers, and a Special Sheet (SS), close to the emulsion stack. The sheets have a plastic base of 800  $\mu$ m coated on both sides by 100  $\mu$ m emulsion layers.

Eight planes of trackers of scintillating fibers (500  $\mu$ m diameter) [6], interleaved between the emulsion stacks, reconstruct the trajectories of the charged

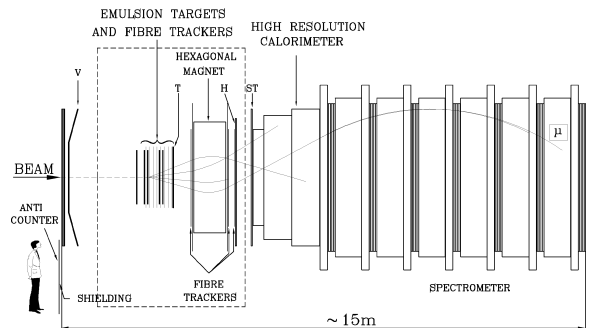


Fig. 2. General layout of the detector.

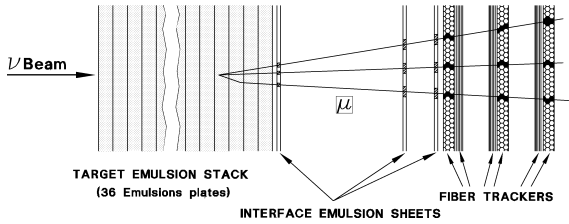


Fig. 3. Layout of an emulsion stack and associated fiber trackers.

particles with a precision of  $150 \mu\text{m}$  in position and  $2 \text{ mrad}$  in angle at the surface of the CS. The layout of an emulsion stack is sketched in Fig. 3.

Downstream of the target region, a magnetic spectrometer performs the reconstruction of charge and momentum of charged particles. An air-core magnet [7] of hexagonal shape produces a pulsed homogeneous field of  $0.12 \text{ T}$ . Field lines are parallel to the sides of the hexagon and the magnetised region extends for a depth of  $75 \text{ cm}$  in the direction of the beam. The tracking before and after the magnet is performed by a high resolution detector made of scintillating fibers ( $500 \mu\text{m}$  diameter) and complemented with few planes of electronic detectors (streamer tube chambers in the 1994, 1995 and the beginning of 1996 runs, honeycomb chambers [8] afterwards). The resulting momentum resolution  $\Delta p/p$  is  $30\%$  at  $5 \text{ GeV}$ .

In addition to the detection elements described above, the air-core hexagonal magnet region has been equipped with emulsion trackers for the 1996 and 1997 runs. The aim was to perform a more precise kinematical analysis of the  $\tau$  decay candidates.

A  $100 \text{ ton}$  spaghetti calorimeter (lead and scintillating fiber [9]) follows the magnetic spectrometer and measures the energy and direction of electromagnetic and hadronic showers.

The calorimeter is followed by a muon spectrometer made of magnetised iron disks interleaved with plastic scintillators and tracking devices. A momentum resolution of  $19\%$  is achieved by magnetic deflection for muons with momenta greater than  $7 \text{ GeV}$ . At lower momenta, the measurement of the range yields a  $6\%$  resolution.

### 3. Data collection

During the 4 years of operation the emulsion target has been exposed to the neutrino beam for an in-

tegrated intensity which corresponds to  $5.06 \times 10^{19}$  protons on target (pot). The data acquisition system recording the response of the electronic detectors was operational for  $90\%$  of the time. The average dead time for the emulsion interaction triggers was  $12\%$ . The trigger efficiency was  $99\%$  for charged current (CC) and  $90\%$  for neutral current (NC) events [10].

### 4. Principle of analysis

The search for  $\nu_\tau$  interactions has been performed for the following two decay modes of the  $\tau$  lepton:

- (1)  $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$ ,
- (2)  $\tau^- \rightarrow h^- (n\pi^0) \nu_\tau$ .

Both decay modes give rise in the emulsions to a *kink* topology: a track from the neutrino interaction vertex showing a change in direction after a short path (of the order of  $1 \text{ mm}$  at the energies typical for this experiment).

The information of the electronic detectors has been used to define two data sets, the  $1\mu$  and  $0\mu$  samples, distinguished by the presence or absence of one reconstructed muon of negative charge. For each sample few kinematical selections are applied to reduce the scanning load, while keeping a high sensitivity to the two decay modes of the  $\tau$ . For the selected events, the track trajectories reconstructed in the fiber trackers are used to guide the scan in the pair of changeable sheets immediately following the stack containing the interaction vertex. The tracks are then followed in the special sheet and then in the target emulsion stacks where the search for the  $\tau$  decay is performed. In the next two sections we give some detail on the selection of the two data sets, the  $1\mu$  and  $0\mu$ , and then we describe the scanning of the emulsions.

