



# Cosmological Evolution of Supermassive Black Holes

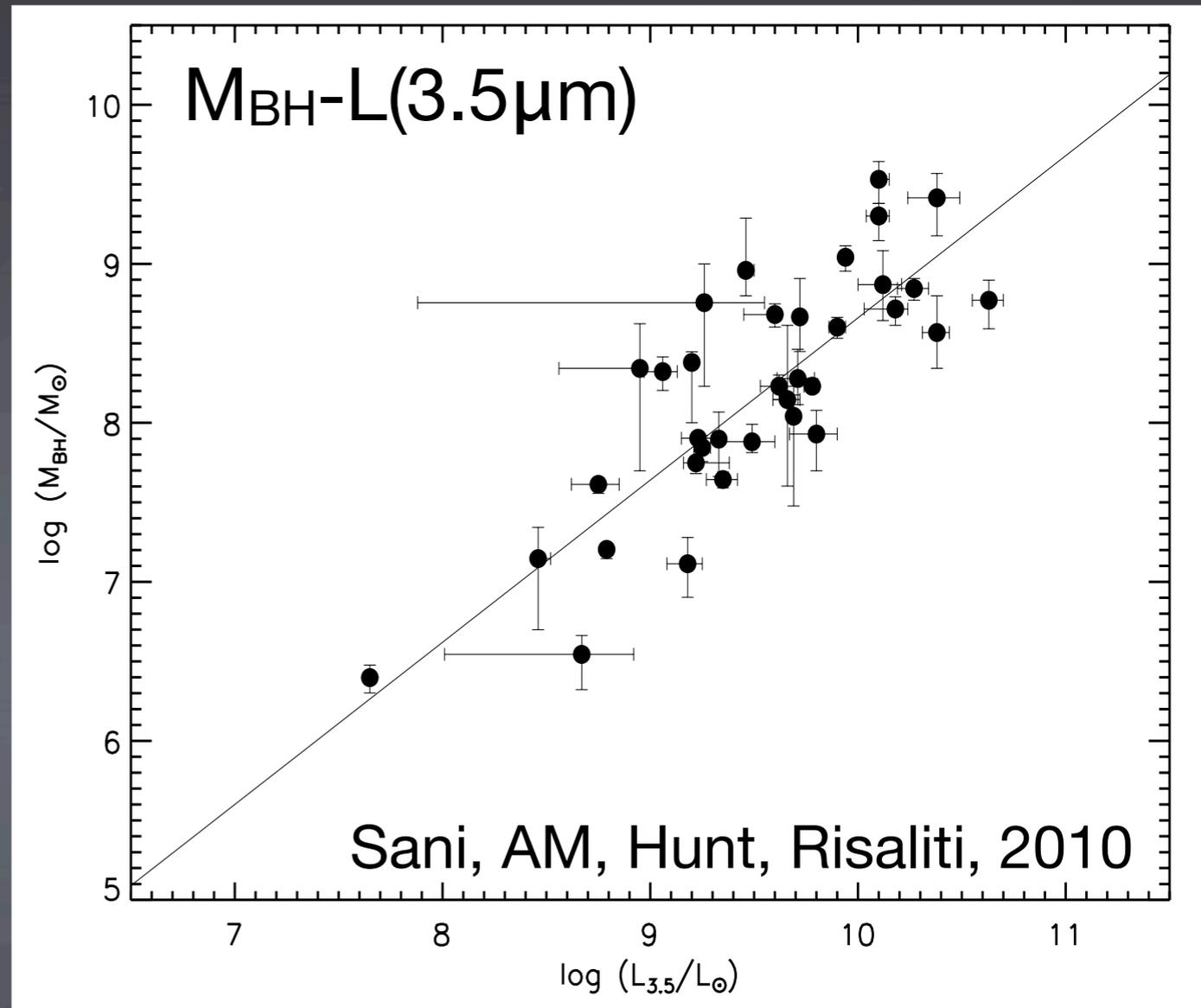
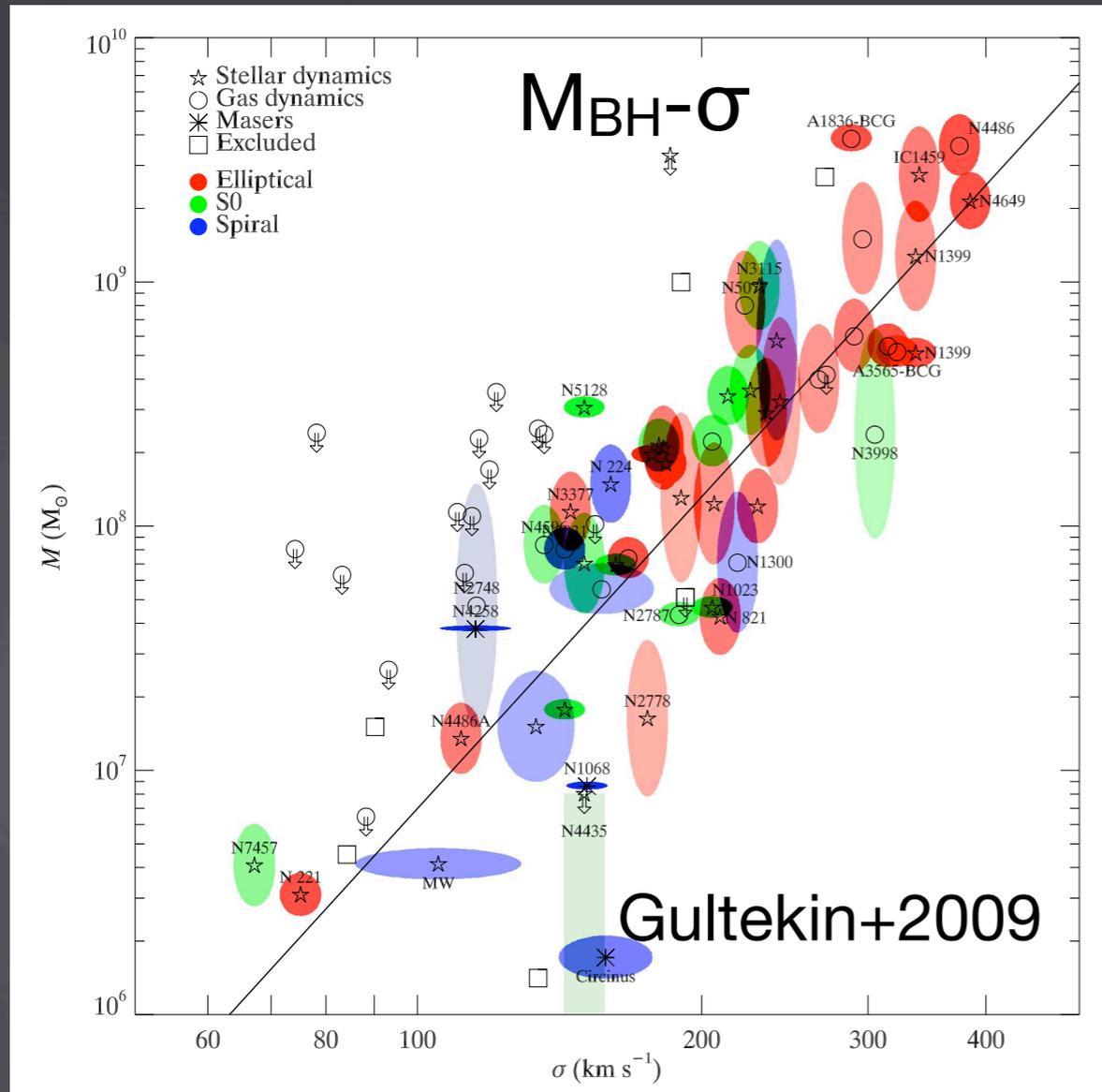
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Mauro Sirigu

# BH vs host galaxy (spheroid): $M_{\text{BH}} - \sigma, L$



- ★ Coevolution of supermassive BHs and their host galaxies;
- ★ Link BH-galaxy is (?) provided by AGN feedback;
- ★ Cosmological evolution of BHs important to understand galaxy evolution.

Kormendy & Richstone 1995;  
 Magorrian+1998; Ferrarese & Merritt 2000, Gebhardt+2000;  
 Graham+2001; Tremaine +2002; Marconi & Hunt 2003;  
 Haring & Rix 2004; Aller & Richstone 2007; Graham 2008

# Local BHs vs relics of AGN activity

Galaxy L or  $\sigma$  functions  
@  $z=0$

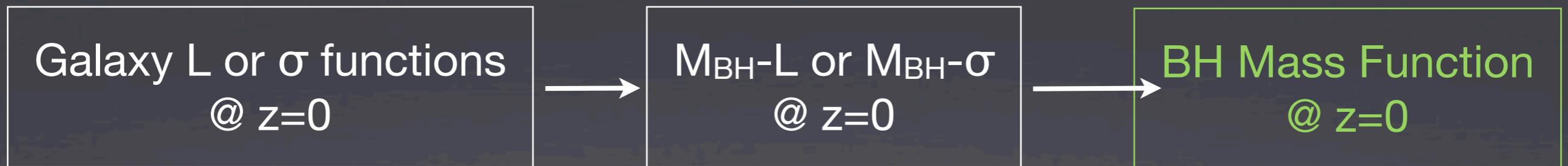


$M_{\text{BH-L}}$  or  $M_{\text{BH-}\sigma}$   
@  $z=0$

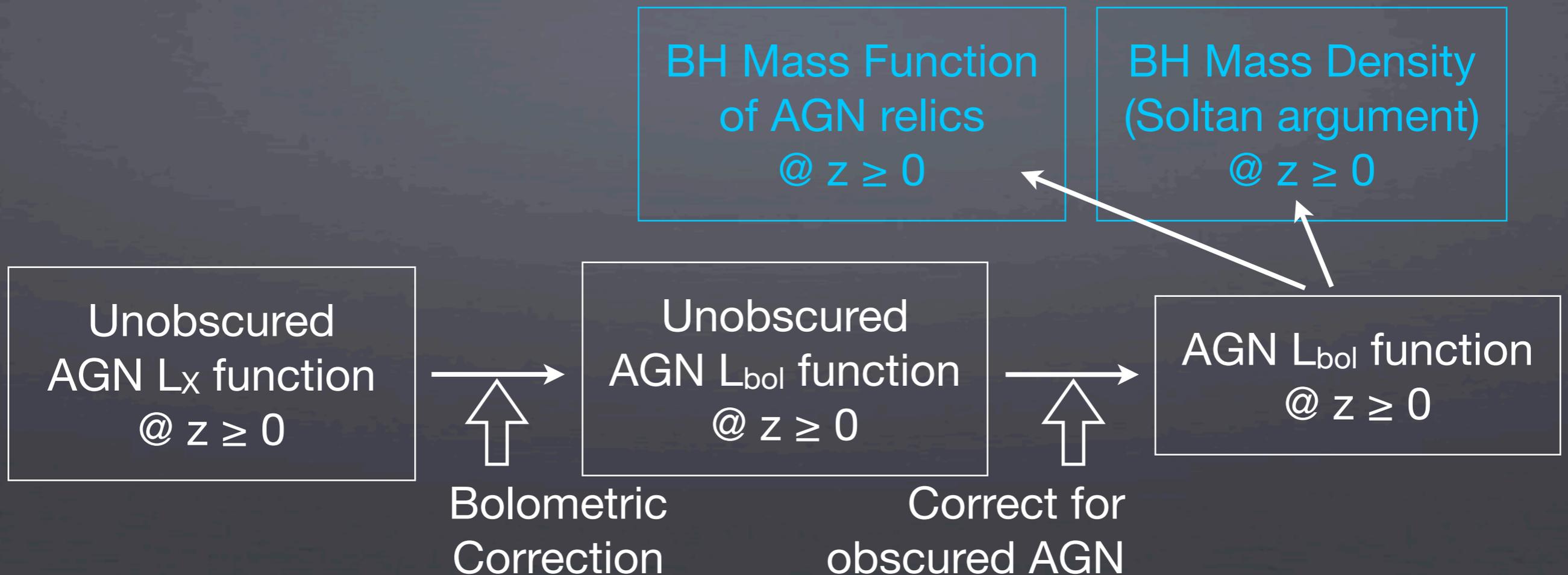
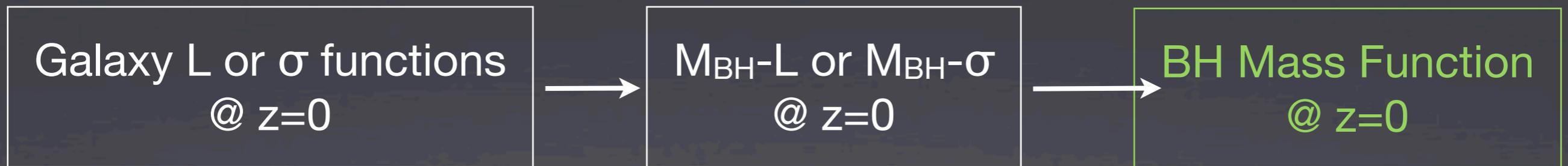