### 5. Data selection

The events kept for the analysis in the emulsions are those for which the scintillating fiber trackers allow track reconstruction and the determination of the interaction vertex position, with the reconstructed vertex position lying in the target emulsions. The

event must contain at least one negative track, as a possible decay product of a  $\tau$ . Note that events with only one reconstructed track were also kept, with the vertex position assumed to be in the middle of the emulsion stack immediately preceding the first plane of fiber tracker hit. The sample contains a few percent contamination of events with the reconstructed vertex wrongly assigned to the target emulsion, while the interaction actually took place in the surrounding material.

### 5.1. The $1\mu$ events

An event belongs to the  $1\mu$  sample if it contains one reconstructed muon track of negative charge. The muon identification and reconstruction is based on the muon spectrometer response. Muons not reaching the spectrometer can in some cases be identified in the calorimeter. Momentum and charge are then measured, with lower precision, by the air-core magnet (for stopping muons the momentum is obtained from the range).

The efficiency for selecting CC events is about 80% and is the product of the efficiency for muon identification and that of the track and vertex reconstruction algorithms. Note that part of the inefficiencies are due to events where the muon track, though correctly identified in the muon spectrometer, does not match with the required precision the track reconstructed in the fiber trackers. Failures in the tracks and vertex reconstruction are mainly due to  $\pi^0$ 's overlapping the tracks of charged secondaries.

The resulting  $1\mu$  sample consists of 713,000 events. The data set to be analysed for the search of  $\tau$  decays was defined by the requirement that the event contains only one muon, with negative charge and momentum smaller than 30 GeV. The 30 GeV selection reduces by 29% the number of events to be scanned. The effect on possible  $\nu_\tau$  interactions depends on the oscillation parameters: the selection would reject 15% of the  $\nu_\tau$  interactions if the  $\nu_\tau$  had the same energy spectrum as the  $\nu_\mu$ . The actual loss in sensitivity is, however, much smaller, since a high energy muon implies most of the times a decay angle too small to be detected.

### 5.2. The $0\mu$ events

The  $0\mu$  sample contains events where no muon is found. Events are selected if tracks have been reconstructed by the scintillating fiber trackers and the reconstructed vertex position lies in the target emulsions.

This sample consists of 335,000 events, with a calculated contamination of about 140,000 misidentified CC interactions and about 20,000 interactions generated by neutrinos other than  $\nu_\mu$ . Out of this sample we select for the emulsion analysis events with at least one track corresponding to a particle of negative charge and momentum in the 1 to 20 GeV interval. The lower bound reduces the large amount of low energy particles from secondary interactions or  $\gamma$  conversions. The upper bound is dictated by the poor momentum resolution at higher energy. A reliable momentum reconstruction has been obtained keeping only tracks which traverse the hexagonal air-core magnet without crossing any of its six spokes, so avoiding large multiple scattering. The momentum fit requires the presence of hits in all the tracking elements: the planes of fiber trackers and the chambers downstream of the air-core magnet (streamer tubes or honeycomb chambers, depending on the running periods). The number of tracks per event selected for the kink search may be larger than one.

### 5.3. The final samples

The negative track, hadron or muon, selected as a candidate for  $\tau$  daughter has to satisfy further requirements. To allow the good functioning of the automatic scanning systems, the angle of the track with the beam axis has to be smaller than 0.4 rad. In view of the large background of muons originating from a nearby secondary beam, tracks at an angle smaller than 0.05 rad from the direction of this beam are also excluded (this selection was only applied on 1994 and 1995 data when the secondary beam was run at high intensity).

After all selections the  $1\mu$  and the  $0\mu$  data sets eligible for emulsion scanning consist of 477,600 and 122,400 events, respectively. The events sent to the automatic scanning procedure — described in the next section — are fewer (355,395 and 85,211, respectively), mainly because of fiducial volume cuts

Table 1  
Data flow chart

Protons on target	$5.06 \times 10^{19}$
$1\mu$ : events with 1 negative muon and vertex predicted in emulsion	713,000
$1\mu$ : $p_\mu < 30$ GeV and angular selections	477,600
$1\mu$ : events scanned	355,395
$1\mu$ : vertex located	143,742
$1\mu$ : events selected for eye-scan	11,398
$0\mu$ : with vertex predicted in emulsion (CC contamination)	335,000 (140,000)
$0\mu$ : with 1 negative track ( $p = 1\text{--}20$ GeV and angular selections)	122,400
$0\mu$ : events scanned	85,211
$0\mu$ : vertex located (corrected number after reprocessing)	23,206 (20,081)
$0\mu$ : events selected for eye-scan	2,282

imposed by the scanning technique and of the bad quality of a few emulsion plates.

The different stages of the reconstruction and selection procedure are summarised in Table 1.

The reconstruction inefficiencies, as well as those originating from the trigger, are well understood and reproduced by detailed MC simulations, both for the  $1\mu$  and the  $0\mu$  data sets.

## 6. Scanning procedure

### 6.1. Vertex location

The emulsion scanning procedure is fully automated using computer controlled microscopes equipped with CCD cameras and fast processors. The processor, which is called *track selector* [11], is capable of identifying tracks inside the emulsions, measuring their parameters on line.