BH Mass Function  
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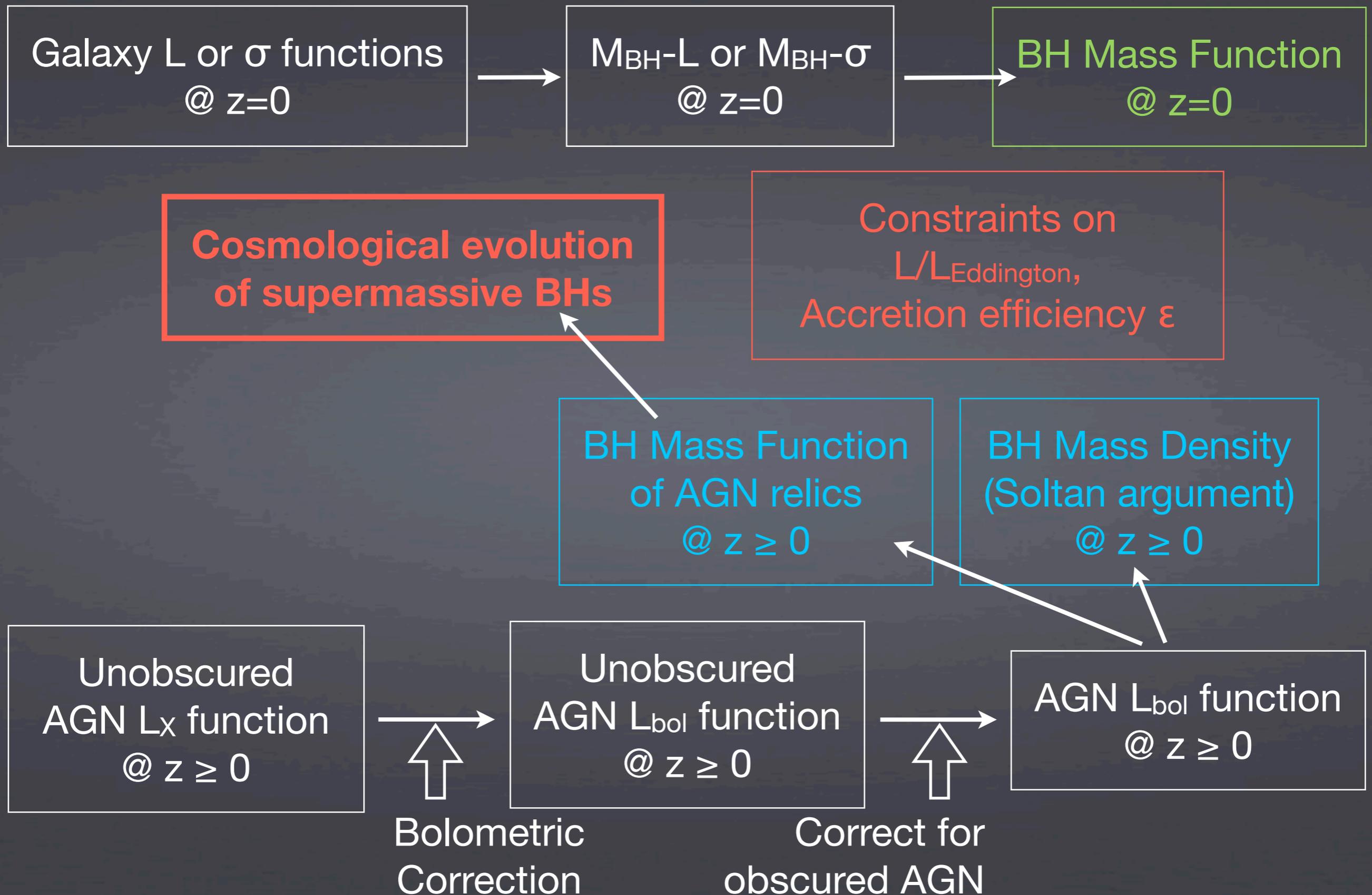
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BH Mass Function  
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Cosmological evolution  
of supermassive BHs

Constraints on  
 $L/L_{\text{Eddington}}$ ,  
Accretion efficiency  $\epsilon$

WFXT  
contribution

BH Mass Function  
of AGN relics  
@  $z \geq 0$

BH Mass Density  
(Soltan argument)  
@  $z \geq 0$

Unobscured  
AGN  $L_x$  function  
@  $z \geq 0$

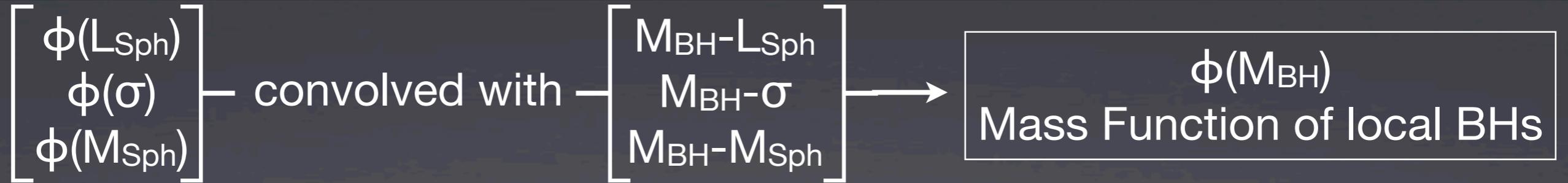
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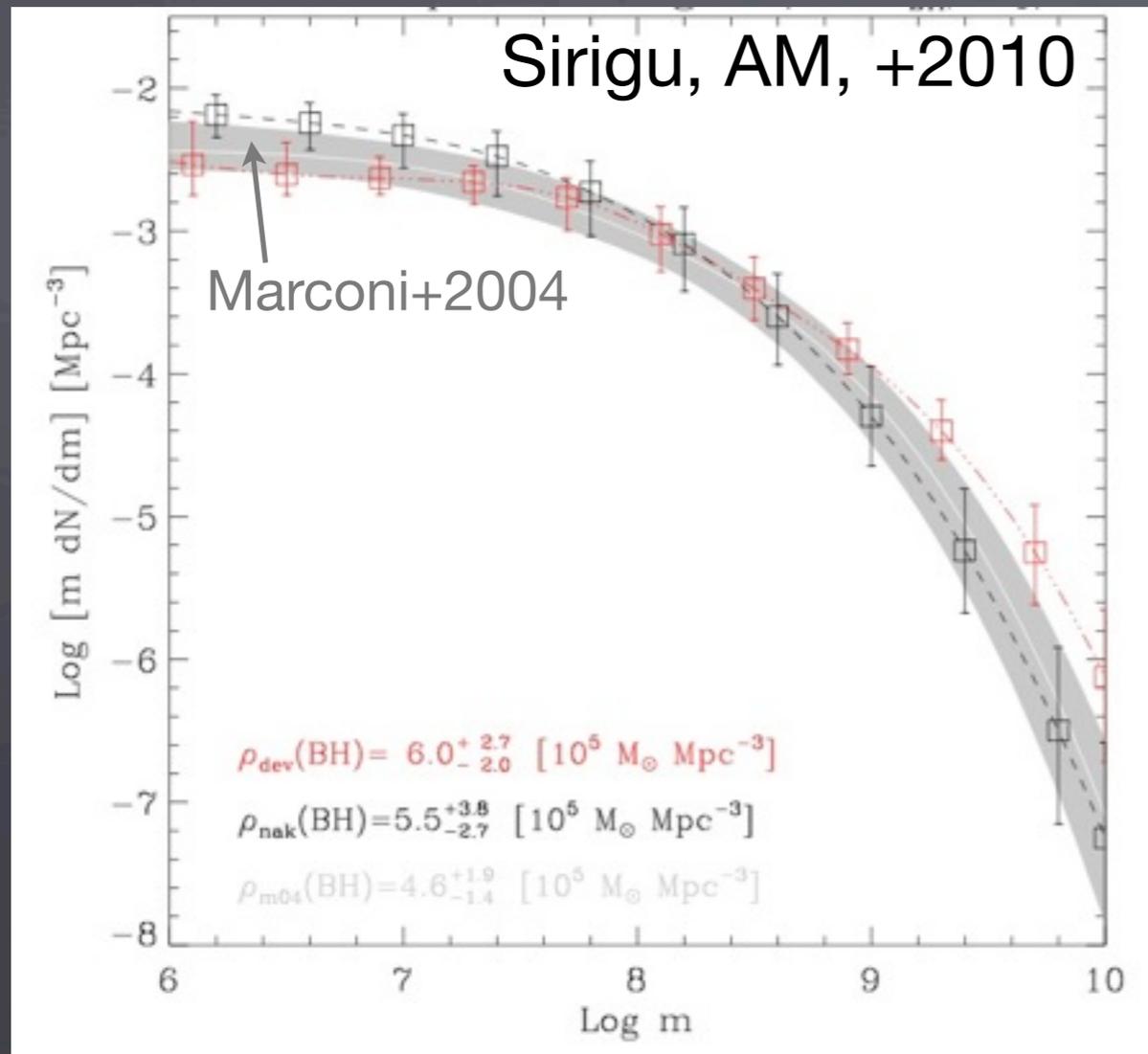
Bolometric  
Correction

Correct for  
obscured AGN

# Demography of local BHs



$$\phi(M_{\text{BH}}) = \int_0^{+\infty} P(M_{\text{BH}} | L_{\text{sph}}) \phi(L_{\text{sph}}) dL_{\text{sph}}$$



Overall there is a general agreement (or not so large disagreement) among estimates from different authors (with exceptions).

The integrated BH mass density is

$$\rho_{\text{BH}} \approx 3 - 6 \times 10^5 M_{\odot} \text{Mpc}^{-3}$$

Uncertainties on:

- \* LF per morphological type;
- \* average Bulge/Disk ratios
- \*  $M_{\text{BH}}\text{-}L/\sigma$  relations

Salucci +99, Yu & Tremaine 02, Marconi +04, Shankar +04, Tundo +07, Hopkins +07, Graham +07, Shankar +08 et many al.