The location of the plate containing the interaction vertex is based on the following back of the selected negative tracks, assumed to be the  $\tau$  daughters. The track is first located in the interface emulsion sheets (CC and SS) with a search initially based on the track parameters measured by the scintillating fiber trackers. A track which is found in the interface emulsion sheets is followed upstream in the target emulsion stack, using track segments reconstructed in the most

upstream 100  $\mu\text{m}$  of each plate, until it disappears. The corresponding plate is defined as the vertex plate, since it should contain the primary neutrino vertex or the secondary (decay) vertex, or both, from which the track originates. The three most downstream plates of each stack are used to validate the matching with the interface emulsion sheets and are not considered as possible vertex plates. The efficiency of this scan-back procedure is almost independent from the track momentum and angle.

The number of located events is given in Table 1, separately for the  $1\mu$  and  $0\mu$  samples. For the  $0\mu$  sample a second number, given in brackets in the table, represents the events actually used for the decay search. This number is smaller than the number of located events because, after the reprocessing through an updated version of the reconstruction program, a fraction of the located events failed to pass the kinematical selections.

As confirmed by a detailed simulation of the scanning, there is a difference on the average location efficiency for  $1\mu$  (40%) and  $0\mu$  events (27%). The reconstruction of the muon in  $1\mu$  events is usually easier than that of the hadron in  $0\mu$  events because the latter is more often overlapping with other tracks from hadronic and e.m. showers. This leads in the first case to more reliable predictions of the track parameters, and hence to a higher location efficiency. Note that for the hadronic decay of the  $\tau$  the vertex finding ef-

efficiency will be higher than that found for  $\nu_\mu$  NC interactions. In fact, coming from the decay of the  $\tau$ , the followed track will generally be more isolated. The Monte Carlo simulation shows that in this case the vertex finding efficiency approaches the value found for the  $1\mu$  events.

### 6.2. Decay search

Once the vertex plate is defined, automatic microscope measurements are performed to select the events potentially containing a decay topology (kink). Different algorithms have been applied as a result of the progress in the scanning procedures and of the improving performance in speed of the scanning devices. The data can be subdivided in three sets according to the scanning methods:

- In the first procedure (applied to part of the 1994 data — mainly  $1\mu$  — and described in [1]) the event is selected either when a significant minimum distance between the scan-back track and any other predicted track is detected, or when the change in the scan-back track direction between the vertex plate and the exit from the emulsions corresponds to an apparent transverse momentum,  $p_T$ , larger than 250 MeV. For the selected events and for those with only one predicted track, digital images of the vertex plate are recorded and are analysed off-line for the presence of a kink. The number of located events treated with this method is about 18,000. The numbers of events selected for eye-scan by the automatic search are 5,768 for the  $1\mu$  and 276 for the  $0\mu$  sample.

- The second procedure is applied to all other events. It is restricted to the search of decay angles greater than 0.025 rad. In that case the vertex plate is assumed to contain the decay vertex of a charged parent produced in a more upstream plate. The upstream part of the vertex plate is scanned in order to find a track crossing within a small tolerance, the direction of the daughter candidate as sketched in Fig. 4. This method also works for events where the decay vertex and the primary vertex occur in the same plate but on opposite sides of the plastic base. The method provides about 85% of the total kink finding efficiency. A total of 125,000  $1\mu$  events and all the  $0\mu$  events have been analysed with this method. Candidates for eye-scan from this search are 5,006  $1\mu$  and 1,823  $0\mu$ .

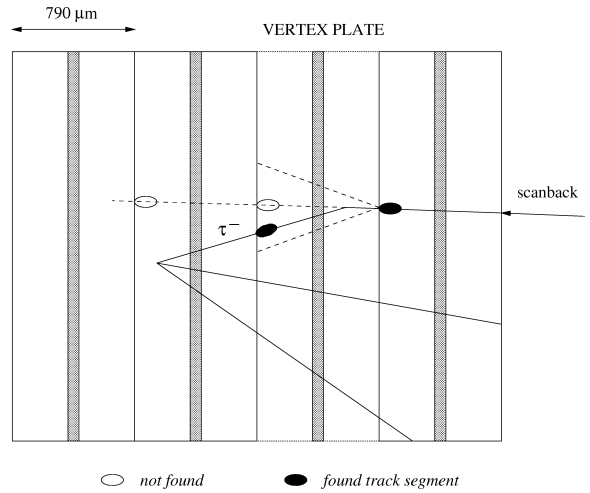


Fig. 4. Schematic view of the second decay search technique described in the text. The dotted lines indicate the cone around the scan-back track in which the search for the parent track is performed.

- A third search technique has been applied to 70% of the  $1\mu$  data of 1995, and to 75% of  $1\mu$  and  $0\mu$  data of 1996 and 1997. In this procedure, once the vertex plate is located by the scan-back track, a search is performed in that emulsion plate for all other tracks reconstructed by the fiber trackers. This scan allows a high precision comparison of the impact parameter of the scan-back track with respect to the vertex in emulsion defined by the other tracks. The method extends the sensitivity to smaller values of the decay path of the  $\tau$  and contributes to about 15% of the total kink finding efficiency. Candidates for eye-scan from this search are 624  $1\mu$  and 183  $0\mu$ .

### 6.3. Eye-scan

A computer assisted eye-scan is performed for all the kink candidates selected during the automatic search. The aim of the eye-scan is to confirm the presence of a secondary vertex. An event is retained as a  $\tau^-$  decay candidate if the secondary vertex appears as a kink without black prongs, nuclear recoils, blobs or Auger electrons. For the selected events the parent and decay particle, as well as the other tracks coming from the interaction vertex, are accurately measured. The measurements are used for the final topological and kinematical selections designed to reject the resid-



ual background. The efficiency of these procedures, the evaluation of the background, and the choice of the final selections are described in the next two sections.

## 7. Efficiency for the detection of $\nu_\tau$ interactions

The efficiency for the detection of  $\nu_\tau$  interactions has been split into two terms: the first one, the acceptance  $A$ , is given by the efficiency of the reconstruction of the neutrino interaction by the electronic detectors and of the location in the emulsions. It also includes the few geometrical and kinematical selections applied before scanning. The second term,  $\epsilon_{\text{kink}}$ , is the efficiency of the kink detection in the emulsions, multiplied by the efficiency of the geometrical and kinematical selections applied once the kink is found.

The error on the absolute value of the acceptance is mainly due to the uncertainties on the reconstruction and location efficiencies. However, these uncertainties affect in a similar way the acceptance for  $\nu_\tau$  and  $\nu_\mu$  induced events. Therefore, their effect largely cancels in the ratio of *observed*  $\nu_\tau$  to *observed*  $\nu_\mu$  events, used to compute the oscillation probability. More critical is the determination of  $\epsilon_{\text{kink}}$ . For that parameter an experimental check of the calculated value is possible by using the data itself, as shown below.

The efficiencies for the signal and the background have been evaluated from large samples of events, generated according to the relevant processes, passed through a GEANT [12] based simulation of the detector response. The output was then processed through the same reconstruction chain used for the data. The response of the emulsion to charged particles was also simulated, so allowing the evaluation of the efficiencies of each step of the scanning.

A partial test of the kink finding efficiency has been carried out by studying hadron interactions. A small fraction of the scan-back tracks are in fact secondary particles originated by the interaction of a hadron in the emulsion, the hadron having been produced in turn in a neutrino interaction. The automatic scanning procedure detects the secondary interaction with an efficiency which is related in a simple way to the kink detection efficiency. As a by-product of part of the decay search applied to the  $0\mu$  sample, 80 neutrino events with a secondary hadron interaction have been detected. This result is in good agreement with the ex-

pected value of 84 computed with a Monte Carlo simulation. Although the decay and interaction topologies have some differences, the agreement constitutes a reliable check of the simulation of the automatic scanning procedure.

## 8. Background evaluation and final selections

The basic requirements adopted to isolate  $\tau$  decay candidates are a selection,  $p_T$  larger than 250 MeV, on the transverse momentum of the decay particle with respect to the parent direction (to eliminate decays of strange particles), and a maximum length for the decay path. For the muonic decay of the  $\tau$ , the kink must occur within five plates downstream of the neutrino interaction vertex plate. Because of the different background sources, a more severe and complicated selection on the decay pattern has been applied to the  $0\mu$  sample. This last selection will be examined after a discussion of all possible sources of background.

An unavoidable background to  $\nu_\mu \rightarrow \nu_\tau$  oscillation is caused by the presence of prompt  $\nu_\tau$ 's in the neutrino beam. Calculations [13] show that it is small compared to other sources of background. For the statistics considered in this paper it amounts to less than 0.1 events and has been neglected.

Apart from this, the background is constituted by any event having a negative track undergoing a deviation of its trajectory in the emulsion target. To obtain a realistic estimation of the number of events expected in absence of an oscillation signal, large samples of all the known background processes have been simulated and processed by the same reconstruction programs as the real data.

One source of background common to all the decay channels of the  $\tau$  is due to charm production, namely:

- the production of negative charmed particles from CC interactions of the anti-neutrino components of the beam. These events constitute a background if the primary  $\mu^+$  or  $e^+$  remains unidentified. Taking into account the appropriate cross-sections and the branching ratios, we expect in the present sample 0.11 events in the  $1\mu$  channel and 0.02 in the  $0\mu$  channel;
- the production of positive charmed mesons in CC interactions, if the primary lepton is not identified and

the charge of the charmed particle daughter is incorrectly measured. In the present sample the expected background amounts to 0.7 events for the  $0\mu$  events. For the  $1\mu$  events the expected background amounts to less than 0.03 events and has been neglected. The fact that this background is much smaller in the  $1\mu$  sample is mainly due to the very low probability of a wrong measurement of the charge in the muon spectrometer;

- the associated charm production both in CC and NC interactions, when one of the charmed particles is not detected and, for CC events, the primary lepton is not identified. The cross-section for this reaction due to the NC interaction has been measured with large errors [14], while for the charged current process only an upper limit is available [14]. Within the present statistics the expected background amounts to less than 0.1 events in total and has been neglected in this analysis. Note that we are currently analysing data on charm production and a direct measurement of the cross-sections of associated charm production is being carried out.