# The Sołtan argument

Local black holes  
 $\rho_{BH} \approx 3-6 \times 10^5 M_{\odot} \text{ Mpc}^{-3}$

From AGN luminosity function derive relics mass density  
(assuming  $L = \epsilon \dot{M} c^2$ )

$$\rho_{BH} = \frac{1 - \epsilon}{\epsilon c^2} U_T = \frac{1 - \epsilon}{\epsilon c^2} \int_0^{z_{max}} \int_{L_{min}}^{L_{max}} L \phi(L, z) \frac{dt}{dz} d \log L dz$$

Accretion efficiency      Total comoving AGN energy density      AGN bolometric luminosity function

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Original Sołtan Estimate (QSO LFs as of 1982):  $\rho_{AGN} \approx 8 \times 10^4 M_{\odot} \text{ Mpc}^{-3}$

Marconi +04:  $\rho_{AGN} \approx 2.2 \times 10^5 M_{\odot} \text{ Mpc}^{-3}$  (hard X LF, Ueda +03)

No correction for “obscured” AGNs ... when taken into account:

Marconi +04:  $\rho_{AGN} \approx 3.5 \times 10^5 M_{\odot} \text{ Mpc}^{-3}$  ( $\epsilon \approx 0.1$ ; hard X LF, Ueda +03)

Shankar +08:  $\rho_{AGN} \approx 4.5 \times 10^5 M_{\odot} \text{ Mpc}^{-3}$  ( $\epsilon \approx 0.07$ ; hard X LF, Ueda +03)

# The “differential” Sołtan argument

Apply **continuity equation to BHMF** (Cavaliere +71, Small & Bandford 92):

$$\frac{\partial f(M, t)}{\partial t} + \frac{\partial}{\partial M} \left[ \langle \dot{M} \rangle f(M, t) \right] = 0$$

Assuming  $\left\{ \begin{array}{l} \text{no “source” term (no merging of BHs)} \\ L = \varepsilon \dot{M} c^2 \\ L = \lambda L_{Edd} = \lambda \frac{M c^2}{t_E} \end{array} \right.$

BH Mass Function (AGN relics)

AGN Luminosity Function

$$\frac{\partial f(M, t)}{\partial t} + \frac{(1 - \varepsilon) \lambda^2 c^2}{\varepsilon t_E^2} \left( \frac{\partial \phi(L, t)}{\partial L} \right) = 0$$

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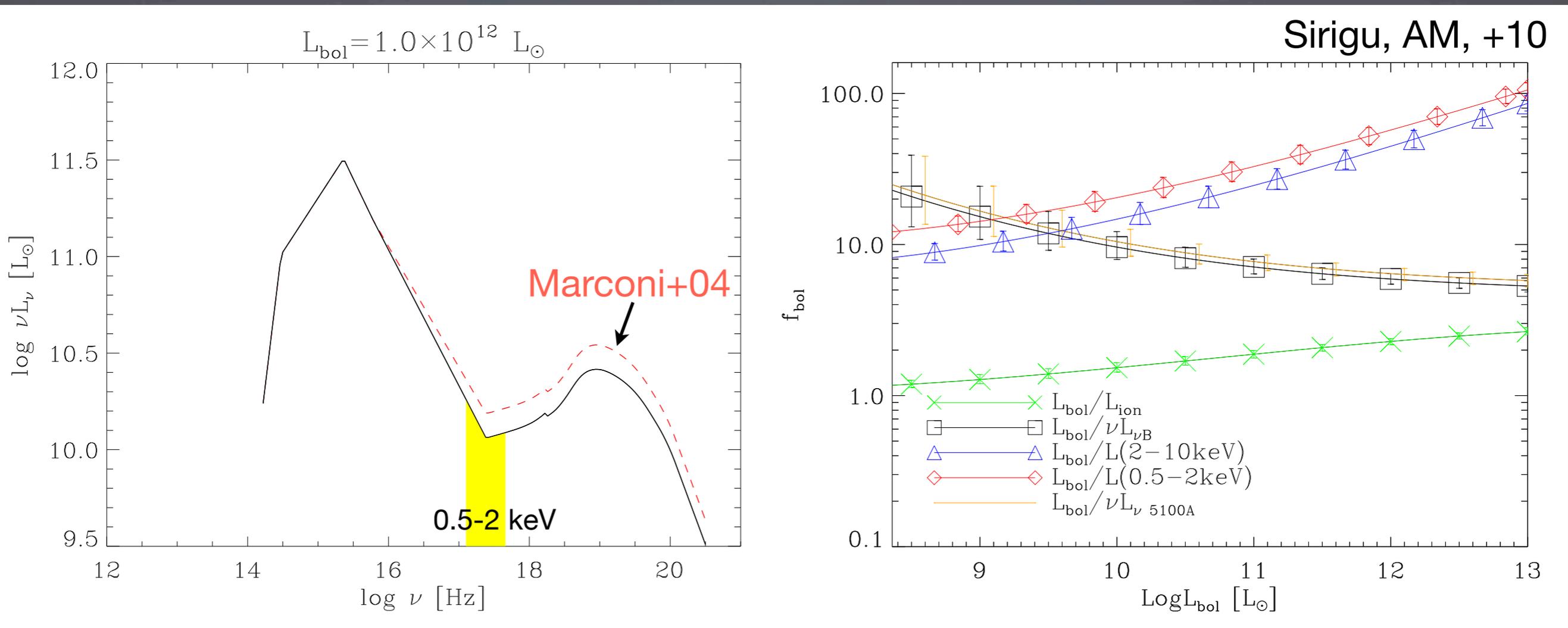
\*  $\phi(L, t)$  is the luminosity function of the **whole** AGN population (usually derived from X-ray LF after correcting for obscured sources)

# Bolometric corrections

Build AGN template spectrum assuming:

- ★ optical power law
- ★ X-ray power-law+cutoff
- ★ connect with L-dependent  $\alpha_{\text{OX}}$  (Kelly+08)

NO IR bump (not directly from accretion!)

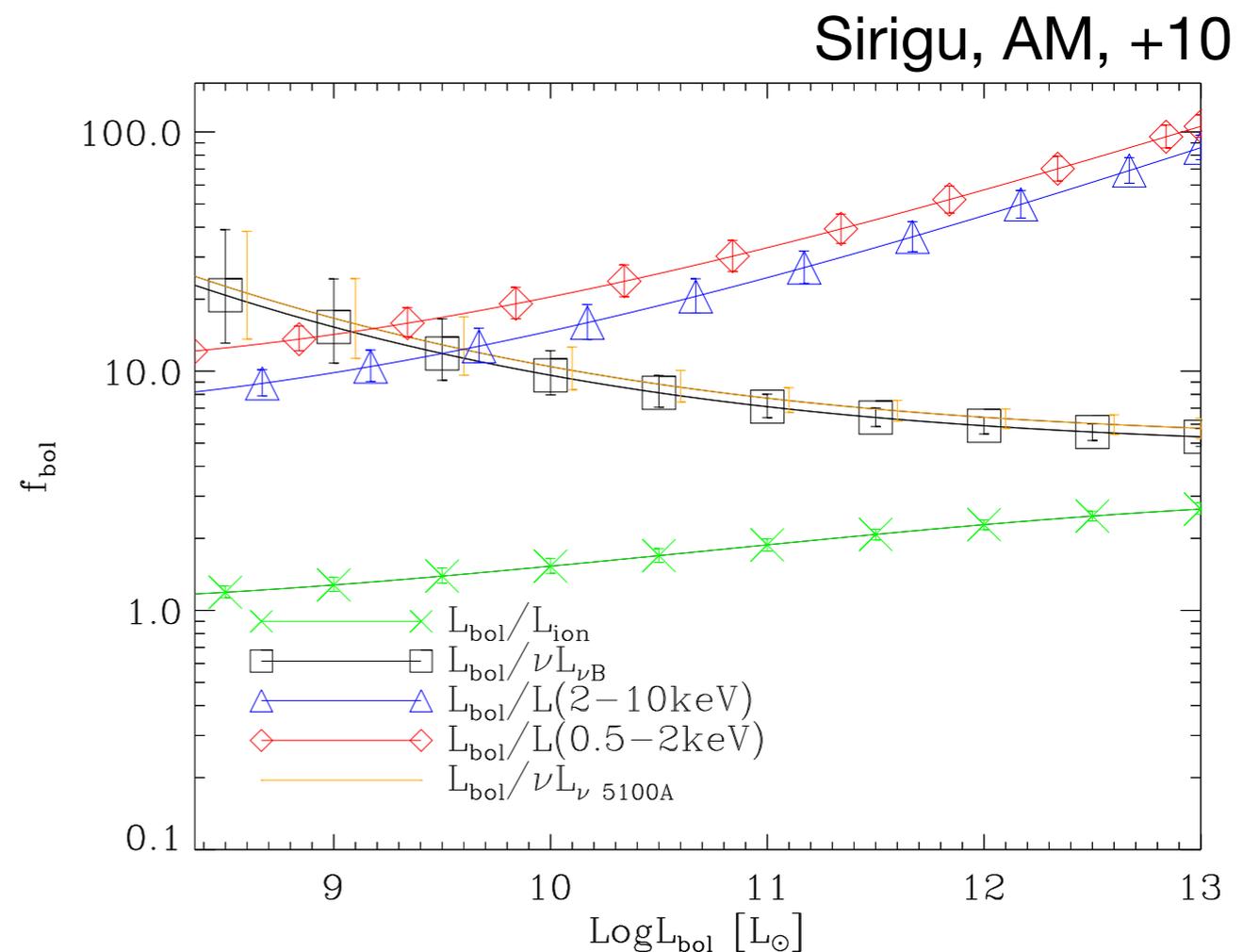
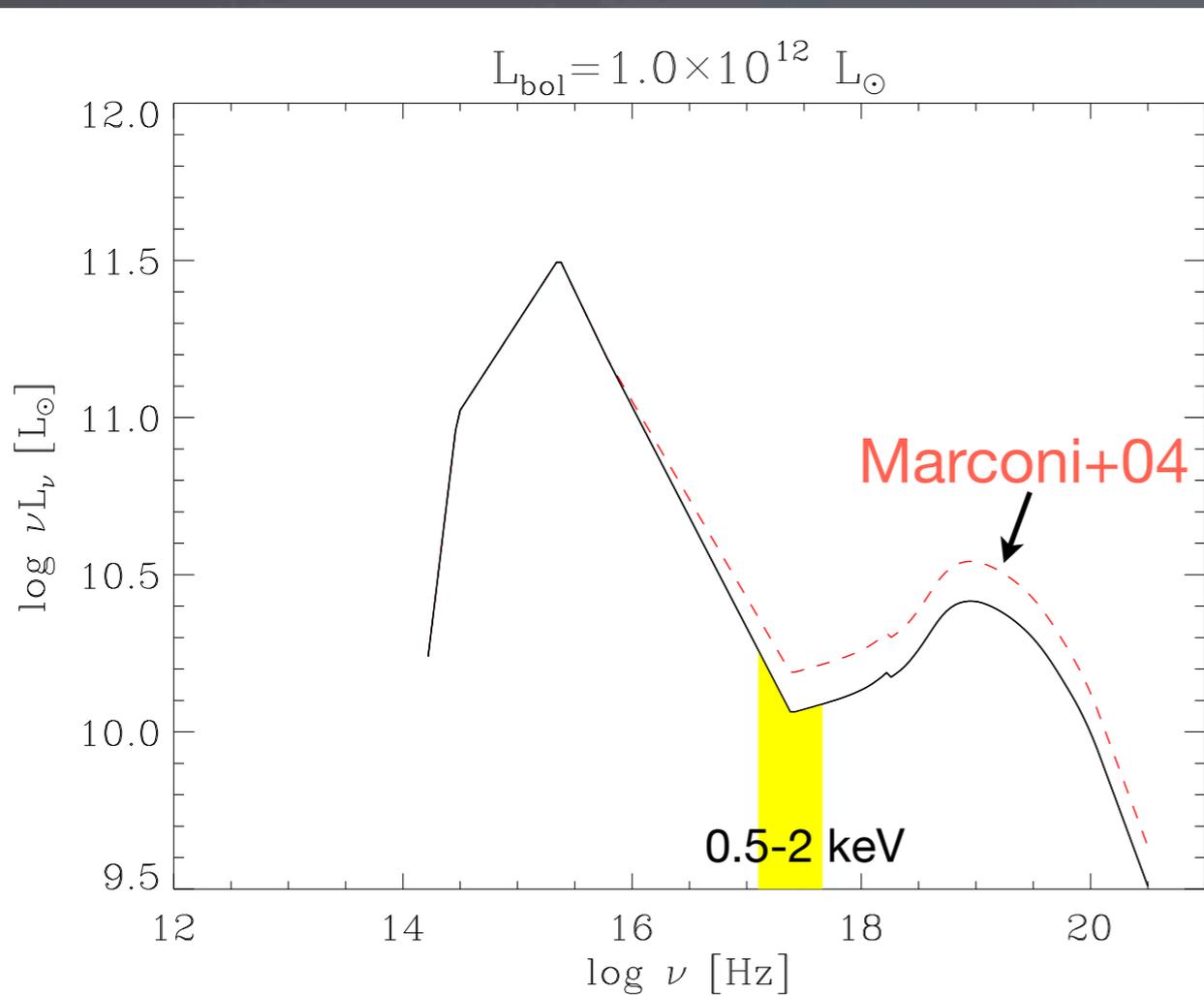