For the decay into a single hadron the largest background rate is due to so-called hadronic *white kinks* (WK), defined as 1-prong nuclear interactions with no heavily ionising tracks or other evidence for nuclear break up (blobs or Auger electrons).

A robust estimation of this background comes from the study of WK events found during the  $\tau$  kink search, at a distance between primary and secondary vertex outside the  $\tau$  signal region. A total of 26 events with these characteristics were found over a total of 243 m of track length scanned back during the location procedure. Out of these, 8 events have an apparent decay  $p_T$  larger than 250 MeV. The corresponding effective WK interaction length is  $24.0 \pm 8.5$  m. A similar result for the background expected before imposing the selection on  $p_T$  has been obtained by a preliminary analysis of the data collected by a dedicated experiment [15]. The experiment has performed WK measurements at CERN with the same emulsion as CHORUS, using pion beams of fixed momentum (2 to 5 GeV). That analysis also suggests that the background of events with  $p_T$  larger than 250 MeV is partly due to the limited momentum resolution and could therefore be reduced by improving the precision of the momentum measurement.

The ratio of WK events outside and inside the signal region has been determined with the help of a Monte Carlo simulation, based on FLUKA [16,17]. The WK events expected within a distance,  $L_k$ , between the primary vertex and the kink point of three plates has been computed to be  $2.6 \pm 0.8$ .

This background can be further reduced by exploiting the difference of its kinematical properties with respect to those of the  $\tau$  signal. Several selections on  $L_k$  have been considered: a simple cut at three plates, as in the past analyses, or selections dependent on the momentum of the scan back hadron,  $p_h$ . A better separation between signal and background is expected in the second case since the  $\tau$  average decay length depends on the daughter momentum while a flat behaviour is predicted for WKs. A useful quantity to reject background events is the angle  $\Phi_{(\tau-h)}$  in the plane transverse to the beam axis, between the direction of the parent candidate, measured in emulsion, and the hadronic shower axis. For true  $\nu_\tau$  events this angle is close to  $180^\circ$  while, when the particle with the kink is part of the hadronic shower as in the WK or charm cases, the angular distribution is flatter, with more a preference for  $0^\circ$ .

The optimisation of the selection has been done maximising the sensitivity to the oscillation, by computing the average limit that would be obtained with the given set of selections, by an ensemble of experiments with the same expected background and no expected signal. The most favorable choice turned out to be a selection on  $L_k$  retaining a fixed fraction of 80% of the  $\tau$  signal in all  $p_h$  bins and the condition  $\Phi_{(\tau-h)} > 90^\circ$ . In Table 2 a summary of the results of the background computation is reported. The table gives the calculated number of background events and the number of observed events with various kinematical selections. In all cases, the number of observed events is consistent with the expected background. This shows, together with the reliability of the background calculation, the lack of any evidence of  $\nu_\tau$  interactions. The chosen set of selections corresponds to zero observed events.

The maximum of the sensitivity is obtained through a compromise between low background and high efficiency for  $\nu_\tau$  detection. To illustrate that efficiency, the last column of Table 2 also displays  $N_\tau^{\max}$ , the number of  $\nu_\tau$  events which would be observed in case all incident  $\nu_\mu$  had converted into  $\nu_\tau$ . For the  $1\mu$

Table 2

Summary table of the expected background events. The observed number of events is also shown, together with the maximum number of  $\nu_\tau$  observable events (see text)

		Charm( $\nu + \bar{\nu}$ )	WK	Total	Observed	$N_\tau^{\max}$
$1\mu$	$L_k < 5$ plates	0.1	–	0.1	0	5,014
$0\mu$	$L_k < 3$ plates	0.7	2.6	3.3	4	2,791
	$(L_k(p_h))_{80\%}$	0.5	1.7	2.2	1	2,537
	$(L_k(p_h))_{80\%}$ and $\Phi_{(\tau-H)} > 90^\circ$	0.3	0.8	1.1	0	2,004

sample this number is given by:

$$(N_\tau^{\max})_{1\mu} = N_{1\mu}^{\text{loc}} \cdot r_\sigma \cdot r_A \cdot \epsilon_{\text{kink}} \cdot \text{Br}_\mu, \quad (1)$$

where:

–  $N_{1\mu}^{\text{loc}}$  is the number of located  $1\mu$  events ( $N_{1\mu}^{\text{loc}} = 143, 742$ );

–  $r_\sigma = \langle \sigma_\tau^{CC} \rangle / \langle \sigma_\mu^{CC} \rangle$  is the neutrino energy weighted CC cross-section ratio. A value  $r_\sigma = 0.53$  has been used; it takes into account quasi-elastic interactions, resonance production and deep inelastic reactions;

–  $r_A = \langle A_\tau \rangle / \langle A_\mu \rangle$  is the cross-section weighted acceptance ratio for  $\nu_\tau$  and  $\nu_\mu$  interactions.  $A_\tau$  and  $A_\mu$  take into account the effect of geometrical and kinematical selections applied before scanning and the reconstruction and location efficiencies. The values of  $r_A$  is close to one ( $r_A = 0.97$ );

–  $\epsilon_{\text{kink}}$  includes the efficiency of the decay search procedure and that of the geometrical and kinematical selections applied after the kink is found. Its average value is 0.39;

–  $\text{Br}_\mu = 17.4\%$  is the branching ratio of the decay  $\tau \rightarrow \nu_\tau \bar{\nu}_\mu \mu^-$ .

The formula giving  $N_\tau^{\max}$  for the  $0\mu$  sample is more complicated because of the contribution of different decay modes of the  $\tau$ . The expression is:

$$(N_\tau^{\max})_{0\mu} = N_{0\mu}^{\text{loc}} \cdot r_\sigma \cdot \sum_{i=1,3} r_{A_i} \cdot \epsilon_{\text{kink}_i} \cdot \text{Br}_i, \quad (2)$$

where  $N_{0\mu}^{\text{loc}}$  is the number of located  $0\mu$  events (20, 081) and  $r_\sigma$  is the same cross-section ratio appearing in Eq. (1). The three decay modes which contribute to the  $0\mu$  category are the  $\tau$  decay in a negative hadron plus neutrals:  $\tau \rightarrow \nu_\tau h^- n h^0$ ; the decay  $\tau \rightarrow \nu_\tau \bar{\nu}_e e^-$ , when the electron behaves similarly to a hadron (no early showering); the decay  $\tau \rightarrow \nu_\tau \bar{\nu}_\mu \mu^-$ , for the

Table 3

Efficiency for the decay detection and relative acceptance, for the  $\tau$  decay modes contributing to the  $0\mu$  sample

Decay mode	Br	$\epsilon_{\text{kink}}$	$r_A$	$\text{Br} \times \epsilon_{\text{kink}} \times r_A$
$\tau \rightarrow \nu_\tau h^- n h^0$	0.495	0.11	2.88	0.157
$\tau \rightarrow \nu_\tau \bar{\nu}_e e^-$	0.178	0.05	2.21	0.020
$\tau \rightarrow \nu_\tau \bar{\nu}_\mu \mu^-$	0.174	0.10	0.69	0.012

fraction of events where the muon is not identified but is still selected by the  $0\mu$  criteria. Table 3 displays the branching ratios of these three channels together with the values of  $\epsilon_{\text{kink}}$ , computed for the final selection as defined in the last line of Table 2, and of  $r_A$ . The interpretation of the values of  $r_A$ , the ratio of acceptances, is in this case not straightforward. In fact, the acceptance for  $\nu_\mu$  interactions takes into account the NC/CC cross-section ratio, since the main contribution to the  $N_{0\mu}^{\text{loc}}$  sample comes from NC interactions (note that in Eq. (2),  $r_\sigma$  is the ratio of CC cross-sections). The kinematical selections have largely different effects on  $\nu_\mu$  and  $\nu_\tau$  interactions and also the reconstruction efficiency, which is included in the acceptance, is in this case different for  $\nu_\mu$  and  $\nu_\tau$ , as explained at the end of Section 6.1.

In concluding this section, we recollect the final result of the search as displayed in Table 2. No  $\tau$  decay candidate is found, neither in the  $1\mu$  sample nor in the  $0\mu$  sample, once the best set of selections is applied (last line of Table 2). The null observation is used to set limits on oscillation parameters. This is shown in the next section.

## 9. Limits on oscillation

Limits on  $\nu_\mu \rightarrow \nu_\tau$  and  $\nu_e \rightarrow \nu_\tau$  oscillation have been computed on the basis of zero candidates as observed both in the  $1\mu$  and  $0\mu$  samples.

### 9.1. Limits on $\nu_\mu \rightarrow \nu_\tau$ oscillation

Within a two flavours mixing scheme, the oscillation probability is written in the usual form:

$$P_{\mu\tau} = \sin^2 2\theta_{\mu\tau} \cdot \sin^2 \left( \frac{1.27 \cdot \Delta m^2 \cdot L}{E} \right). \quad (3)$$

The average values of  $L$  and  $E_{\nu_\mu}$  are 0.6 km and 27 GeV, respectively.

For large  $\Delta m^2$  values, when the energy dependent term of the probability averages to 1/2, the upper limit on the oscillation probability is obtained from the equation:

$$P_{\mu\tau} \leq \frac{N_\tau}{(N_\tau^{\max})_{1\mu} + (N_\tau^{\max})_{0\mu}}, \quad (4)$$

where, in the absence of a signal,  $N_\tau$  is the upper limit on the number of  $\tau$  decay candidates (the derivation of the upper limit will be discussed later in the text) and the two  $N_\tau^{\max}$  are defined in the previous section. When  $\Delta m^2$  is comparable or smaller than the  $E/L$  ratio the spectrum of the  $\nu_\tau$  resulting from oscillation is modified by the energy dependent term of Eq. (3). Then, to compute limits on the oscillation parameters, appropriate integrations are performed to take into account the effect of energy dependent cross-sections, acceptances and efficiencies. Fig. 5 shows the dependence from the neutrino energy of the global analysis efficiency,  $A_\tau \cdot \epsilon_{\text{kink}}$ , of  $\nu_\tau$  interactions. It includes the effects of the full analysis chain, i.e., the event reconstruction, the vertex location, the kink search and the kinematical cuts.