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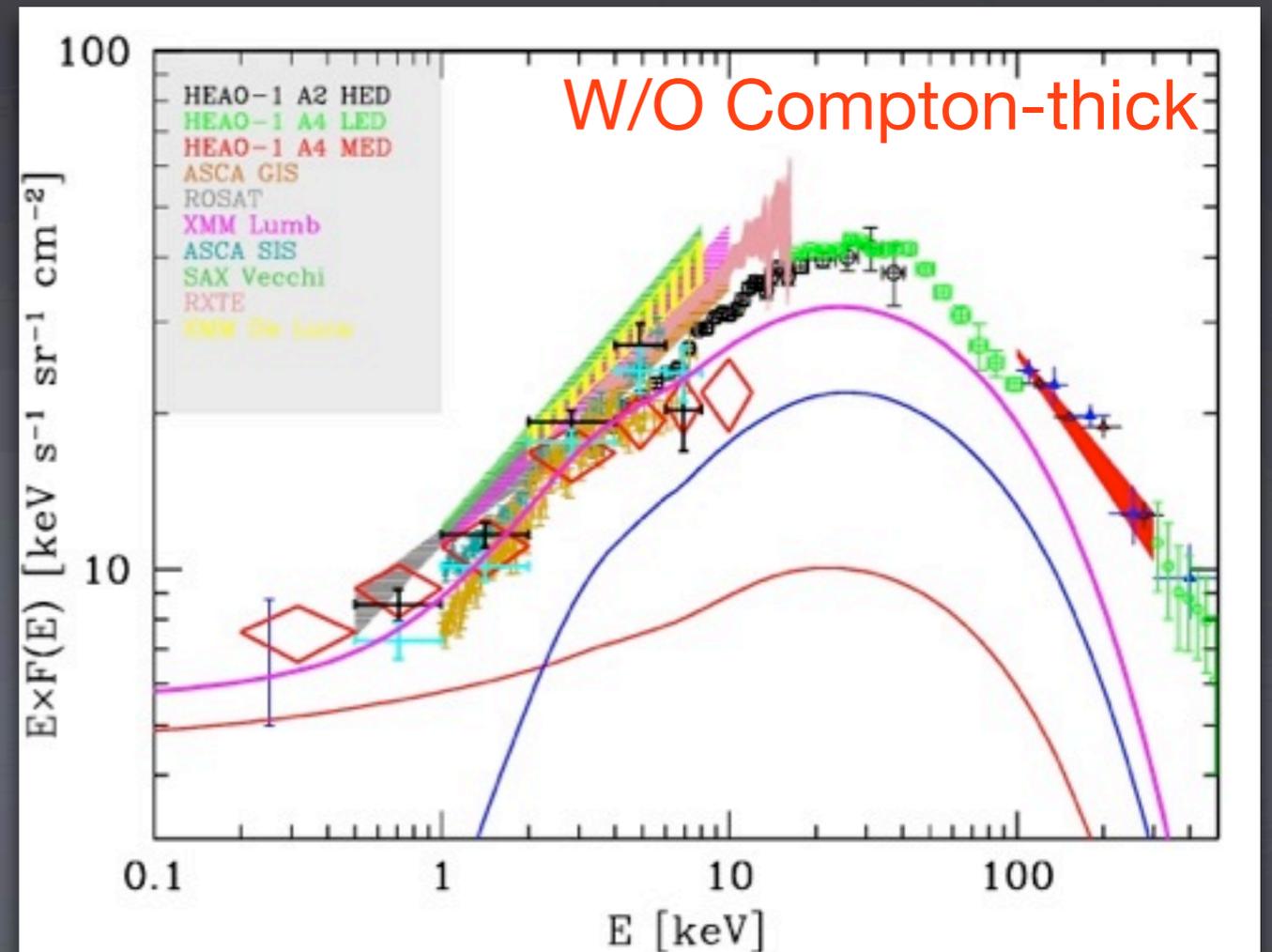
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# Constraints from X-ray Background

Models of the XRB take into account the whole AGN population  
→ also Compton-thick AGNs.

Their number density could be determined independently by XRB modeling (eg Gilli +07).