The decrease at high energy is mainly due to the cuts applied on the momentum of the  $\tau$  daughter candidate before scanning.

The size of the upper limit  $N_\tau$  is determined by the statistics and by the systematic error affecting the denominator of Eq. (4). The latter receives different contributions. The errors on the  $\tau$  branching ratios and from the Monte Carlo statistics are negligible. The error on the  $\sigma_\tau^{CC}/\sigma_\mu^{CC}$  ratio is also small. The calculation of the acceptances and an experimental

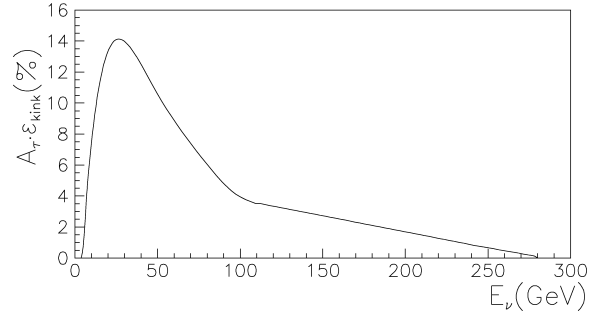


Fig. 5. Total efficiency,  $A_\tau \cdot \epsilon_{\text{kink}}$ , for  $\nu_\tau$  interactions detection as a function of the neutrino energy.

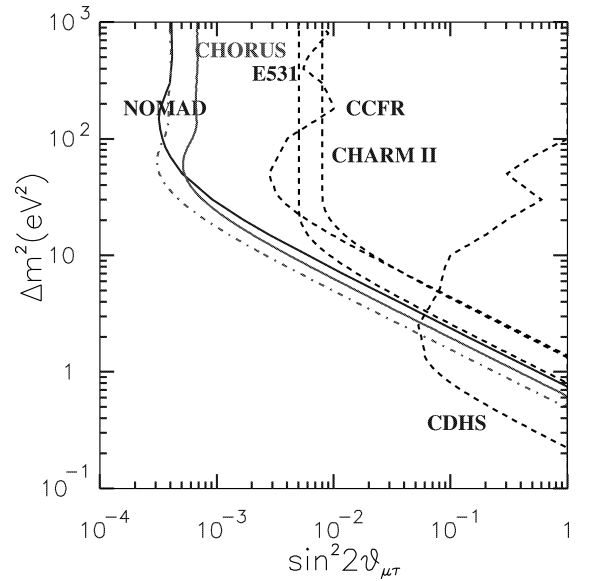


Fig. 6. Present limit on  $\nu_\mu \rightarrow \nu_\tau$  oscillation compared to the results of previous experiments [19–22] (dashed lines) and to the recent NOMAD result [23] (full line); the meaning of the second CHORUS curve (dash-dotted), is explained in the text.

check of the kink detection efficiency were discussed in Section 7. We estimate the overall systematic error on the denominator of Eq. (4) to be 17%.

For the determination of  $N_\tau$ , i.e., the upper limit on the number of  $\nu_\tau$  candidates, we have used the method proposed by Junk [18] which allows the combination of different channels, taking into account the errors on the background and on the signal.

The overall 90% C.L. upper limit on the number of  $\tau$  decays is 2.4. It is based on the null observation in the two independent channels,  $1\mu$  and  $0\mu$ . The

limit on the  $\nu_\mu \rightarrow \nu_\tau$  oscillation probability obtained through Eq. (4) is:

$$P_{\mu\tau} \leq 3.4 \times 10^{-4}. \quad (5)$$

The 90% C.L. excluded region in the  $(\sin^2 2\theta_{\mu\tau}, \Delta m^2)$  parameter space is represented in Fig. 6. Full mixing between  $\nu_\mu$  and  $\nu_\tau$  is excluded at 90% C.L. for  $\Delta m^2 > 0.6 \text{ eV}^2$ . Large  $\Delta m^2$  values are excluded at 90% C.L. for  $\sin^2 2\theta_{\mu\tau} > 6.8 \times 10^{-4}$ .

Fig. 6 also displays the recent NOMAD result [23]. Their result should not be directly compared with ours, since the statistical treatment of the data is different. The problem of calculating upper limits has recently received great attention. Many different methods have been suggested, consistently with the fact that different, statistically correct choices can be made to evaluate 90% C.L. The NOMAD Collaboration has adopted the technique proposed by Feldman and Cousins (FC) [24] which, applied to our data — zero events observed — gives an upper limit of 1.4 events, much more stringent than the one we have used to draw the exclusion curve. The tightness of the upper limit resulting from the FC method in some particular cases, has already been questioned in the literature [25,26]. We agree with the observation by Cousins [27] that these results are understood and statistically correct, since they reflect the low probability of the observed data set for a given expectation of background plus signal. However, the upper limit of 2.4 events, equally well founded statistically, gives information more directly connected to the common use of an exclusion plot, since it is related to the size of that signal which would have less than 10% probability of resulting in the observation of zero events. Note that results close to 2.4 are obtained using techniques other than the one proposed by Junk (see, e.g., [25,26]).

For the sake of a direct comparison with the result of NOMAD, the curve corresponding to the upper limit of 1.4 events ( $\sin^2 2\theta_{\mu\tau} < 4.0 \times 10^{-4}$  for large  $\Delta m^2$ ) is also shown in Fig. 6 (dash-dotted line).

### 9.2. Limits on $\nu_e \rightarrow \nu_\tau$ oscillation

The SPS neutrino beam contains a  $\nu_e$  component which amounts to 0.9% of the integrated  $\nu_\mu$  flux. The negative result of the search for  $\nu_\tau$  interactions can therefore be used to set limits on the  $\nu_e \rightarrow$

$\nu_\tau$  oscillation. The evaluation of the limit has been performed with the same technique used for the  $\nu_\mu \rightarrow \nu_\tau$  oscillation, this time in the assumption that the  $N_\tau$  events are coming from the oscillation of the  $\nu_e$  component of the beam. To account for the uncertainty on the  $\nu_e/\nu_\mu$  flux ratio the overall systematic error has been increased to 28% in this case. The difference between the  $\nu_\mu$  and  $\nu_e$  energy spectra — the average energy of  $\nu_e$  component is 13 GeV higher — leads to differences in the acceptance for  $\nu_\tau$  interactions. In the case of the  $\nu_e$  beam, the increase of the cross-section with energy improves the sensitivity to  $\nu_\tau$  interactions, while the kinematic constraints and reconstruction inefficiencies affecting high energy events contribute to lower the acceptance.

Using the present sample the following 90% C.L. limit has been obtained

$$P_{e\tau} \leq 2.6 \times 10^{-2}. \quad (6)$$

The 90% C.L. excluded region in the  $(\sin^2 2\theta_{e\tau}, \Delta m^2)$  parameter space is shown in Fig. 7, together with the recent NOMAD [23] result. Full mixing between  $\nu_e$  and  $\nu_\tau$  is excluded at 90% C.L. for  $\Delta m^2 > 7.5 \text{ eV}^2$ ; large  $\Delta m^2$  values are excluded at 90% C.L. for  $\sin^2 2\theta_{e\tau} > 5.2 \times 10^{-2}$ .

The dash-dotted curve represents the result obtained by applying to our data the statistical method adopted by NOMAD.

## 10. Conclusions

The data collected by CHORUS in its four years of activity (1994–1997) have been analysed searching for the 1-prong decay of the  $\tau$ . No evidence for  $\nu_\tau$  interactions has been found and stringent limits on the parameters of the oscillation have been set.

In the future the sensitivity of the experiment will be extended to reach its design value ( $P_{\mu\tau} = 1 \times 10^{-4}$ ). Primary factors to achieve this goal are the substantial progress in the automatic scanning speed and various improvements in the reconstruction programs. It is now possible to scan more tracks per event and to digitize the emulsion grains in the vertex region for all located events. This will allow to increase the vertex location efficiency and to perform a detailed analysis of the located events, with a consequent increase of the kink detection efficiency as well. Work for an

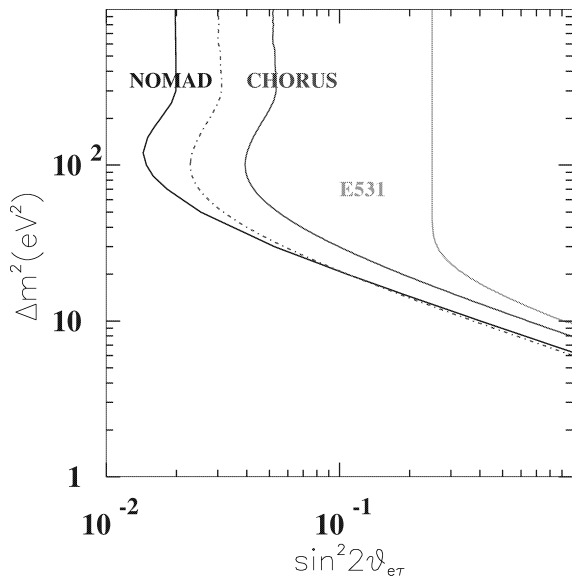


Fig. 7. Present limit on  $\nu_e \rightarrow \nu_\tau$  oscillation compared to the result of E531 [19] and to the recent NOMAD result [23]; the meaning of the second CHORUS curve (dash-dotted), is explained in the text.

improvement in the hadron momentum measurement is in progress. It should allow to reduce the expected WK background.

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