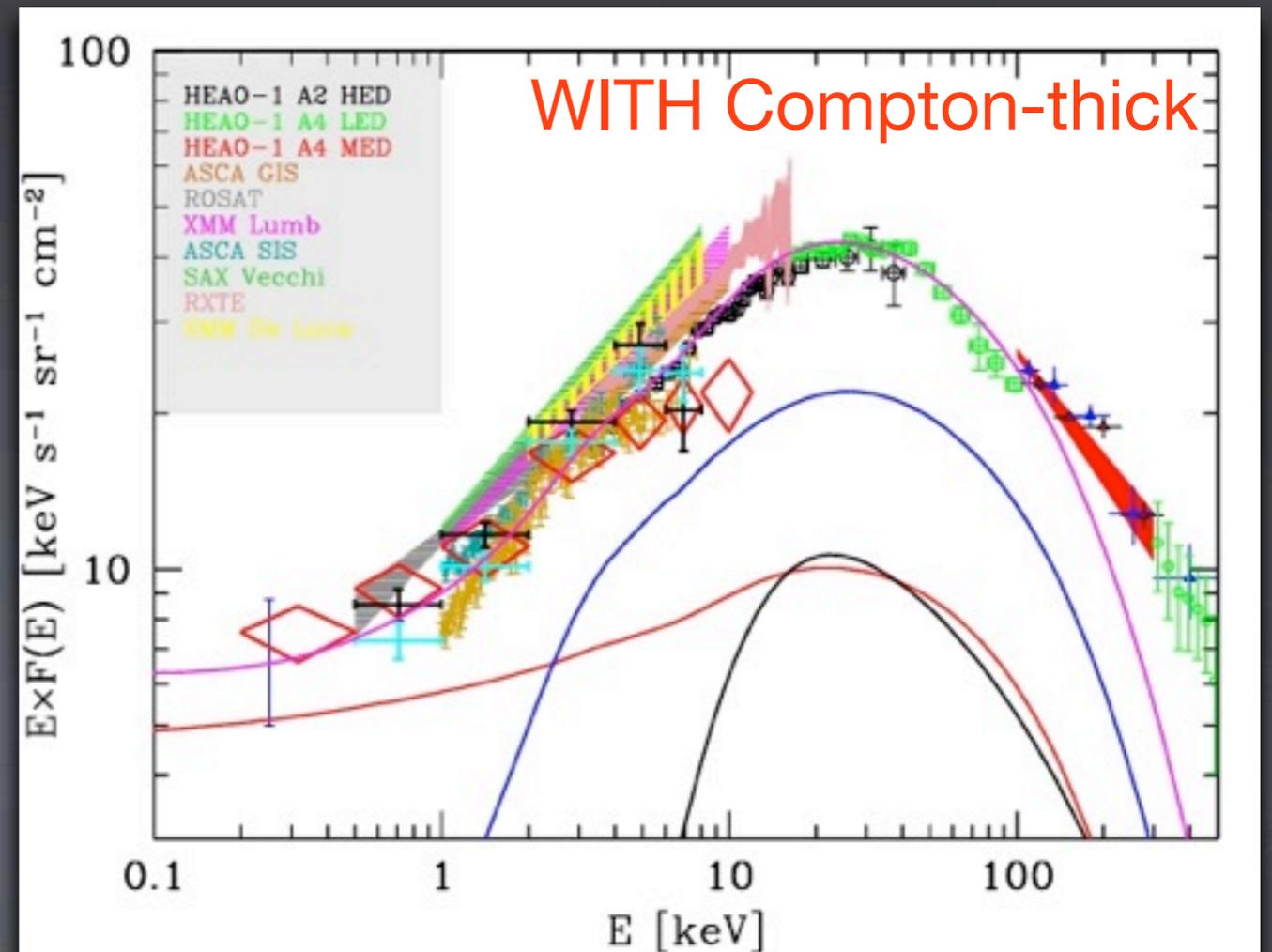


Gilli, Comastri & Hasinger +07

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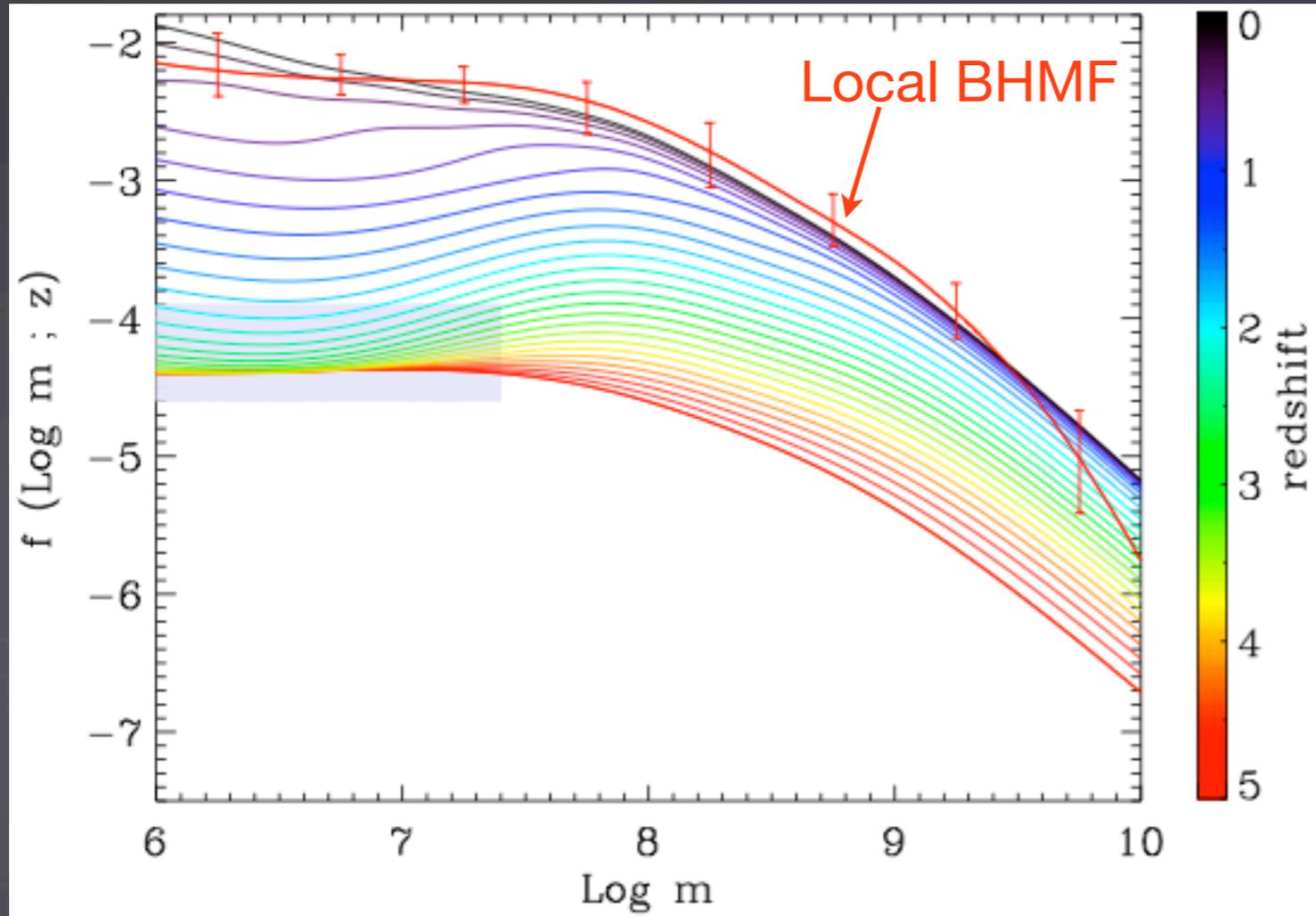
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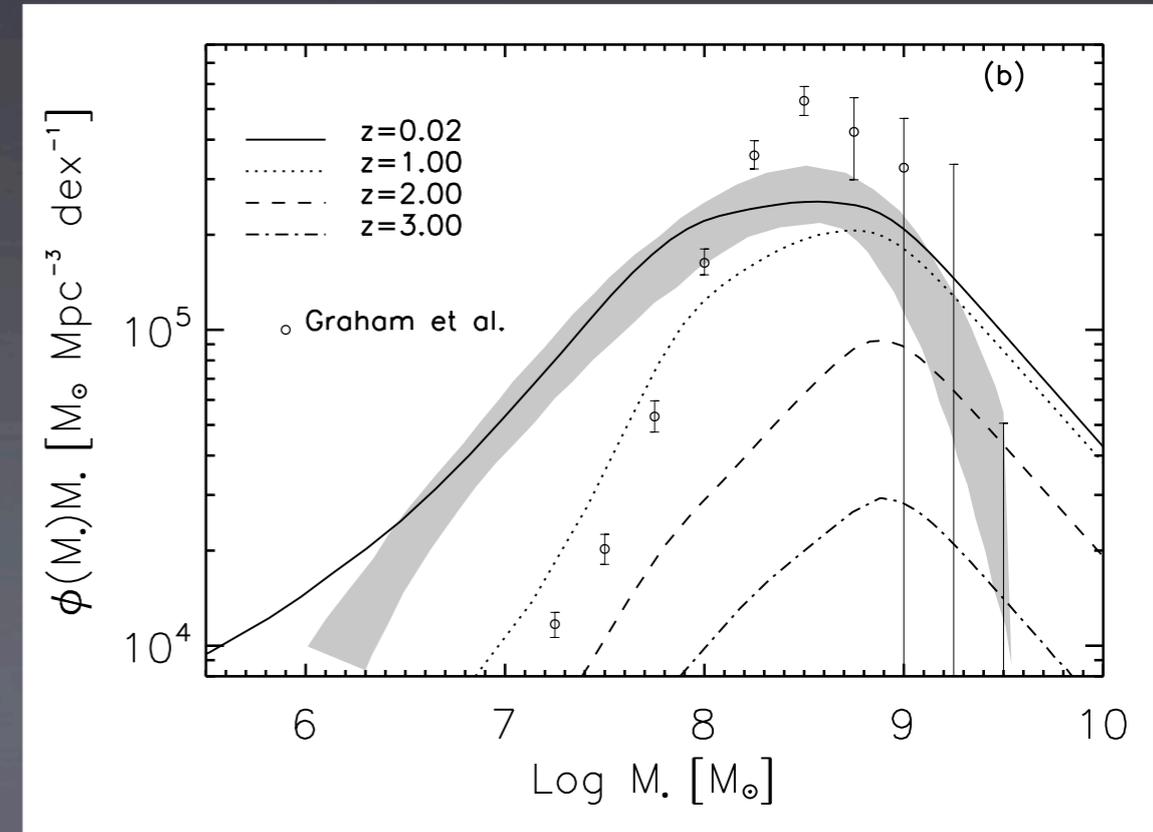


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# Local BHs vs AGN relics



Sirigu, AM +10 ( $\epsilon=0.063$ ,  $\lambda=0.2$ )

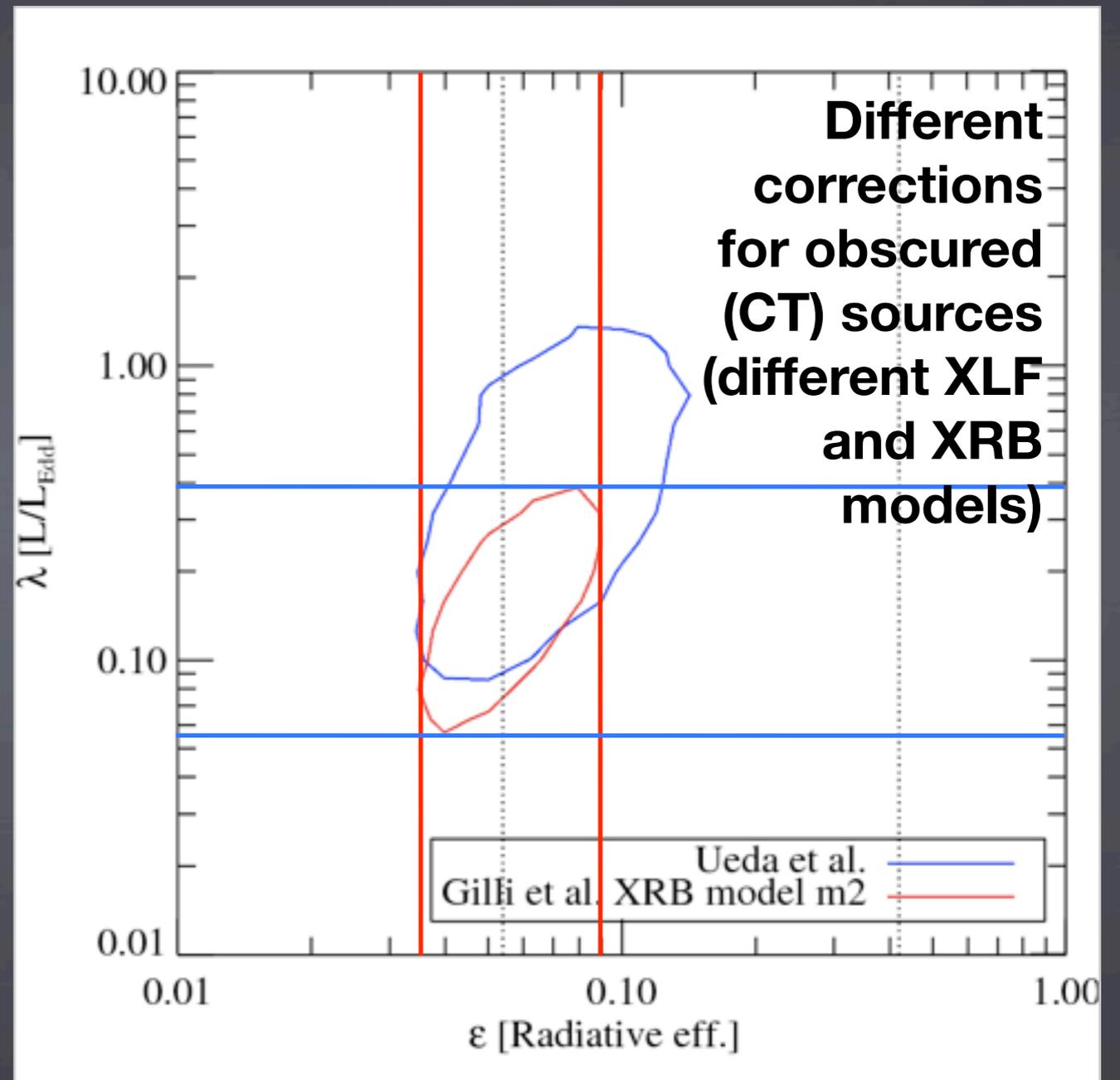


Shankar +08 ( $\epsilon=0.065$ ,  $\lambda=0.42$ )

In general there appears to be a good agreement between local BHs and AGN relics with  $\epsilon \approx 0.06$ ,  $\lambda \approx 0.2-0.4$  (see also Merloni & Heinz 2008)

# Radiative Efficiency and $L/L_{\text{Edd}}$

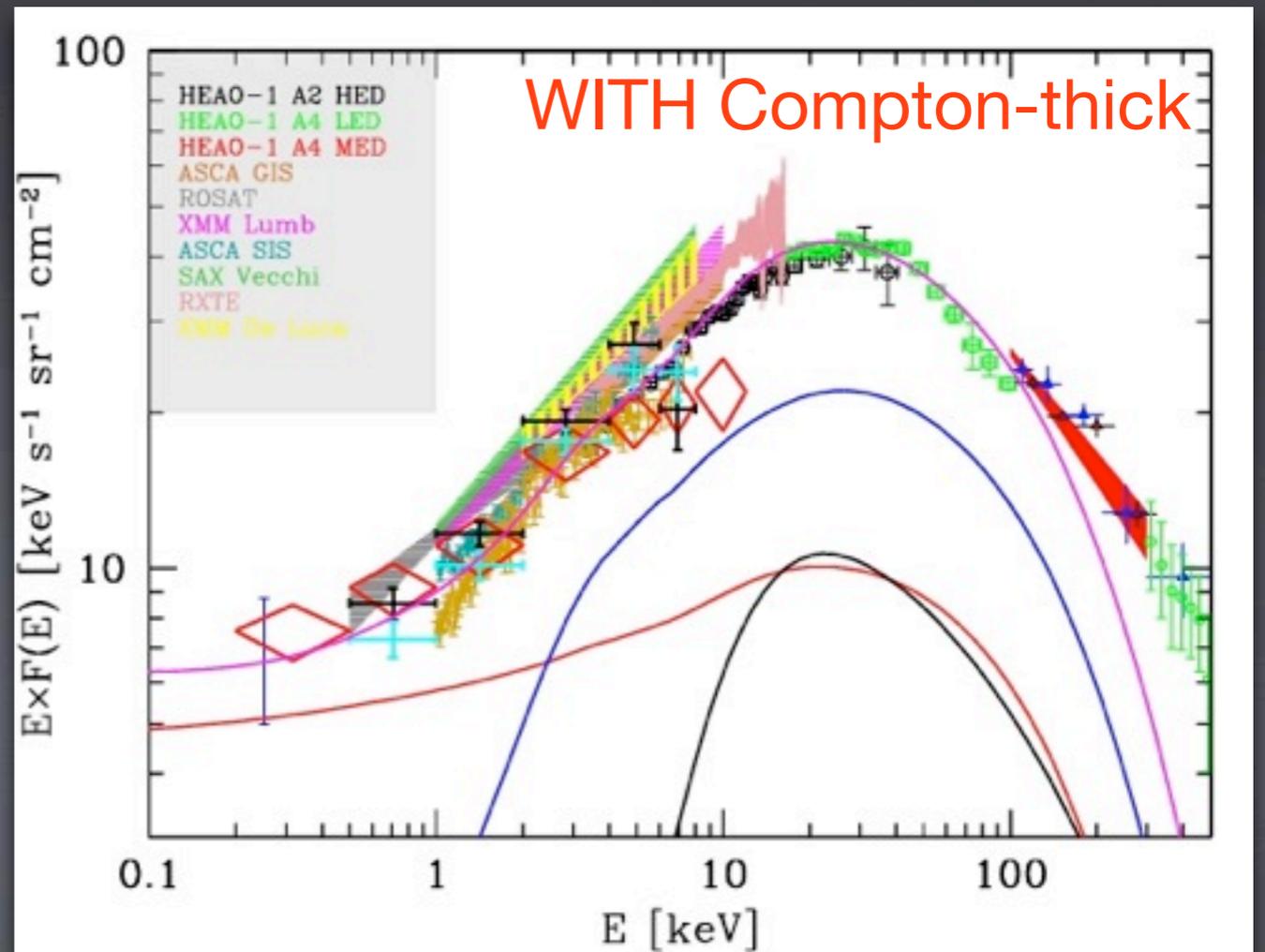
- Efficiency and fraction of Eddington luminosity are the only free parameters!
- Determine locus in  $\epsilon$ - $\lambda$  plane where there is the best match between local and relic BHMF!
- $\epsilon=0.04-0.09$   $\lambda=0.06-0.4$  which are consistent with common 'beliefs' on AGNs
- Marconi et al. 2004 found using Ueda et al. 2003:  $\epsilon=0.04-0.16$  and  $\lambda=0.1-1.7$  method is robust!



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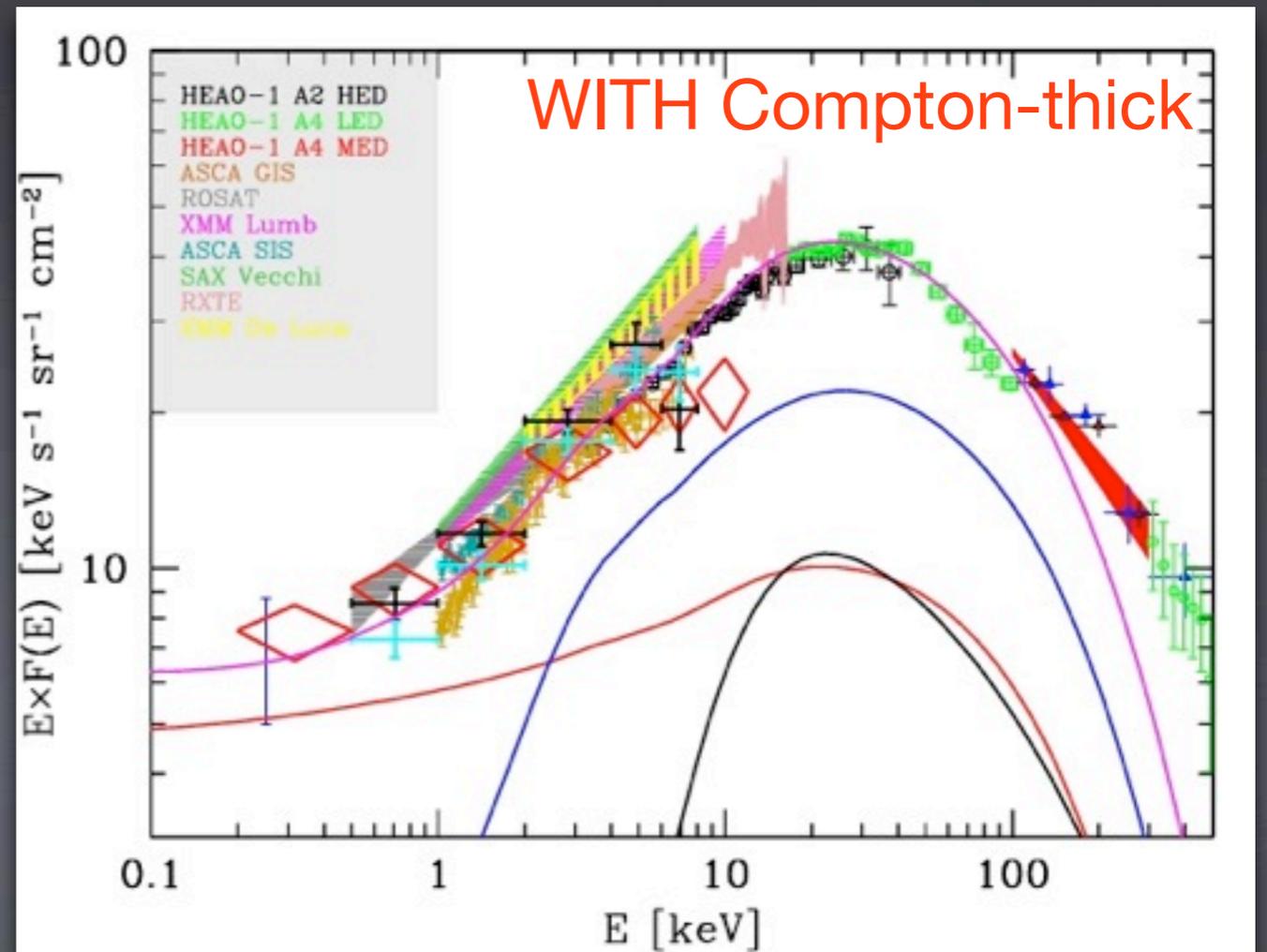
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But ...



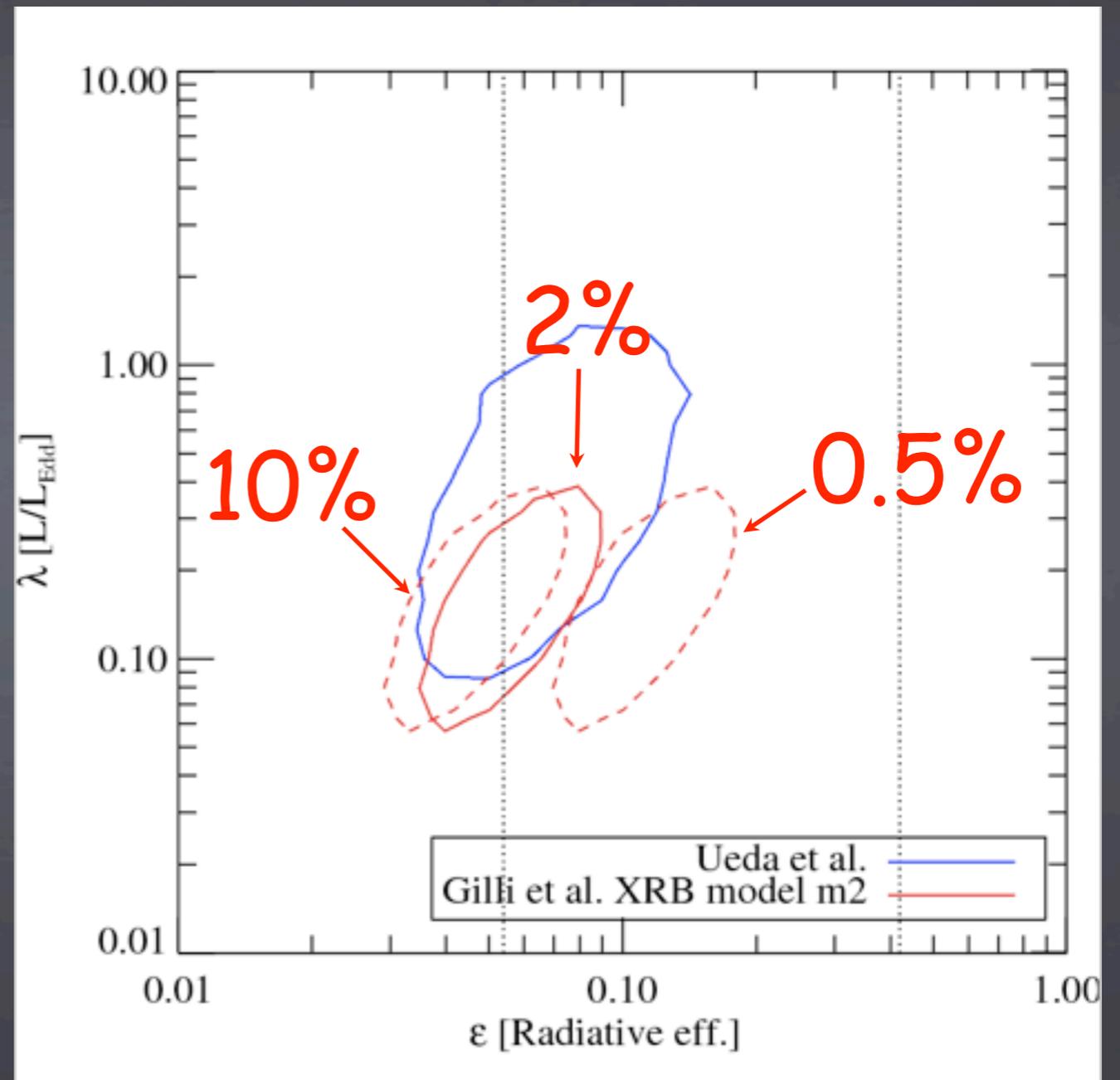
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The spectrum of fully Compton thick AGNs is the reflection spectrum whose normalization depends of the **ASSUMED** average scattering efficiency!

The number of Compton-thick AGNs depends on the **ASSUMED** scattering efficiency (~2%) for which there are almost no estimates available!

# Radiative Efficiency and $L/L_{\text{Edd}}$

- Effect of changing scattering efficiency to compute pure reflection spectra of Compton-Thick sources.
- Fundamental to constrain Obscured (CT) AGN fraction independently from the XRB background!
- Most important contribution from CT sources is at  $z \sim 0-2$ , because of time (90% of age of universe).



# Too many free parameters ...

Adopting the total AGN luminosity function as derived by the Gilli +07 model and matching the local BH mass function (Marconi +04) it is possible to write:

$$\frac{1 - \varepsilon}{\varepsilon} \left[ 1 + R_{\text{Thin}} + R_{\text{MThick}} + R_{\text{HThick}} \left( \frac{0.02}{f_{\text{scatt}}} \right) + X_{\text{Enshrouded}} \right] \simeq \begin{cases} 50 & (L > 2 \times 11 L_{\odot}) \\ 150 & (L < 2 \times 11 L_{\odot}) \end{cases}$$

R = Ratio obscured/unobscured

Compton Thin  
( $21 < \log N_{\text{H}} < 24$ )

Highly Compton Thick  
( $\log N_{\text{H}} > 25$ )

Mildly Compton Thick  
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Completely  
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Equazione G.R.A.M.A.  
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using Gilli +07 best model [R = 4+4 (low L); R= 1+1 (high L); Compton-Thick are ~ lower obscuration AGNs] and  $\varepsilon \sim 0.06$ .

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Example: assuming  $X \sim 4$  then with  $\varepsilon \sim 0.08$  (LL), 0.12 (HL) we can still satisfy the above equation! Little constraints from XRB and local BH mass function!

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**We need to know the fraction of Compton-Thick sources independently from XRB synthesis models → WFXT**

Compton-Thin  
( $21 < \log N_{\text{H}}$ )

Intermediate Obscuration  
( $24 < \log N_{\text{H}} < 25$ )

Marco Salvati  
Andrea Comastri

G.R.A.M.A.

Salvati

Gilli

Marconi

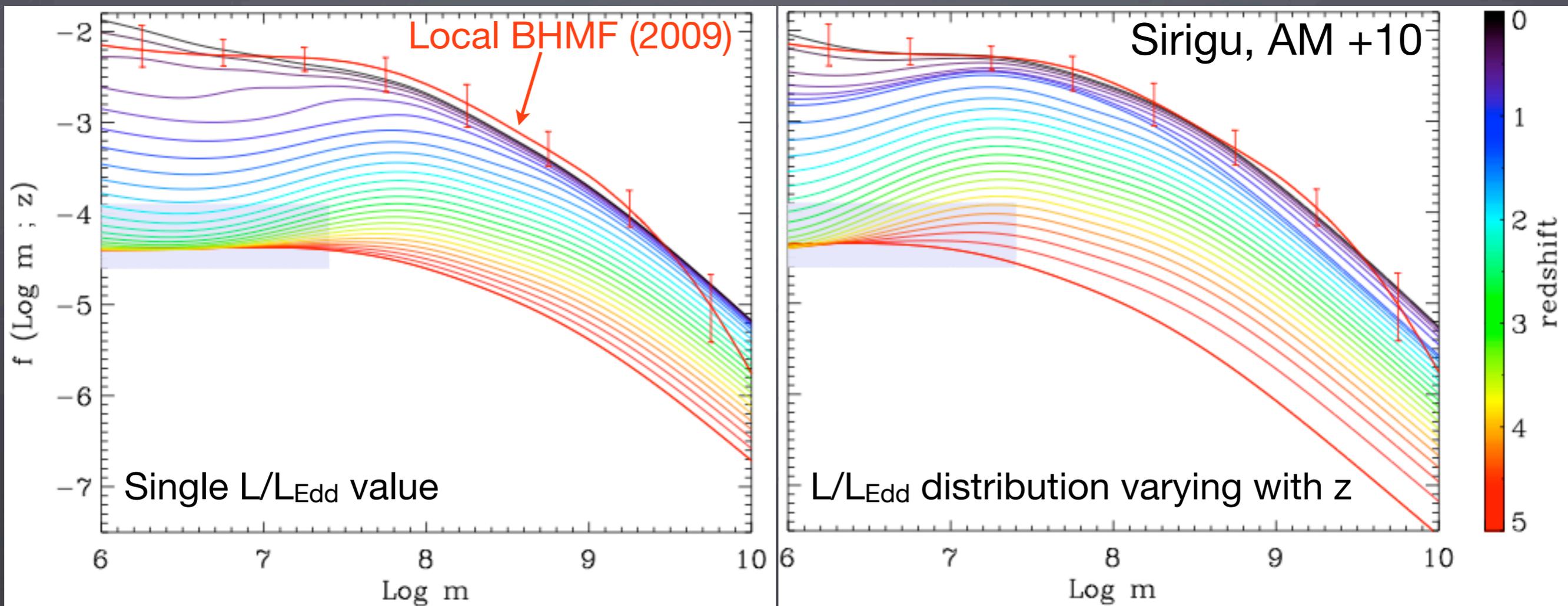
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# Allowing for a $L/L_{\text{Edd}}$ distribution

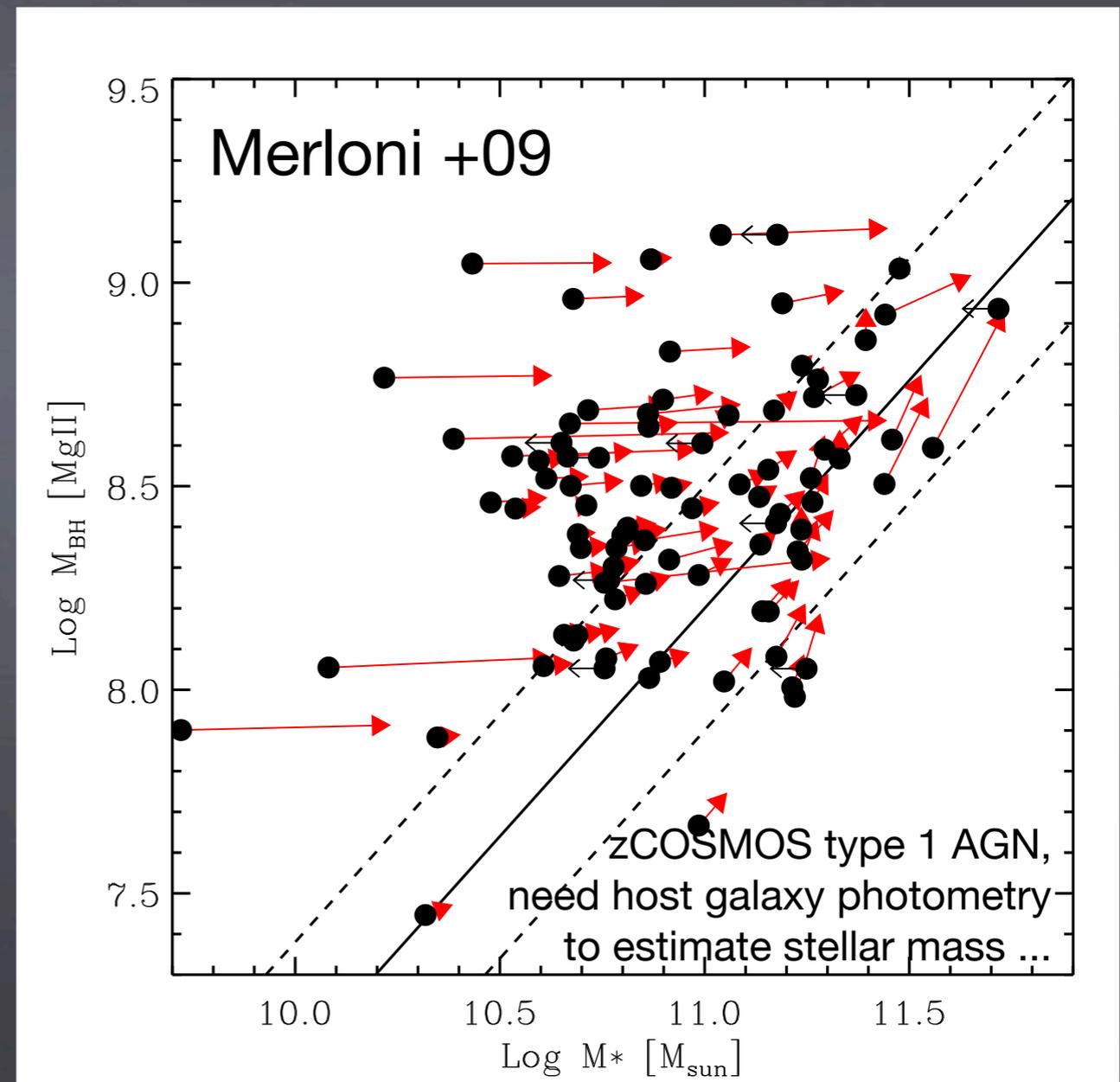
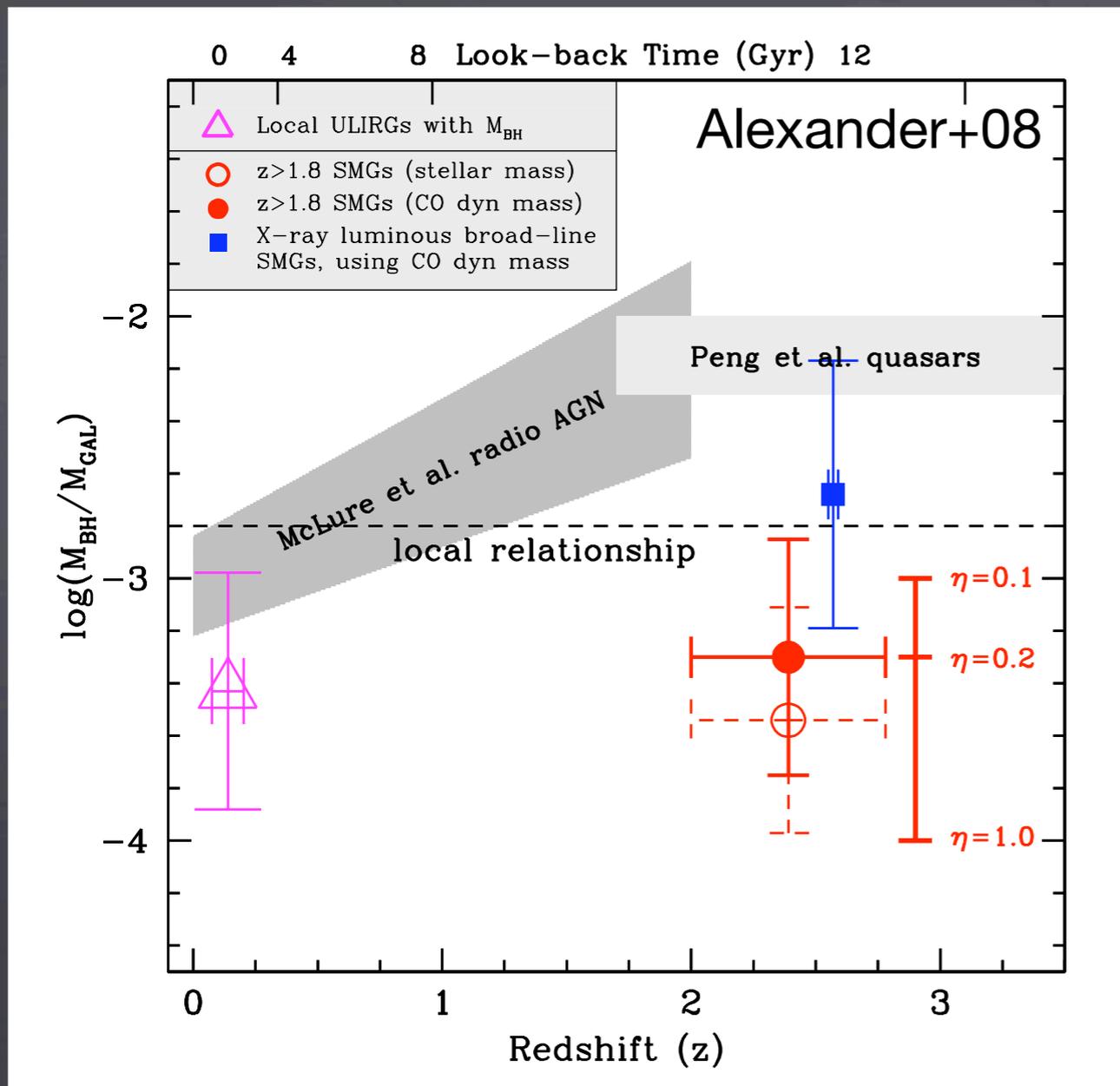
$$\frac{\partial f(M, t)}{\partial t} + \frac{1 - \epsilon}{\epsilon c^2} \frac{\partial}{\partial M} \left( \int L \mathcal{P}(M|L, t) \phi(L, t) dL \right) = 0$$

- ★ The single  $L/L_{\text{Edd}}$  for all  $L, z$  still provides the best match of local BH MF.
- ★ Need to take into account  $z, L$  dependence of  $L/L_{\text{Edd}}$  distributions for improvement but small changes on final results.
- ★ Too many free parameters, need observational constraints on  $L/L_{\text{Edd}}$  distr.
- ★ Only possibility is to measure virial  $M_{\text{BH}}$  in type 1 AGN at all  $z$ .



# z evolution of BH-galaxy relations

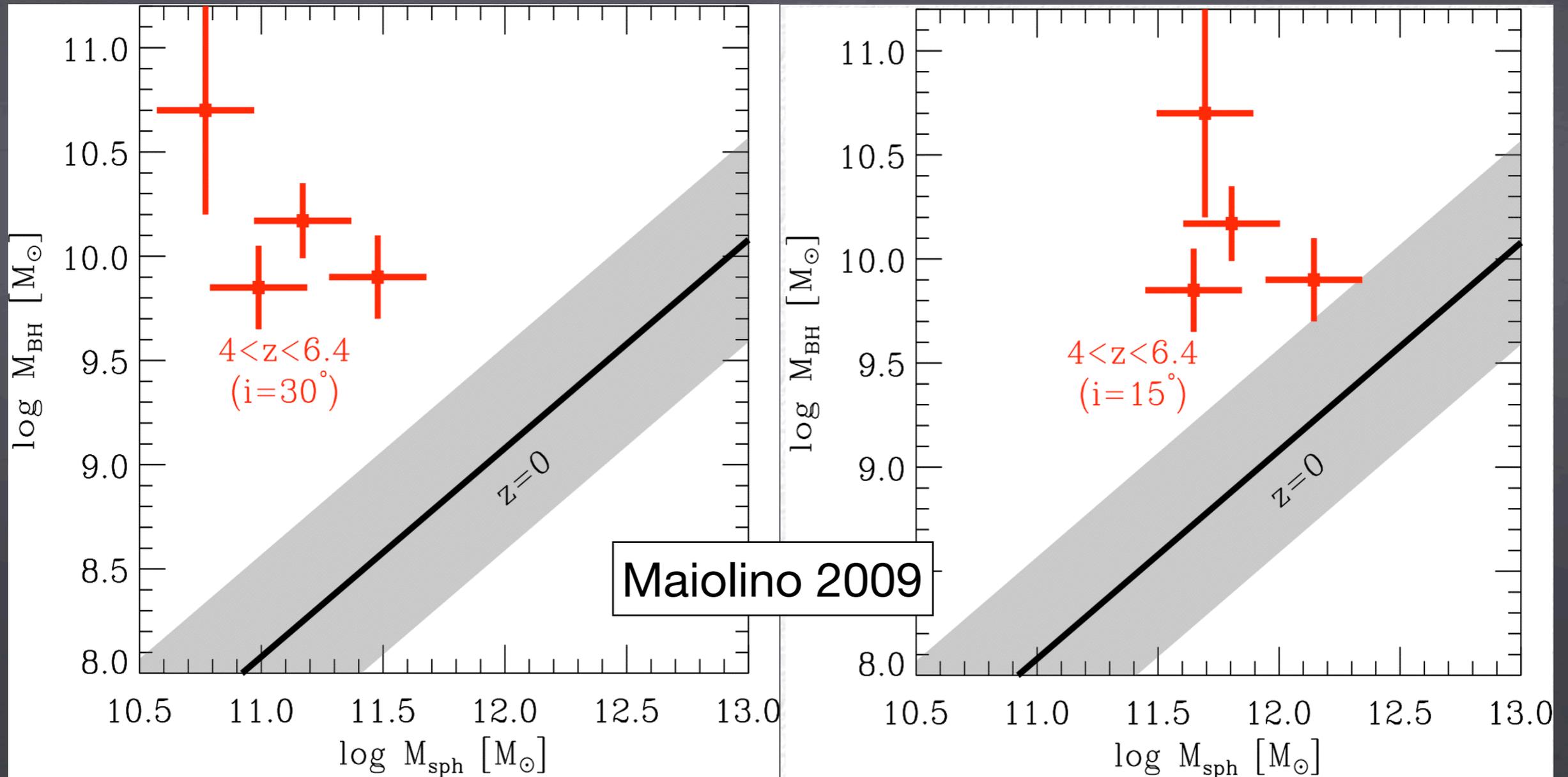
BH growth appear to precede galaxy growth in luminous quasars (but many uncertainties do BH mass estimates, deconvolution AGN-host galaxy, etc.). Sub-mm galaxies appear to have small BHs (eg Alexander+08). These puzzling results might just represent selection effects (Lamastra+09)



# $M_{\text{BH}}$ -galaxy in very high- $z$ quasars

$4 < z < 6.4$  quasars with  $M_{\text{sph}}$  estimate from CO line width ( $\rightarrow$  host galaxy mass, depends on assumed inclination) and virial  $M_{\text{BH}}$ .

Even reducing to low inclination, very high  $M_{\text{BH}}/M_{\text{sph}}$  compared to local value!

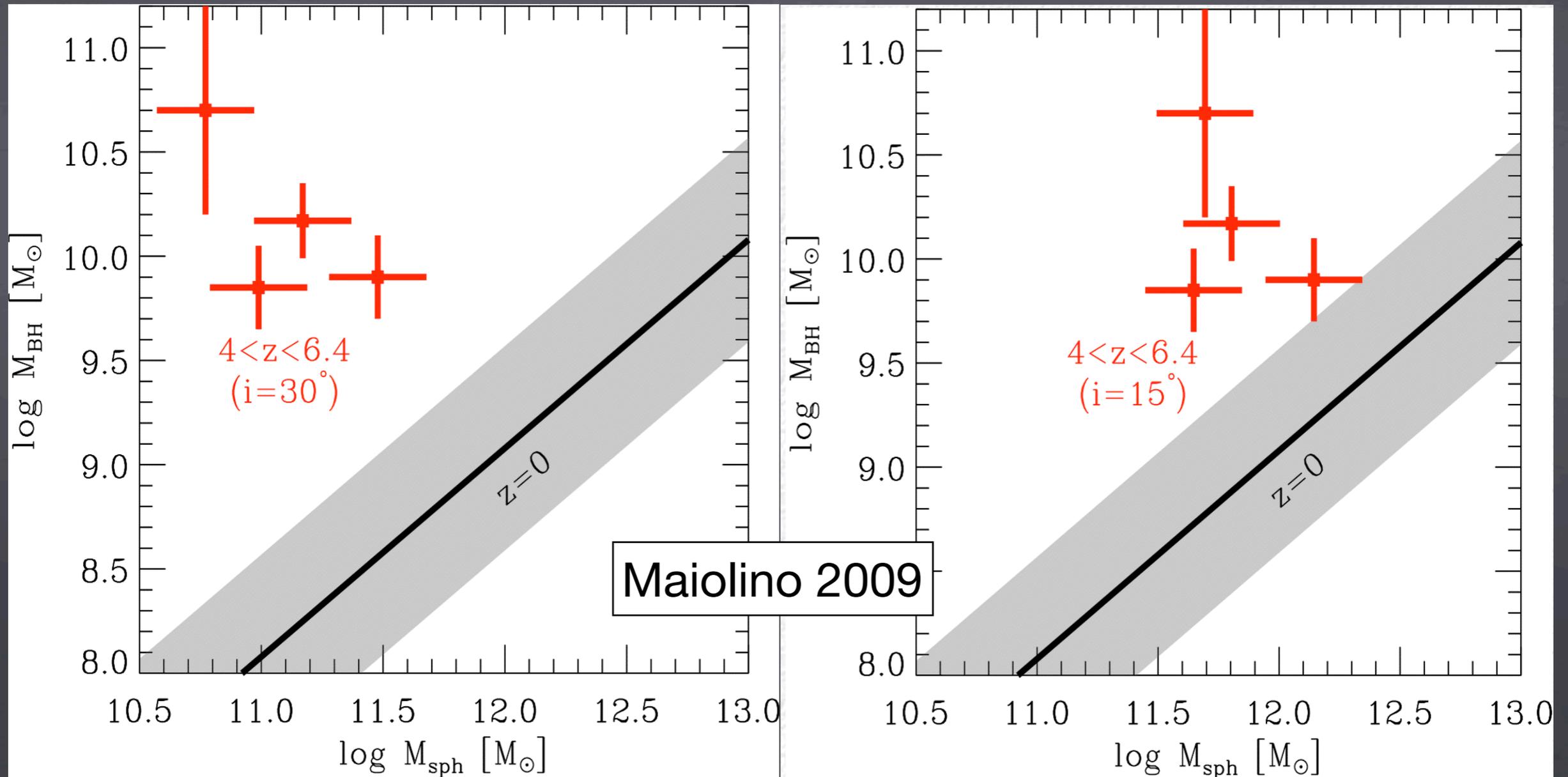


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**Importance of measuring host galaxy kinematics  
in submm  $\rightarrow$  strong synergies with ALMA**



# Enough time to grow high z BHs?

Highest redshift quasar @z=6.41 has  $M_{\text{BH}} \sim 6 \times 10^9 M_{\odot}$  [Willott+2003, updated]

With updated virial relation:  $M_{\text{BH}} \sim 1.2 \times 10^{10} M_{\odot}$

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Emission at fraction  $\lambda$   
of Eddington Luminosity  $L = \lambda L_{Edd} = \lambda \frac{M_{BH} c^2}{t_{Edd}}$

e-folding time:  $t_{Salp} = \frac{\varepsilon}{(1 - \varepsilon)\lambda} t_{Edd} \simeq 0.05 \text{ Gyr}$  with  $\varepsilon = 0.1$ ,  $\lambda = 1$

Minimum time required for growth:  $t = t_{Salp} * \ln \frac{M_{BH}(t)}{M_{BH}(t_0)}$

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With direct collapse to BH (“quasistars” Begelman+2007) “seeds” have:

$$\begin{array}{lll} z(t_0) \simeq 30 & M_{BH}(t_0) \simeq 10^3 M_{\odot} & t_{BH} = 0.83 \text{ Gyr} \\ & M_{BH}(t_0) \simeq 10^4 M_{\odot} & t_{BH} = 0.71 \text{ Gyr} \end{array}$$

# Enough time to grow high z BHs?

Highest redshift quasar @z=6.41 has  $M_{BH} \sim 6 \times 10^9 M_{\odot}$  [Willott+2003, updated]

With updated virial relation:  $M_{BH} \sim 1.2 \times 10^{10} M_{\odot}$

Was there enough time to grow the BH?

Emission at fraction  $\lambda$   
of Eddington Luminosity  $L = \lambda L_{Edd} = \lambda \frac{M_{BH} c^2}{t_{Edd}}$

e-folding time:  $t_{Salp} = \frac{\varepsilon}{(1 - \varepsilon)\lambda} t_{Edd} \simeq 0.05 \text{ Gyr}$  with  $\varepsilon = 0.1$ ,  $\lambda = 1$

Minimum time required for growth:  $t = t_{Salp} * \ln \frac{M_{BH}(t)}{M_{BH}(t_0)}$

With direct collapse to BH (“quasistars” Begelman+2007) “seeds” have:

$$\begin{array}{l} z(t_0) \simeq 30 \\ \cancel{M_{BH}(t_0) \simeq 10^3 M_{\odot}} \quad \cancel{t_{BH} = 0.83 \text{ Gyr}} \\ M_{BH}(t_0) \simeq 10^4 M_{\odot} \quad t_{BH} = 0.71 \text{ Gyr} \end{array}$$

Elapsed time is:  $t(z = 6.41) - t(z = 30) = 0.74 \text{ Gyr}$

# Summary

## USING

x-ray sources from WFXT **WITH** accurate optical/NIR spectroscopy

$10^{7.2}$  AGN

$10^{5.9}$  AGN with  $N(H) > 10^{23} \text{ cm}^{-2}$

$10^{3.4}$  at  $z > 6$

$10^{2.7}$  Compton-thick at  $z > 1$

## WE CAN

Constrain average radiative efficiency (spinning BHs?) &

Obtain the cosmological evolution of supermassive BHs (BH MF @  $z \sim 0-6$ )

- ★ Luminosity function of Compton-Thin AGN ( $z \sim 0-6$ )
- ★ Constraints on Compton-Thick fraction ( $z \sim 0-2$ )
- ★ Spectral Energy Distributions (optical - X) as a function of  $L$ ,  $M_{\text{BH}}$
- ★  $L/L_{\text{Edd}}$  distribution of type 1 AGN as a function of  $L$

$M_{\text{BH}}$ -galaxy relation at high  $z$  (synergies with ALMA for host galaxy)

BH growth (&  $M_{\text{BH}}$ -galaxy) at  $z > 6$